NUMERICAL SIMULATIONS OF THE POSSIBLE ORIGIN OF THE TWO SUB-PARSEC SCALE AND COUNTER-ROTATING STELLAR DISKS AROUND SGRA*

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ABSTRACT

We present a high resolution simulation of an idealized model to explain the origin of the two young, counter-rotating, sub-parsec scale stellar disks around the supermassive black hole SgrA* at the Center of the Milky Way. In our model, the collision of a single molecular cloud with a circum-nuclear gas disk (similar to the one observed presently) leads to multiple streams of gas flowing towards the black hole and creating accretion disks with angular momentum depending on the ratio of cloud and circum-nuclear disk material. The infalling gas creates two inclined, counter-rotating sub-parsec scale accretion disks around the supermassive black hole with the first disk forming roughly 1 Myr earlier, allowing it to fragment into stars and get dispersed before the second, counter-rotating disk forms. Fragmentation of the second disk would lead to the two inclined, counter-rotating stellar disks which are observed at the Galactic Center. A similar event might be happening again right now at the Milky Way Galactic Center. Our model predicts that the collision event generates spiral-like filaments of gas, feeding the Galactic Center prior to disk formation with a geometry and inflow pattern that is in agreement with the structure of the so called mini-spiral that has been detected in the Galactic Center.

Keywords: Galaxy: center – methods: numerical – ISM: clouds – disk formation

1. INTRODUCTION

Recently the Milky Way Galactic Center (GC) region has again sparked a lot of interest. A number of remarkable discoveries were made, including the detection of two large gamma-ray bubbles (Su et al. 2010). The bubbles are perpendicular to the galactic plane, extending 50° above and below the GC and could be linked to the GC star formation event described in this paper, as pointed out by Zubovas et al. (2011). The model we describe in this work leads to the infall of multiple times $10^4 M_{\odot}$ onto the black hole within a short time. This could be the origin of the accretion event that created the gamma-ray bubbles. The age of the stars observed at the GC which, according to our model formed as a result of this accretion event, tells us that this event happened more than 6 ± 2 Myr ago (taking into account that it takes a while for the stars to form) which coincides roughly with the age of the lobes of 10 Myr.

A new feature has also been detected in the GC region which previously was only identified partially and thought of as separate components: the 100 pc elliptical and twisted ring of cold and dense molecular clouds (Molinari et al. 2011). This structure fits nicely into the 'stuff within stuff' scenario described by Hopkins & Quataert (2010) to explain the radial transport of material through the galactic disk. According to this scenario, gravitational instabilities generate a series of rings, bars and spirals within each others from galactic

scales down to the central few parsec region. On a smaller scale compared to the 100 pc ring we find the circum-nuclear disk (CND) which is again a ring of gas (Becklin et al. 1982) extending roughly from 1.5 pc to around 7 pc.

Inside the central evacuated region of the CND the so-called mini-spiral can be found (Ekers et al. 1983; Lo & Claussen 1983), a spiral-like structure of hot gas with a total mass of around 10^2 to 10^3 M_{\odot} on its way towards the black hole. At even smaller distances we find two inclined and counter-rotating disks of young stars, extending from 0.05 pc to around 0.5 pc (Lu et al. 2009; Genzel et al. 2003; Ghez et al. 2005; Paumard et al. 2006; Bartko et al. 2009) which are the main focus of the work presented here.

All the central gas is embedded into a nuclear star cluster of about 10^7 M_{\odot}. The cluster follows a density profile that has a core of roughly 0.5 pc size (the stellar disks) and decreases in density up to around 30 pc (Genzel et al. 2003).

Finally, very recently a small gas and dust cloud has been found, called G2. The cloud will reach its pericenter distance of only 9×10^{-4} pc on its orbit around the black hole as soon as in mid 2013 (Gillessen et al. 2012, 2013). This will provide the unique opportunity for numerical simulations to make predictions of the future evolution of G2 and its interaction with the environment that will be tested directly by observations within the next years. One prediction that was already made is that the cloud might originate from the inner edge of one of the two stellar disks (Burkert et al. 2012; Schartmann et al. 2012; Murray-Clay & Loeb 2012).

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In this work we will focus on the formation of the two stellar disks, which are an important ingredient in understanding the GC region. In Alig et al. (2011) (denoted as AL1 from here on) we tested a model that was suggested by Wardle & Yusef-Zadeh (2008) to explain the formation of the progenitor accretion disk (which then should fragment into a stellar disk) by a cloud which crosses over the black hole in parts during infall. This way parts of the cloud pass the black hole in the clockwise direction, while the other parts move around the black hole counter-clockwise, leading to efficient redistribution of angular momentum at the focal point of collision, downstream. This model is able to explain the formation of a compact accretion disk. In AL1 we used parameters for the initial cloud that are common in the GC region (Miyazaki & Tsuboi 2000: Güsten & Philipp 2004), which leads to a disk that is somewhat larger than the one observed in the GC.

The IMF of the disk-stars is quite unique, Bartko et al. (2010) argue that it is extremely top-heavy whereas Lu et al. (2013) more recently find that it is not as extreme as suggested by Bartko et al. (2010) but still top-heavy compared to a standard Salpeter-slope. This provides a hint to the origin of the stellar disks from an eccentric hot accretion disk. A hot accretion disk would imply a larger Jeans length and thus a small number of high mass clumps compared to a large number of small clumps for a cold disk. The mean eccentricity of the disk stars is measured to be around 0.34 \pm 0.06 (Bartko et al. 2009). It has already been shown that in an eccentric accretion disk, the formation of low mass clumps can be suppressed due to tidal disruption during pericenter passage (Alexander et al. 2008). In addition an eccentric disk will be heated quite efficiently during pericenter passage of the gas. These mechanisms as well as the feedback from the already formed stars which could again disrupt low mass clumps, will lead to a strong suppression of the low mass end of the IMF and could explain the observed top-heavy IMF.

The papers of Bonnell & Rice (2008) and very recently Mapelli et al. (2012) also explain the formation of a progenitor accretion disk by infall of a cloud with very low angular momentum into the GC. They studied the subsequent fragmentation and star formation inside the accretion disk and found that clouds with masses of the order 10^5 M_{\odot} can lead to a top-heavy clump mass function.

The one disadvantage of those models is that they can only explain the formation of a single disk. Since the stars in both disks are almost equal in age (6 ± 2 Myr, Paumard et al. (2006)) they must have formed almost at the same time. The two stellar disks are sharing the same region, which is not possible for two gaseous counter-rotating accretion disks. They therefore must have formed at least shortly one after another. The basic idea here is that the first accretion disk has enough time to fragment, before the formation of the second accretion disk. The fragments and stars are then frozen into their orbits and can share the volume of the second accretion disk, which later on also fragments thus forming the second stellar disk. The infall of a cloud with a mass larger than 10^4 M_{\odot} with a sub-parsec impact parameter is already very unlikely. For the two disk scenario a second cloud has to fall into the central region very shortly after the first cloud, with a similar small impact parameter but inclined with respect to the first clouds orbital plane and with opposite angular momentum.

In the model of Hobbs & Nayakshin (2009) this problem is addressed by assuming the collision of two clouds further away from the black hole. This way two streams of gas can make their way into the central region, leading to the formation of an inner compact accretion disk surrounded by a ring of gas. The paper of Lucas et al. (2013) tries to explain the formation of two disks by the infall of a turbulent cloud.

In this paper we present a new model in which a single event, the interaction of a cloud with a gaseous disk around the central black hole, naturally leads to the subsequent formation of multiple inclined and counter rotating accretion disks around the central black hole. We present a high resolution simulation which uses initial parameters taken from a low resolution parameter study to reproduce the observed stellar disk parameters as good as possible. This model is inspired by observational evidence which shows that a similar event to what presumably happened more than 6 Myr ago might be happening again right now in the GC. The paper of Montero-Castaño et al. (2009) shows evidence for the so called GC 20 $\frac{\mathrm{km}}{\mathrm{c}}$ cloud crashing into the CND, leading to the inflow of gas into the central parsec region. This event has already been discussed before and was presented first in the paper of Jackson et al. (1993). The gaseous disk in our model has similar parameters compared to the currently observed CND.

The extreme parameters of the two disks are quite challenging to reproduce. First they are almost equal in size, largely inclined and counter-rotating. Second the total mass in stars is quite high with $10^4 M_{\odot}$ for the clockwise rotating disk and $0.5 \times 10^4 M_{\odot}$ for the counter-clockwise disk (Genzel et al. 2010).

In section 2 we present our formation model in detail, as well as a description of the algorithms we are using for our simulation and the parts we added to the standard version of the code. We also summarize the initial parameters for the simulations. The simulations are shown in section 3. Finally in section 4 we discuss the results and give a summary of our work.

2. MODEL AND NUMERICAL METHOD

First we describe the basic physical ingredients of our model in section 2.1. In section 2.2 we present the hydrodynamics code we employed for running our simulations and the numerical parameters used for the simulations. The parameters used to model the Galactic Center environment are summarized in section 2.2.

2.1. Model

Inspired by observations of Montero-Castaño et al. (2009) we simulate the collision of a cloud with a

gaseous disk (GD) around the central black hole. The angular momentum direction of the cloud is chosen to be opposite to the GD angular momentum. A similar model has been tested by Vollmer & Duschl (2001, 2002) in their work of prograde and retrograde encounters of clouds with the observed CND to investigate the mass infall into the central region, but they do not relate this process to the formation of the two stellar disks.

Since the simulated GD is destroyed in the process, the parameters do not necessarily have to be the same as the currently observed CND. However, the general idea for the creation of the CND is that a number of clouds with similar angular momentum are captured within the central region forming a gaseous ring within the galactic plane. Hydrodynamical simulations of this model have been carried out by Coker et al. (2003). This simple process could also have happened before, thus we assume the parameters of our GD to be similar to the CND currently observed. Even if this is not true, it makes sense that a progenitor disk co-rotates with and lies within the galactic plane, since the overall source for the gas is the galactic disk.

In our first low resolution parameter study we have chosen a number of different inclinations between the GD orbital plane and the cloud orbital plane. These studies have shown that the best choice, if we want to create a small compact accretion disk, is always to choose those planes to be equal. This choice also makes sense given the fact that the CND (and thus also our GD) is aligned with the galactic plane (Paumard et al. 2006) and that the GC clouds are mostly confined to the galactic plane (Miyazaki & Tsuboi 2000). Thus the probability for a cloud to approach the CND/GD within the same orbital plane is high.

As long as clouds with the same angular momentum direction as the galactic disk and thus also the GD fall in, the GD will grow in mass. Once in a while (a crude estimate from the two data points we have would be roughly every 10 Myr) a cloud with opposite angular momentum direction enters the region. This leads to the destruction of the GD, resulting in the formation of spiral-like accretion filaments that feed the Galactic Center and subsequently form a single or multiple stellar disk(s).

There is a high degree of freedom in the choice of our initial parameters. The basic simplifications we assume are as follows. The cloud is always assumed to be spherical and homogeneous. The GD is also assumed to be homogeneous with an inner cavity. Observations show that the observed CND is a rather clumpy structure with a volume filling factor of a few percent (Launhardt et al. 2002). However, it turns out to be hard to model the clumpy structure of the CND without any additional stabilizing mechanism besides self-gravity. The clumps are quickly tidally torn apart, reverting the disk into a homogeneous state. Since we do not want to deal with the question of clump stability, we use a homogeneous disk as a first approximation. This point will be discussed further in section 3.4 and 4. Another simplification is the assumption that the cloud and the GD always have the same mass. This is a strong restriction and could very well be different but in order to reduce the degree of freedom we need a starting point. In a subsequent paper we plan to study the effect of different masses and non-homogeneous density distributions. Our current simulations do not include any feedback from the black hole or stellar feedback. Again we discuss possible implications of this simplification in section 4.

In our second low resolution parameter study we always started with the GD aligned with the xy-plane, rotating counter-clockwise. For the infalling clockwise rotating cloud, we vary the radius, mass, impact parameter and offset in z-direction. As already explained we now assume no inclination between the cloud's orbital plane and the GD orbital plane. For the GD we vary the outer and inner radius and always set the mass equal to the cloud mass. We present the numerical values of the final set of parameters used for the high resolution simulation in section 2.3.

2.2. Numerical Setup

We carry out our hydrodynamical simulations using the N-Body Smoothed Particle Hydrodynamics (SPH) Code Gadget3 (Springel et al. 2001; Springel 2005), which makes use of the entropy-conserving formulation of SPH. Gadget3 improves the parallel performance of the previous version by adding a new domain decomposition scheme, which balances work and memory-load at the same time by a more fine grained distribution of the particles among the CPUs, requiring slightly more communication between tasks. For our setup, where the time-steps of particles in the vicinity of the black hole are much smaller than in the outer parts, this already significantly improves the efficiency of the code compared to previous versions. Additionally, we are using some modifications of the code as described in the following paragraphs.

The extremely high velocity in the vicinity of the black hole puts great stress on the domain decomposition. After only a few iterations, particle properties need to be communicated to other domains, which could reside on non-local CPUs. This strongly increased need for communication slows down the overall performance. Usage of the new hybrid OpenMP-MPI implementation in Gadget3 helps to overcome this problem. Here we reduce the number of MPI tasks to the number of physical CPUs on each node and for every MPI task we spawn additional OpenMP tasks corresponding to the number of cores on each of the CPUs. With this approach a larger number of particles can be processed locally without the need of MPI communication. Tests have shown that with our simulation setup we can expect a factor of 3-4 in performance over the standard MPI only approach.

Our low resolution parameter studies have shown that after crashing into the GD, the cloud is compressed into a flat pancake like shape. This leads to strong fragmentation right from the beginning of the simulation. In order to prevent the time step from becoming too small due to the high density fragments we allow SPH particles to merge during the simulation. This is similar to using sink particles although we do not replace a large number of SPH particles by a single non-SPH particle, we only replace two SPH particles by a single SPH particle of higher mass. Since we only allow equal mass particles to merge and also only allow them to merge up to 3 times, the maximum mass of a high mass SPH particle can only be 8 times higher compared to the common SPH particle mass.

Merging is only allowed for particles which are exactly at the minimum hydro smoothing length (see the end of this section). All of these particles are in a totally collapsed region, artificially prevented from further collapse by the choice of the minimum hydro smoothing length. The minimum hydro smoothing length sets an upper limit on density which should always be higher than any normal region of interest inside the simulation. Only Jeans unstable fragments which are infinitely collapsing then reach the minimum hydro smoothing length.

With this prescription we reduce the number of particles within a fragment. To make sure that we still resolve the fragment with a certain number of SPH particles, we only allow merging to start if the number of possible candidates within the hydro smoothing length of a starting particle (a candidate being a particle at the minimum hydro smoothing length) is at least equal to the number of SPH neighbors which is 50 in our case.

Two particles are merged by using the center of mass position and velocity of the two particle system for creating the replacement particle. This way linear momentum is conserved but not angular momentum. However, due to the fact that only particles within a minimum hydro smoothing length are able to merge, the error is extremely small and tests have shown that this does not influence the results at all. The particle merging approach is a trade off between the sink particle formalism and a brute force calculation of the fragments. Tests have shown that we can expect a factor of 4 or better in simulation speed compared to a brute force calculation.

To account for the thermodynamics of disk formation, we use the same cooling formalism as in AL1, namely that of Stamatellos et al. (2007). It approximates cooling processes for optically thin, as well as optically thick regions by applying an approximative radiative transfer mechanism using the diffusion approximation. The method is suited for a wide range of temperatures (T = 10 - 10⁶ K), a wide range of densities ($\rho = 10^{-19}$ g/cm³ (and lower) - 10^{-2} g/cm³) and optical depths in the range of $0 < \tau < 10^{11}$ as shown in tests performed by Stamatellos et al. (2007).

In order to prevent small particle time steps in the vicinity of the black hole we define an accretion radius $r_{\rm acc}$ (given in section 2.3) within which all SPH particles are considered to be accreted by the black hole. Those particles are removed from the simulation and will no longer take part in the dynamical evolution. The fixed-position sink is not associated with a particle.

The number of SPH neighbors is set to $n_{\text{neigh}} = 50 \pm 5$ and the fixed gravitational softening length is set to $\epsilon = 10^{-3}$ pc. The hydro-smoothing length is adaptive, with the minimum allowed length set to be equal to the gravitational softening length to prevent suppression or amplification of artificial fragmentation according to Bate & Burkert (1997). Gadget3 treats gravitational forces as Newtonian up to 2.8 times the gravitational softening length.

We assume a cloud (and thus also GD) mass of 6 × $10^4 M_{\odot}$. The number of particles in the cloud is 10^6 , so that the mass of a single SPH particle is $m_{\rm SPH} = 0.06 M_{\odot}$. Since the GD contains the same number of particles as the cloud, the SPH particle masses are also the same. Our choice for the particle mass leads to a minimum resolvable mass (Bate & Burkert 1997) of $m_{\rm min} = n_{\rm neigh} \times m_{\rm SPH} = 3 M_{\odot}$.

2.3. Modeling the Galactic Center Environment

Like in our previous work (AL1) the black hole is included as a static point mass potential, located at the origin of a Cartesian coordinate system. However, to account for newer data from observations we increased the mass of the black hole to $4.4 \times 10^6 \,\mathrm{M_{\odot}}$ (Genzel et al. 2010) compared to $3.5 \times 10^6 \,\mathrm{M_{\odot}}$ in AL1. For the black hole accretion radius we chose a value of $r_{\rm acc} = 0.1 \,\mathrm{pc}$.

In addition to the black hole potential we also include the potential of the old cluster of stars at the GC. The density distribution is taken from observations by Genzel et al. (2003) and has the form

$$\rho_{\star}(R) = 1.2 \times 10^{6} \left(\frac{R}{0.4 pc}\right)^{-\alpha} [M_{\odot} pc^{-3}]$$

with $\alpha = 2.0$ for $R \ge 0.4$ pc and $\alpha = 1.4$ for R < 0.4 pc.

The initial cloud has constant density and a radius of $r_{cloud} = 2$ pc. For the mass given in section 2.2 (6 × 10⁴ M_☉) this corresponds to a density of around $10^{-19} \frac{g}{cm^3}$.

We assume an ideal gas with an adiabatic equation of state, with the cooling mechanism included as described in section 2.2. The initial cloud and GD temperature is 100 K. The global minimum allowed temperature is also set to 100 K to account for the background UV field from the old cluster of stars at the GC.

The cloud's center of mass is initially placed at an offset of $x_0 = -10$ pc on the x-axis and an offset of $y_0 = 5.2$ pc on the y-axis. There is no offset in z-direction, however due to the random particle distribution there is a slight (0.1 percent) abundance of mass above the xy-plane which effectively acts like a small z-offset. The cloud velocity is initially set to $v_{cloud} = 145 \frac{\text{km}}{\text{s}}$ in the x-direction, thus the cloud's orbit is clockwise around the black hole.

The GD is modeled as a flat disk with an inner edge of $r_{i,cnd} = 1.8$ pc and an outer edge of $r_{o,cnd} = 7.5$ pc. It is



Figure 1. The initial setup is shown in (a) together with the simulation parameters. In (b) the two resulting accretion disks are shown at the same time.

placed within the xy-plane and rotates counter-clockwise. Fig. 1 depicts the simulation parameters for the initial setup and the final state.

3. RESULTS

In this section we present the results from our high resolution simulation. First we describe the evolution of the infall of the cloud and the interaction with the GD in 3.1. The amount of mass concentrated around the black hole over time is shown in 3.2. In 3.3 we present the angular momentum distribution of the compact accretion disks and in 3.4 we investigate their Toomre parameter. Finally in 3.5 we shortly present results on the similarity between the inflow pattern of gas during the cloud-GD interaction and the observed mini-spiral.

3.1. Evolution of the cloud-GD interaction

Fig. 2 shows a large scale view of the evolution of the cloud-GD interaction. The surface density is given in units of $\frac{M_{\odot}}{\text{pc}^2}$ and the length units are given in pc. A closer view of the inner region can be seen in Fig. 3 using the same units and time slices as Fig. 2.

Figures 2 (a) and 3 (a) show the initial setup with the cloud approaching the counter-clockwise rotating GD from the left side. In Fig. 2 (b) the cloud just crashed into the GD and reached the opposite side. The cloud is strongly compressed and fragments are forming inside its high density region. The formerly evacuated central region of the CND is filling up with low angular momentum gas, better seen in Fig. 3 (b).

Following its highly eccentric orbit, the cloud moves outside the central 5 pc region (Fig. 2 (c)) and thus will no longer be visible on the next plots. The cloud is tidally torn apart and a stream of gas forms that slowly falls back towards the black hole, seen on the lower right in Fig. 2 (c). Fig. 3 (c) shows the first sub-parsec scale accretion disk that has formed around the black hole at its peak mass. The disk has very low mass $(6.5 \times 10^2 \text{ M}_{\odot})$, is short lived (roughly 0.1 Myr) and highly eccentric. There is still a lot of material inside the GD, which is now spiraling towards the center.

The tight stream of gas entering from the bottom of

Fig. 2 (d) still originates from the cloud. This stream mixes with the ambient gas from the GD (Fig. 3 (d)), by this loosing angular momentum, and winds up around the black hole. This leads to the formation of the second accretion disk shown in Fig. 2 (e) and Fig. 3 (e).

The disk has a high mass $(1.35 \times 10^4 M_{\odot})$ and exists for a long time (roughly 0.5 Myr). Besides forming the first high mass accretion disk the stream also collides with material inside the GD, thus slowly reducing the angular momentum (due to the collision with material of opposite angular momentum) of the GD material, moving it further towards the center.

The high mass accretion disk is now slowly eroded by GD gas with opposite angular momentum falling in at the outer edges. This destroys the disk from the outside in. A detailed study of the evolution of nested accretion disks with opposite angular momentum close to supermassive black holes has been carried out by Nixon et al. (2012)). They find that accretion rates can increase more than 100 times above the accretion rate of a single planar viscously evolving accretion disk. This provides a very efficient way to feed SMBHs.

After the disk has vanished another short lived (roughly 0.1 Myr), low mass $(9.5 \times 10^2 M_{\odot})$ and high eccentricity accretion disk forms (Fig. 2 (f) and Fig. 3 (f)). The GD is now almost completely destroyed by the stream of gas flowing back in from the cloud.

Transition into the final steady state is shown in the series of plots (g-l) in Fig. 2 and Fig. 3. In Fig. 2 (g) the last material remaining in the GD starts its last orbit, crossing the stream of backwards flowing gas from the cloud in Fig. 2 (h). All this material now winds up around the central black hole and forms the second high mass accretion disk ($5.65 \times 10^3 M_{\odot}$), presented in Fig. 2 (i) and Fig. 3 (i) at peak mass.

When most of the GD gas has fallen inwards the gas from the clockwise rotating stream, resulting from the disrupted gas cloud cannot lose angular momentum anymore and feeding of the central accretion disk stops. Fig. 2 (j) shows the stream of gas from the cloud overshooting



Figure 2. Large scale view of the cloud-GD interaction evolution. Shown is the logarithmic surface-density in units of $\frac{M_{\odot}}{pc^2}$ and the length units are given in pc. In (a) the initial setup with the cloud approaching from the left is shown. The cloud crashes into the GD and gets strongly compressed (b). Next the cloud reaches the opposite side of the GD and the first low mass accretion disk forms (c). A stream of cloud material flows backward into the inner region of the GD and starts winding up around the black hole (d). Plot (e) shows the first high mass accretion disk at peak mass. After the high mass accretion disk is destroyed by gas of opposite angular momentum eating it up from the outside in, another low mass, high eccentricity and short lived accretion disk forms, shown in (f). A small amount of material left from the original GD starts its last orbit (g), crossing the stream of gas from the cloud can overshoot the GD region in (j). This leads to the formation of a large eccentric ring of gas around the central accretion disk (k). This ring slowly circularizes, leading to the final steady state shown in (l).



Figure 3. Shown is the logarithmic surface-density in units of $\frac{M_{\odot}}{pc^2}$ and the length units are given in pc. In (a) the initial setup with the cloud approaching from the left is shown. Velocity vectors are all the same length and only indicate direction. Panels (b) to (k) give a close view of the inner region of the cloud-GD interaction evolution. The cloud crashes into the GD and the inner cavity of the GD starts to fill up with material (b). Formation of the first low mass accretion disk is shown in (c). The stream of cloud material which flows backward into the inner region of the GD winds up around the black hole (d). Plot (e) shows a close view of the first high mass accretion disk at maximum mass. In (f) the second low mass accretion disk can be seen. The remaining GD material is moving into the central area leading to the formation of the final step (l), the outer ring of gas is almost completely circular and replaces the original CND at lower density and with opposite angular momentum.

the GD region since there is no more material from the GD left to collide with.

Finally in Fig. 2 (k) the stream of gas from the cloud forms a large, eccentric ring of gas around the inner compact accretion disk. The ring slowly dissipates kinetic energy and circularizes, leading to the final steady state at 4.5 Myr shown in Fig. 2 (Î). An interesting feature of this ring is that it almost replaces the original GD (concerning location and width, although with a much lower density) but now rotates clockwise (compare velocity vectors in Fig. 3 (a) and (l)), as it is comprised almost completely of cloud material. The subsequent infall of additional clouds with the same angular momentum as the initial cloud could now add to the mass of this new GD eventually building up the currently observed CND. The infall of a cloud with opposite angular momentum could trigger the next accretion phase onto the supermassive black hole, which we might be witnessing currently (Montero-Castaño et al. 2009). The inner accretion disk is no longer affected by the infall of gas and remains more or less steady (Fig. 3 (j, k)).

A comparison of the density of the two high mass accretion disks in the z=0 pc plane is shown in Fig. 4. Several points which we investigate in more detail later are already visible from these plots. First the disks are clearly counter-rotating, the first accretion disk rotates clockwise, the second accretion disk counter-clockwise. Second the disks are inclined with respect to the xy-plane. They are rotated along the connection of the high density parts in Fig. 4, almost horizontal for (a) and almost vertical for (b). The disks can not be inclined in the same way, since the axes of rotation are nearly perpendicular to each other.

3.2. Amount of mass within the central region

We now look at the amount of mass within the central 0.6 pc around the black hole against time. This radius is taken simply because it is a bit further out than the radius of the largest accretion disk that formed. We distinguish between contributions from the cloud and the GD. This provides a good first hint for the formation of the various disks around the black hole and about their sense of rotation. A peak in the mass distribution represents a compact accretion disk. If the contribution to the mass of the disk is dominated by the cloud we expect the disk to be rotating clockwise, if the GD dominates we expect the disk to be rotating counter-clockwise. In our low resolution parameter study this provided a quick way to identify good models.

The arrows in Fig. 5 indicate the points at which we plotted the disks in section 3.1. First we can see that the two low mass disks at 0.2 Myr and 1.3 Myr are indeed very short lived and contain almost no mass above the ambient level, thus they are completely negligible. On the other hand the first high mass disk contains around 11 percent $(1.35 \times 10^4 \text{ M}_{\odot})$ and the second high mass disk around 4 percent $(5.65 \times 10^3 \text{ M}_{\odot})$ of the total initially available mass $(1.2 \times 10^5 \text{ M}_{\odot})$. The lifetime of the first disk of around 0.5 Myr should be long enough for the disk to fragment if it was unstable. A typical value for the fragmentation time of such a disk is 0.2 to 0.3 Myr as found in the simulations of Bonnell & Rice (2008), Mapelli et al.

(2012) and our own accretion disk fragmentation studies.

The main contribution to the mass of the first disk comes from the cloud, thus the disk is rotating clockwise. Although the disk is smaller compared to the second high mass disk, it contains more mass and thus is closer to being able to fragment as we will show in 3.4. For the second disk, the contribution to the mass is higher from the GD leading to a counter-clockwise rotating disk.

The mass in our disks is opposite to what is seen in observations. The observed larger disk has double the mass $(10^4 M_{\odot})$ in stars compared to the smaller disk $(0.5 \times 10^4 M_{\odot})$. In our simulation the smaller disk contains roughly three times the mass of the larger disk (Note that we compare the observed stellar disks to the simulated gaseous accretion disks). However, we regard this as a matter of fine tuning, like a more fine grained search over the initial cloud radius or GD size, which is beyond this first approach.

Fig. 6 shows the accretion rate and total accreted mass over time. In total around 10^5 M_{\odot} are accreted over 2 Myr and the mean accretion rate is roughly 0.05 M_☉/yr. Accretion in our case represents the flow of material below the accretion radius $r_{\rm acc}$ and is not connected to a black hole accretion rate. The material could settle into an actual black hole accretion disk at much smaller radii. The Lense-Thirring effect aligns the disk angular momentum with the black hole angular momentum, thus removing the accretion rate amplifying effect of counterrotating gas falling in at later times. The accretion disk then could evolve viscously, thus feeding the black hole at lower rates compared to Fig. 6.

3.3. Angular momentum distribution and disk orientation

To visualize the disk configuration better, we fitted each of the high mass accretion disks with a thin sheet at the times shown in Fig. 3 (e) and Fig. 3 (i), positioned at the midplane of the disks. Then we combined the results into a single plot, shown in Fig. 7 (a) and (b) for different viewing angles. Clearly the disks are inclined with respect to each other and share the same volume. The smallest angle between the disks (see Fig. 1 (b)) is roughly $\alpha_{\rm disk} = 15^{\circ}$ in our case, compared to 70° inferred from observations (Bartko et al. 2009). For comparison, the best fit of the observational data can be seen in Fig. 20 in Bartko et al. (2009). Although the second high mass disk is weakly warped in our case, the warp is not as strong as the observed one. However, there are also cases in the low resolution runs in which a highly warped disk was produced.

In Fig. 8 we show a histogram of the binned cosine of the angular momentum vector with respect to the x,y and z-axis for all the gas particles within the central 0.6 pc from the black hole. The first disk, shown in Fig. 8 (a) has a strong peak in the z-component near -1, thus the z-component of angular momentum is anti-parallel to the z-axis for all the gas inside the disk. On the other hand the second high mass disk peaks near 1, thus the z-component of angular momentum is parallel to the z-axis.



Figure 4. Density cut in the z=0 pc plane in units of $\frac{M_{\odot}}{pc^3}$. We compare the density in the z=0 plane of the two high mass accretion disks forming at 0.7 Myr (a) and 1.86 Myr (b). Velocity vectors are all the same length and only indicate direction. The disks are counter-rotating, inclined with respect to the xy-plane and with respect to each other.



Figure 5. Amount of mass within the central 0.6 pc versus simulation time. The black (solid) line shows the total mass, the blue (dashed) line the contribution from the cloud and the red (dotted) line the contribution from the GD to the total mass. The arrows indicate the points at which we plotted the disks in Fig. 3.

On the plane of sky, the GD is seen almost edge on from earth. One of the observed stellar disks is seen almost completely face on in the plane of sky. The second stellar disk is again seen almost edge on, but perpendicular to the GD. This configuration is not too far from what our simulation shows. None of our simulated disks lies within the plane of the GD, both of them are inclined with respect to the GD and with respect to each other, making our model an attractive formation mechanism for the stellar disks.

To show that the disk angular momentum distribution



Figure 6. Accretion rate (red, solid line) and total accreted mass (black, dashed line) over time. The plot is cut beyond 2 Myr since the accretion rate stays near zero until the end of the simulation at 4.5 Myr.

is determined by the mixture of cloud and GD material we now look only at the first high mass accretion disk. We isolate all the particles within the disk at 0.7 Myr and trace them back to the initial setup. For every snapshot we then plot the mean of the cosine of angular momentum with respect to the x,y and z-axis of those isolated particles.

To measure how strongly the material is mixed, we determine for every snapshot the mean number of particles from the GD within the hydro-smoothing length of every cloud particle, as well as the other way around. If a particle is within the hydro-smoothing length of another particle it contributes to its density,



Figure 7. The two high mass accretion disks combined in a single plot, fitted at midplane at the times shown in Fig. 3 (e) at 0.7 Myr and Fig. 3 (i) at 1.86 Myr from different viewing angles.



Figure 8. Histogram of the cosine of angular momentum with respect to the x,y and z-axis. The black (solid) line shows the cosine of angular momentum with respect to the z-axis, the blue (dashed) line with respect to the y-axis and the red (dotted) line with respect to the x-axis. The two peaks near -1 and 1 for the first (a) and second (b) high mass accretion disks show that the z-component of angular momentum is opposite for the two disks.

which by definition means that the two particles are interacting (or more sloppy formulated "mixed").

The distribution of the mean cosine of angular momentum over time obtained this way is shown in Fig. 9 (a), (b) and (c). For comparison the mean number of neighbors from the opposite component can be seen in Fig. 9 (d). In the beginning, cloud and GD are well separated, with no particle from the opposite component nearby and with the angular momentum only aligned parallel and anti-parallel to the z-axis. At around 0.12 Myr the cloud reaches the opposite side after crashing into the GD. The interaction of cloud and GD leads to mixing of the particles and now each of the components has a small number of neighbors from the opposite component. This is also reflected in the mean cosine distribution, taking the z-component (Fig. 9 (c)), one can clearly see that a fraction of the GD material is affected and now co-rotates with the cloud material.

At around 0.4 Myr formation of the accretion disk

starts. Now the number of neighbors from the opposite component steeply rises for both the GD and the cloud. This is mirrored in the angular momentum distribution, again best seen in the z-component (Fig. 9 (c)). The plots show that there is a strong correlation between mixing of the two components and the angular momentum distribution. The contribution of GD material to the cloud material reduces its angular momentum, so that it can settle into a tight orbit around the black hole. Fig. 9 (b) shows that the particles from the cloud which end up inside the accretion disk already have a small ycomponent in their angular momentum, which leads to the inclination of the accretion disk with respect to the xy-plane. This asymmetric distribution originates from the small imbalance of mass above and below the xyplane due to the random particle setup, which effectively acts like a small cloud offset in z-direction. A higher mass imbalance or a non zero cloud offset in z-direction would increase the inclination, which we confirmed in test-simulations.





Figure 9. Shown in (a), (b) and (c) is the mean cosine of angular momentum with respect to x,y and z-axis of the subset of particles from the first high mass accretion disk over time. The black (solid) line shows the angular momentum orientation for the cloud particles and the red (dashed) line for the GD particles. In (d) we show the mean number of neighbors within the hydro-smoothing length from the opposite component for each of the components (GD and cloud). Again only the subset of particles inside the first high mass accretion disk at 0.7 Myr is shown. This provides a way to see how well "mixed" the two components are. The mean number of neighbors from the GD for the GD material is shown as black (solid) line and the mean number of neighbors from the cloud for the GD material is shown as red (dashed). There is a clear correlation between mixing and angular momentum distribution.

3.4. Toomre parameter and disk fragmentation

After we have formed gaseous accretion disks, the next important step is disk instability. Our scenario assumes that the first high mass accretion disk fragments into cores before the gaseous component gets destroyed and the second high mass accretion disk forms, leaving a collisionless disk of star forming cores from the first accretion disk. After that the second accretion disk fragments, leaving two inclined disks of cores which turn into stars and probably undergo further evolution (e.g. change of inclination, warping) leading eventually to the stellar disks observed today.

To investigate the fragmentation behavior we look at the Toomre instability parameter for our two high mass accretion disks, shown in Fig. 10. For this we rotate each of the disks into the xy-plane and calculate Q for different radial bins. The Toomre parameter for the first high mass accretion disk, plotted in black (solid), drops to Q=2.8 at around 0.22 pc distance from the black hole, which is still in the stable regime. An even higher value is seen for the second high mass accretion disk



Figure 10. Toomre Q at peak mass for both compact accretion disks. Plotted is the Toomre parameter in radial bins against distance from the black hole. The black (solid) line shows the first high mass accretion disk which formed around 0.7 Myr, the red (dashed) line the second high mass accretion disk which formed around 1.86 Myr.



Figure 11. Logarithmic surface-density in units of $\frac{M_{\odot}}{pc^2}$. A test case with different initial conditions from the simulation presented throughout the paper leads to a high mass accretion disk that breaks up into fragments.

shown in red (dashed) in Fig. 10. Here Q=23 represents the lowest value reached at around 0.36 pc. Thus both our disks are stable against fragmentation.

This is not unexpected since we set up our initial conditions with a rather low total mass. As already pointed out in the introduction, simulations which use a cloud of low angular momentum captured by the black hole need up to $10^5 M_{\odot}$ of mass in the cloud to explain the top-heavy IMF in a single disk. In our case we have a starting mass of $1.2 \times 10^5 M_{\odot}$ that is potentially available for a total of two disks.

The low initial mass comes from considerations about cloud and GD stability. We already discussed the problem of stabilizing clumps within the GD/CND in section 2.1. At high masses corresponding to several times $10^5 M_{\odot}$ the disk and the GD quickly become unstable and start fragmenting.

Observations indicate that there are around 10^4 to $10^5~{\rm M}_{\odot}$ of gas inside the currently observed CND and that the CND is a transient structure ($t_{life} < 10^5$ yrs) (Guesten et al. 1987). However there are also models which assume the CND to be a rather stable structure $(t_{life} > 10^7 \text{ yrs})$ (Vollmer et al. 2003). Our simulations start with a progenitor of the current CND, so the mass does not necessarily have to be the same as the current CND mass, leaving us some freedom in the choice. The issue of how to stabilize the GD or a cloud goes beyond the scope of our work. Hence, our choice of parameters is a trade-off between a GD and cloud stable enough to survive the first encounter given our limited physics and a preferably high initial mass. Turbulent, rotating clumps inside the GD together with a magnetic field could be ingredients needed to stabilize such a system.

However, even at our current initial mass we were able to find initial conditions which lead to enough mass inside the first high mass accretion disk so that it becomes unstable. Fig. 11 shows such a simulation in which the first high mass accretion disk that forms quickly becomes unstable and breaks up into cores. Unfortunately this simulation evolves very slowly and we are not yet far beyond the point at which the simulation is shown. The results of this improved model will be shown in a subsequent paper.

A number of clumps, originating from the cloud after crashing into the GD and fragmenting, are spread out over a large area (up to 40 pc) around the central black hole. Those clumps might represent the population of young massive stars at radii larger than 0.5 pc that were recently found by Nishiyama & Schödel (2013).

3.5. Formation of the mini-spiral

The inflow pattern of gas especially at the beginning of our simulations always consists of multiple streams of gas flowing into the central region from different points of the inner edge of the GD. In one particular case of a low-resolution test simulation, the inflow pattern resembles the mini spiral surprisingly good. We present this case in Fig. 12. The mini spiral has already been credited as source for the black hole SgrA* in its bright state (Czerny et al. 2012).

A comparison to observations, e.g. Fig. 2 in Zhao et al. (2009) shows that the 2D velocity field matches observations quite well, especially the small loop forming at the upper right half of the plot. In our picture the eastern-arm (stream of gas on the left side of the plot) crosses the black hole from below and also forms the so called bar below the black hole. From the north we have the northern-arm flowing past the black hole on the left side, colliding with the bar at the crossing point of the streams.

A detailed comparison of the 3D structure of the inflow pattern to the fit from observations by Zhao et al. (2009) is still necessary and will be postponed to a future publication. The formation of a structure similar to the mini-spiral seems to be a natural feature of our model for the formation of the two counter-rotating sub-parsec



Figure 12. Density cut in the z=0 pc plane in units of $\frac{M_{\odot}}{pc^3}$ through the inflow pattern of gas from a low-resolution test simulation that resembles the mini-spiral. The 2D velocity field agrees with observations presented in Zhao et al. (2009), but a detailed 3D comparison still has to be undertaken.

scale accretion disks, suggesting that we observe a similar event today at the GC which happened 10 Myr ago and lead to the formation of the disks.

4. DISCUSSION AND SUMMARY

We presented a simple, plausible model for the formation of two counter-rotating accretion disks. This model is for the first time able to explain the formation of the puzzling configuration of the two stellar disks which are observed at the Galactic Center (GC) without relying on long chains of individual events.

So far it was assumed that a single cloud with a very small (sub-parsec) impact parameter gets captured and disrupted by the black hole to form a single accretion disk. To form a second disk, one would need within a short time a second, counter-rotating cloud with equally small impact parameter. Already the existence of a single cloud with a sub-parsec impact parameter is highly unlikely. It would have to be created very close to the black hole from the beginning. However, the only real source of gas close to the black hole is the circum-nuclear disk (CND) (for the current event) or our simulated gaseous disk (GD) (for the previous event), so it is likely that the gas which formed the accretion disks originates there.

The CND/GD is placed far enough from the black hole so that collisions with clouds become possible. Observations even confirm that there is currently a cloud colliding with the CND. Test simulations have shown that it is easy to create multiple accretion disks using this model. There are cases with up to four compact accretion disks forming. Sometimes all the disks have the same rotational direction, sometimes only a single disk forms. But in all cases the formation of an accretion disk due to low angular momentum gas winding up around the black hole is possible. The inflow patterns of the streams of gas can even resemble the mini-spiral which is currently observed at the GC.

Due to the high degree of freedom in our initial conditions we don't expect to get a perfect match to observations. For our high resolution simulation we took the parameters from a low resolution simulation that produced two prominent, counter-rotating disks of roughly the correct size compared to observations, in order to show the basic mechanism of our proposed model.

The stellar disks themselves had a long time to evolve since their formation and there is a number of papers (Ulubay-Siddiki et al. 2009; Kocsis & Tremaine 2011; Madigan et al. 2009; Ulubay-Siddiki et al. 2012) that deal with how the disks could become warped with time or increase their inclination. In this work we concentrate on the initial formation of the progenitor accretion disks and hence a perfect fit to all observed characteristics of the stellar disks is not intended. Test simulations have shown that increasing the mass imbalance above and below the xy-plane, as well as allowing a small cloud offset in z-direction also leads to a larger inclination, thus an improved simulation later on could also be able to explain the high inclination directly.

We have made a number of simplifications which could impact our results, which will be briefly presented here. First we always assume the cloud and the GD to have equal mass. A naive improvement judging from Fig. 10 would be to increase the mass in the GD so that the second high mass accretion disk becomes more massive, since the main contribution to mass in this disk comes from the GD. This could also push the first high mass accretion disk over the fragmentation point. In addition this would bring the disks closer to the observed mass ratio of 1:2 (10^4 M_{\odot} in the clockwise disk and $0.5 \times 10^4 \text{ M}_{\odot}$ in the counter-clockwise disk).

Feedback from the black hole would depend on the orientation of the black hole spin axis with respect to the accretion disks. A real first hint on the spin axis orientation might be given by the recent possible detection of a jet-like outflow from SgrA* (Yusef-Zadeh et al. 2012). Such a jet could prevent the formation of a second disk after material from the first disk feeds the black hole.

Another important point to keep in mind is the possible impact of stellar feedback. We do not include stellar feedback in our simulations. If there are stars forming in the first accretion disk, they could possibly influence the formation of the second accretion disk, given enough time between the two events. Thus it is desirable that the disks form as short after one another as possible.

On the other hand, the disks must have enough time to fragment at all. This last point does not seem to be overall problematic judging from our test simulations. Simulations of fragmenting high mass ($10^5 M_{\odot}$) accretion disks close (< 0.5 pc) to SgrA* typically only need around 0.2 to 0.3 Myr to form clumps and protostellar cores, as already pointed out in section 3.2.

Even in cases where we had four high mass accretion disks forming, each single accretion disk existed for around 0.2 Myr and thus would have had enough time to fragment.

More problematic is the time between the formation of the two disks. In our case it takes roughly 1 Myr between formation of the two disks, during which feedback from the stars forming in the first disk could become already important. However, taking the stellar models of Ekström et al. (2012) into account this should be short enough, so that stellar feedback even from high mass stars (> 60 M_{\odot}) should not play a role.

Compared to observations we are well within the uncertainty of age determinations of the stars of 2 Myr. The stellar and black hole feedback problem also applies to the low angular momentum cloud capture model and is not a special property of our particular formation model.

Overall, seeing how easy it is to create multiple disks, we are still confident that our results will hold when including additional physics. This first study already produced a reasonable fit when compared to observations and future refinements will surely increase the agreement. For the first time we are able to create two massive, sub-parsec scale counter-rotating accretion disks which are inclined with respect to each other and with respect to the CND.

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REFERENCES

- Alexander, R. D., Armitage, P. J., Cuadra, J., & Begelman, M. C. 2008, ApJ, 674, 927
- Alig, C., Burkert, A., Johansson, P. H., & Schartmann, M. 2011, MNRAS, 412, 469
- Bartko, H., Martins, F., Fritz, T. K., et al. 2009, ApJ, 697, 1741 Bartko, H., Martins, F., Trippe, S., et al. 2010, ApJ, 708, 834
- Bate, M. R., & Burkert, A. 1997, MNRAS, 288, 1060
- Becklin, E. E., Gatley, I., & Werner, M. W. 1982, ApJ, 258, 135
- Bonnell, I. A., & Rice, W. K. M. 2008, Science, 321, 1060
- Burkert, A., Schartmann, M., Alig, C., et al. 2012, ApJ, 750, 58 Coker, R. F., Christopher, M. H., Stolovy, S. R., & Scoville, N. Z. 2003, Astronomische Nachrichten Supplement, 324, 629

- Czerny, B., Karas, V., Kunneriath, D., & Das, T. K. 2012, ArXiv e-prints, 1211.1226
- Ekers, R. D., van Gorkom, J. H., Schwarz, U. J., & Goss, W. M. 1983, A&A, 122, 143
- Ekström, S., Georgy, C., Eggenberger, P., et al. 2012, A&A, 537, A146
- Genzel, R., Eisenhauer, F., & Gillessen, S. 2010, Reviews of Modern Physics, 82, 3121
- Genzel, R., Schödel, R., Ott, T., et al. 2003, ApJ, 594, 812
- Ghez, A. M., Salim, S., Hornstein, S. D., et al. 2005, ApJ, 620, 744
- Gillessen, S., Genzel, R., Fritz, T. K., et al. 2012, Nature, 481, 51 - 2013, ApJ, 763, 78
- Guesten, R., Genzel, R., Wright, M. C. H., et al. 1987, ApJ, 318, 124
- Güsten, R., & Philipp, S. D. 2004, in The Dense Interstellar Medium in Galaxies, ed. S. Pfalzner, C. Kramer, C. Staubmeier, & A. Heithausen, 253
- Hobbs, A., & Nayakshin, S. 2009, MNRAS, 394, 191
- Hopkins, P. F., & Quataert, E. 2010, MNRAS, 407, 1529
- Jackson, J. M., Geis, N., Genzel, R., et al. 1993, ApJ, 402, 173
- Kocsis, B., & Tremaine, S. 2011, MNRAS, 412, 187
- Launhardt, R., Zylka, R., & Mezger, P. G. 2002, A&A, 384, 112
- Lo, K. Y., & Claussen, M. J. 1983, Nature, 306, 647
- Lu, J. R., Do, T., Ghez, A. M., et al. 2013, ArXiv e-prints
- Lu, J. R., Ghez, A. M., Hornstein, S. D., et al. 2009, ApJ, 690, 1463
- Lucas, W. E., Bonnell, I. A., Davies, M. B., & Rice, K. 2013, ArXiv e-prints
- Madigan, A.-M., Levin, Y., & Hopman, C. 2009, ApJ, 697, L44 Mapelli, M., Hayfield, T., Mayer, L., & Wadsley, J. 2012,
- Astrophys.J., 749, 168 Miyazaki, A., & Tsuboi, M. 2000, ApJ, 536, 357
- Molinari, S., Bally, J., Noriega-Crespo, A., et al. 2011, ApJ, 735, L33
- Montero-Castaño, M., Herrnstein, R. M., & Ho, P. T. P. 2009, ApJ, 695, 1477
- Murray-Clay, R. A., & Loeb, A. 2012, Nature Communications, 3 Nishiyama, S., & Schödel, R. 2013, A&A, 549, A57
- Nixon, C. J., King, A. R., & Price, D. J. 2012, MNRAS, 422, 2547 Paumard, T., Genzel, R., Martins, F., et al. 2006, ApJ, 643, 1011
- Price, D. J. 2007, Publications of the Astronomical Society of Australia, 24, 159
- Schartmann, M., Burkert, A., Alig, C., et al. 2012, ApJ, 755, 155
- Springel, V. 2005, MNRAS, 364, 1105
- Springel, V., White, M., & Hernquist, L. 2001, ApJ, 549, 681 Stamatellos, D., Whitworth, A. P., Bisbas, T., & Goodwin, S.
- 2007, A&A, 475, 37 Su, M., Slatyer, T. R., & Finkbeiner, D. P. 2010, ApJ, 724, 1044 Ulubay-Siddiki, A., Bartko, H., & Gerhard, O. 2012, ArXiv
- e-prints, 1210.4750 Ulubay-Siddiki, A., Gerhard, O., & Arnaboldi, M. 2009, MNRAS, 398, 535
- Vollmer, B., & Duschl, W. J. 2001, A&A, 377, 1016
- 2002, A&A, 388, 128
- Vollmer, B., Duschl, W. J., & Zylka, R. 2003, Astronomische Nachrichten Supplement, 324, 613
- Wardle, M., & Yusef-Zadeh, F. 2008, ApJ, 683, L37
- Yusef-Zadeh, F., Arendt, R., Bushouse, H., et al. 2012, ApJ, 758, L11
- Zhao, J.-H., Morris, M. R., Goss, W. M., & An, T. 2009, ApJ, 699.186
- Zubovas, K., King, A. R., & Nayakshin, S. 2011, MNRAS, 415, L21