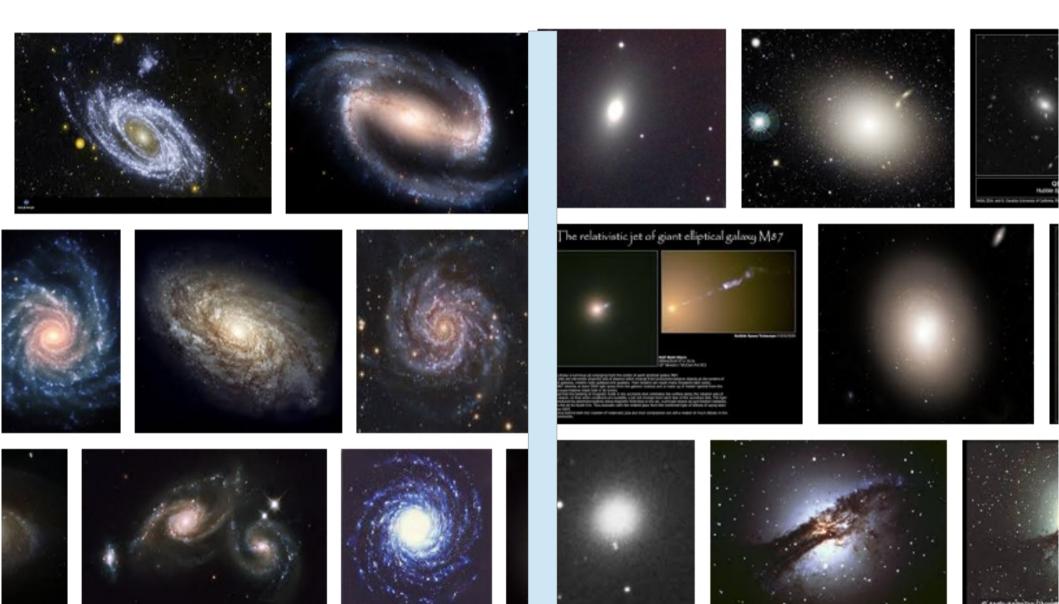
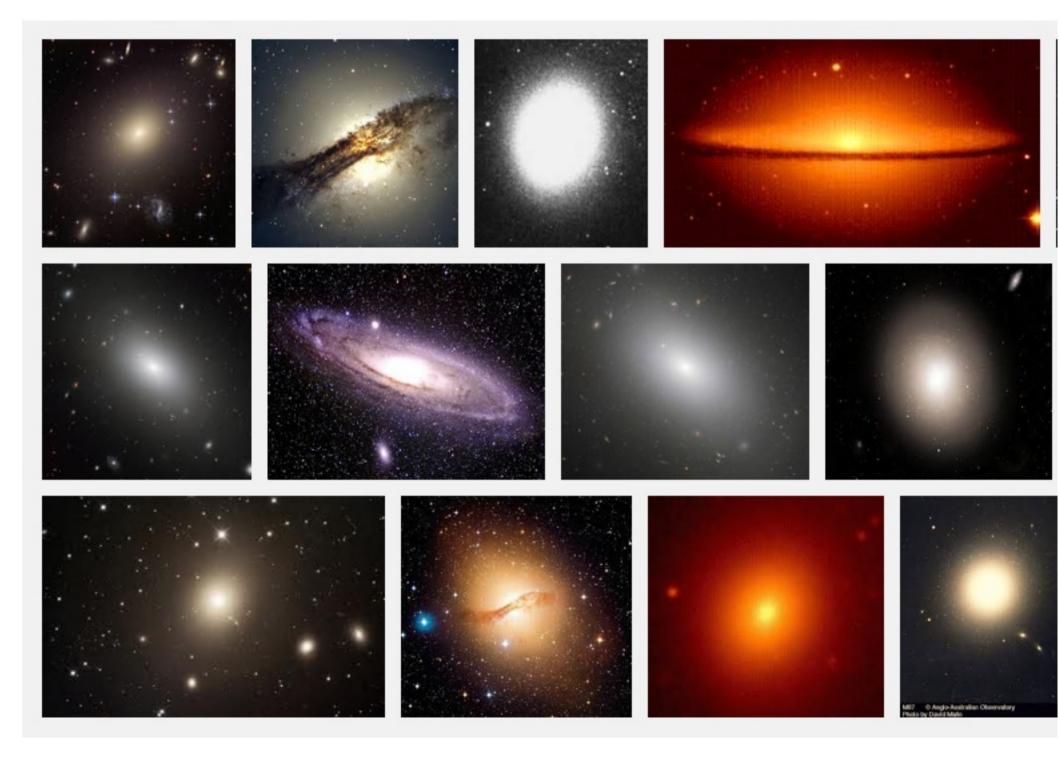
# Spiral and Elliptical Galaxies: what are their properties and how did they form?





## (i) deVaucouleurs (R<sup>1/4</sup>) and Sersic (R<sup>1/n</sup>) Laws

de Vaucouleurs noticed (1948) that for many ellipticals  $\mu \propto R^{1/4}$ The fit is usually good over all but the inner and outermost regions (typically 0.03 - 20 R<sub>o</sub>)

The law is usually written:

$$I(R) = I_e \exp \left(-7.67 \left[ (R/R_e)^{1/4} - 1 \right] \right)$$
 (7.3)

It has the following properties:

$$L_{\text{tot}} = 7.22 \pi R_{\text{e}}^{2} I_{\text{e}}$$

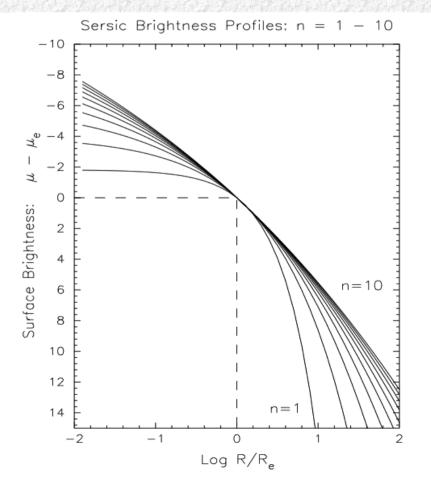
- I(0) = 2000 I
- $< I(<R_e)> = 3.61 I_e$  (which we abbreviate to  $< I_e >$  and equivalently  $< \mu_e >$ )
- Asymptotically, at small R,  $I(R) \propto R^{-0.8}$  while at large R,  $I(R) \propto R^{-1.7}$
- In terms of surface brightness:  $\mu(R) = \mu_e + 8.325[(R/R_e)^{1/4} 1] = \mu(0) + 8.325(R/R_e)^{1/4}$

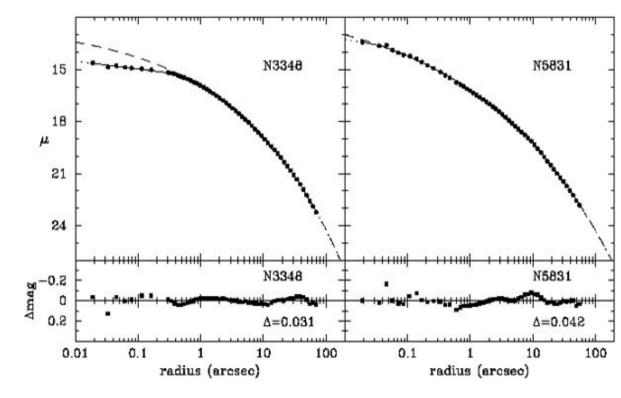
The deVaucouleurs law is a special case of a more general, Sersic (1963,1968), law:

$$I(R) = I_e \exp\left(-b\left[\left(R/R_e\right)^{1/n} - 1\right]\right) \tag{7.4}$$

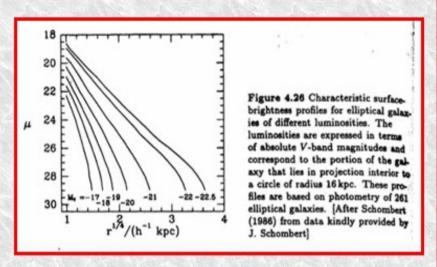
#### Where

- b = 1.999 n 0.327 (n>1) ensures  $0.5 L_{tot} = L(< R_e)$
- n=4 gives the de Vaucouleurs  $R^{1/4}$  law with b = 7.67
- n=1 gives an exponential profile with b=1.67

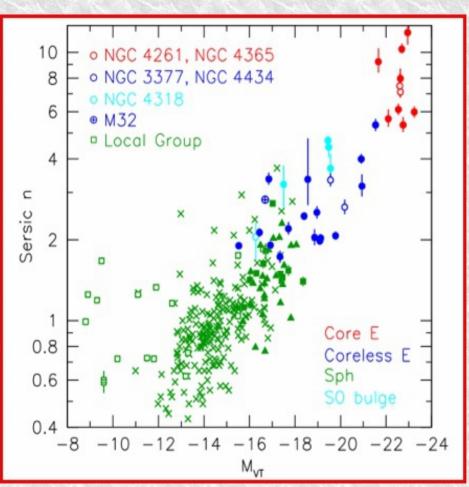




## More Luminous E's are More Concentrated



Surface brightness profiles for Ellipticals with a range of luminosity. The x axis is R<sup>1/4</sup> in kpc<sup>1/4</sup>. Clearly, more luminous galaxies are bigger, but also larger n-index since if the profile curves down the n-index is less than 4, but if it curves up it is more than 4.



Clear trend for more luminous Elliptical galaxies to have higher n-index (more concentrated profiles). Note the low luminosity dwarf spheroids have Sersic n in the same range as for disks. [Figure 33 from

#### (ii) Size & Luminosity vs Surface Brightness (Kormendy) Relation

A couple of correlations suggest larger, more luminous galaxies have lower surface brightness

#### $\leq I > correlates with R$ : Kormendy Relation

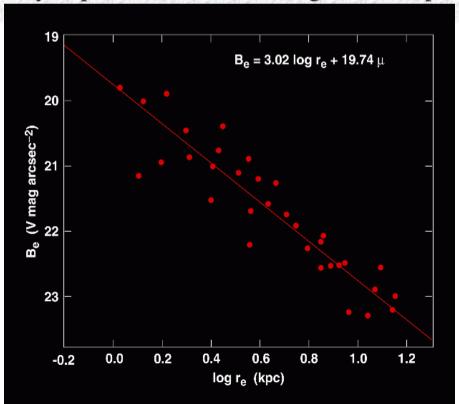
$$Arr R_e \simeq < I_e > ^{-0.83 +/-0.08}$$

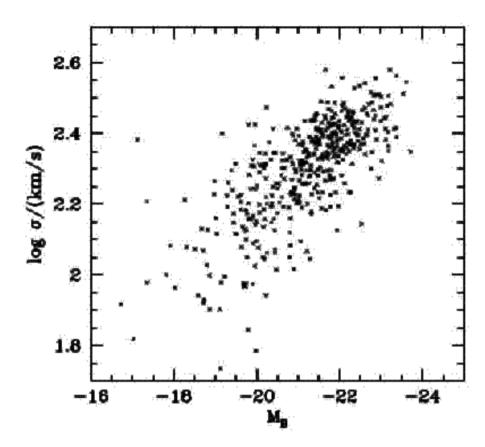
# $\leq$ I $\geq$ correlates with L $_{\rm tot}$ : $_{\rm tot}$ $\propto$ < I $_{\rm e}$ > $^{-2/3}$

$$L_{tot} \propto < I_e > ^{-2/3}$$

• this follows from the above relation, given  $L_e = 1/2 L_{tot} = pi < I_e > R_e^2$ 

We conclude: larger and more luminous galaxies are fluffier with lower densities An interpretation is not yet too clear, though galaxy formation models must explain it. One inference: low-luminosity ellipticals formed with more gaseous dissipation than giant ellipticals.





Faber-Jackson relation between central velocity dispersion and total magnitude of elliptical galaxies

$$L_B \propto \sigma^4$$

### (b) The 3-Parameter Fundamental Plane

The above 2-parameter correlations have considerable **real scatter**Furthermore, the residuals in one plot correlate with those in another.
This suggests we look for a tighter correlation among **three** parameters:

- A tilted **plane** of points in 3-D volume, which
- Projects onto 2-D planes as the (looser) correlations seen above
- One example is:  $\text{Log R}_{e} = a \text{ Log } \sigma + b \text{ Log I}_{e} + c$

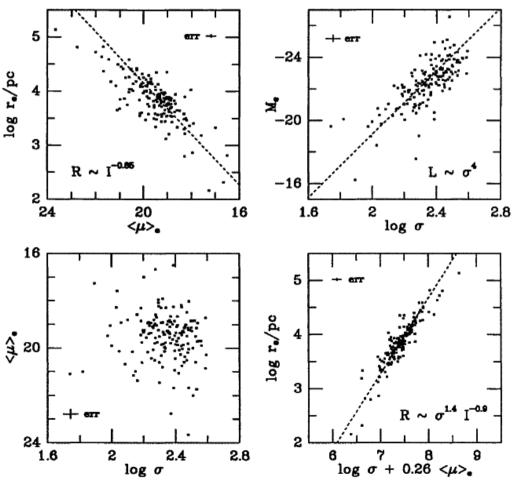


Figure 2 Projections of the fundamental parameter plane of elliptical galaxies. Top panels:

## (iv) The Physical Basis of the Fundamental Plane

The following gives some insight into the origin of the F-P relation: Consider:

$$\cdot < I_e > = \frac{1}{2} L_{tot} / \pi R_e^2$$
 (just a definition)

• M/R<sub>e</sub> =  $c \sigma_e^2$  (virial equilibrium, KE  $\propto$  PE; c = "structure parameter" containing all details)

Taken together, these give:

• 
$$R_e = (c/2\pi) (M/L)^{-1} \sigma_e^2 < I_e > 1$$
 or equivalently,

• Log R<sub>e</sub> = Log [(c/2
$$\pi$$
) (M/L)<sup>-1</sup>] + 2 Log  $\sigma_e$  - Log < I<sub>e</sub> > or

• Log R<sub>e</sub> = Log [(c/2
$$\pi$$
) (M/L)<sup>-1</sup>] + 2 Log  $\sigma_e$  + 0.4 <  $\mu_e$  > (since <  $\mu_e$  > = -2.5 Log < I<sub>e</sub> > )

So, if c and M/L are constants, then we expect

• Log R<sub>e</sub> = 
$$2 \text{ Log } \sigma_{\text{e}} + 0.4 < \mu_{\text{e}} > + \text{ Log } [(c/2\pi) (M/L)^{-1}]$$

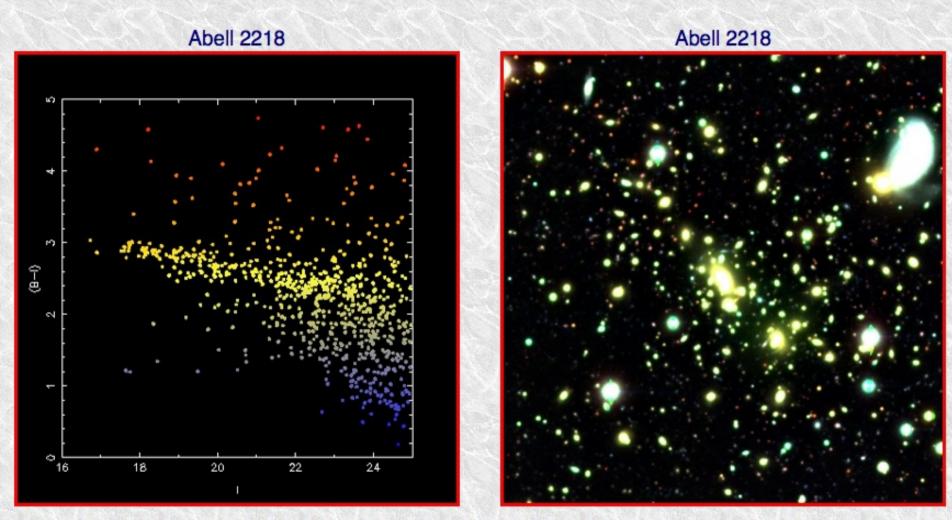
Which is close to, but not quite, the F-P relation:

• Log R<sub>e</sub> = 1.4 Log 
$$\sigma_e$$
 + 0.36 <  $\mu_e$  > + const

To bring these into agreement, we require:

• 
$$(2\pi/c)$$
  $(M/L) \propto M^{1/5} \propto L^{1/4}$ 

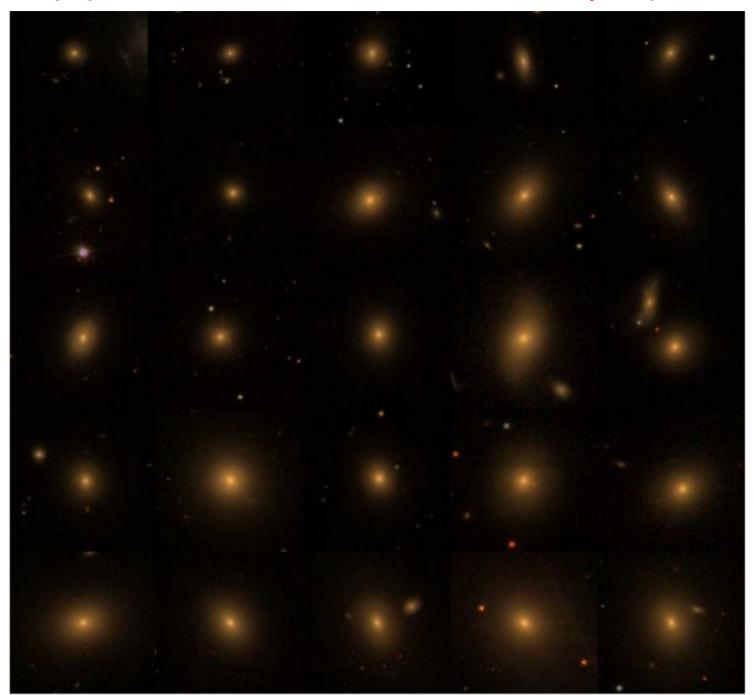
## **Color-Magnitude Relation**



Colors and magnitude for galaxies in the field of Abell 2218. Many fain background galaxies are included, but the primary early-type color-magnitude strip is clearly visible.

## Stellar populations as a function of stellar velocity dispersion

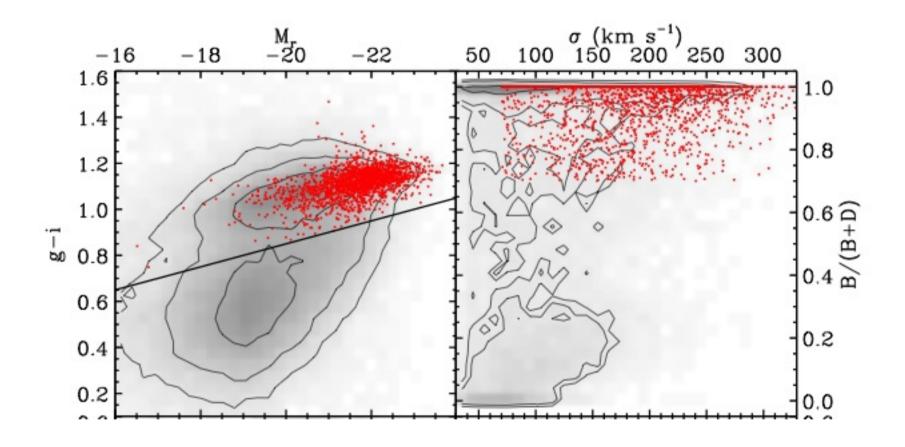
70 km/s

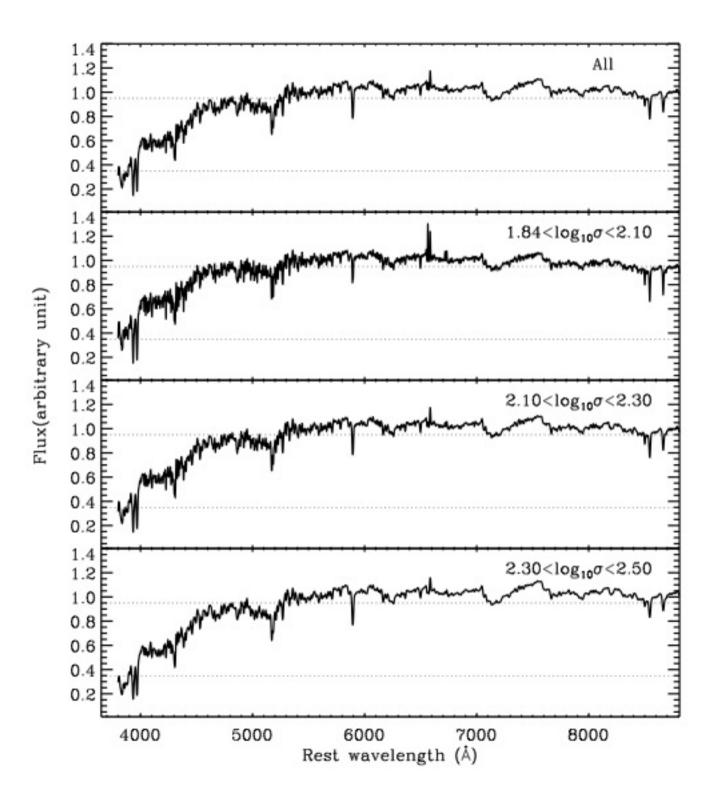


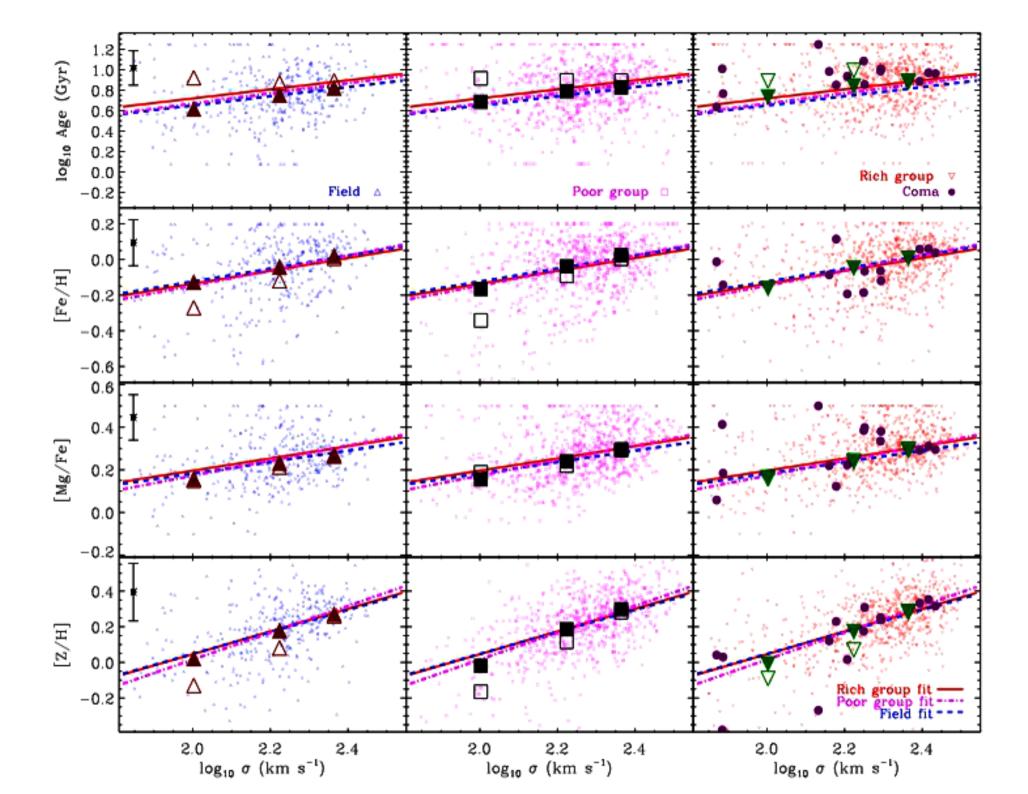
325 km/s

Fig. 1.— Randomly selected examples in the final Elliptical sample. We show the images, combined from images in gri bands, of 25 galaxies in ascending order of velocity dispersion (σ) from 70 km s<sup>-1</sup> to 325 km s<sup>-1</sup>, from top to bottom and from left to right.

# Ellipticals compared to the full population in the Sloan Digital Sky Survey







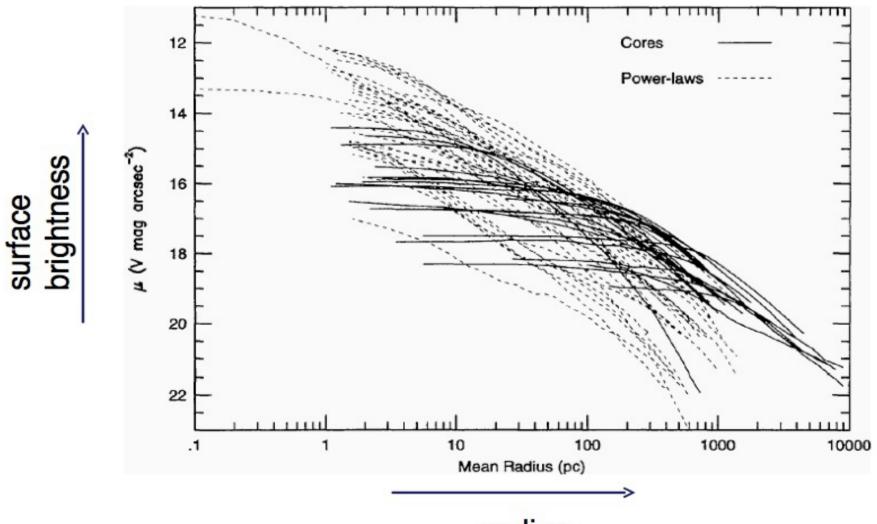
Profile of elliptical galaxies can deviate from the R<sup>1/4</sup> law at both small and large radius.

#### Close to the center:

- Some galaxies have cores region where the surface brightness flattens and is ~ constant
- Other galaxies have cusps surface brightness rises steeply as a power-law right to the center

- The most luminous ellipticals have cores (typically a slope in the surface brightness distribution ~R<sup>-0.3</sup> or flatter)
- Low luminosity ellipticals have power law cusps extending inward as far as can be seen
- At intermediate luminosities, mixture of cores and cusps

#### Results from HST



radius



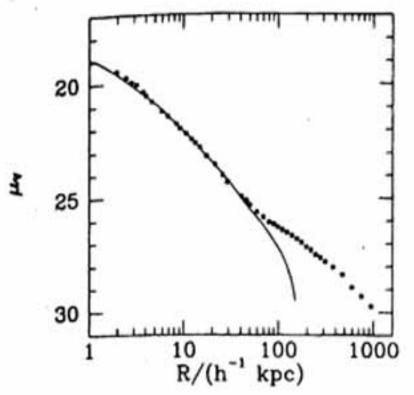
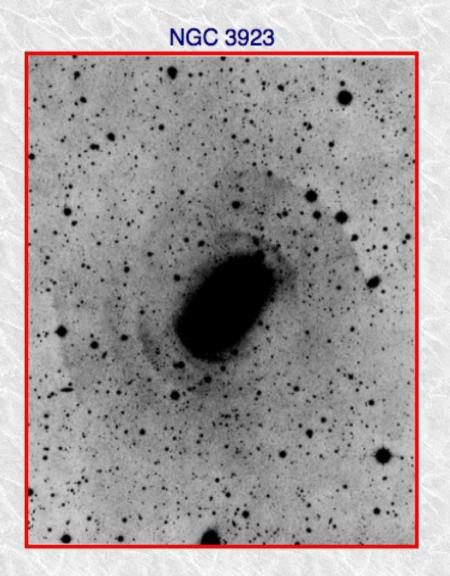
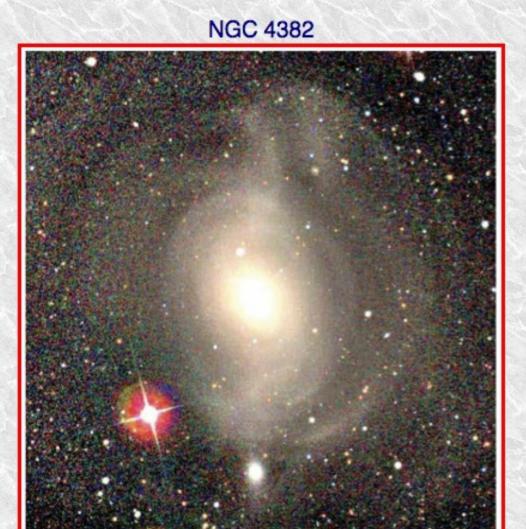
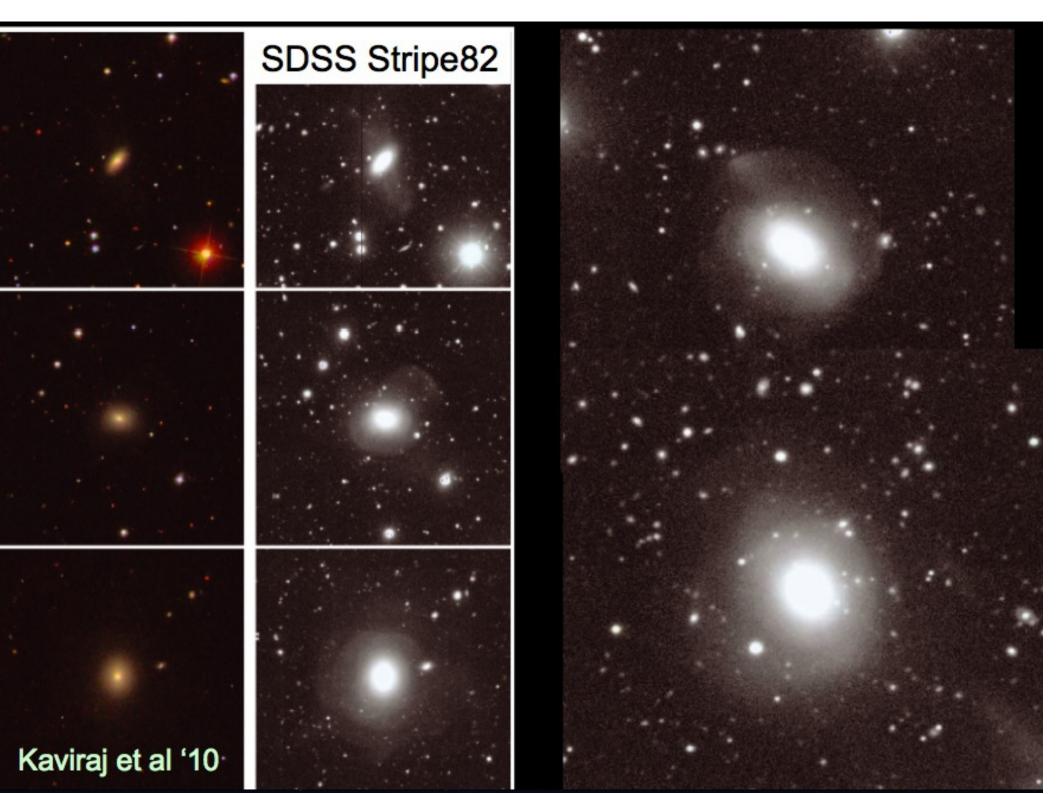


Figure 4.28 The surface-brightness profile of the cD galaxy that lies at the center of the cluster Abell 1413 (points). The line shows the R<sup>1/4</sup>-law that best fits the inner points. [From data kindly provided by J. Schombert based on the work of Oemler (1976).]

# **Ellipticals with Shells**







# Combine many galaxy images to probe low surface brightness light in outer galaxy

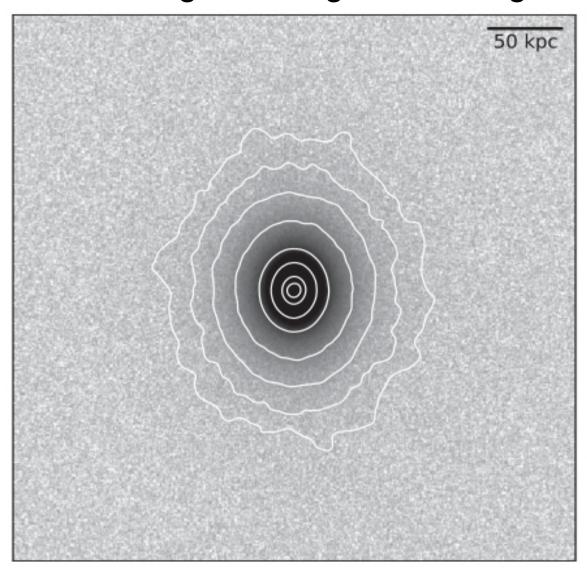
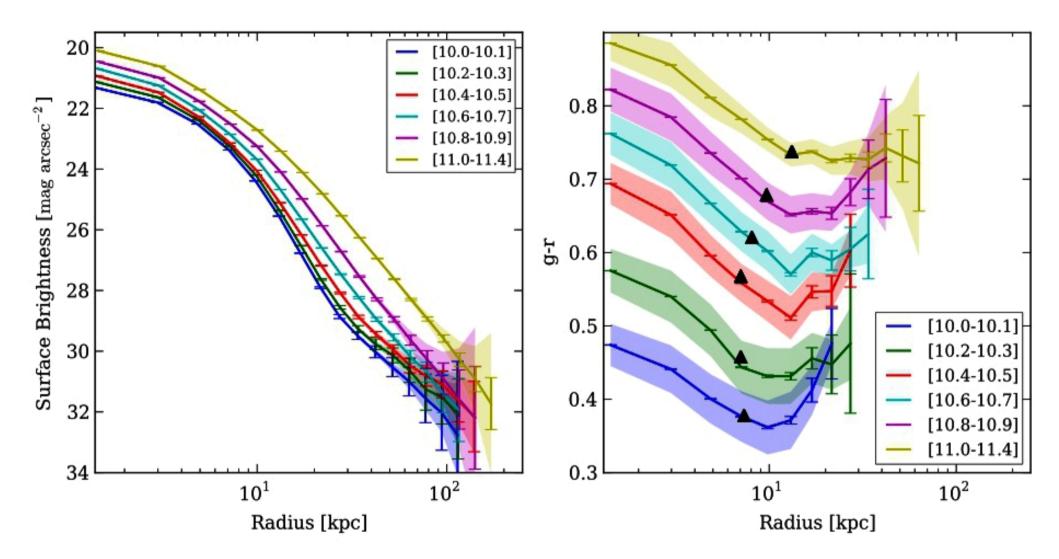


Figure 5. The stacked image consisting of 4040 images in the mass range  $10^{11.0} \,\mathrm{M}_{\bigodot} < M_* < 10^{11.4} \,\mathrm{M}_{\bigodot}$  and C > 2.6. Elliptical contours are drawn at 5, 10, 20, 30, 50, 70, 90 and 110 kpc.



# **GALAXY MERGERS AND INTERACTIONS**

#### GALACTIC BRIDGES AND TAILS

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#### ABSTRACT

This paper argues that the bridges and tails seen in some multiple galaxies are just tidal relics of close encounters. These consequences of the brief but violent tidal forces are here studied in a deliberately simple-minded fashion: Each encounter is considered to involve only two galaxies and to be roughly parabolic; each galaxy is idealized as just a disk of noninteracting test particles which initially orbit a central mass point.

As shown here, the two-sided distortions provoked by gravity alone in such circumstances can indeed evolve kinematically into some remarkably narrow and elongated features: (i) After a relatively direct passage of a *small* companion, the outer portions of the primary disk often deform both into a near-side spiral arm or "bridge" extending toward this satellite, and into a far-side "counterarm." (ii) A similar encounter with an *equal* or more massive partner results typically in a long and curving "tail" of escaping debris from the far side of the victim disk, and in an avalanche of near-side particles, most of which are captured by the satellite.

Besides extensive pictorial surveys of such tidal damage, this paper offers reconstructions of the orbits and *outer* shapes of four specific interacting pairs: Arp 295, M51 + NGC 5195, NGC 4676, and NGC 4038/9. Those models can be found in the fairly self-explanatory figures 19, 21, 22, and 23.

Our present demonstrations will actually share the foremost of those flaws with Pfleiderer and Siedentopf: Like their examples, ours will be based exclusively on restricted three-body computations performed with massless particles which we pretend constitute the outer disks of pairwise interacting galaxies. By supposing these elements of either disk to move simply under inverse-square forces from the two mass points representing the bulk of each galaxy, we too will ignore all explicit self-gravity of the disk material (except in certain final estimates). Obviously this is an important sin of omission, and it is one which ought soon to be remedied, perhaps via some proper N-body calculations.

# Retrograde encounters produce only small perturbations

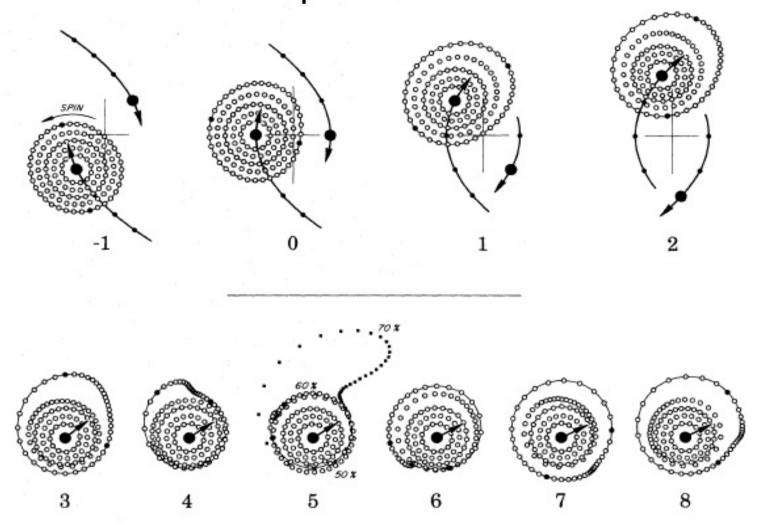
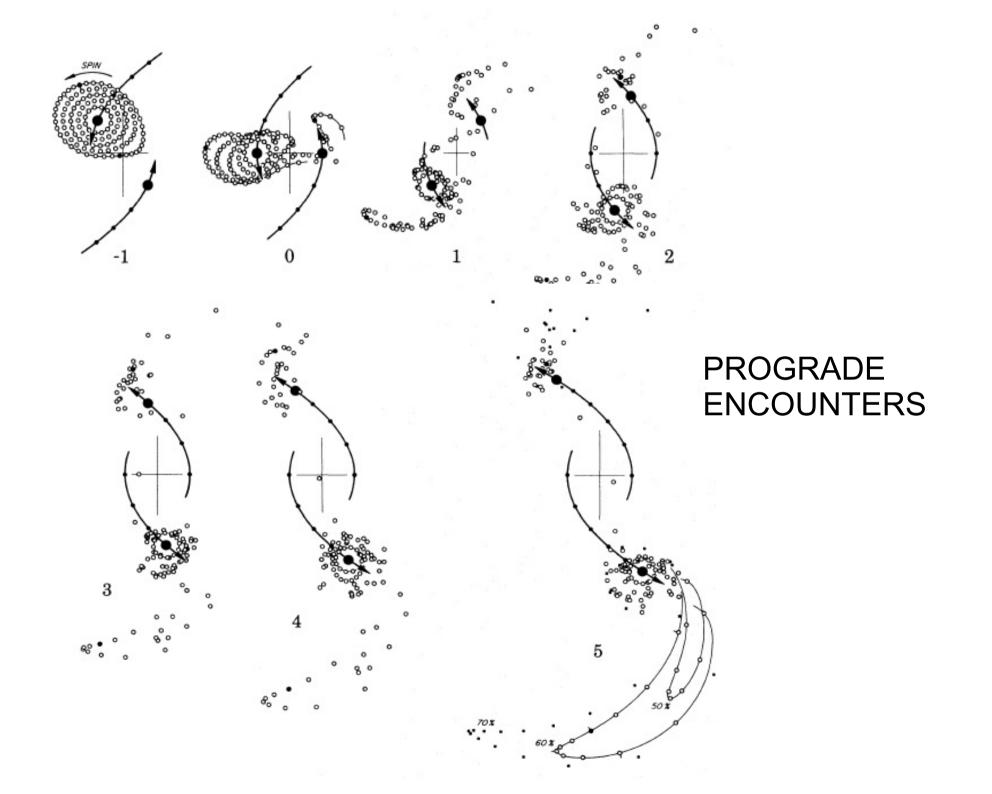


Fig. 1.—A flat retrograde ( $i = 180^{\circ}$ ) parabolic passage of a companion of equal mass. The two small filled circles denote test particles from the  $0.6R_{\min}$  ring which, in the absence of the encounter, would have reached positions exactly to the right and left of the victim mass at t = 0. The filled squares at t = 5 depict additional test particles from  $0.7R_{\min}$ . (Note the partial interpenetrations of the outermost rings at t = 4, 5, and 6, and their continuing oscillations thereafter.)



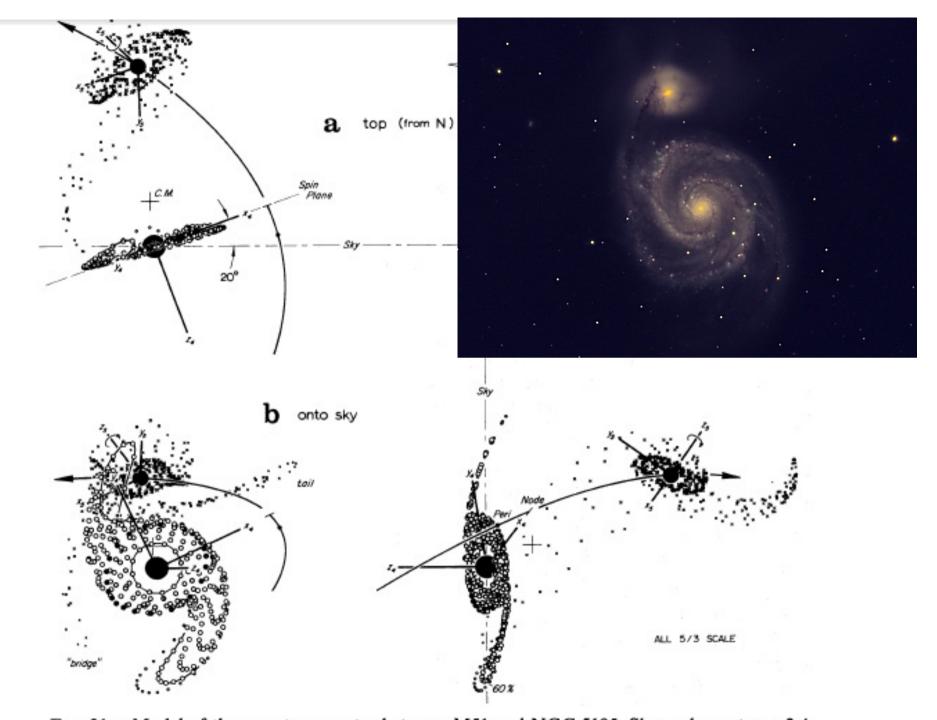


Fig. 21.—Model of the recent encounter between M51 and NGC 5195. Shown here at t=2.4 are three mutually orthogonal views of the consequences of a highly elliptic e=0.8 passage of a supposedly disklike "5195." This satellite was chosen to be one-third as massive, and of exactly 0.7 times the linear dimensions, of the "5194" primary—which itself contains particles from initial

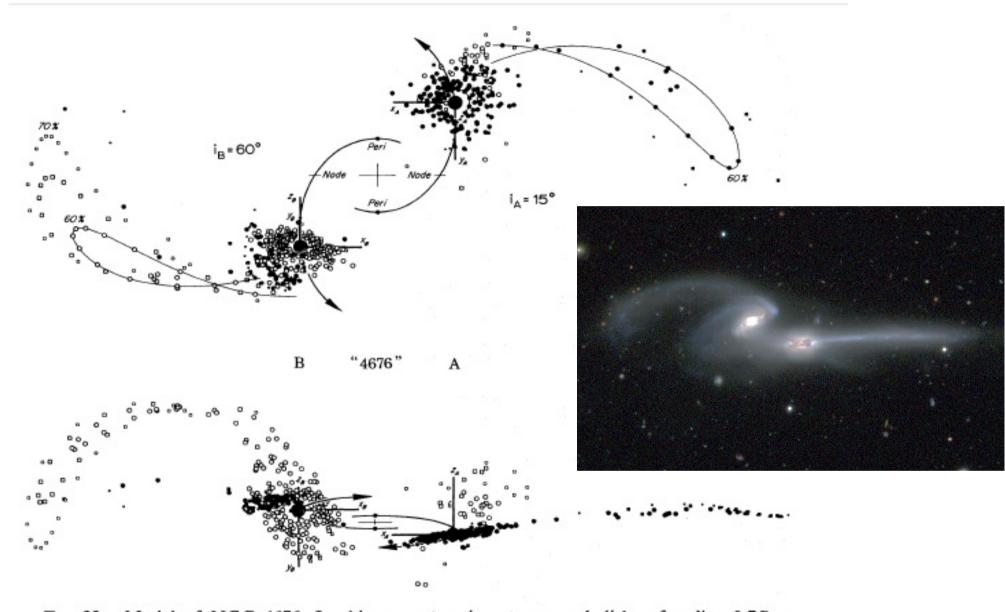


Fig. 22.—Model of NGC 4676. In this reconstruction, two equal disks of radius  $0.7R_{\rm min}$  experienced an e=0.6 elliptic encounter, having begun flat and circular at the time t=-16.4 of the last apocenter. As viewed from either disk, the adopted node-to-peri angles  $\omega_A=\omega_B=-90^\circ$  were identical, but the inclinations differed considerably:  $i_A=15^\circ$ ,  $i_B=60^\circ$ . The resulting composite object at t=6.086 (cf. fig. 18) is shown projected onto the orbit plane in the upper diagram. It is viewed nearly edge-on to the same—from  $\lambda_A=180^\circ$ ,  $\beta_A=85^\circ$  or  $\lambda_B=0^\circ$ ,  $\beta_B=160^\circ$ —in the lower diagram meant to simulate our actual view of that pair of galaxies. The filled and open symbols distinguish particles originally from disks A and B, respectively.

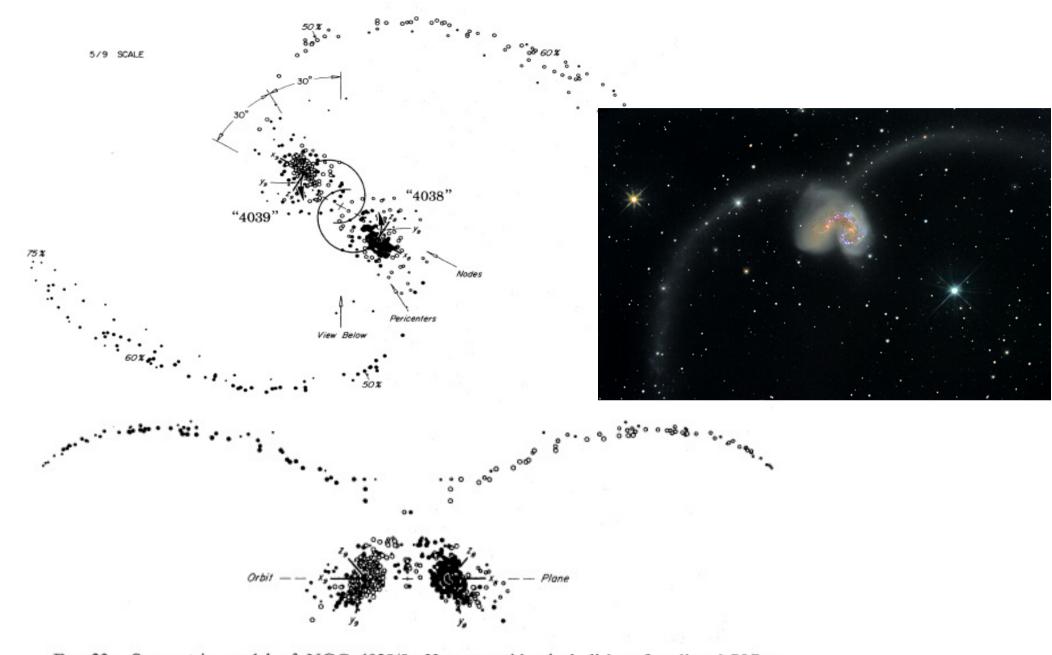


Fig. 23.—Symmetric model of NGC 4038/9. Here two identical disks of radius  $0.75R_{\rm min}$  suffered an  $e\approx 0.5$  encounter with orbit angles  $i_8=i_9=60^\circ$  and  $\omega_8=\omega_9=-30^\circ$  that appeared the same to both. The above all-inclusive views of the debris and remnants of these disks have been drawn exactly normal and edge-on to the orbit plane; the latter viewing direction is itself 30° from the line connecting the two pericenters. The viewing time is t=15, or slightly past apocenter. The filled and open symbols again disclose the original loyalties of the various test particles.

#### c) Stoking the Furnace?

We have deliberately not touched earlier on the well-known tendency (e.g., Burbidge et al. 1963; Zwicky 1967; Arp 1969b, 1971b; Stockton 1972) of the various tails, plumes, and intergalactic bridges to involve at least one galaxy whose own color or spectrum is often unusual, or which has a high surface brightness, or which contains oddly placed absorbing material and/or emitting regions.

That such intrinsic evidence of "strangeness" has itself contributed to the reluctance to regard the external features as tidal is both clear and understandable. Nevertheless—well short of such really exotic cases as the "jets" of M87 and 3C 273—we cannot help feeling that even this share of reluctance has been somewhat excessive: Would not the violent mechanical agitation of a close tidal encounter—let alone an actual

merger—already tend to bring *deep* into a galaxy a fairly *sudden* supply of fresh fuel in the form of interstellar material, either from its own outlying disk or by accretion from its partner? And in a previously gas-poor system or nucleus, would not the relatively mundane process of prolific star formation thereupon mimic much of the "activity" that is observed?

#### TRANSFORMATIONS OF GALAXIES. II. GASDYNAMICS IN MERGING DISK GALAXIES

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#### ABSTRACT

In mergers of disk galaxies, gas plays a role quite out of proportion to its relatively modest contribution to the total mass. To study this behavior, we have included gasdynamics in self-consistent simulations of collisions between equal-mass disk galaxies. The large-scale dynamics of bridge- and tail-making, orbit decay, and merging are not much altered by the inclusion of a gaseous component. However, tidal forces during encounters cause otherwise stable disks to develop bars, and the gas in such barred disks, subjected to strong gravitational torques, flows toward the central regions where it may fuel the kiloparsec-scale starbursts seen in some interacting disk systems. Similar torques on the gas during the final stages of a collision yield massive gas concentrations in the cores of merger remnants, which may be plausibly identified with the molecular complexes seen in objects such as NGC 520 and Arp 220. This result appears insensitive to the detailed microphysics of the gas, provided that radiative cooling is permitted. The inflowing gas can dramatically alter the *stellar* morphology of a merger remnant, apparently by deepening the potential well and thereby changing the boundaries between the major orbital families.

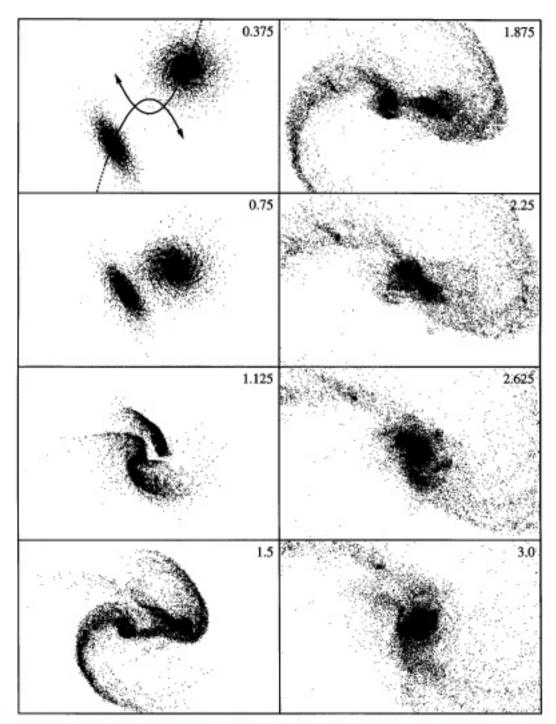
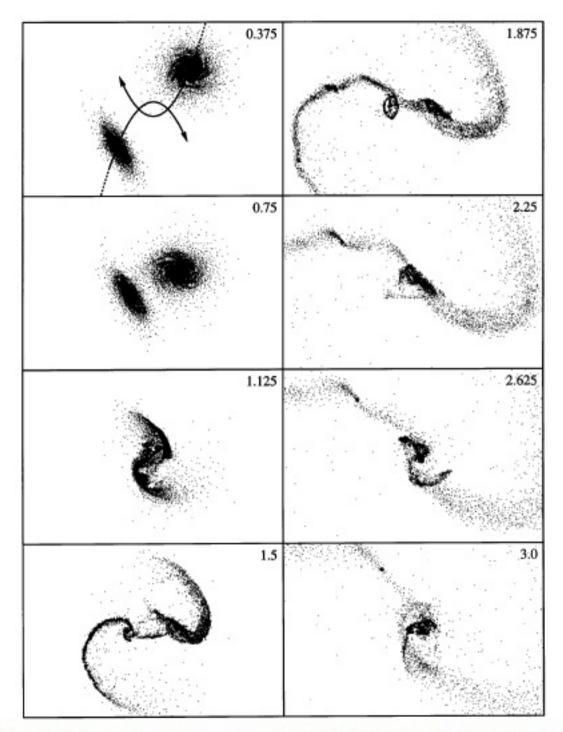


Fig. 4.—Evolution of the stellar distribution in encounter A, projected onto the orbital plane. The scale is the same as in Fig. 3.



Fxc. 3.—Evolution of the gas distribution in encounter A, projected onto the orbital plane. These frames are 3.6 × 2.4 length units; elapsed time is shown t the upper right of each. The first frame also shows the projected parabolic orbits of the infalling galaxies.

# Remnants of simulations of the merger of two equal mass galaxies

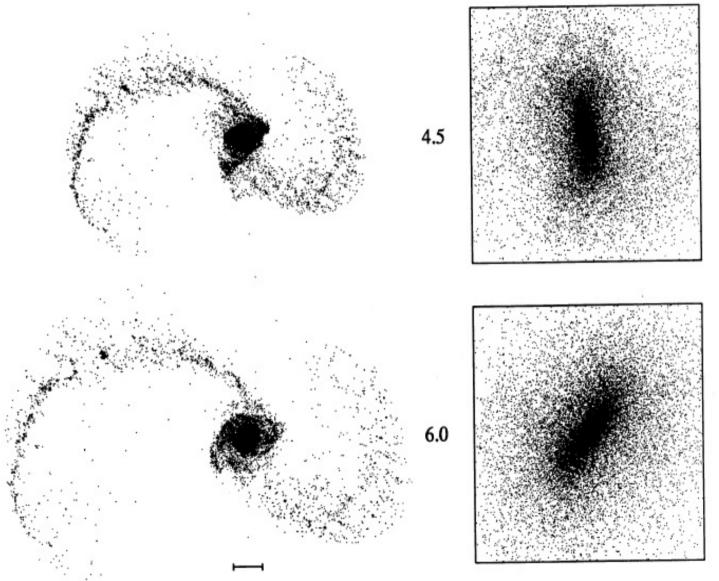


Fig. 11.—Large-scale (left) and small-scale (right) structure of the merger remnant in encounter A, projected onto the orbital plane, at times 3, 4.5, and 6. The boxes, enlarged by a factor of 10 from their unframed counterparts, are 0.8 × 0.8 length units. Again, only 50% of the bulge particles are plotted.

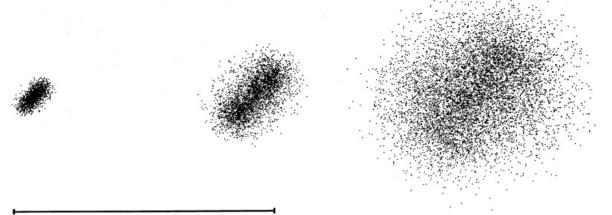
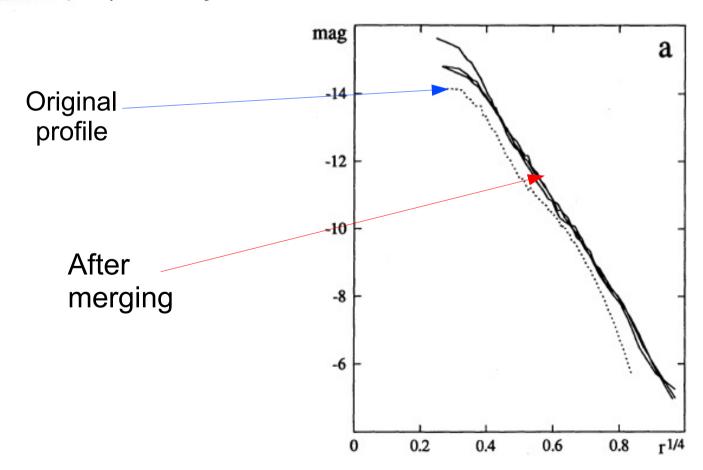


Fig. 15.—Luminous particles from the remnant produced by encounter A at time t = 6, binned by their specific binding energy. On the left is the 0%–25% bin, thinned by a factor of 2 to reduce crowding. In the middle is the 25%–50% bin, thinned by a factor of 2. On the right is the 50%



# Major mergers with gas

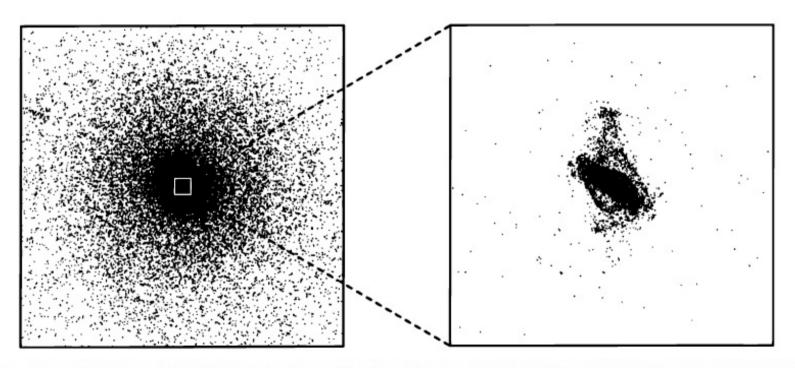
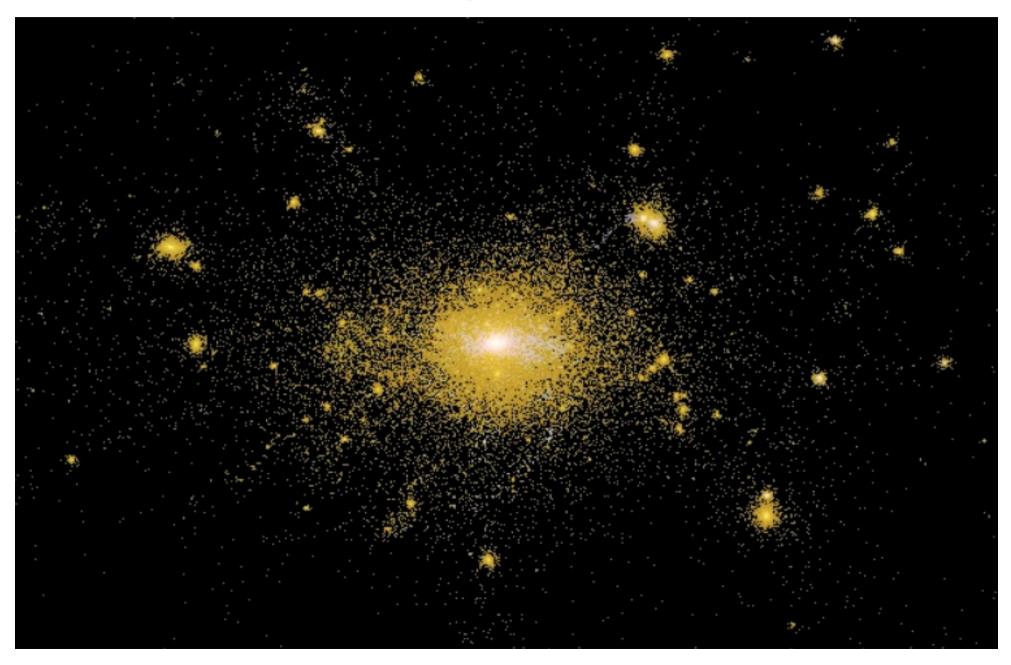


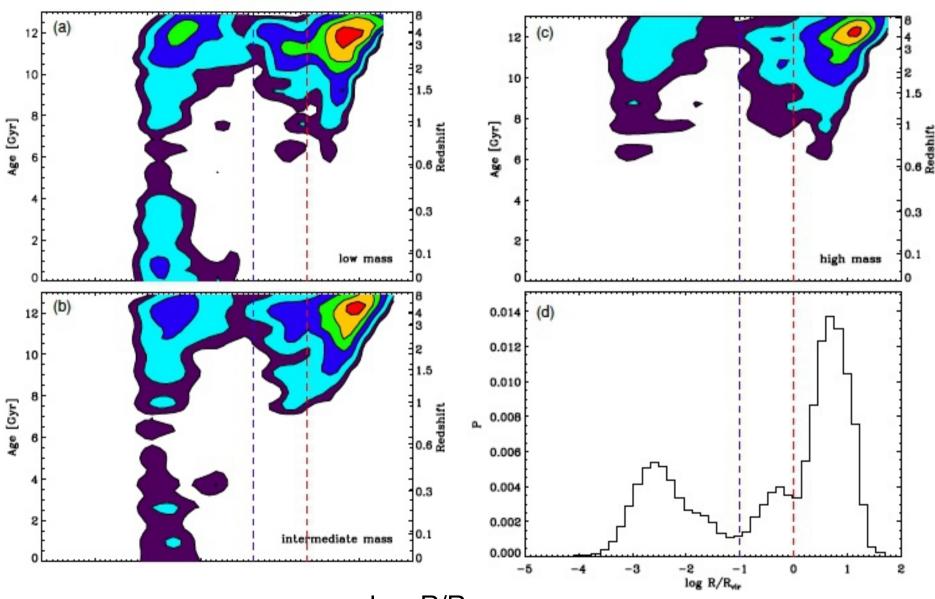
Fig. 14.—Views of stars (left) and gas (right) in the merger remnant produced by encounter A at time t = 6. The stellar view is  $0.8 \times 0.8$  length units, while the view of the gas is enlarged by a factor of 20. Over 60% of all the gas in this remnant lies in this dense central blob.

# Formation of elliptical galaxies in a cosmological context

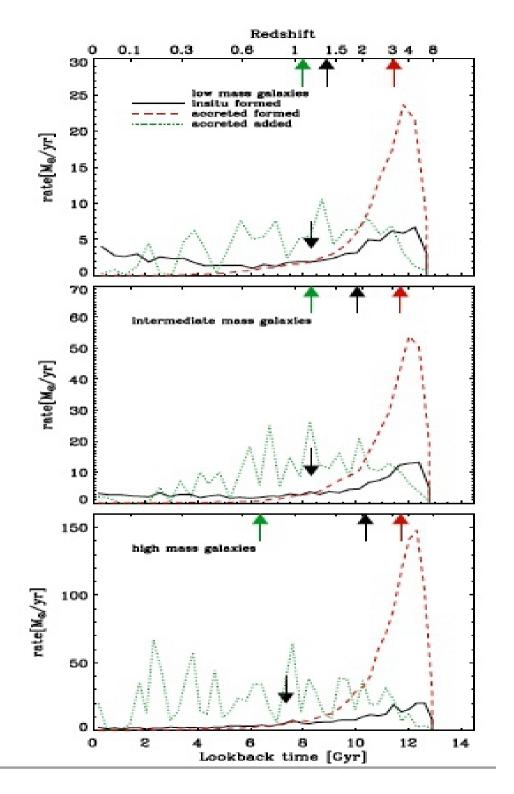


## Two-phase model

Location where stars form as a function of age



log R/R<sub>vir</sub>

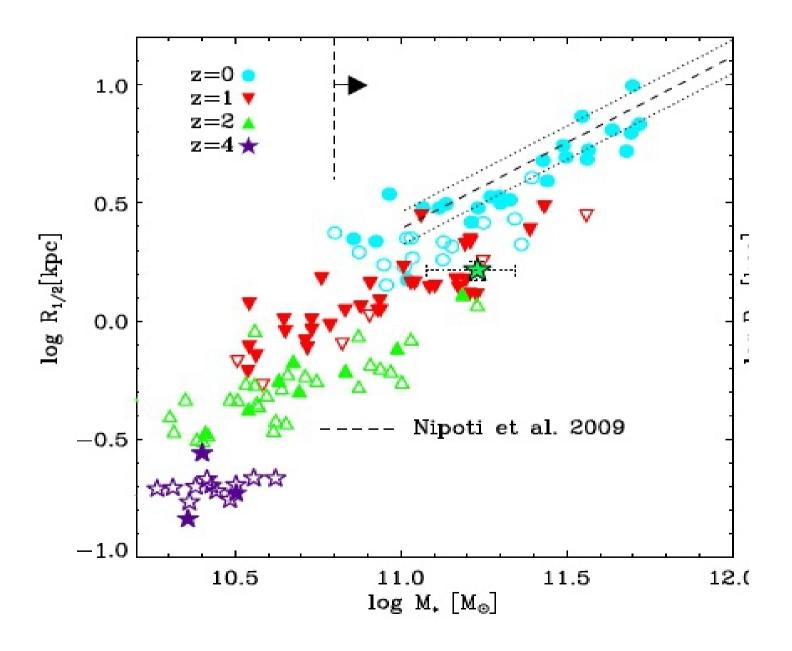


"In situ formed": stars formed from cooling gas in central galaxy

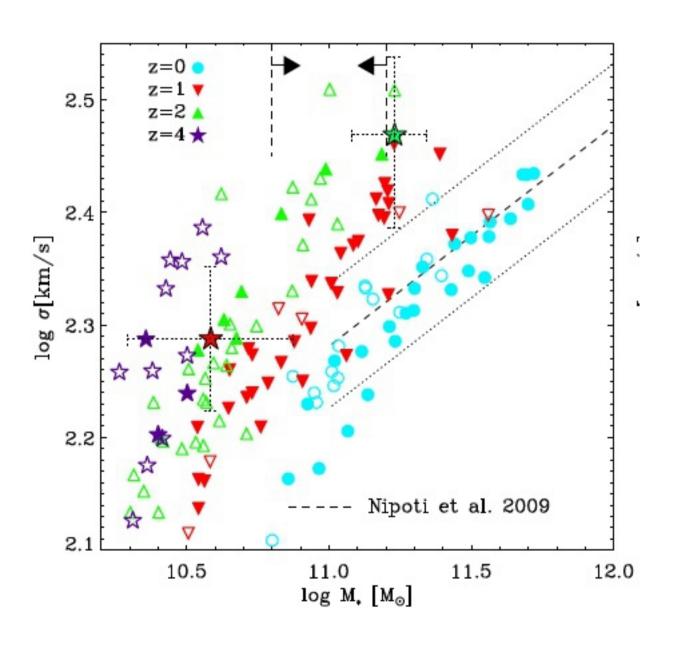
"In situ accreted formed": star formed from gas accreted by central galaxy in merging satellites.

"Accreted added": stars added by merging satellites

# Size-mass relation at different redshifts



## Velocity dispersion-mass relation



## A CLOSER LOOK AT THE ACCRETED COMPONENTS

