## **IMPRS lectures 2013**

# Galaxy formation

## **Simon White**



## Cosmological context and initial conditions for galaxy formation



A direct image of the pregalactic Universe:  $z \sim 1100$ , t = 380,000 years Appears to be an (almost) perfect gaussian random field Power spectrum an excellent fit to the concordance  $\Lambda$ CDM model At that time ~65% dark matter, ~10% baryons, ~25% radiation ( $\gamma$ 's and  $\nu$ 's) No nonlinear structure, no elements heavier than Li Structure directly imaged down to scales corresponding to galaxy clusters.

## Small-scale pregalactic structure is visible in Ly $\alpha$ forest



The ACDM model continues to provide an excellent fit down to the smallest scales measurable through absorption of distant quasar light by H in the (non-uniform) intergalactic medium.

These scales are smaller than those which collapse to form even dwarf galaxies

keVThus. IC's are fully<br/>characterised on all0.100scales relevant for<br/>making galaxies

## Structure growth in the DM distribution is well understood

- Growth of DM structure in a representative cosmic slice
- DM structure today -- a pattern across many scales
- DM structure today -- a flight through the Millennium Simulation
- Growth of the DM structure in a "Milky Way" dark halo

This provides detailed <u>quantitative</u> information on the abundance, internal structure, assembly history and spatial distribution of dark matter halos/subhalos

## Baryonic evolution is more complex and so less well understood

- Formation of a rich cluster (shocks, but no cooling, star formation...)
- Formation of a disk galaxy (Eris + cooling, star formation, SN feedback..)
- A collision of disk galaxies (+ black holes and BH feedback..)



## Galaxy and halo abundances have different shapes

A formation efficiency which matches abundance of "Milky Ways" overproduces the number of "Fornax's" by a factor of 30!





The stellar mass of the central galaxy increases rapidly with halo mass at small halo mass, but slowly at large halo mass The characteristic halo mass at the bend is 5 x  $10^{11}$  M<sub> $\odot$ </sub>

## The efficiency of galaxy formation is low!



 $M_*/M_{halo}$  maximises at 3.5% at halo masses of ~  $10^{12} M_{\odot}$ This is much less than the global baryon fraction ~ 17%Conversion of halo baryons to stars has maximum efficiency ~20 to 30% and is much smaller at higher and lower halo mass

## Observations of abundances now available back to $z \sim 8$ , covering >95% of all galaxy formation



Scaling relations between global properties are well characterised at  $z \sim 0$ 



9.4

9.2

Gas metallicity-

stellar mass

Galaxy internal structure is observed in great detail and in many components (stars, gas, B-field, cosmic rays, dark halos (via lensing)....)

Galaxy interiors are more heterogenous but also more observationally accessible than, for example, stellar interiors.







The clustering of galaxies depends on their luminosity, colour, morphology, SFR, AGN status...

Galaxies are influenced by (and influence) their environment





Planck Collaboration 2013

Shock Heating

In galaxy groups and clusters, the shock heated gas is directly visible through X-rays and the SZ effect

In the nearest and brightest systems the shocks are directly visible





### Gas cooling and condensation

Is seen in cooling flows in clusters and groups but is not yet clearly identified on galaxy scale











Are triggered by mergers, interactions + ?, and are visible when active through strong line and IR emission, and when complete through large fractions of intermediate age stars

## Stellar evolution

is also visible through colour and <sup>2</sup> spectral evolution of populations





### Galactic winds

are seen in emission in nearby starburst galaxies, in absorption in distant starforming and post-starburst galaxies, and through the heavy elements they deposit at large galactocentric radius





## AGN Feedback

Substantial effects of feedback on the largescale environment are seen both for quasars and for radio galaxies





Z = 0.64 [OIII] $\lambda 5007$ 



### Mergers

Are observed in the field, at the centres of rich clusters and in the Milky Way's archeological record







Tidal and ram-pressure stripping

are seen to be removing gas and stars from galaxies in the Virgo cluster

Mihos et al 2005



Diffuse Light in Virgo

Mihos etal 2005

## **Galaxy Formation**

- The initial/boundary conditions are precisely known

   ---material and radiation content
   ---structure (initially linear on all scales)
   ---cosmological context (ΛCDM)
- The nonlinear evolution of the dominant DM component can be characterised precisely and in detail
- Population statistics available over the entire formation period ---abundances

---scaling relations (M, SFR, size, kinematics, Z, gas content..) ---internal structure (morphology, concentration...)

---clustering

• Almost all the processes driving formation/evolution have now been observed directly in individual systems

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- Almost all the processes driving formation/evolution have now been observed directly in individual systems

## Galaxy formation is inherently complex, but very highly constrained

## Textbook published in 2010

## Galaxy Formation and Evolution

Houjon Mo, Frank van den Bosch and Simon White

CAMBRIDGE

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## 840 pages160 figures

## \$85 from Amazon or Barnes & Noble



Fig. 4.1. The linear growth rates in cosmological models with  $\Omega_{m,0} = 0.1, 0.2, 0.3, 0.5$  and 1. The left panel assumes  $\Omega_{\Lambda,0} = 0$  while the right panel assumes  $\Omega_{m,0} + \Omega_{\Lambda,0} = 1$ . The rates are all normalized so that D(z=0) = 1.



FIG. 1.—Angular momentum normalized to the value predicted by linear theory is shown as a function of expansion factor for the particles which end up in groups of more than 100 members in two N-body experiments. Fig. 1*a* is a simulation of a neutrino-dominated universe, while in Fig. 1*b* the particles were initially distributed uniformly at random. Solid lines show the mean for all rich groups in each model while dashed lines show the behavior of "typical" individual groups. The dotted lines show the relationships  $J \propto a^{5/2}$  which would be obeyed if angular momentum grew at second order in perturbation theory, and J = const which is expected at late times.



Fig. 4.3. The evolution for adiabatic neutrino perturbations with various  $k/k_{\nu}$ . The scale factor is normalized to be unity at a redshift  $z = z_{nr} = 57300(m_{\nu}/30 \text{ eV})$ . [Adapted from Bond & Szalay (1983) by permission of AAS]

## The exclusion of neutrinos as a DM candidate





## Dark matter halos are the basic units of nonlinear structure

Is all dark matter part of some halo?

Was this always the case?

How do halos grow? accretion? merging?

How are they distributed?

What is their internal structure?

- -- density profile
- -- shape
- -- subhalo population mass/radial distributions, evolution

-- caustics

How do these properties affect DM detection experiments? How can they be used to test the standard paradigm? How do they affect/are they affected by the baryonic matter




FIG. 11.—Self-similar accretion of a  $\gamma = 5/3$ ,  $\Omega_b \ll 1$  collisional gas moving in the potential of the  $\Omega = 1$  collisionless solution. The velocity V, density D, pressure P, and mass M are plotted vs. radius  $\lambda$ , with units given by eqs. (2.9) and (3.2), with  $\rho_H$  reduced by a factor of  $\Omega_b$ .

Gas hits an infall shock very close to the outermost caustic, and is static inside it with a density profile sillar to that of the DM

If the density field is smoothed using a sharp filter in kspace, then each step in the random walk is independent of all earlier steps

A Markov process

The walks shown at positions **A** and **B** are equally probable



At an early time  $\tau_1$ A is part of a quite massive halo

**B** is part of a very low mass halo or no halo at all



Later, at time τ<sub>2</sub>
A's halo has grown slightly by accretion
B is now part of a moderately massive halo



A bit later, time  $\tau_3$ A's halo has grown further by accretion

**B**'s halo has merged again and is now more massive than **A**'s halo





The assembly history of a halo is <u>independent</u> of its future

The assembly history of a halo is <u>independent</u> of its environment

The internal structure of a halo is <u>independent</u> of its environment

The mass distribution of progenitors of a halo of given M and z is obtained simply by changing the origin to  $\sigma_o^2(M)$  and  $\delta_c/D(z)$ 

The resulting formulae can be used to obtain descendant distributions and merger rates

A similar argument gives formulae for the clustering bias of halos



# **Does it work point by point?**



#### Boylan-Kolchin et al 2009



Mo & White 2002



Abundance of rich cluster halos drops rapidly with z

Abundance of Milky Way mass halos drops by less than a factor of 10 to z=5

 $10^{9}M_{\odot}$  halos are almost as common at z=10 as at z=0

Mo & White 2002 3 2 0  $\log\,n/(h^{-1}Mpc)^{-3}$ -2 -8 $12 \log 1$ T) 5 101520 0  $\mathbf{Z}$ 

Temperature increases with both mass and redshift  $T \propto M^{2/3} (1 + z)$ 

Halos with virial temperature  $T = 10^7$  K are as abundant at z = 2 as at z=0

Halos with virial temperature  $T = 10^{6}$  K are as abundant at z = 8 as at z=0

Halos of mass  $>10^{7.5}M_{\odot}$  have T > 10<sup>4</sup> K at z=20 and so can cool by H line emission

Mo & White 2002



Half of all mass is in halos more massive than  $10^{10}M_{\odot}$ at z=0, but only 10% at z=5, 1% at z=9 and 10<sup>-6</sup> at z=20

1% of all mass is in halos more massive than  $10^{15}M_{\odot}$ at z=0

40% of all mass at z=0 is in halos which cannot confine photoionised gas

1% of all mass at z=15 is in halos hot enough to cool by H line emission

Mo & White 2002



Halos with the abundance of  $L_*$  galaxies at z=0 are equally strongly clustered at all z < 20

Halos of given mass or virial temperature are more clustered at *higher* z

Mo & White 2002



The remnants (stars and heavy elements) from all star-forming systems at z>6 are today more clustered than  $L_*$  galaxies

The remnants of objects which at any z > 2 had an abundance similar to that of present-day  $L_*$  galaxies are today more clustered than  $L_*$  galaxies

#### Bias as a function of v



#### Halo clustering depends on formation history!



Gao, Springel & White 2005

The 20% of halos with the *lowest* formation redshifts in a 30 Mpc/h thick slice

 $M_{halo} \sim 10^{11} M_{\odot}$ 

#### Halo clustering depends on formation history!



Gao, Springel & White 2005

The 20% of halos with the <u>highest</u> formation redshifts in a 30 Mpc/h thick slice

 $M_{halo} \sim 10^{11} M_{\odot}$ 

#### Bias as a function of v and formation time



#### Bias as a function of v and concentration



### Bias as a function of v and main halo mass fraction



#### Bias as a function of v and spin



# Halo assembly bias: conclusions

The large-scale bias of halo clustering relative to the dark matter depends on halo mass through  $v = \delta_c / D(z) \sigma_c(M)$  and also on

- -- formation time
- -- concentration
- -- substructure content
- -- spin

The dependences on these assembly variables are different and <u>cannot</u> be derived from each other, e.g. more concentrated halos are more strongly clustered at low mass but less strongly clustered at high mass; rapidly spinning halos are more strongly clustered by equal amounts at all masses.

These dependences are likely to be reflected in <u>galaxy</u> bias

Millennium Simulation cosmology:  $\Omega_m = 0.25, \ \Omega_A = 0.75, \ n=1, \ \sigma_8 = 0.9$ 



Millennium Simulation cosmology:  $\Omega_m = 0.25, \ \Omega_A = 0.75, n=1, \sigma_g = 0.9$ 





$$\Omega_{m} = 0.25, \ \Omega_{\Lambda} = 0.75, n=1, \sigma_{8} = 0.9$$

If these Markov random walks are scaled so the maximum variance is 720 and the vertical axis is multiplied by  $\sqrt{720}$ , then they represent <u>complete</u> halo assembly histories for random CDM particles.

An ensemble of walks thus represents the probability distribution of assembly histories

Millennium Simulation cosmology:  $\Omega_{m} = 0.25, \ \Omega_{\Lambda} = 0.75, \ n=1, \ \sigma_{8} = 0.9$ 



Millennium Simulation cosmology:

#### $\Omega_{m} = 0.25, \ \Omega_{\Lambda} = 0.75, \ n=1, \ \sigma_{o} = 0.9$



Millennium Simulation cosmology:  $\Omega_m = 0.25, \ \Omega_A = 0.75, \ n=1, \ \sigma_8 = 0.9$ 



Millennium Simulation cosmology:  $\Omega_{m} = 0.25, \ \Omega_{\Lambda} = 0.75, \ n=1, \ \sigma_{8} = 0.9$ 



Millennium Simulation cosmology:  $\Omega_{m} = 0.25, \ \Omega_{\Lambda} = 0.75, \ n=1, \ \sigma_{8} = 0.9$ 



Millennium Simulation cosmology:  $\Omega_m = 0.25, \ \Omega_A = 0.75, n=1, \sigma_8 = 0.9$ 



# **EPS** halo assembly: conclusions

The typical first halo is much more massive than the free streaming mass

First halos typically collapse quite late  $z \sim 13$ 

Halo growth occurs mainly by accretion of much smaller halos

There are rather few "generations" of accretion/merger events

Major mergers are not a major part of the growth of many halos

#### **A Halo Merger Tree**

Halo trees can be built from EPS theory, but many galaxies may be in a (cluster) halo.

Galaxies correspond better to subhalos than to halos

redshift



Total progenitor mass is not conserved because of diffuse (unresolved) infall onto halos



Two orthogonal slices through a 10% growing mode density perturbation imposed on a glass initial load in an EdS cosmology

Initial conditions a = 1



Two orthogonal slices through a 10% growing mode density perturbation imposed on a glass initial load in an EdS cosmology



Two orthogonal slices through a 10% growing mode density perturbation imposed on a glass initial load in an EdS cosmology


Self-similar evolution from scale-free ICs in EdS: matched nonlinear masses M<sub>\*</sub>

## The dark matter structure of ACDM halos

#### A rich galaxy cluster halo Springel et al 2001

#### A 'Milky Way' halo Power et al 2002



# **ACDM galaxy halos (without galaxies!)**

Halos extend to  $\sim 10$  times the 'visible' radius of galaxies and contain  $\sim 10$  times the mass in the visible regions

Halos are not spherical but approximate triaxial ellipsoids -- more prolate than oblate

-- axial ratios greater than two are common

"Cuspy" density profiles with outwardly increasing slopes --  $d \ln \rho / d \ln r = \gamma$  with  $\gamma < -2.5$  at large r $\gamma > -1.2$  at small r

Substantial numbers of self-bound subhalos contain ~10% of the halo's mass and have  $dN/dM \sim M^{-1.8}$ 

Most substructure mass is in most massive subhalos

# **Density profiles of dark matter halos**



The average dark matter density of a dark halo depends on distance from halo centre in a very similar way in halos of all masses at all times -- a universal profile shape --

$$\rho(r)/\rho_{crit} \approx \delta r_s/r(1 + r/r_s)^2$$

Less massive halos and halos that form earlier have higher densities (bigger  $\delta$ )

Concentration  $c = r_{200} / r_s$  is an alternative density measure Beware variety of definitions!

# NFW profiles may not be pretty....



# ...but they work surprisingly well



"Milky Way" halo z = 1.5 $N_{200} = 3 \times 10^{6}$  "Milky Way" halo z = 1.5 $N_{200} = 94 \times 10^{6}$  "Milky Way" halo z = 1.5 N<sub>200</sub> = 750 x 10<sup>6</sup>

# How well do density profiles converge?

Aquarius Project: Springel et al 2008



Mass and length resolution vary by factors of 2000 and 35

Convergence excellent to radii well below that of the Sun's orbit

Real DM profile will be modified by growth of the visible Galaxy

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Mass and length resolution vary by factors of 2000 and 35

Convergence excellent to radii well below that of the Sun's orbit

Real DM profile will be modified by growth of the visible Galaxy

#### **Concentration scatter and trend with M and z**

Gao et al 2008



# **The Aquarius halos**

#### Springel et al 2008



# The Einasto profile fits the inner cusps

Navarro et al 2009



# The Einasto profile fits the inner cusps

Navarro et al 2009



# The Einasto profile fits the inner cusps

Navarro et al 2009



Einasto's (1965) profile:  $\ln \rho(r) / \rho_{-2} = -2 / \alpha [(r / r_{-2})^{\alpha} - 1]$ 

#### The Einasto α varies with mass

Gao et al 2008

#### Results for stacked halos in the Millennium Simulation



Einasto's (1965) profile:  $\ln \rho(r) / \rho_{2} = -2 / \alpha [(r / r_{2})^{\alpha} - 1]$ 



# A lensing test of the DM paradigm?

Hayashi & White 2008



Gravitational lensing allows *measurement* of these mean profiles The characteristic shape is a direct test of the DM paradigm

### **Velocity dispersion profiles**

Navarro et al 2009



Velocity dispersion and anisotropy peak at intermediate radii

Navarro et al 2009



Results are well converged

Velocity dispersion and anisotropy peak at intermediate radii Profiles vary significantly between halos

#### **Pseudo-phase-space density profiles**

Navarro et al 2009



Shape variations in the density and velocity dispersion profiles compensate to make  $\rho(r) / \sigma(r)^3$  an almost universal power law

### Halo profiles: conclusions

The NFW formula fits spherically averaged profiles of most objects to within 10% out to at least 2  $r_s$ 

The characteristic density (or concentration) varies with mass, redshift and cosmology

The Einasto formula fits better – its additional shape parameter varies systematically with mass

There is no indication of any "asymptotic inner power law"

The scatter among halos is larger than the Einasto-NFW difference

Mean profiles change shape dramatically at large radius ( $\delta < 10$ )

Velocity dispersion profiles show considerable variation

Variations in  $\rho(r)$  and  $\sigma(r)$  compensate to give power law  $\rho/\sigma^3$ 

# Halo profiles: observational issues

ΛCDM halos agree well with the observed structure of Galaxy halos (10 to 200 kpc: lensing, satellite motions) Cluster halos (30 to 2000 kpc: lensing, X-ray data on gas)

They appear to disagree with data in the inner parts of galaxies Milky Way  $M_{200} = 1(2) \times 10^{12} M_{\odot} \rightarrow M(R_{\odot}) = 3.3(4.5) \times 10^{10} M_{\odot}$ to compare with  $M_*(R_{\odot}) = 5 \times 10^{10} M_{\odot}$ LSB/dwarf galaxies Rotation curves rise slower than expected The "Cusp Problem"

Baryonic physics complicates this comparison Adiabatic compression increase may central DM densities Sudden expulsion of gas may decrease central DM densities both are quite uncertain

#### High quality rotation curves for nearby dwarfs: I



#### High quality rotation curves for nearby dwarfs: II







IC2574

# Inner rotation curves of low SB galaxies







Kuzio de Naray et al 2006



# **M 33**



#### Shapes of halo equidensity surfaces



Jing & Suto 2002

Shapes become systematically less spherical with decreasing radius

There is a lot of scatter between halos

Principal axes may change direction

#### Shapes of halo equidensity surfaces



Jing & Suto 2002

Shapes become systematically less spherical with increasing mass

A simple scaling leaves a "universal" result for the axis ratio distributions

#### Halo spin distributions

Bett et al 2007



The distribution of spin parameter  $\lambda$  is approximately lognormal. It depends little on mass, but significantly on halo definition.

#### How uniform are subhalo populations?









# How well does substructure converge?

Aquarius Project: Springel et al 2008

Convergence in the size and maximum circular velocity for individual subhalos cross-matched between simulation pairs.

Biggest simulation gives convergent results for

 $V_{max} > 1.5 \text{ km/s}$  $r_{max} > 165 \text{ pc}$ 

<u>Much</u> smaller than the halos inferred for even the faintest dwarf **galaxies** 

#### How uniform are subhalo populations?




#### Subhalos have subhalos have subhalos...

#### Springel et al 2008



## **Substructure: conclusions**

Substructure is primarily in the outermost parts of halos

The radial distribution of subhalos is almost mass-independent

Subhalo populations scale (almost) with the mass of the host

The subhalo mass distribution converges only weakly at small m

Subhalos contain a small fraction of the mass in the inner halo

# A Milky Way satellite problem?



# of small subhalos in  $\Lambda$ CDM halos  $\gg$  # of MW satellites

Maybe most of them just didn't make stars?

Subhalos with stars must be less massive than many without stars?



## Too big to fail – another satellite problem?

20

#### Boylan-Kolchin et al2011



ACDM simulations of the formation of halos like that of the Milky find many satellite subhalos with central densities bigger than any MW dSph.
Note that LMC, SMC and the Sagittarius dwarf not included. *Resolutions?*-- Lower mass MW halo?

- -- Lower mass MW halo? -- WDM?
  - -- Baryonic effects during star formation?

## Maybe Dark Matter can be detected in a laboratory









Maybe the annihilation of Dark Matter will be seen by Fermi?

2.0 Log(Intensity)

## **Small-scale structure and DM detection**

Direct detection involves bolometers/cavities of meter scale which are sensitive to particle momentum

- -- what is the density structure between m and kpc scales?
- -- how many streams intersect the detector at any time?

Indirect detection involves annihilation radiation  $L \propto \int \rho^2(\mathbf{x}) \langle \sigma v \rangle dV$ -- what is the density distribution around individual CDM particles on the annihilation interaction scale?

Predictions for detection experiments depend on the CDM distribution on scales <u>far</u> below those accessible to simulation

We require a good theoretical understanding of mixing and small-scale structure

## **Physics for Galaxy Formation Modelling**

#### Gas Cooling and Condensation

Sensitive to metal content, phase structure, UV background... Star Formation

No *a priori* understanding -- efficiency? IMF? Stellar Feedback

SF regulation, metal enrichment, galactic winds Stellar Aging

Population synthesis — luminosities, colours, spectra, (dust?) AGN physics

Black hole formation, feeding, AGN phenomenology, feedback Environment interactions

Galaxy mergers, tidal effects, ram pressure effects



**Cooling curve for metal**free, optically thin gas in collisional ionisation equ.

Luminosity/unit volume is  $L = n^2 \Lambda(T)$ 

No cooling occurs below  $10^4$ K unless  $H_{\gamma}$  can form

Cooling curve for metalfree, optically thin gas in collisional ionisation equ.



Optically thin cooling time  $t_{cool} \propto n_e T / L \propto T / n_e \Lambda(T)$ 

c.f. gravitational collapse time  $t_{dyn} \propto (G \rho)^{-1/2} \propto n_e^{-1/2}$ 



**Cooling curve for metal**free, optically thin gas in collisional ionisation equ.

Luminosity/unit volume is  $L = n^2 \Lambda(T)$ 

No cooling occurs below  $10^4$ K unless  $H_{\gamma}$  can form

Addition of UV background suppresses line cooling density-dependent heating

#### Radiative processes in galaxy formation



Rees & Ostriker 1977 Silk 1977 Binney 1977

When gas clouds of galactic mass collapse:

(i) shocks are radiative and collapse unimpeded, when  $t_{cool} < t_{dyn}$ (ii) shocks are non-radiative and collapse arrested, when  $t_{cool} > t_{dyn}$ where quantities are estimated at virial equilibrium

Galaxies form in case (i) since fragmentation is possible

Primordial cooling curve  $\longrightarrow$  characteristic mass  $10^{12} M_{\odot}$ 

#### Radiative processes in galaxy formation



Rees & Ostriker 1977 Silk 1977 Binney 1977

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Primordial cooling curve  $\longrightarrow$  characteristic mass  $10^{12} M_{\odot}$ 

## Towards a "modern" theory



Adding : (i) dark matter, (ii) hierarchical clustering, (iii) feedback -- cooling always rapid for small masses and early times

- -- only biggest galaxies sit in cooling flows
- -- feedback à la Larson (1974) needed to suppress small galaxies

A good model: 
$$\Omega_{\rm m} = 0.20$$
,  $\Omega_{\rm gas} / \Omega_{\rm DM} = 0.20$ ,  $\alpha = 1/3$  (n = -1)

## Towards a "modern" theory



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A good model: 
$$\Omega_{\rm m} = 0.20$$
,  $\Omega_{\rm gas} / \Omega_{\rm DM} = 0.20$ ,  $\alpha = 1/3$  (n = -1)

## Spherical similarity solutions for infall



Infall of DM +  $\gamma = 5/3$  gas onto a point mass in an EdS universe -- accretion shock at ~1/3 of turn-round radius

- -- gas almost static inside shock
- -- pre-shock gas has density about 4 times the cosmic mean --  $kT(r) / \mu \sim GM(r) / r = V_c^2$ ;  $R \sim V_c t$ ,  $M \sim V_c^3 t / G$

## Spherical similarity solutions for cooling



## Putting it together in a sCDM universe





# Radiative cooling in spherical infall models

Forcada-Miró & White 1997 astro-ph/9712204

Spherical, isothermal infall model with  $V_{circ} = 220$  km/s and  $f_{gas} = 0.05$ 

Non-equilibrium H and He ionization and radiation

At early times  $r_{cool}$  and  $r_{shock}$ coincide; interior dynamic cooling flow has  $\rho \propto r^{-1.5}$ 

At later times  $r_{cool}$  and  $r_{shock}$ separate, enclosing a near static region:  $\rho \propto r^{-2.0}$ 

#### Shock and cooling radius evolution in isothermal models



Forcada-Miró & White 1997



Cooling radius breaks away from shock as both near similarity shock radius

Cooling radius then follows the Bertschinger solution  $r_{cool} \propto t^{0.5}$ 

Shock asymptotes to the non-radiative sim. solution

 $r_{\rm shock} \propto t$ 

#### Cold and shocked mass evolution in isothermal models



## Transition from infall- to cooling-dominated flow



Forcada-Miró & White 1997

Infall dominated flow switches to cooling from static atmosph.

 $r_{cool} \approx r_{shock} \rightarrow r_{cool} < r_{shock}$ when the cooling time for gas at the post-shock temperature and density in the *nonradiative* solution is equal to the age of the system

This is the "semi-analytic" criterion suggested by White & Frenk (1991) and is equivalent to the shock stability criterion of Birnboim & Dekel (2003)

## Radiation from shocks

For collisional ionisation equilibrium, the radiation from shocks would be dominated by He II 304 for  $70 \text{ km/s} < V_{sh} < 270 \text{ km/s}$ 



## Radiation from shocks

For collisional ionisation equilibrium, the radiation from shocks would be dominated by He II 304 for 70 km/s  $< V_{sh} < 270$  km/s ...but, in fact, non-equilibrium processes affect line emission strongly, particularly enhancing H I 1216 (Ly  $\alpha$ )



## Cooling in SPH compared to a SA model



Comparison of implementation in the *same* N-body ΛCDM cluster formation simulation of cooling (a) with SPH (b) with a standard SA model

Masses of central objects in halos agree well once above the SPH resolution limit (~ 50 particles)

Range checked includes transition from efficient to inefficient cooling

Different SPH implementations give different results

## Other physical complications

- **Radiative mixing layers** (Begelman & Fabian 1990) on the interface between cold clouds and a hot phase may radiate much of the cooling energy at an intermediate temperature
- **Cosmic ray populations** (e.g. Miniati et al 2001) from large-scale shocks or radio galaxies may add pressure support and also provide additional heating and energy transport
- **Metal enhanced cooling instability** may occur in differentially enriched regions. The more metal-rich regions cool and condense faster, dropping preferentially out of the hot phase
- **Winds/outflows** from AGN and from star-forming regions interact with infalling gas driven by gas/radiation pressure, CR's..
- **Radiative transfer** effects modify shock structure and emitted spectral energy distribution
- Magnetic fields as always...

Fall & Efstathiou 1980



Massive and extended dark halos are needed if tidal torques are to produce the angular momentum of galaxy disks (conclusion predates  $\Lambda$ CDM).

Mo, Mao & White 1998



Figure 2. Rotation curves for disc galaxies formed in haloes with an initial density distribution described by the NFW profile. The shape of the rotation curves depends only on the concentration parameter, c, the fraction of mass in the disc,  $m_d$ , and the spin parameter,  $\lambda' \equiv (j_d/m_d)\lambda$ . The total mass of a halo determines both the disc scalelength and the amplitude of the rotation curve. Four panels are shown for different sets of c,  $m_d$  and  $\lambda'$ . The disc mass is assumed to be  $M_d = 5 \times 10^{10} h^{-1} M_{\odot}$ . The rotation velocities induced by the disc and the dark matter are shown using long-dashed and short-dashed lines, respectively, while the total rotation velocity is shown by a solid line. The rotation velocity induced by the disc reaches a peak at about two disc scalelengths. The rotation velocity at  $r_{200}$  is indicated by thick horizontal bars and is identical to the rotation velocity at all radii for a singular isothermal sphere with the same mass. The upper left panel should be viewed as the reference panel. Only one parameter is varied between this panel and any other. Notice how both the prominence and amplitude of the peak in the rotation curve change between panels.

Mo, Mao & White 1998



Figure 3. Critical values of  $\lambda' (\equiv \lambda j_d/m_d)$  for disc instability as a function of The second favours cold  $m_d$ . Results are shown for three choices of  $\epsilon_m$ . For a given  $m_d$ , discs are stable if  $\lambda' > \lambda'_{crit}$ . The dependence on halo concentration, c, is weak, and is shown only for  $\epsilon_m = 1$ .

Mo, Mao & White 1998



Figure 4. Model predictions for  $R_d$  as a function of  $V_c$  for stable discs assembled at z = 0 and at z = 1 in the SCDM and ACDM models. The solid lines give the relations for critical discs when  $m_d = 0.05$ , while short-dashed lines give the corresponding relations for  $m_d = 0.025$ . Stable discs must lie above the line for the relevant value of  $m_d$ . The long-dashed lines correspond to  $m_d = j_d$  and  $\lambda = 0.1$ ; at most 10 per cent of discs should lie above these lines. The data points are the observational results of Courteau (1996, 1997) for a sample of nearby normal spirals.

Observed disks follow the expectations for moderately stable disks with  $m_d = j_d$  and  $m_d < 0.05$ .

Modest evolution towards smaller sizes is predicted to  $z \sim 1$ 

Mo, Mao & White 1998



Figure 6. Tully–Fisher (TF) relations for stable discs at z = 0 in the SCDM and  $\Lambda$ CDM cosmogonies. Monte Carlo samples of the predicted luminosity–rotation velocity distribution are shown for three choices of  $\epsilon_m$ . We have converted stellar mass (in the model) into *I*-band luminosity using  $\Upsilon = 1.7h$  (Bottema 1997). The solid lines give the linear regressions of absolute magnitude against log  $V_c$ . The dashed lines show the observed TF relation as given by Giovanelli et al. (1997).

Predicted Tully-Fisher relations for *stable* disks with *constant*  $m_d$  are compared with the observed relation for three stability criterion choices.

...but why is  $m_d = j_d$  = constant appropriate?

## Empirical star formation "laws"



Kennicutt-Schmidt "laws" are actually observational scaling relations between mean gas surface density and mean SFR surface density:

 $M_* \propto M_{gas}^{1.4}$  or  $M_* \propto M_{gas} / t_{dyn}$ 

where definitions and proportionality constants are set purely empirically

- -- which gas density? (atomic, molecular, , total?)
- -- which averaging area?
- -- thresholds?

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after Bigiel et al 2008

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## The stellar Initial Mass Function (IMF)



Total mass set by the turnover at low masses Luminosity, ionising and mechanical feedback set by high mass tail Usually assumed "universal" -- little theoretical/observational basis Some indications for variations but little consensus so far

• a <u>major</u> systematic uncertainty in galaxy formation models


Pre- and post-main sequence evolutionary tracks must be combined with

- -- stellar atmosphere models (to predict colours and spectra)
- -- with stellar wind and PN models (to predict material returned to ISM)
- -- with nucleosynthesis modelling (to predict yields of heavy elements)
- -- with supernova models (for energetic and chemical feedback)
- -- with ISM modelling (to predict line emission and dust obscuration)

## **Stellar Population Synthesis**



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### **Stellar Population Synthesis**



For real galaxies, the colours and integrated optical/IR spectra are affected by

- -- the stellar age distribution
- -- the stellar metallicity distribution
- -- the local and large-scale dust distributions

In practice, these three aspects are <u>strongly</u> correlated

→ Major degeneracies in inferring formation history from observation. Even inferring colours from a specific model is hindered by dust, TP-AGB...

# **Adding the baryons: hydrodynamics**

After recombination the baryons are in the form of a diffuse, near-uniform mixture of neutral H and He - no stars, almost no elements heavier than He, no magnetic fields (?)

Need to solve hydrodynamics equations for the gas in addition to N-body equations for the DM

 $\partial \rho / \partial t + \nabla .(\rho u) = 0$  Mass conservation  $\partial (\rho u) / \partial t + u . \nabla (\rho u) + \nabla p + \rho \nabla \Phi = 0$  Momentum cons. + Energy conservation

Main solution techniques

- -- discretise on a regular fixed mesh (Eulerian hydro)
- -- discretise on a variable, adaptive Eulerian mesh (Adaptive Mesh Refinement)
- -- discretise using a finite set of fluid elements

(Smoothed Particle Hydrodynamics: SPH)

-- discretise on an irregular quasi-Lagrangian mesh (e.g. a Voronoi tesselation, AREPO)

# Hydrodynamics and cluster formation

Structure formation produces shocks which transform the K.E. of fluid motions into heat

Bremsstrahlung and line emission from cluster gas is observable in X-rays  $S = \int dl \rho^2 \Lambda(T)$ 

Cluster "shadows" are observable against the CMB through the Sunyaev-Zeldovich effect  $\Delta T \propto \int dl p$ 

Hierarchical growth of structure produces the phenomenology observed in images of clusters Abell 3667

--asymmetries and sublumps

--shocks --cold fronts --cold cores





## **Gas cooling and galaxy formation**

Gas cooling times due to bremsstrahlung and line emission scale as  $t_{cool} \propto T / \rho \Lambda(T)$  while objects at cosmic time *t* have typical density  $\rho \propto t^{-2}$ . Hence  $t_{cool} / t \propto t T / \Lambda(T)$ —rapid cooling in lower mass objects and at early times —efficient galaxy formation with little hot halo gas. —strong feedback needed to offset gas condensation

When seen in cosmological simulations this was hailed as a "new paradigm" of cold flows. However, the novelty lies only in the characterisation of flow *morphology*. Low entropy gas from filaments can stream through hot halos to fuel galaxy formation.

The effect is important near the transition halo mass  $10^{1i-12}M_{\odot}$ It depends strongly on the hydrodynamics scheme used It will be affected by interaction between inflows and winds

### Gas cooling in cosmological simulations





# Cold and hot accretion modes

Half or more of all SPH particles accreted onto galaxies never heat above a few  $10^4$  K "Cold" accretion dominates in halos with  $V_{circ}$  less than about 100 km/s

Same point as transition from infall to cooling domination in spherical models?



### In-shock cooling





A radiative shock in a shock tube followed with SPH  $t_{cool} \sim h / V_{sh}$ 

Immediately behind a strong shock the gas heats to a temperature  $T = 3\mu V_{sh}^2 / 16 k$ ~ 1.4 x 10<sup>5</sup> (V<sub>sh</sub> / 100 km/s)<sup>2</sup>

Collisional thermalisation, ionisation and radiation processes then all occur simultaneously, often far from equilibrium

Many numerical hydrodynamics schemes broaden the shock heating region over several zones (grid) or smoothing lengths (SPH)

When post-shock cooling times are short this leads to spurious temperature evolution

#### Cold flows in an AMR simulation



Dekel et al 2009

A slice at z=2.5 through a  $\Lambda$ CDM simulation centred on a halo of virial mass  $10^{12}$  M<sub> $\odot$ </sub>

<sup>0.5</sup> Circle is virial radius, colour scale gives entropy, arrows show flow velocity.

Note the shock just outside the virial radius and the cold streams penetrating the hot halo and apparently reaching the galaxy

#### Cold flow fractions in differing hydro schemes



The maximum past temperature of gas elements accreted by z=2halos (bottom) and galaxies (top) as a function of halo mass.

Note similarity/ difference for accretion onto halos/galaxies.

# Cold flow fractions in differing hydro schemes



Past maximum temperatures (normalised to halo virial temperature) for gas accreted by halos (dotted) and galaxies (solid) in bins of z=2 halo mass.

For AREPO this peaks just above 1 for both components and all masses -Gas is always heated to just above the halo virial temperature. For GADGET this is not true for gas accreted onto higher mass galaxies

### Cold flow fractions in differing hydro schemes



Nelson et al 2013

This is not due to differences in accretion morphology, but rather to differences in dissipative heating and mixing.

Note that these simulations still do not have sufficient feedback to produce a realistic galaxy population.

## Feedback/galactic wind issues

Can supernova feedback drive galactic winds?

Can these reproduce the masselement abundance relation?

Can they enrich intergalactic gas with heavy elements?

Can these enhance formation of disks over bulges?

What about feedback from Active Galactic Nuclei?



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# Including the formation and evolution of stars

Stars form where gas is dense, cold and self-gravititating

Star formation is *not* resolved in galaxy formation simulations a simple *sub-grid* prescription is needed, for example  $\dot{\rho}_* = \alpha \ \rho_{gas} / t_{dyn}$ 

Aging of stars affects their brightness and colour

Supernovae, explosions of massive stars put energy and heavy elements into surrounding gas – *feedback, chemical enrichment* 

Feedback processes are also not resolved and must also be implemented with phenomenological recipes

Implementation details *strongly* affect galaxy formation models

The Aquila Project

Scannapieco et al 2011







projected mass density $[\log(M_{\odot} / kpc^{s})]$								
6.50	<b>Y.00</b>	7.50	8.00	8.50	9.00	9.50	10.00	10.50





#### The Aquila Project

Scannapieco et al 2011



#### The Aquila Project

Scannapieco et al 2011

# Simulating the formation of individual galaxies

Systems which have a *major merger* after most of their stars have formed end up looking like **Elliptical galaxies** 

Systems which have no major merger at late times end up having a substantial disk and looking like **Spiral galaxies** Disks grow inside-out and late,

It has proved hard to make spiral galaxies with small bulges



It's also hard to match the low formation efficiencies required by abundance matching....

. ..or to get get enough heavy elements out of galaxies
Resolution and feedback problems?

An alternative to following the gas within halos by direct hydro is to use simplified "semi-analytic" formulations of each of the major processes and integrate the resulting system of equations down the merger trees of all subhalos in a high-resolution DM simulation "semi-analytic" or galaxy population simulations For the baryonic components associated with each halo  $(\Omega_{\rm h} / \Omega_{\rm m}) M_{\rm halo} = M_{\rm hot} + M_{\rm cold} + M_{\rm ejecta} + M_{\rm star} + M_{\rm BH}$ black hole quasar mode accretion radio mode accretion RM feedback cooling cold interstellar **IGM** hot halo gas stripping ▲ISM reheating



 $(\Omega_{\rm h} / \Omega_{\rm m}) M_{\rm halo} = M_{\rm hot} + M_{\rm cold} + M_{\rm ejecta} + M_{\rm star} + M_{\rm BH}$  $\dot{M}_{_{\rm BH}} = \varepsilon \left( M_{_{\rm hot}} / M_{_{\rm halo}} \right) M_{_{\rm BH}} T_{_{\rm hot}}^{3/2}$ black hole quasar mode accretion radio mode accretion RM feedback cooling cold interstellar **IGM** hot halo gas stripping ▲ISM reheating gas infall SN feedback stellar mass 💌 loss winds star formation stars ejected gas  $\dot{\Sigma}_{\text{star}} = \alpha \left( \Sigma_{\text{cold}} - \Sigma_{\text{thr}} \right) / t_{\text{disk}}$ 



z = 0 galaxy light from a semianalytic model





Light-cone with the simulated formation/evolution of  $2x10^7$  galaxies from z = 10 to z = 0

Kitzbichler & White 2007

#### Population simulations predict: (i) galaxy abundances e.g the stellar mass function



Note that the simulated mass function fits the data over 5 dex in stellar mass! This is a result of adjusting various parameters in the physical model



Population simulations predict:(i) galaxy abundances e.g the stellar mass function

Luminosity functions of satellites around 1500 "Milky Ways" i.e. isolated disk galaxies with  $\log M_* = 10.8$ 

Note that the result depends on a "new" parameter describing the effectiveness of reionisation

Guo et al 2011







#### Population simulations predict: (iv) galaxy evolution

 $\triangle$  Perez-Gonzalez et al 2008

Marchesini et al 2009

Lower mass galaxies log  $M_* < 10.5$ form too early

Efficiency of starformation is too high in lower mass objects at high z?

Guo et al 2011

#### How do we learn from population simulations?



#### How do we learn from population simulations?



When simulating the astrophysics of galaxy formation, agreement with data is a measure of success...

...but it is the failures which show where there is missing or inadequate physics

cosmology? star formation? enrichment and feedback? environmental effects?

Guo et al 2011



#### How do we learn from population simulations?

