

Secular Evolution and Structural Properties of Stellar Bars in Galaxies

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ABSTRACT

I present results from the modeling of stellar bars in nearly 300 barred galaxies in the local universe through parametric multi-component multi-band image fitting. The surface brightness radial profile of bars is described using a Sérsic function, and parameters such as bar effective radius, ellipticity, boxiness, length and mass, and bar-to-total luminosity and mass ratios, are determined, which is unprecedented for a sample of this size. The properties of bars in galaxies with classical bulges and pseudo-bulges are compared. For a fixed bar-to-total mass ratio, pseudo-bulges are on average significantly less massive than classical bulges, indicating that, if pseudo-bulges are formed through bars, further processes are necessary to build a classical bulge. I find a correlation between bar ellipticity and boxiness, and define bar strength as the product of these two quantities. I also find correlations between bar strength and normalised bar size, between the sizes of bars and bulges, and between normalised bar size and bulge-to-total ratio. Bars with different ellipticities follow parallel lines in the latter two correlations. These correlations can arise if, starting off with different normalised sizes and ellipticities, bars grow longer and stronger with dynamical age, as a result of angular momentum exchange from the inner to the outer parts of galaxies, in agreement with previous theoretical predictions. As a consequence, bar pattern speeds should become lower with bar dynamical age, and towards galaxies with more prominent bulges.

Key words: galaxies: bulges – galaxies: evolution – galaxies: formation – galaxies: fundamental parameters – galaxies: photometry – galaxies: structure

1 INTRODUCTION

Many recent studies, from observational and theoretical viewpoints, have established that stellar bars in disc galaxies can play an important role in galaxy evolution (see Sellwood & Wilkinson 1993; Kormendy & Kennicutt 2004; Gadotti 2009a, for reviews). Theoretical work indicates that the redistribution of angular momentum, induced by the bar, in the galaxy interstellar medium, as well as in the stellar and dark matter components, has a number of important consequences (e.g. Athanassoula & Misiriotis 2002; Athanassoula 2003; Martinez-Valpuesta et al. 2006; Berentzen et al. 2006). Gas lying beyond the bar ends is driven outwards, whereas gas lying within the bar ends is driven to the central regions (e.g. Schwarz 1981; Combes & Gerin 1985; Athanassoula 1992; Friedli & Benz 1993; Friedli et al. 1994; Piner et al. 1995). This secular evolution scenario has been partially confirmed, at least qualitatively, with observational

evidence that barred galaxies show flatter chemical abundance (O/H) radial gradients (Zaritsky et al. 1994, further, Martin & Roy 1994 find that the stronger the bar the flatter the gradient) and higher central concentrations of molecular gas (CO – Sakamoto et al. 1999). This movement of gas to the centre might in principle help build a young and kinematically cold stellar bulge component, i.e. a disc-like bulge (see Athanassoula 2005). Indeed, observations suggest that disc-like bulges exist and have formation processes linked to dynamical disc instabilities, such as bars, as opposed to the old and kinematically hot classical bulges (e.g. Carollo et al. 1997; Gadotti & dos Anjos 2001; Erwin et al. 2003; Fisher 2006; Drory & Fisher 2007; Fisher & Drory 2008; Gadotti 2009b, and references therein).

Theory also suggests how bars evolve with time. Broadly speaking, bars slow down their pattern rotation speed, and get longer and thinner (i.e. more eccentric and stronger) during the course of their evolution, capturing stars from the disc. Observations suggest that the strong bar in NGC 4608 has increased in mass by a factor of

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≈ 1.7 , through the capture of $\approx 13\%$ of the disc stars (Gadotti 2008). In addition, more evolved bars also show more rectangular-like face-on isophotal shapes, i.e. they are more boxy. In detail, however, simulated bars can become abruptly shorter and thicker a few Giga-years after their formation, due to the onset of dynamical vertical instabilities that originate box/peanut bulges. (These seem to be simply the inner parts of bars that buckle off the disc plane and can be seen in inclined systems.) Then, about 1 Gyr later, they recover the original evolutionary trends. Furthermore, a substantial gas component in the disc can also complicate the picture of the evolution of bar properties, halting how these properties change, and in some cases even reversing the trends (e.g. Bournaud & Combes 2002; Bournaud et al. 2005; Debattista et al. 2006; Berentzen et al. 2007). To date, there is no study aimed directly at providing observational evidence on how bar properties change with time. This is partially due to the difficulty of estimating bar dynamical ages. Although some first steps have been done in this direction (see Gadotti & de Souza 2005, 2006; Pérez et al. 2009), the results are as yet inconclusive, and the methods developed require large amounts of telescope time.

Moreover, bars are found very often in disc galaxies, and the fraction of disc galaxies hosting bars seems to increase with time, i.e. the fraction is lower at redshift $z \sim 1$, as compared to $z \sim 0$ (see Sheth et al. 2008, and references therein, but see also Barazza et al. 2008 and Jogee et al. 2004). In addition, weaker, but also global non-axisymmetric structures, such as oval distortions in the disc, can as well efficiently produce such redistribution of angular momentum. Therefore, the consequences of the presence of such structures should be conspicuous, and studies on the properties of bars and their host galaxies at $z \approx 0$, as well as higher redshifts, can give direct clues on galaxy evolution.

The first and easier step in observational studies of barred galaxies is to identify bars, and there are a number of studies on the fraction of disc galaxies with bars (e.g. Eskridge et al. 2000; Barazza et al. 2008; Marinova et al. 2009). Other studies have used ellipse fits to the images of barred galaxies to obtain bar properties such as ellipticity and length (e.g. Marinova & Jogee 2007; Barazza et al. 2008, 2009), although it has been shown that ellipse fits can lead to an underestimation of the bar ellipticity (or an overestimation of the bar axial ratio, Gadotti 2008). In Martin (1995), bar axial ratios and lengths were visually assessed, and a relation was found between bar length and the normalised diameter of the bulge. Ten years later, Erwin (2005) measured bar lengths using ellipse fits and found that bar size scales with disc size, and confirmed previous results that bars in early-type disc galaxies are clearly larger than those in late-type galaxies (see also Aguerri et al. 2009). He went further and argued that this observational evidence can be qualitatively consistent with the simulations that show bars getting larger with time, if indeed secular evolution produces early-type disc galaxies from late-type ones (see also Friedli & Benz 1995; Martin & Friedli 1997; Gadotti & de Souza 2005, 2006). Applying ellipse fits to 2MASS images of 151 spiral galaxies, Menéndez-Delmestre et al. (2007) obtained measurements of bar length and axial ratio, and found a weak trend of higher ellipticities for larger bars, which is also consistent with the results from simulations.

More recently, Durbala et al. (2008, see also de Jong

1996; Laurikainen et al. 2005, 2007; Gadotti 2008) used 2D bulge/bar/disc decompositions of 97 Sb, Sbc and Sc galaxies, employing *i*-band images from the Sloan Digital Sky Survey (SDSS) to obtain parameters such as bar length and bar-to-total luminosity ratio. Weinzirl et al. (2009) did a similar work using *H*-band images of 143 spirals and explored also the stellar mass content in bars. About 60% of the galaxies in both samples are barred. In this paper, I explore the results of 2D bulge/bar/disc decompositions of 291 barred galaxies, using SDSS images in the *g* and *i* bands, from Gadotti (2009b, hereafter Paper I). This allows me to study bar properties in a level of detail which is unprecedented for a sample of this size. A thorough characterization of bars in massive galaxies in the local universe is thus put forth in Sect. 3.1, after a description of the data at hand in the next section. In Sect. 3.2, the properties of bars in galaxies with classical and pseudo-bulges are compared. In Sect. 3.3, I explore correlations between bar properties in order to test the predictions from simulations on the secular growth of bars. These results are discussed in Sect. 4, while Sect. 5 summarises the paper.

2 DATA

The reader is referred to Paper I for a detailed account of the sample selection and image decomposition. Here I summarise the most relevant aspects of these procedures to the present study.

In Paper I, I have performed careful and detailed image fitting of all galaxies in a sample of 946 systems, from bulgeless to elliptical galaxies. The sample was designed to be concomitantly suitable for structural analysis based on image decomposition and a fair representation of the galaxy population in the local universe. It was drawn from all objects spectroscopically classified as galaxies in the SDSS Data Release Two (DR2) at redshifts $0.02 \leq z \leq 0.07$, and with stellar masses larger than $10^{10} M_{\odot}$. This parent sample is thus a volume-limited sample of *massive* galaxies, i.e. a sample which includes all galaxies more massive than $10^{10} M_{\odot}$ in the volume defined by the redshift cuts and the DR2 footprint. In order to produce reliable decompositions, and avoid dust and projection effects, I have applied another important selection criterion to produce the final sample: it contains only galaxies close to face-on, i.e. with an axial ratio $b/a \geq 0.9$, where *a* and *b* are, respectively, the semi-major and semi-minor axes of the galaxy at the 25 *g*-band mag arcsec⁻² isophote. This criterion also eases the identification of bars, which are difficult to see in very inclined projections. I have found that the final sample is representative of the local population of massive galaxies. This was done by comparing the distributions of several main galaxy properties, such as absolute magnitude, $D_n(4000)$ and concentration, in the volume-limited and final samples, and verifying that these distributions are similar.

Two-dimensional fits were performed using the BUDDA code (de Souza et al. 2004; Gadotti 2008) and SDSS images in the *g*, *r* and *i* bands, including up to three components in the models, namely bulge, disc and bar.¹ The presence

¹ Results are available at <http://www.mpa-garching.mpg.de/~dimitri/buddaonsdss/buddaonsdss.html>.

of these components was assessed by individual inspection of images, surface brightness radial profiles and isophotal maps. Given the typical redshift of the galaxies in the sample, $z \approx 0.05$, and the typical FWHM of the PSF in SDSS images, $\text{FWHM} \approx 1.5$ arcsec, the typical physical spatial resolution in these images is thus 1.5 kpc. This means that I likely missed most bars with semi-major axis shorter than $L_{\text{bar}} \approx 2-3$ kpc, typically seen in very late-type spirals (later than Sc – Elmegreen & Elmegreen 1985). The whole of these faint bars is typically within 2 – 4 seeing elements, and thus they do not imprint clear signatures in either the isophotal contours or the intensity profile. The results presented here thus concern the typical, bonafide bars seen in early-type spirals and lenticulars. Note that, in contrast, bulges with effective radius r_e of the order of one PSF HWHM can still be identified in the intensity profile, since they usually contain a much larger fraction of the galaxy light than these short and faint bars. The final sample includes 291 barred galaxies, which are the subject of the present paper. Classical bulges and pseudo-bulges are separated using the Kormendy (1977) relation, where pseudo-bulges can be identified as outliers in an objective fashion. It is worth noting that pseudo-bulges here refer to disc-like bulges, not box/peanut bulges, since the sample contains only face-on galaxies, and bars are included in the fitted models (see Paper I).

Bulge, disc and bar are described as concentric ellipses, which can have different positions angles and ellipticities. They also follow a surface brightness radial profile: in case of the disc, this is an exponential (Freeman 1970) profile. Bulge and bar follow a (Sérsic 1968) profile, in which the Sérsic index is a free parameter that controls the shape of the profile. A large Sérsic index corresponds to a highly centrally concentrated profile with important wings, whereas a small Sérsic index corresponds to a flatter profile with a fast declining outer part. It should be noted that, although both bulge and bar have surface brightness profiles following the same parametric function, there is little space for degenerate solutions, since bars are generally more extended and eccentric than bulges, and have lower Sérsic indices.

Since I have done multi-band decompositions, I was able to estimate the $g - i$ integrated colour of each component separately. Using the relation between $g - i$ and the stellar mass-to-light ratio in the i -band from Kauffmann et al. (2007), I have all parameters necessary to accurately calculate the stellar masses of all components, including the bars, of the galaxies in the sample.

The structural parameters obtained in Paper I used in this work are thus:

- disc scale length h ;
- bulge effective radius r_e (i.e. the radius that contains half of the light coming from the bulge);
- bulge-to-total luminosity ratio B/T ;
- bar effective radius $r_{e,bar}$ (i.e. the radius that contains half of the light coming from the bar);
- bar-to-total luminosity ratio Bar/T (lum.);
- bar-to-total mass ratio Bar/T (mass);
- bar Sérsic index n_{Bar} ;
- bar ellipticity ϵ , defined as $1 - b/a$, where a and b are, respectively, the bar semi-major and semi-minor axes;
- bar boxiness c , defined through the equation of the gen-

eralised ellipse used to fit the bar (see Athanassoula et al. 1990):

$$\left(\frac{|x|}{a}\right)^c + \left(\frac{|y|}{b}\right)^c = 1, \quad (1)$$

where, again, a and b are, respectively, the bar semi-major and semi-minor axes, and x and y are the pixel coordinates of the ellipse points;

- bar length (semi-major axis) L_{bar} .

It is worth noting that the bar length as determined through the image decompositions is usually larger than the radius of the peak in ellipticity inside the bar, a parameter commonly used to define bar size, estimated through ellipse fitting. However, L_{bar} agrees well with two other parameters used to define bar size, namely the first minimum in ellipticity outside the ellipticity peak in the bar, and the point where the position angle of the fitted ellipses differ by more than 10° from the position angle of the bar (see Gadotti 2008, fig. 4), which are known to provide more accurate estimates (see discussion in Erwin 2005).

Two other parameters used in this paper were obtained from the SDSS database:

- r_{24} : the radius of the galaxy 24 r -band mag arcsec $^{-2}$ isophote;
- R90: the radius containing 90 per cent of the total galaxy light.

All these parameters refer to measurements using the i -band image, unless otherwise noted. In the remaining of the paper, I will explore these physical properties firstly to provide a comprehensive description of the structure of stellar bars in massive galaxies in the local universe, and, secondly, to verify if one can test the theoretical predictions described in the previous section about how such bars evolve in time.

3 RESULTS

3.1 The structural properties of bars

As discussed at the Introduction, large-scale stellar bars play a fundamental role in galaxy evolution. It is thus clearly very important to put forth a description of their structural properties as detailed as possible. With the data described above, I do this in Fig. 1. This gives us a thorough portrayal of bars in the local universe, which is useful in many ways. For instance, if one wants to put bars ad hoc in a theoretical framework to describe barred galaxies today, it is most likely that one would want such bars to be consistent with those studied here. Conversely, theoretical studies aiming at the evolution of bars in time should be able to explain the existence of bars today with the properties depicted in Fig. 1. In addition, a comparison between the properties of bars at different redshifts gives us directly a way to see how bars evolve in time.

Some features in Fig. 1 are worth mentioning. First, the typical value of the bar Sérsic index ($n_{\text{Bar}} \approx 0.7$) depicts a profile which is about half way between a Gaussian (Sérsic index equals 0.5) and an exponential (Sérsic index equals 1). The distribution of bar ellipticities peaks at ≈ 0.6 , which is about 20% higher than the peaks found in studies based on ellipse fits (e.g. Menéndez-Delmestre et al. 2007; Marinova &

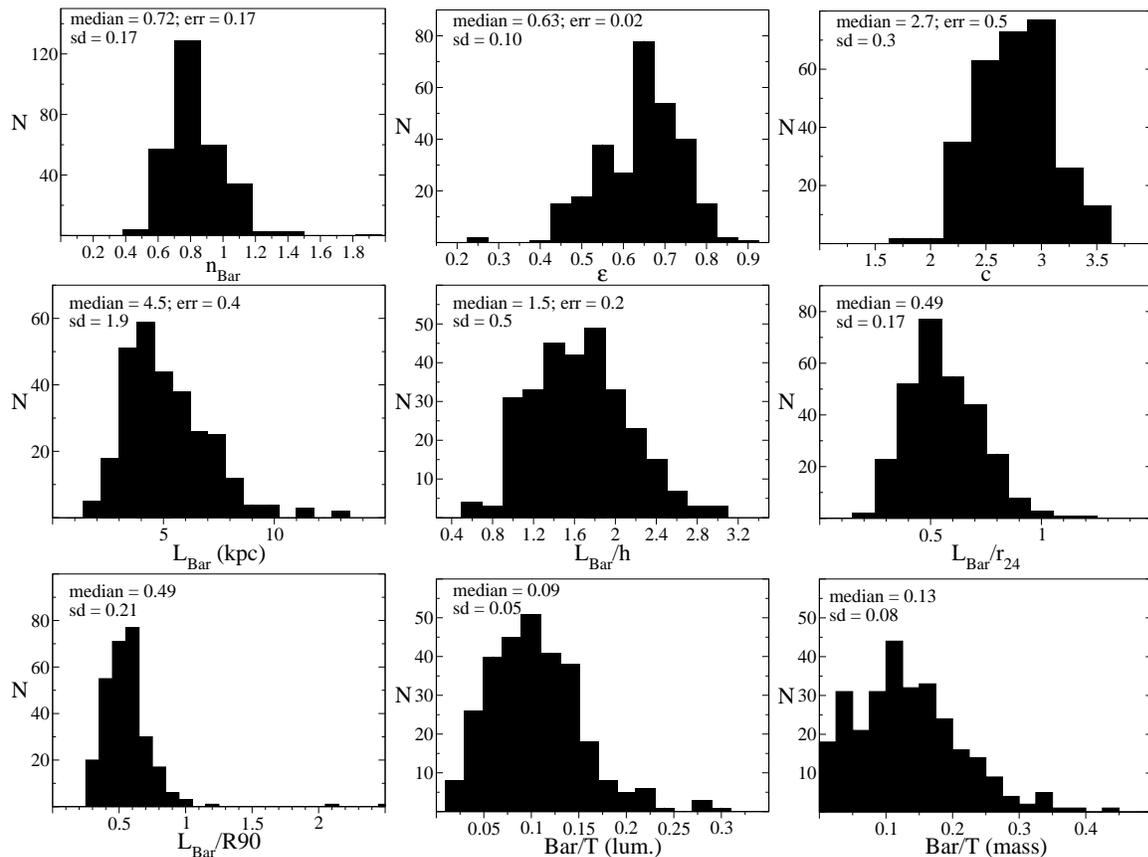


Figure 1. Distributions of several bar properties. From top to bottom and left to right: Sérsic index, ellipticity, boxiness, length (semi-major axis), length normalised by disc scale-length, length normalised by the radius of the 24 r -band mag arcsec $^{-2}$ isophote, length normalised by the radius containing 90 per cent of the total galaxy light, bar-to-total luminosity ratio, and bar-to-total mass ratio. Marked at each panel are the median and standard deviation values of the corresponding distribution, as well as the mean 1σ error of a single measurement, when available. Bin sizes are $\approx 1 - 2\sigma$.

Jogee 2007; Barazza et al. 2008; Marinova et al. 2009). This difference is due to the fact that the isophotes enclosing bars are slightly rounder than the bar itself, due to the contribution of the axisymmetric light distribution from bulge and disc, and thus the ellipse fits to those isophotes will also be rounder than the bar. In 2D fits, however, the light from bulge and disc is taken into account and thus a better estimate of the bar ellipticity can be obtained in this way. This effect was clearly demonstrated in Gadotti (2008). In fact, it was shown that ellipse fits indicate bar ellipticities which are, on average, 20% lower than those measured using 2D fits, employing the same galaxy images. Furthermore, Marinova et al. (2009) found that their ellipticity estimates are higher on average in bulgeless galaxies. Also, most bars are not well fitted with a pure ellipse, i.e. a generalised ellipse with $c = 2$, since bar boxiness peaks at $c = 3$. This is important to keep in mind when one does 2D fitting of images of barred galaxies.

The distribution of bar length peaks at values which are similar to those found by Marinova & Jogee (2007), Durbala et al. (2008) and Aguerri et al. (2009). However, the distribution presented by Barazza et al. (2008) peaks at a value which is about twice as low. This difference can likely be explained by differences in the samples and in the way bar length is defined. The sample used in Barazza et al. (2008)

is at a redshift range of $0.01 < z < 0.03$, while the sample studied here is at $0.02 < z < 0.07$. Since they also used SDSS images, this means they have better spatial resolution to resolve shorter bars. In addition, they used the position of the peak in the ellipticity profile in the bar as a measure of bar length, which is known to usually result in lower values than other definitions of bar length (see e.g. discussion in Athanassoula & Misiriotis 2002; Erwin 2005). It is also interesting to note that no bar extends to a radius larger than ≈ 3 times the disc scale length, and that almost all bars are shorter than r_{24} and R90. The distribution of the bar-to-total luminosity fraction shows a peak at ≈ 0.1 . The corresponding peak for the *mass* fraction is at a higher value, as expected, since bars are usually mostly made up of old stars. As one can see, bars can contain up to about 40% of the total galaxy stellar mass.

3.2 Bars in galaxies with classical and pseudo-bulges

As mentioned in the Introduction, classical bulges seem to be formed in relatively fast and violent processes, such as the merging of smaller units, as opposed to pseudo-bulges, which are thought to be formed from disc instabilities, such as bars. It is thus important to ask if bars in galaxies hosting pseudo-

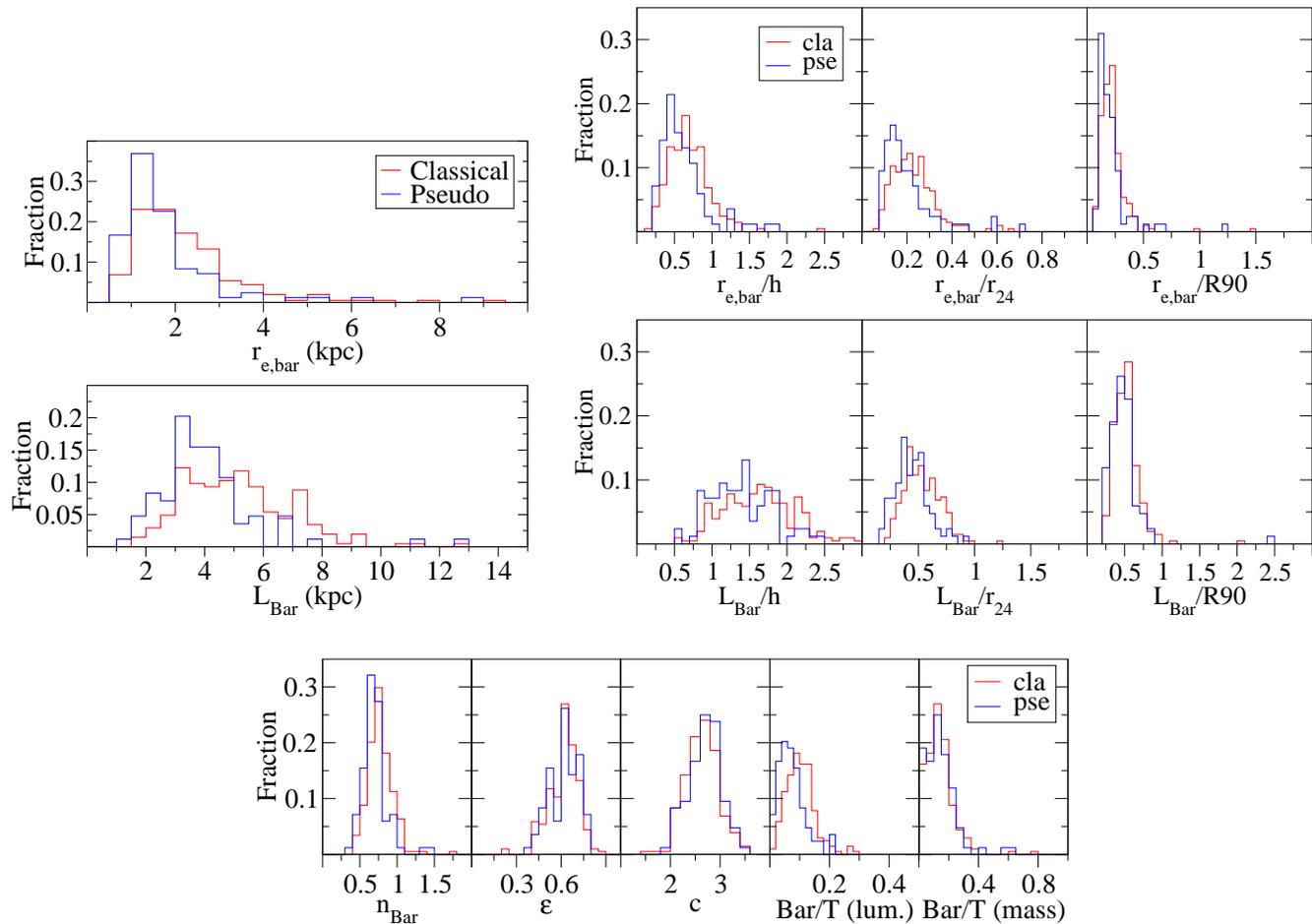


Figure 2. Distributions of bar properties for galaxies with classical and pseudo-bulges. Bars in galaxies hosting classical bulges tend to be larger than those in galaxies with pseudo-bulges. This is seen for all parameters used to define bar size, although the overlap is significant. The bar-to-total luminosity ratio is also larger in galaxies with classical bulges. Considering all other measured bar properties, including bar-to-total *mass* ratio, galaxies with classical and pseudo-bulges host similar bars.

bulges are in any sense different from their counterparts in galaxies hosting classical bulges. This question is answered in Fig. 2. The only meaningful difference I find concerns bar length. Bars in galaxies hosting classical bulges tend to be longer than bars in galaxies with pseudo-bulges. This is consistent with previous results that show that bars are longer in early-type disc galaxies (e.g. Erwin 2005; Aguerrí et al. 2009), since such galaxies generally host classical bulges, although there are many examples of early-type disc galaxies hosting pseudo-bulges (see e.g. Erwin et al. 2003; Laurikainen et al. 2007). There is also a trend in which bars in galaxies with classical bulges have larger bar-to-total luminosity ratios, but this vanishes when one considers the mass ratio.

One can also ask whether pseudo-bulges relate to their corresponding bars differently than classical bulges, and this is explored in Fig. 3. It shows that, for a fixed bar-to-total mass ratio, pseudo-bulges are on average clearly less massive than classical bulges. If pseudo-bulges are formed through disc instabilities such as bars then this suggests that indeed one needs more than disc instabilities alone to build a classical bulge.

Conversely, if bars are generally quite similar in galaxies

with classical and pseudo-bulges, as Fig. 2 indeed indicates, then there is no reason to believe that secular effects related to the evolution of the bar do not occur in galaxies with classical bulges. In fact, since bars in the latter tend to be longer, their effects might well be stronger. This suggests that the possibility of having composite bulges, i.e. galaxies hosting both a classical and a pseudo-bulge, is actually quite likely. This has been explored in Gadotti (2009b), where some bulges were found to have mixed properties: while they appear classical from a structural point of view, the presence of a spectral signature of young stellar populations is typical of pseudo-bulges. Such combination of features naturally appears if one has a more massive and extended classical bulge component, in which a small and young pseudo-bulge is embedded. The classical bulge component produces an imprint in the structural analysis, while the young stellar population from the pseudo-bulge component shows up in the spectral analysis. It seems natural that a disc galaxy can undergo the processes that lead to the formation of a classical bulge *and* those that lead to a pseudo-bulge. Curiously, Nowak et al. (2010) describe two examples of galaxies with composite bulges, in which the classical component is actually smaller.

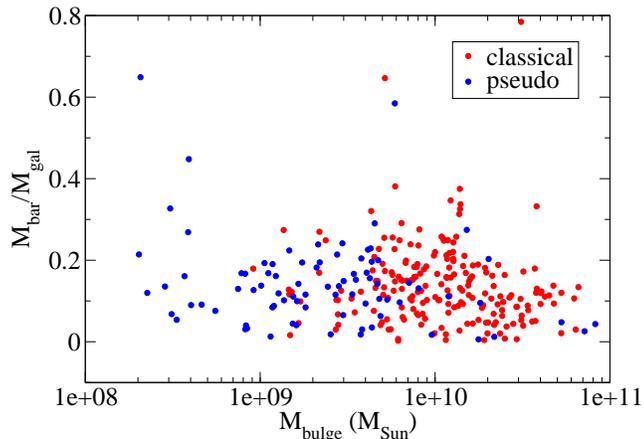


Figure 3. Stellar mass of the bar divided by stellar mass of the galaxy (i.e. the bar-to-total mass ratio) plotted against bulge mass, for classical and pseudo-bulges, as indicated. Clearly, for a fixed bar-to-total mass ratio, pseudo-bulges are on average less massive than classical bulges.

3.3 Bar strength and growth

In this section, I will look for correlations using the structural properties of bars and their host galaxies that can serve as a test to the theoretical predictions on the secular growth of bars. Essentially, one should check if bars indeed grow longer and stronger in time, and thus one first needs to define bar strength. One readily accessible measure of bar strength is the bar ellipticity. All things equal, a more eccentric bar induces stronger non-axisymmetric forces and torques on the otherwise close to axisymmetric potential of a disc galaxy (see e.g. Martin 1995, and references therein). A more sophisticated measure of bar strength involves directly estimating the torques induced (Block et al. 2004; Laurikainen et al. 2004; Buta et al. 2005). Such torques are normalised by the axisymmetric component of the galaxy potential, which means that, all things being equal, a bar in a galaxy with a more massive bulge is weaker (according to this estimate) than an identical bar in a galaxy with a less massive bulge. This estimate is thus more related to the impact of the bar on the overall galaxy evolution rather than to strength of the bar itself. Hence, in the context of this study, bar ellipticity is a more useful measure.

Evidently, bar mass, length and even bar boxiness are related to bar strength. In fact, the simulations in Athanassoula & Misiriotis (2002) indicate that bars grow stronger in time by getting longer, more eccentric and more boxy, which is consistent with the results from Fig. 4, which shows that bar ellipticity and boxiness are correlated (for both galaxies with classical and pseudo-bulges). Since both parameters are related to bar strength, I will use the product of the two, i.e., $\epsilon \times c$, as a measure of bar strength. I find out that the trends discussed below are stronger when I use $\epsilon \times c$ as a measure of bar strength rather than either ϵ or c alone. However, there is no improvement if I use $\epsilon \times c$ times the bar mass or the bar-to-total luminosity and mass ratios.

With a definition for bar strength at hand, I now need a definition for bar size. Figure 5 shows, consistently with previous results, that bar size correlates with galaxy size, and this is regardless of whether one uses the bar semi-major

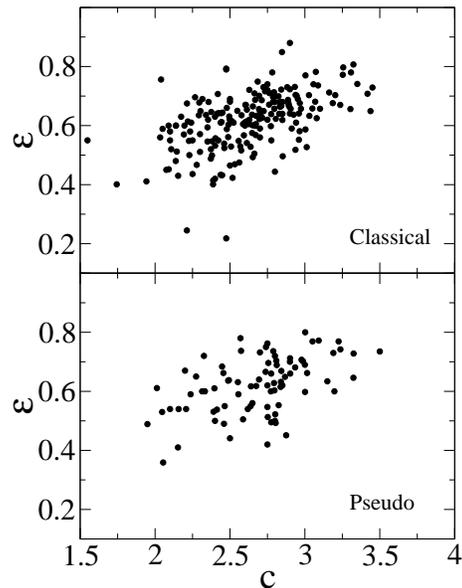


Figure 4. Correlation between bar ellipticity and boxiness for galaxies with classical and pseudo-bulges, as indicated.

axis L_{bar} , or the bar effective radius $r_{e,bar}$, for the former and h , r_{24} or R90 for the latter. It also shows that L_{bar} and $r_{e,bar}$ are well correlated, as expected. Because larger bars are in larger galaxies, a definition for bar size in the context of this study has to be normalised by galaxy size. Figure 5 shows that one can use any combination between L_{bar} or $r_{e,bar}$ and h , r_{24} or R90 to define the normalised bar size.

Figure 6 shows that there is a positive trend between all applicable definitions of normalised bar size and bar strength for both galaxies with classical and pseudo-bulges. I.e., longer bars tend to be stronger, consistent with the expectations from theoretical work, although clearly there is considerable scatter in some of the plots.

Figure 7 shows that bar size also correlates with bulge size (see also Athanassoula & Martinet 1980), which is perhaps not too surprising, but, interestingly, this correlation depends on bar ellipticity. In fact, the correlation is weaker for bars with $\epsilon > 0.7$. Surprisingly, $r_e/r_{e,bar}$ shifts to lower values for more eccentric bars. This effect is consistent with the previous finding that more eccentric, stronger bars are longer, and will be further explored below.

We have already seen that longer bars are stronger, but the theoretical work I aim to test here also predicts that longer and stronger bars are dynamically old, i.e. they have had more time to evolve. This would happen, for instance, to a bar that resides in a galaxy that have reached a dynamically matured state earlier.² Given the current cosmological picture of galaxy evolution, more massive galaxies reach this point earlier (something referred to as “downsizing” – see discussion in Sheth et al. 2008). But more massive galaxies tend to be those in which the bulge-to-total ratio is larger (see e.g. Gadotti 2009b), and thus if the theoretical work is correct one should find a trend in the sense that longer bars are found in galaxies with larger B/T . This is consistent with

² This assumes that bars are long-lived structures and not recurrent as in the picture proposed by Bournaud & Combes (2002).

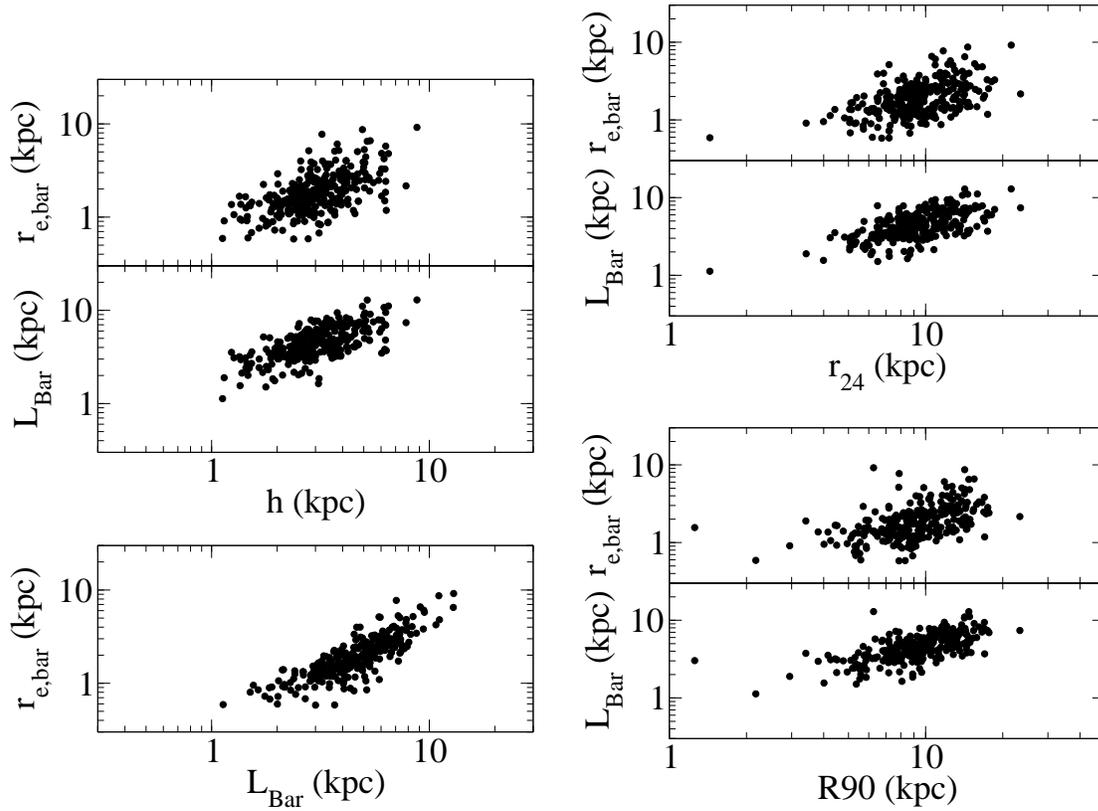


Figure 5. Correlations between the different parameters used to define bar size. They show that, as expected, larger bars reside in larger galaxies. In addition, bar effective radius is equivalent to bar length, and h , r_{24} and $R90$ can be similarly used to obtain normalised bar sizes.

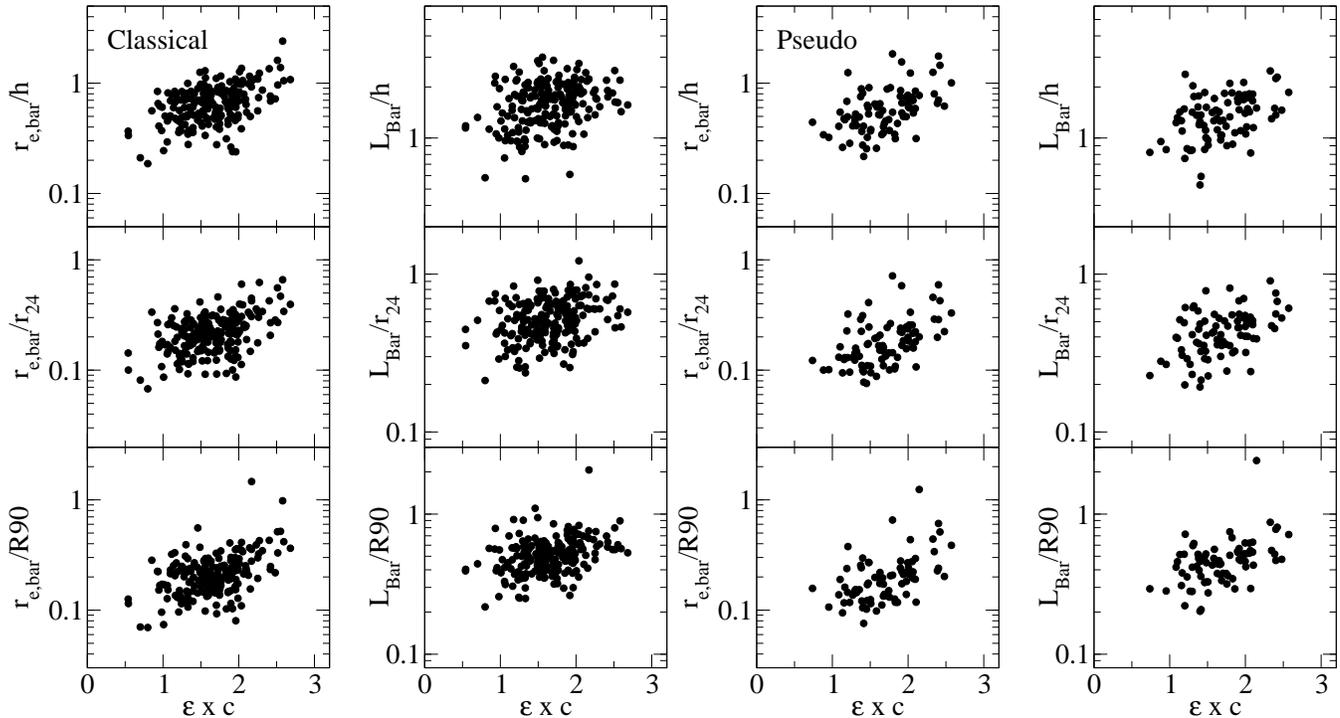


Figure 6. All different measures of normalised bar size plotted against bar strength for galaxies with classical and pseudo-bulges, as indicated. Although a few plots display large scatter, it is clear that longer bars tend to be stronger.

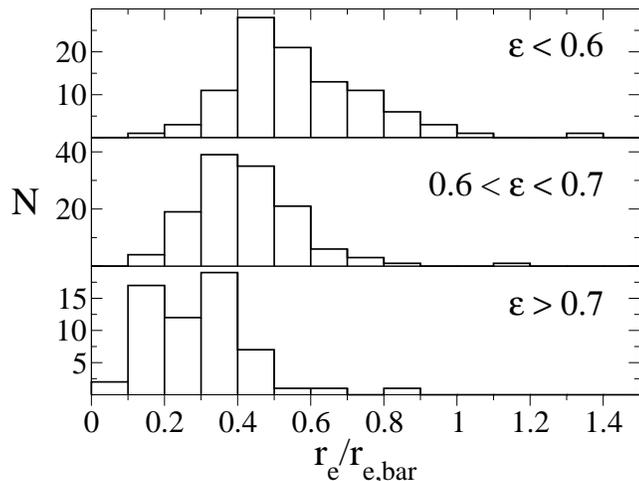


Figure 7. Histograms of the ratio between bulge effective radius and bar effective radius for bars in three bins of ellipticity, as indicated. It is clear that both parameters are correlated, at least when $\epsilon < 0.7$. Note that the peaks in these distributions shift successively to lower values from bars with $\epsilon < 0.6$ to bars with $0.6 < \epsilon < 0.7$ and finally to bars with $\epsilon > 0.7$.

previous observational results that longer bars tend to be in early-type galaxies, but since I have measurements of B/T I can test it directly.

Figure 8 shows the different measures of normalised bar size plotted against bulge-to-total ratio. This is done for bars in three bins of ellipticity, as in Fig. 7, for reasons that will be clear shortly below. Although there is considerable scatter in some of these plots, one sees clearly that longer bars tend to be hosted by galaxies with more conspicuous bulges, which is thus consistent with the theoretical expectations. If these plots are done with all bars grouped together, regardless of their ellipticities, this relation is more difficult to see. The reason for that is that bars with different ellipticities follow parallel lines in these plots, and their combined scatter dilutes the relation. This is easier to see in the bottom right panels in Fig. 8. The top panel shows L_{Bar}/r_{24} plotted against B/T , with colour coding indicating bar ellipticity. The black solid line is a fit to all points. The bottom panel shows separate fits to these data points, separated in different ellipticity bins. The solid, coloured lines are fits to these points, produced with the slope fixed at the value found when the fit is done to all points and regardless of bar ellipticity, such that the change in intercept is made more clear. It should be noted, however, that leaving the slope free in the fit does not change the outcome substantially, and that one sees this effect concerning the intercept in these relations for all measures of normalised bar size.

4 DISCUSSION

4.1 Possible biases

Some of the physical parameters explored in this study are difficult to measure, such as bar boxiness, in particular considering that the physical spatial resolution of the images used is relatively poor. In Gadotti (2008), I presented a study using images of 14 nearby galaxies ($z \sim 0.005 - 12$

of them barred galaxies) and images of the same galaxies artificially redshifted to $z = 0.05$, which results in the same physical spatial resolution of the sample used here. The redshifted and original images were decomposed using the same methodology as in Paper I. By comparing the results from such decompositions, it was verified that parameters such as disc scale length, bulge effective radius, bulge-to-total ratio and bar-to-total ratio can be reliably estimated in the low resolution regime. Bulge parameters are particularly sensitive to seeing effects, though, if $r_e < 0.8 \times \frac{1}{2} \text{FWHM}$, but, as shown in Paper I, 97% of the bulges in the sample have r_e above this threshold.

I can now use the results from the decompositions in Gadotti (2008) to verify if the other bar structural parameters discussed here can also be reliably obtained in this low resolution regime. Figure 9 thus compares the estimates for bar Sérsic index, length, ellipticity and boxiness from the original and artificially redshifted images of the 12 barred galaxies in Gadotti (2008).³ It shows that estimates of such parameters are indeed robust even at the resolution of the images used here. No clear systematic biases are seen, except for a tendency for lower ellipticities, as measured in the redshifted images. This likely results from the rounding and dilution of the bar light at low resolution. It might suggest that the peak in the distribution of bar ellipticity in Fig. 1 is slightly offset to lower values. However, the difference is on average only a few percent, and is the same through the whole range of values obtained, and thus not harmful to the results presented here.

One could also be worried that bars might show up more eccentric and boxy in galaxies with less conspicuous bulges, where there is less contamination from bulge light in the bar isophotes. While this is a concern for results based on ellipse fits, it should be stressed that the bulge light is modeled in image decomposition, and thus such concern does not apply here (see fig. 6 and discussion in Gadotti 2008). Further, the results shown above point out the opposite: more eccentric and boxy bars are longer and hosted by bulge-dominated galaxies.

Finally, in the same context, one could argue that higher values of ellipticity and boxiness are easier to obtain in the case of longer bars, since these have a larger fraction of themselves away from the bulge dominant light. However, Fig. 9 shows that boxiness can be reliably measured at the low resolution regime, i.e. even when bar light is diluted. Furthermore, considering the four galaxies that have their ellipticities underestimated at the low resolution regime (see lower left panel in Fig. 9), one sees no tendency for them to be particularly short (these galaxies are NGC 4314, 4394, 4477 and 5701).

4.2 Bar length in simulations

As discussed in Erwin (2005), to compare bar lengths in observations and simulations one should use L_{Bar}/h . He provides this value for a number of models from the literature (his Table 8) and argues that there is clearly a lack of short

³ Note that two bars in this sample become overly faint in the redshifted images and are thus not fitted in these images.

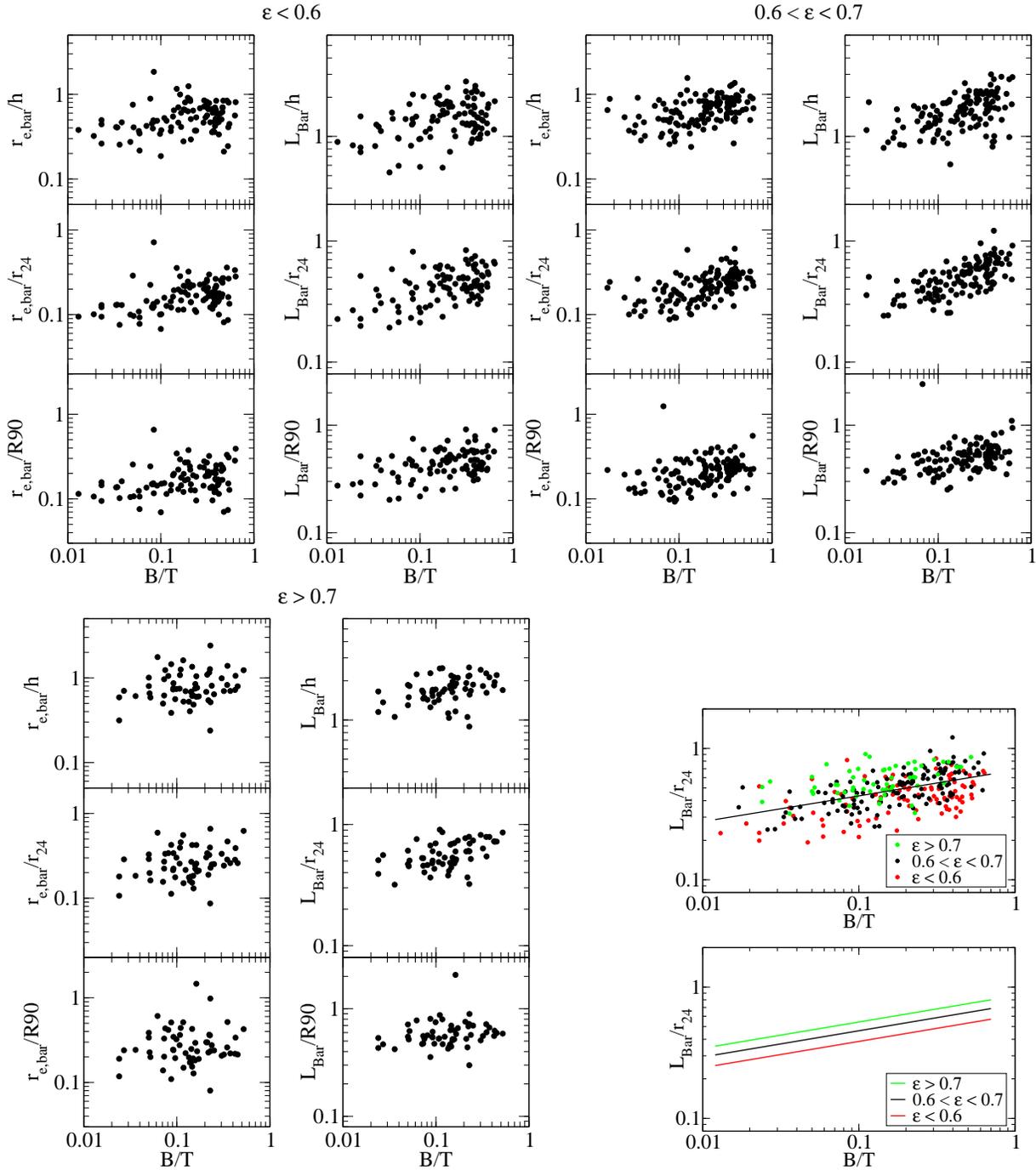


Figure 8. All different measures of normalised bar size plotted against bulge-to-total ratio, for bars in three bins of ellipticity, as indicated. Although some panels show considerable spread, in most of them a clear relation is seen in the sense that longer bars tend to reside in galaxies with more conspicuous bulges. Bars with different ellipticities describe parallel lines in this relation. This is better seen in the lower right panels: the top one shows the data for all bars in the panels where L_{Bar}/r_{24} is plotted against B/T , colour coded by bar ellipticity (the solid line is a fit to all points); the bottom one shows separate fits in the different ellipticity bins, with the slope fixed at the value in the fit to all points.

bars in simulations, as compared to observations. Considering only those models in which a live dark matter halo is used (Berentzen et al. 1998; Athanassoula & Misiriotis 2002; Valenzuela & Klypin 2003; Holley-Bockelmann et al. 2005) one sees that indeed most of them produce bars which are in high end tail of the distribution of L_{Bar}/h shown in

Fig. 1. In fact, Berentzen et al. (1998) and Athanassoula & Misiriotis (2002) report results in which $L_{\text{Bar}}/h > 3$, a value not found in the sample studied here, which is nevertheless biased towards *large* bars.

The models that produce the shortest bars are models A_1 ($L_{\text{Bar}}/h = 1.4 - 1.5$), A_2 ($L_{\text{Bar}}/h = 1.1 - 1.3$) and B

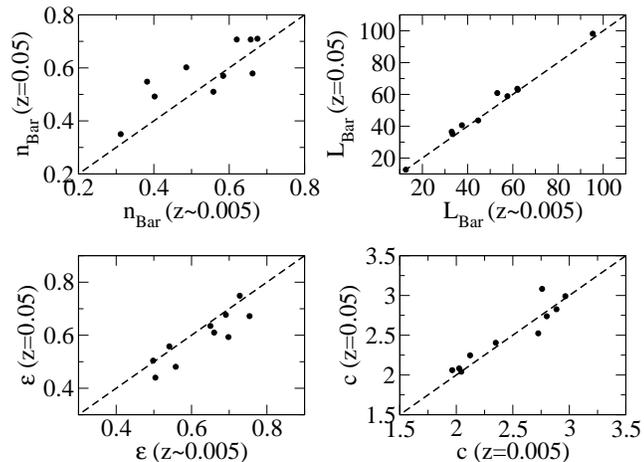


Figure 9. Bar structural parameters, as determined with the redshifted images, plotted against the same parameters obtained with the original images. The dashed lines indicate a perfect correspondence. L_{Bar} is in arcseconds, and measurements from the redshifted images are scaled back to the original galaxy distance. No clear systematic biases are seen, except for a trend in which bar ellipticities, as measured in the redshifted images, have slightly lower values, compared to those measured with the original images. The difference is on average only a few percent, and is the same through the whole range of values obtained, and thus is not harmful to the results presented here.

($L_{\text{Bar}}/h = 0.8 - 1.0$) in Valenzuela & Klypin (2003). The main difference between models A₁ and A₂ is that the latter is kinematically colder than the former in the central region. Model B has a smaller halo and a more massive disc. It appears that a less efficient transfer of angular momentum between disc and halo is the cause of these bars being short.

A related issue is that at least in some models (see e.g. Martinez-Valpuesta et al. 2006) long bars are formed quickly, i.e. after 1 – 2 Gyr only, while the results above suggest that long bars are old. As both bar size and disc size change in time, it would be most useful if theoretical work presents how L_{Bar}/h (or L_{Bar}/r_{24}) evolve with time.

4.3 Secular evolution of bars

Although there seem to be some quantitative disagreement between theory and observations concerning bar sizes, the results above suggest a qualitative agreement: the general trend showing bars getting longer and stronger with time, seen in simulations, is consistent with the observational results presented here. This is not the whole picture, though. As discussed in the Introduction, some simulations show that bars can get very large quite fast, quickly become shorter at the onset of the first vertical buckling instability, and then start growing slowly again. Furthermore, simulations taking the effects of gas into account show that the secular growth of bars can be halted, or even reversed, if the gas content is enough.

Since the sample studied here is biased towards large bars, it is likely that most of these bars have evolved enough, and already went through the first vertical buckling instability. For the same reason, and also because all galaxies in the sample have stellar masses above $10^{10} M_{\odot}$, the gas con-

tent in these barred galaxies is likely on the lower end of the corresponding distribution. This might have helped to make the trends in Figs. 6, 7 and 8 more apparent. Nevertheless, the complicating effects from gas dynamics and the vertical buckling are probably contributing to the spread seen in these figures. A similar work, with a sample of short bars, in gas-rich system, is likely to shed light on these issues.

With a different methodology, Elmegreen et al. (2007) found that normalised bar size correlates with bar strength and galaxy central density, and also conclude that their results “suggest that bars grow in length and amplitude over a Hubble time”. Sheth et al. (2008) found that more massive galaxies have their bars in place at higher redshifts, whereas less massive galaxies form bars at later times. They suggest that discs in more massive systems reach a dynamical maturity earlier than those in less massive systems, and thus are able to form bars at earlier times, in qualitative agreement with the results and interpretations given here.

Observational results like those in e.g. Rautiainen et al. (2005, and references therein) indicate that most bars end near their corotation radius. Along with our current understanding of the orbital structure in barred galaxies, this tells us that bars cannot grow longer if they do not slow down. Therefore, the results presented here also suggest that bars slow down with time, which is again qualitatively consistent with theory, and with bulge prominence. Such a relation between the bar pattern speed Ω_{B} and B/T is in the sense that bars rotate slower in galaxies with more prominent bulges, since these galaxies have longer bars. This relation can also be seen as a dependence of Ω_{B} on Hubble type, although there is some scatter in the relation between B/T and Hubble type (e.g. Laurikainen et al. 2007; Graham & Worley 2008). On direct observational grounds, no solid conclusion can currently be drawn about a dependence of bar pattern speed on Hubble type, and this is due to the difficulty of obtaining reliable estimates of Ω_{B} , in particular for late-type galaxies (see e.g. Gerssen et al. 2003; Treuthardt et al. 2007; Corsini 2010).

An outstanding and unforeseen new result in this study is the existence of parallel tracks in the correlation between bar normalised size and B/T , for bars with different ellipticities (see Fig. 8). A straightforward way of interpreting the existence of these parallel tracks is to conceive that bars should form with different normalised sizes and ellipticities, and then follow a somewhat parallel growth. This is a new aspect that can be investigated with theoretical work. It would be very interesting to study bars formed with different normalised sizes and ellipticities in simulations, and check whether they follow similar evolutionary paths.

5 CONCLUSIONS

I have explored the results from detailed 2D image decomposition of nearly 300 barred galaxies with stellar masses above $10^{10} M_{\odot}$, at $z \sim 0$, concerning mainly the structural properties of bars. This results in a thorough description of bonafide stellar bars in the local universe, including distributions of bar Sérsic index, ellipticity, boxiness, length and bar-to-total luminosity and mass ratios. The interplay between bars and the bulges and discs in their host galaxies was also examined. Such detailed characterization of local

bars can be compared with similar results from studies with samples at higher redshifts, in order to directly investigate how the structure of barred galaxies evolve in time. It can also be compared to results from theoretical work, in order to assess how well theory can describe the structural properties of such bars. Furthermore, a complete description of the properties of local bars is useful to insert ad hoc models of bars in a theoretical framework.

Bars in galaxies hosting classical and pseudo-bulges share similar properties, except that bars in the former are on average larger than those in the latter, considering both absolute and normalised sizes. This is consistent with previous results comparing bar sizes in early- and late-type disc galaxies, as usually the former host classical bulges, whereas the latter host pseudo-bulges. For a fixed bar-to-total mass ratio, pseudo-bulges are on average significantly less massive than classical bulges. This indicates that, if pseudo-bulges are formed through disc instabilities such as bars, then more than that is necessary to build a classical bulge.

Normalised bar size is correlated with bar strength and bulge-to-total ratio, qualitatively consistent with expectations from theoretical work, which suggests that evolved bars grow longer and stronger in time, lowering their pattern speed, at least when effects caused by gas dynamics are sufficiently small. Bars with different ellipticities follow parallel tracks in the trend between normalised bar size and B/T , suggesting that bars form with different normalised sizes and ellipticities but still follow similar evolutionary paths.

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