

Critical Tests of Theory of the Early Universe using the Cosmic Microwave Background

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Breakthrough in Cosmological Research

- We can actually **see** the physical condition of the universe when it was very young

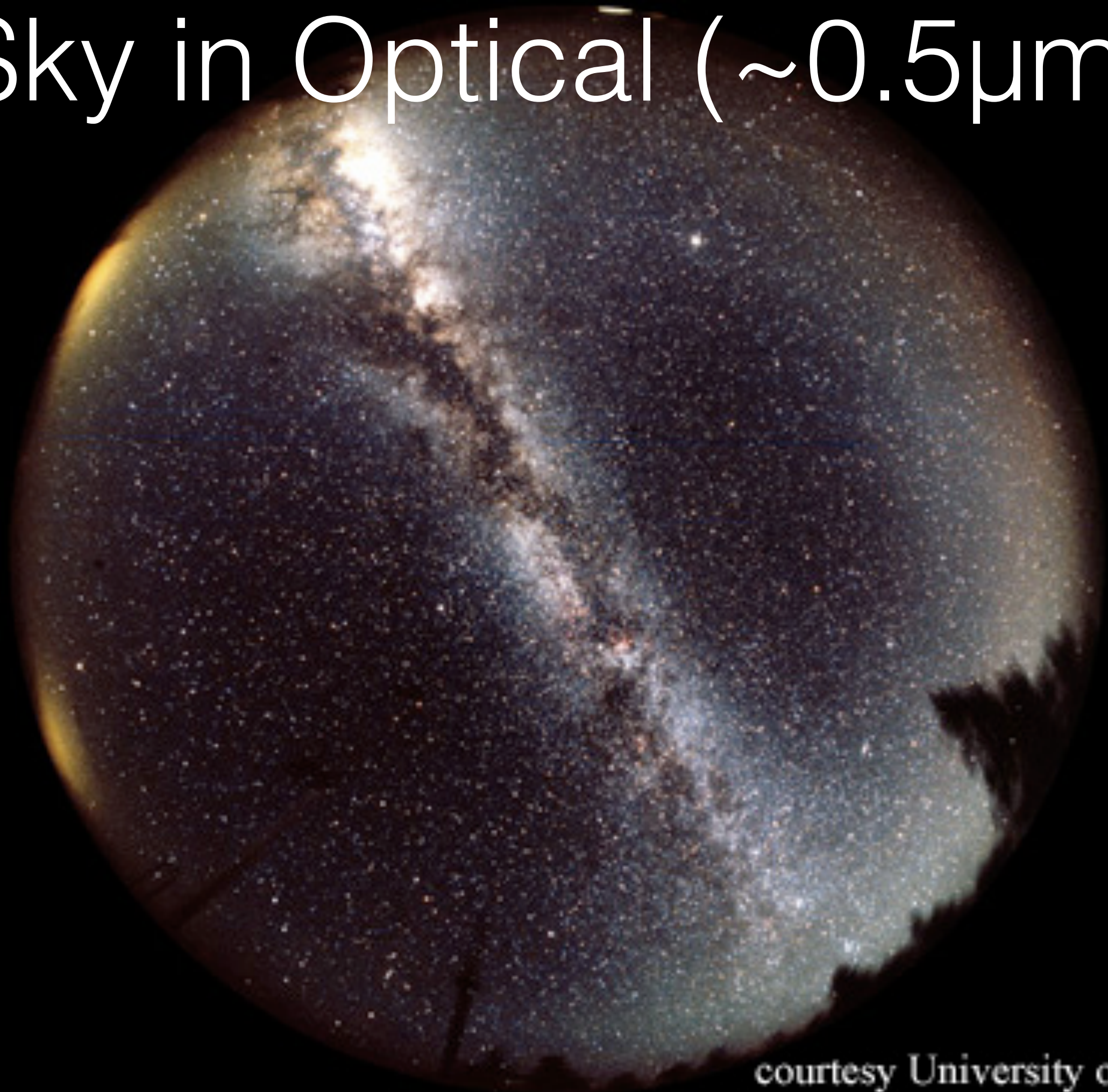


From "Cosmic Voyage"

Where did photons go?

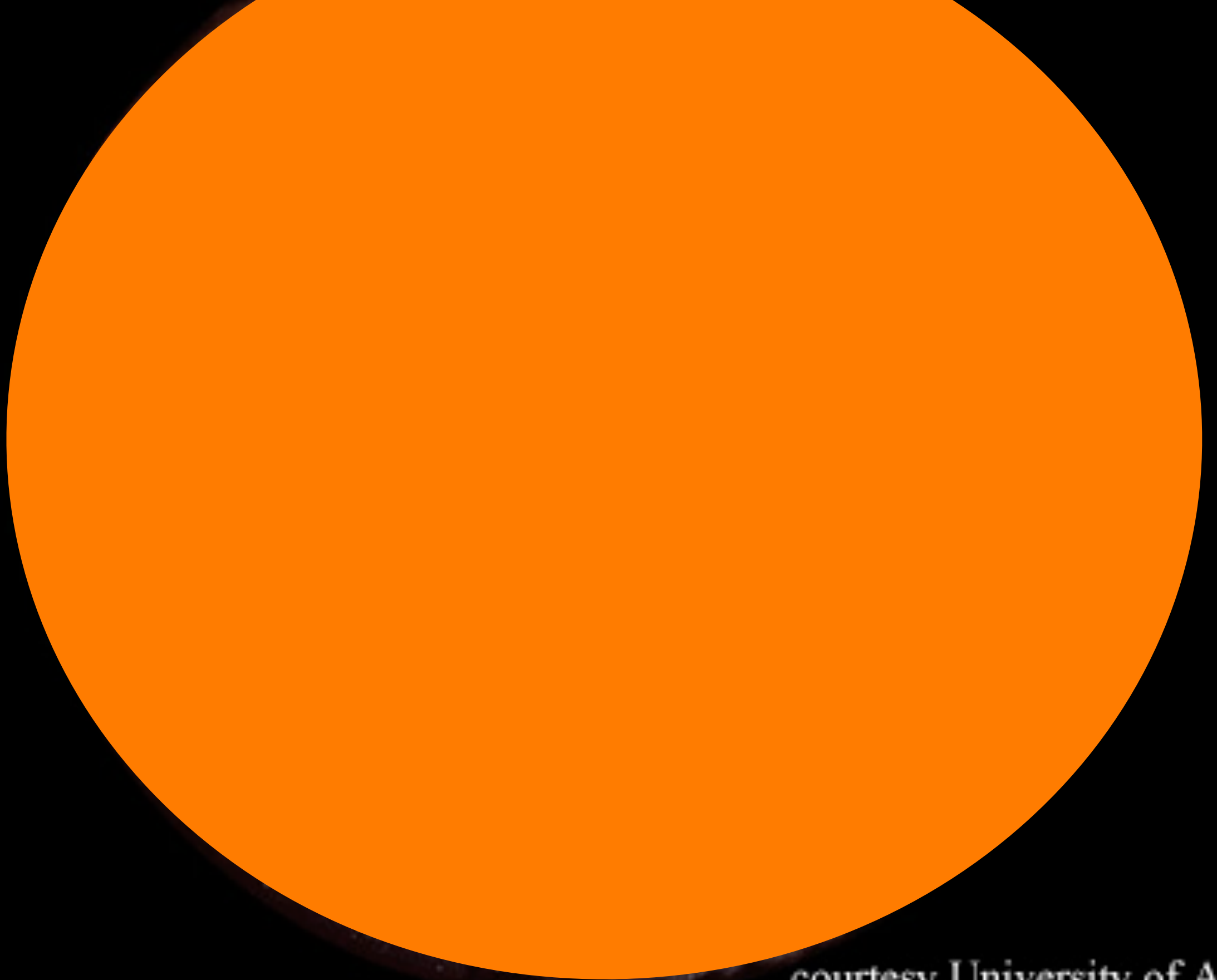
- The Universe was hot, dense, bright in visible wavelengths. Where are these photons now?

Sky in Optical ($\sim 0.5\mu\text{m}$)



courtesy University of Arizona

Sky in Microwave ($\sim 1\text{mm}$)



courtesy University of Arizona

Sky in Microwave ($\sim 1\text{mm}$)

*Light from the fireball Universe
filling our sky (2.7K)*

**The Cosmic Microwave
Background (CMB)**

410 photons
per
cubic centimeter!!



Full-dome movie for planetarium

Director: Hiromitsu Kohsaka

HORIZON

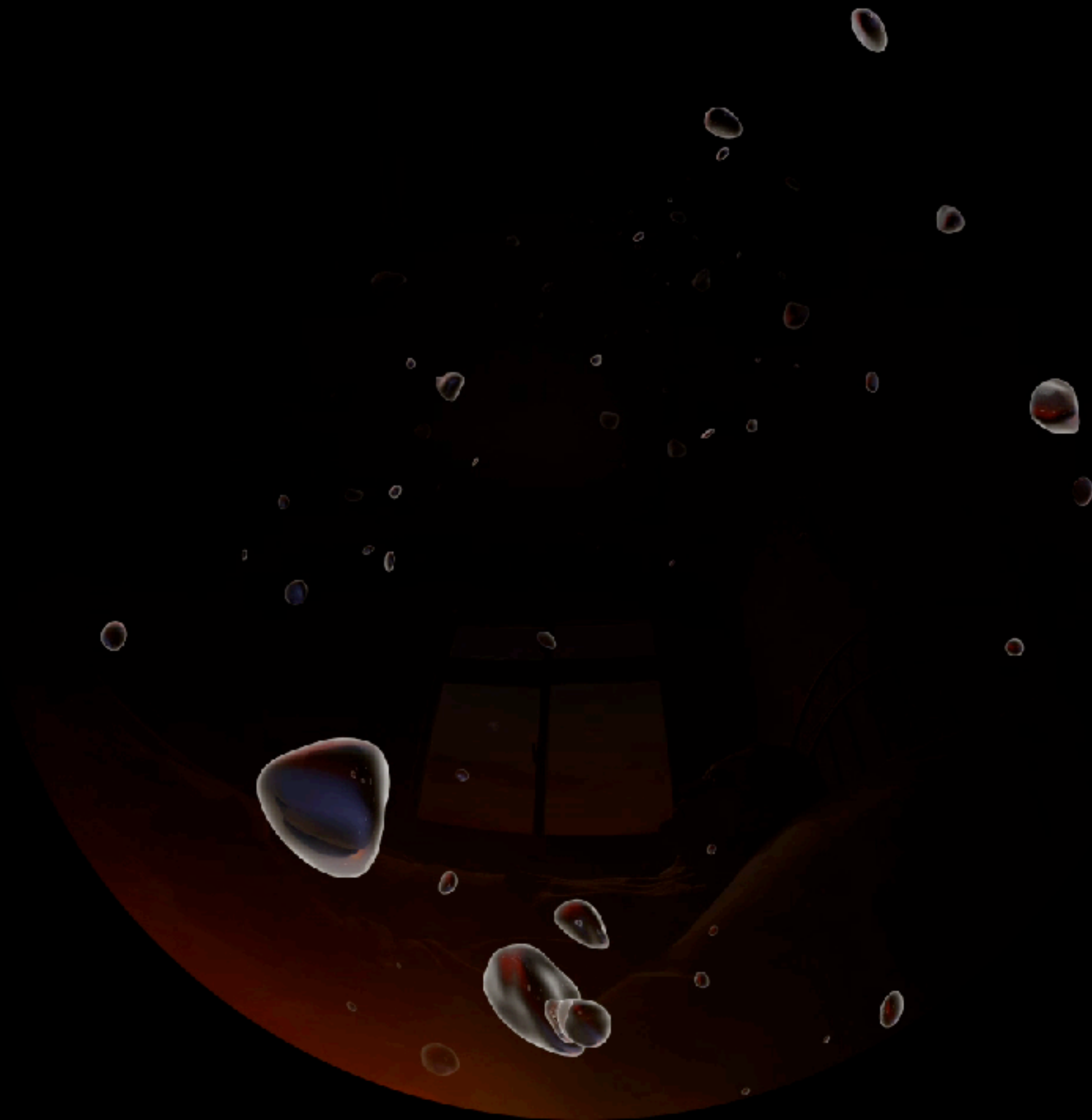
Beyond the Edge of the Visible Universe

**Nominated for one of 12 movies at
“FullDome Festival” at Jena, May 23–26, 2018**



2:27 / 2:51



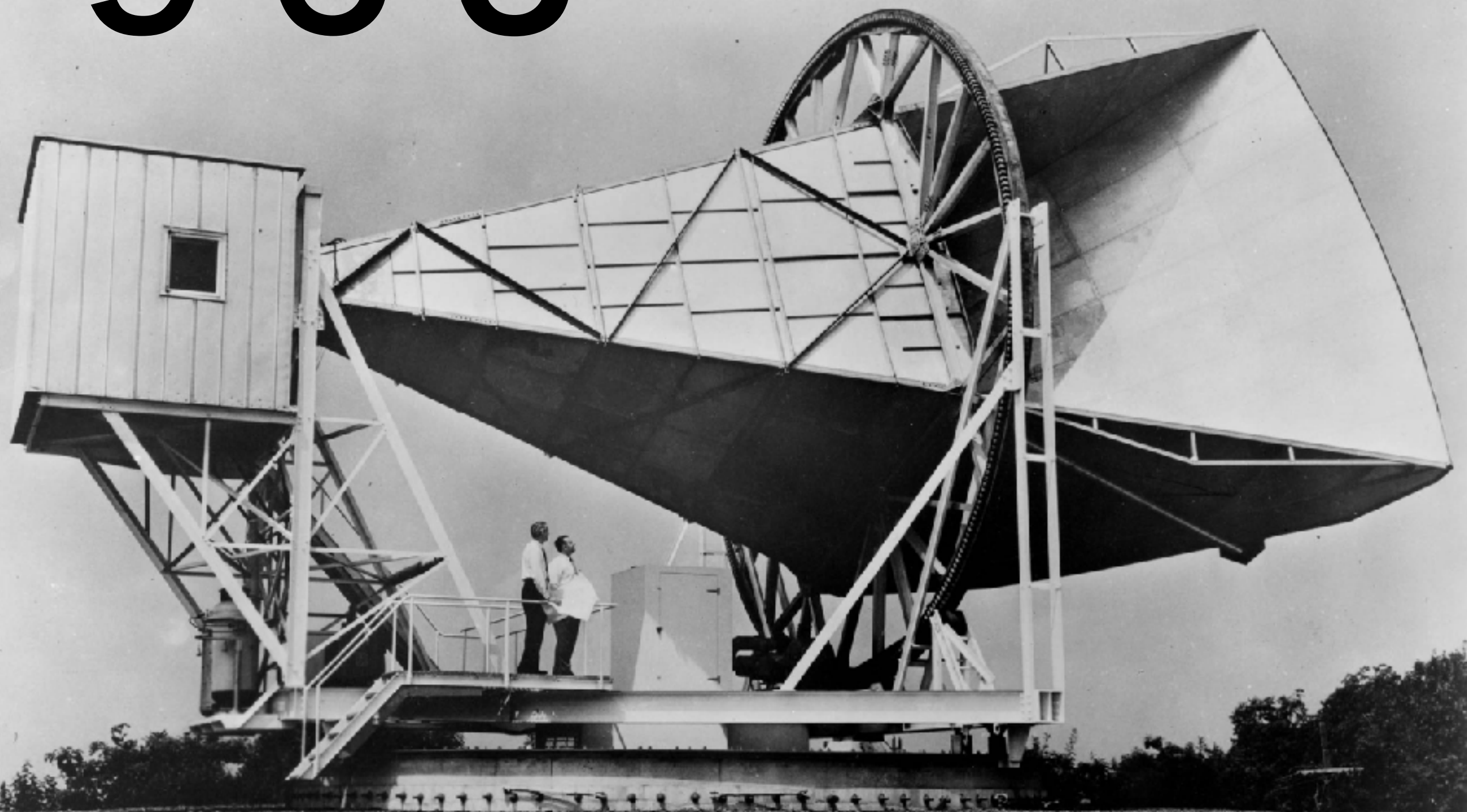


A photograph of Prof. Hiranya Peiris, a woman with long dark hair, wearing a black cardigan over a black top with a colorful patterned collar. She is holding a vintage, light-colored television set with a handle. The television screen displays a blue, grainy, noisy pattern. The background is dark, and a wooden ledge is visible at the bottom.

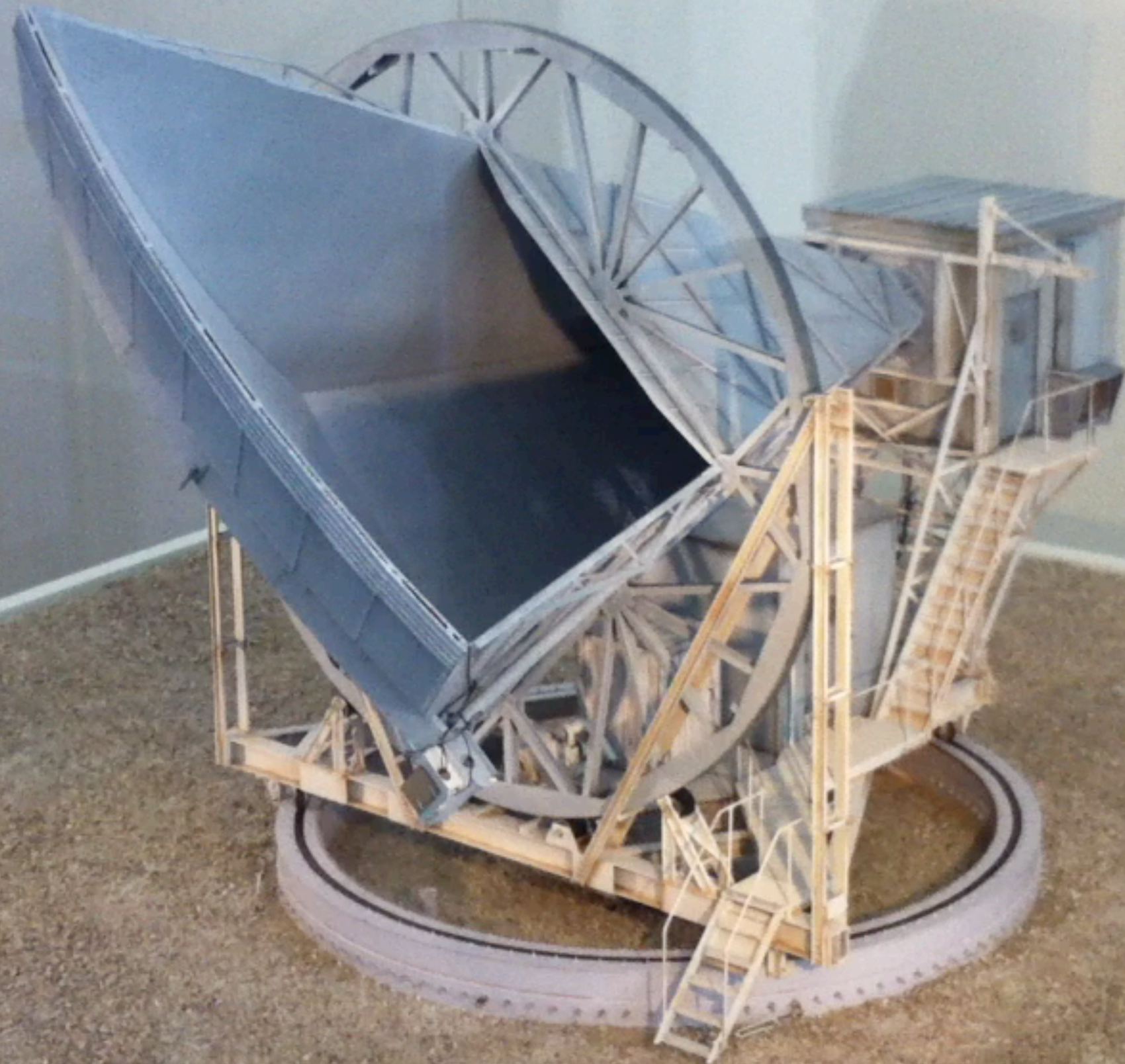
Prof. Hiranya Peiris
(Univ. College London)

All you need to do is to detect radio waves. For example, 1% of noise on the TV is from the fireball Universe

1965



1:25 model of the antenna at Bell Lab
The 3rd floor of Deutsches Museum



The real detector system used by Penzias & Wilson

The 3rd floor of Deutsches Museum



**Donated by Dr. Penzias,
who was born in Munich**



Horn antenna

Calibrator, cooled
to 5K by liquid helium

Amplifier

Recorder

Hornantennenanschluss

Hohlleiterzug

V
Vergleichs-
quelle

R
Rauschquelle

F
Frequenzmischer
und Verstärker

M
MASER-Verstärker

Schreiber

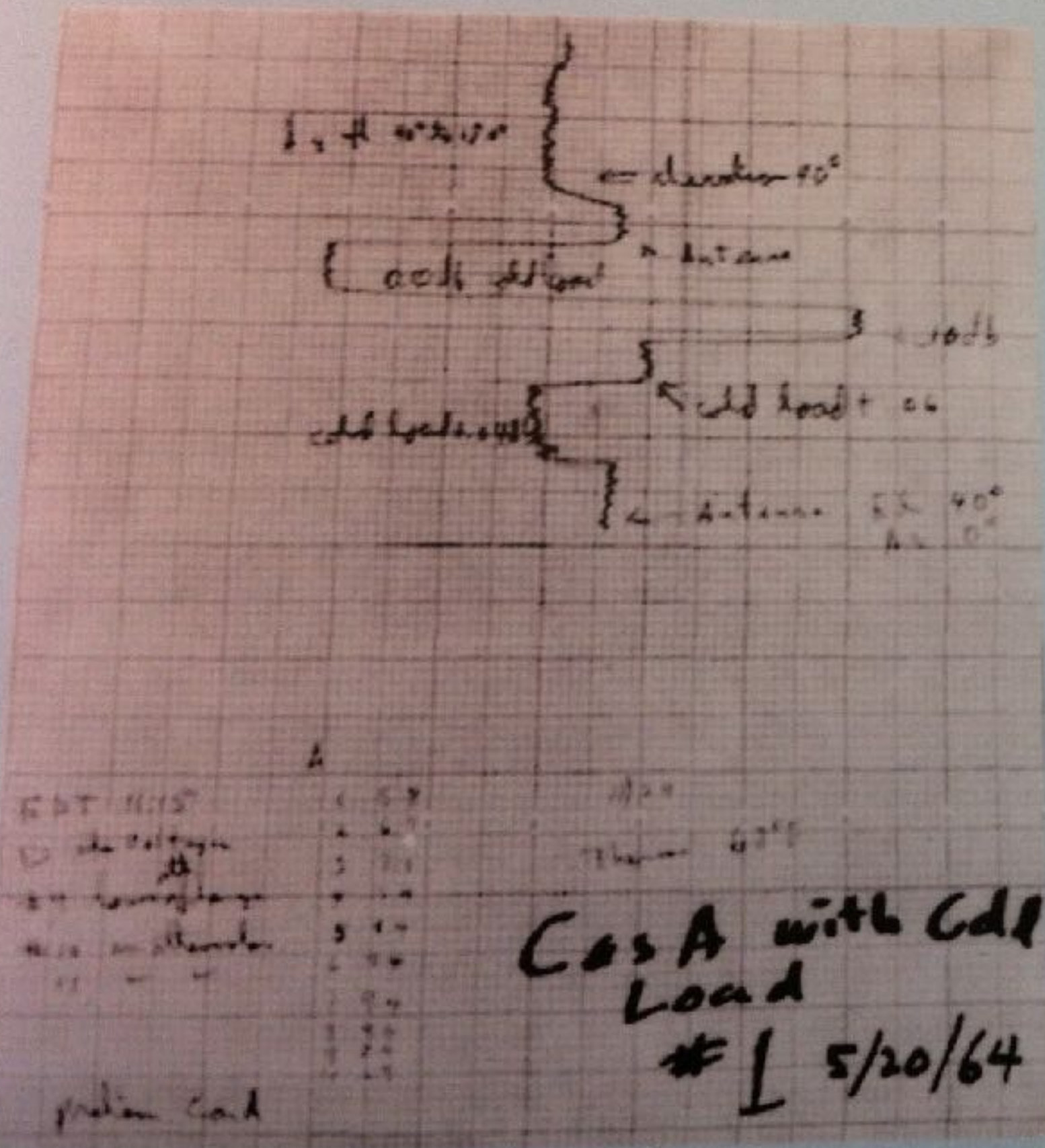
many
radio

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May 20, 1964 CMB Discovered

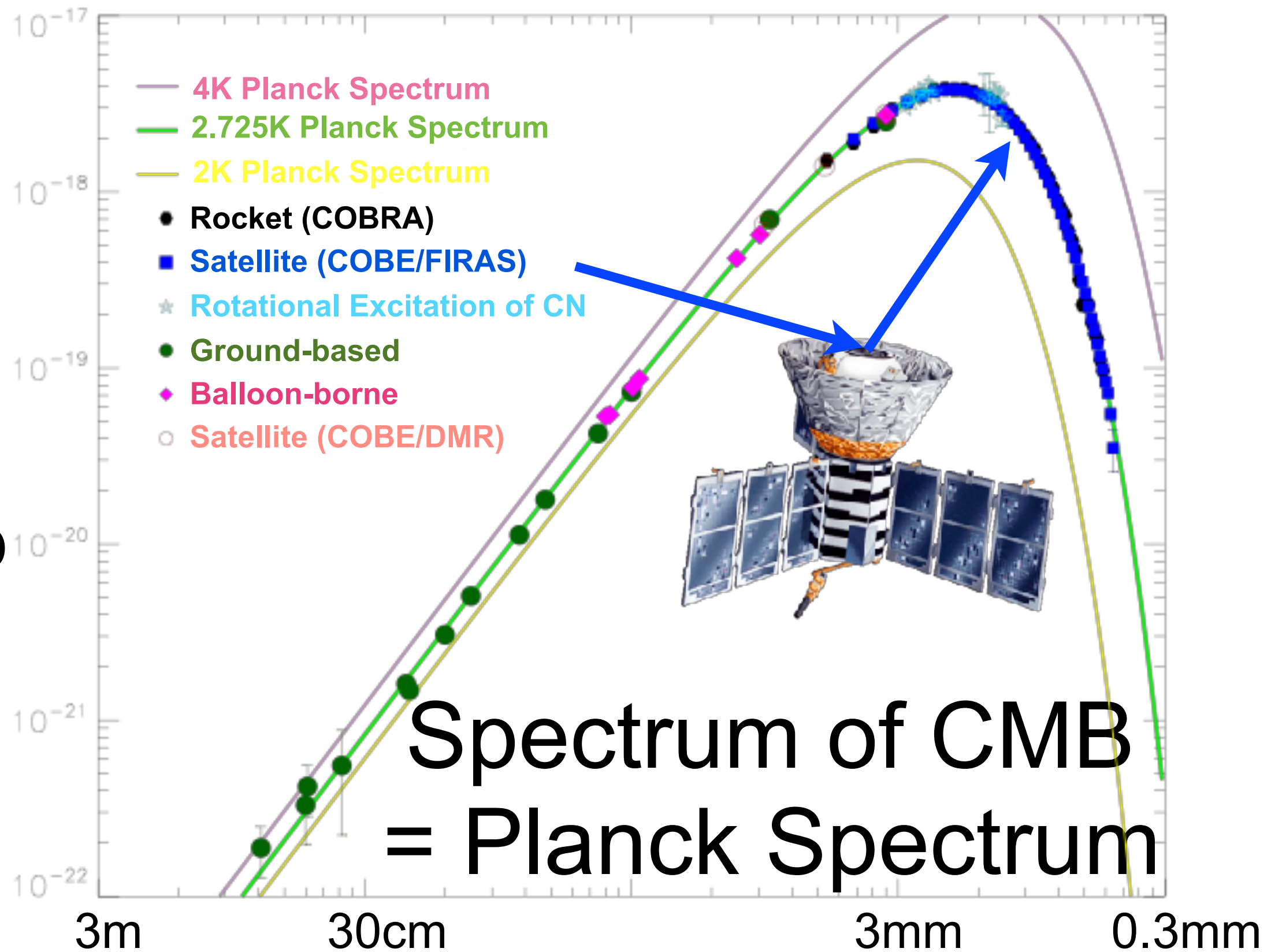
$$6.7 - 2.3 - 0.8 - 0.1 \\ = 3.5 \pm 1.0 \text{ K}$$

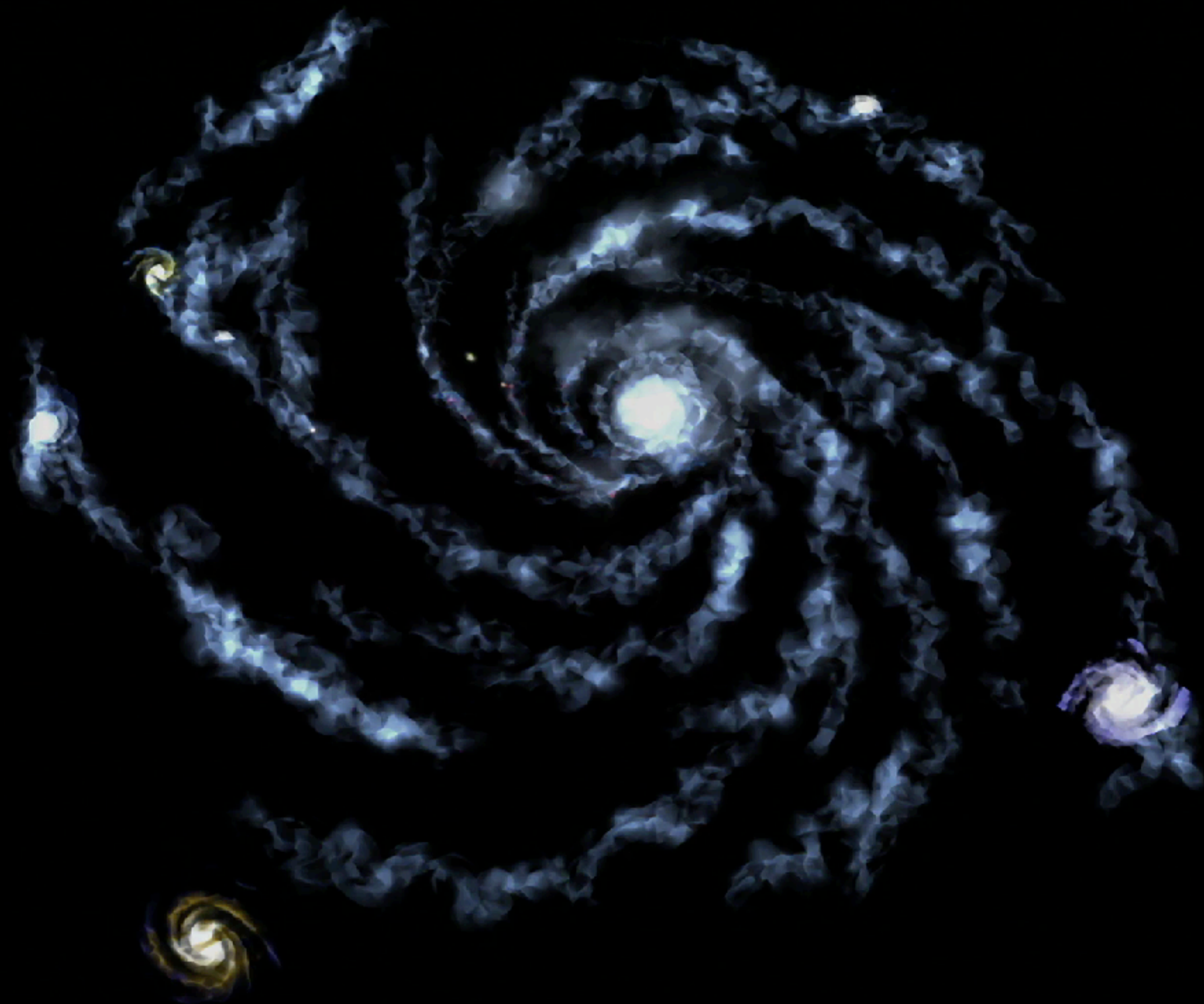


Schreiberaufzeichnung der ersten Messung des Mikrowellenhintergrundes am 20.5.1964

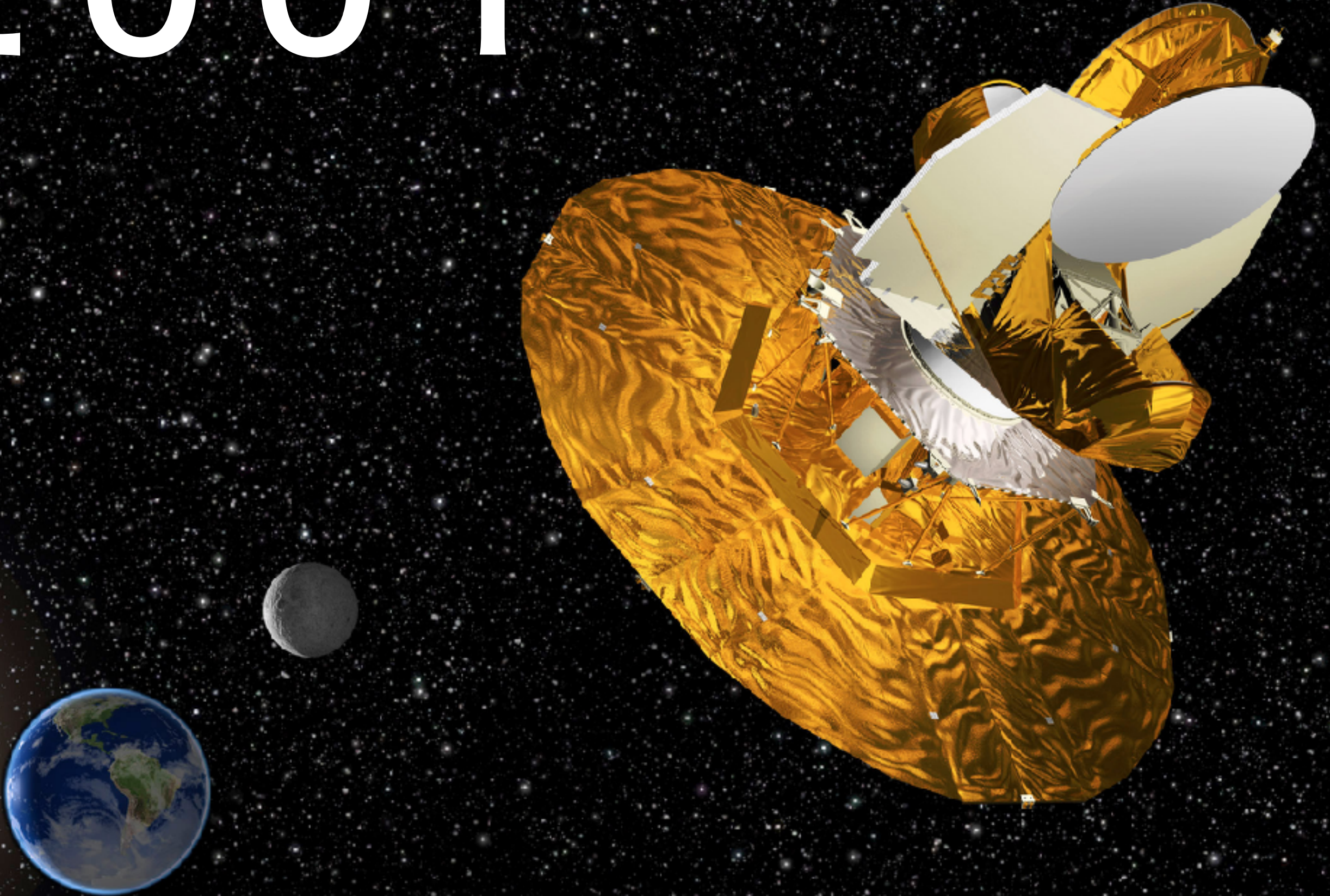
Recording of the first measurement of cosmic microwave background radiation taken on 5/20/1964.

Brightness





2001

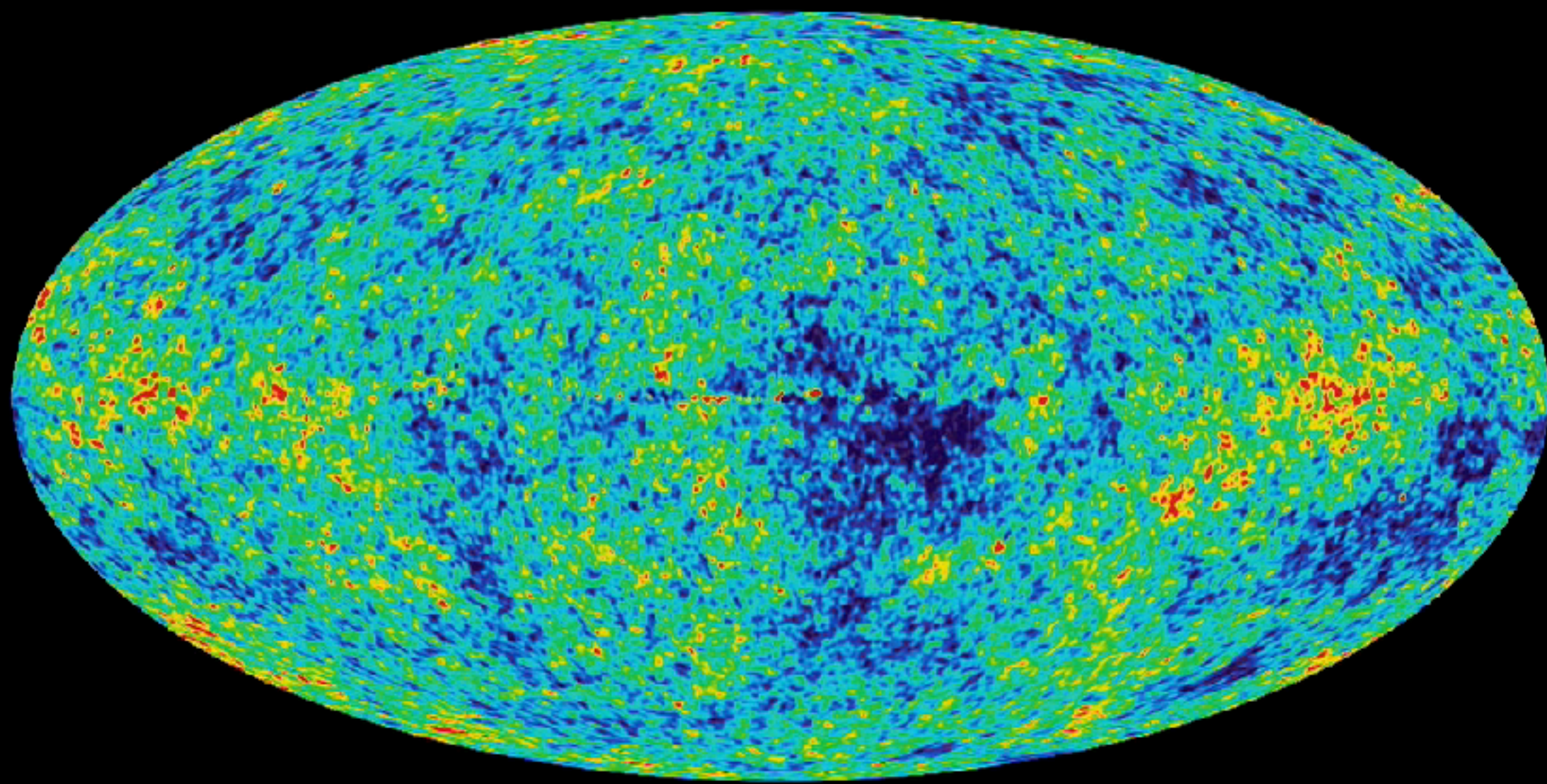


WMAP Science Team

July 19, 2002

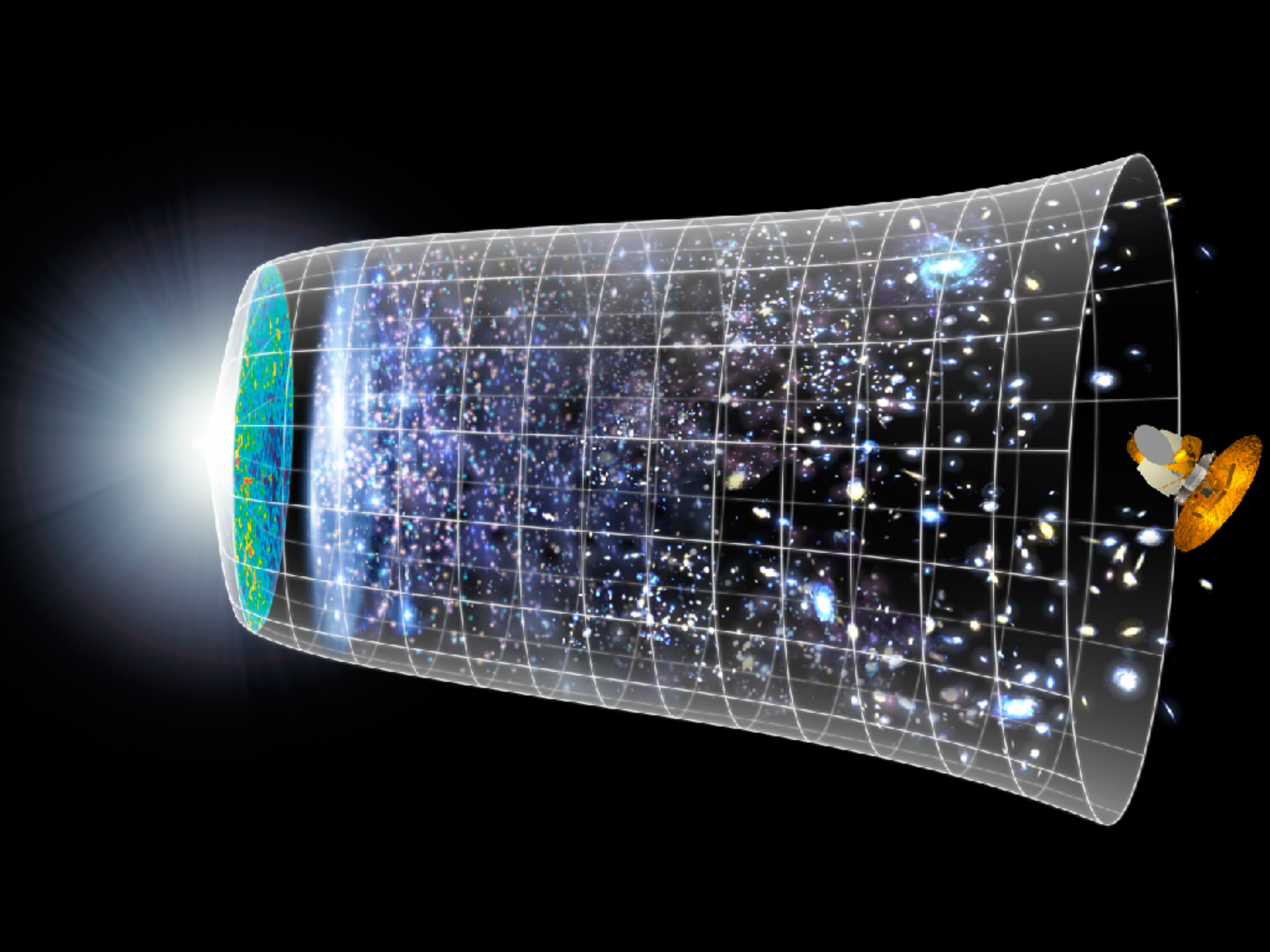


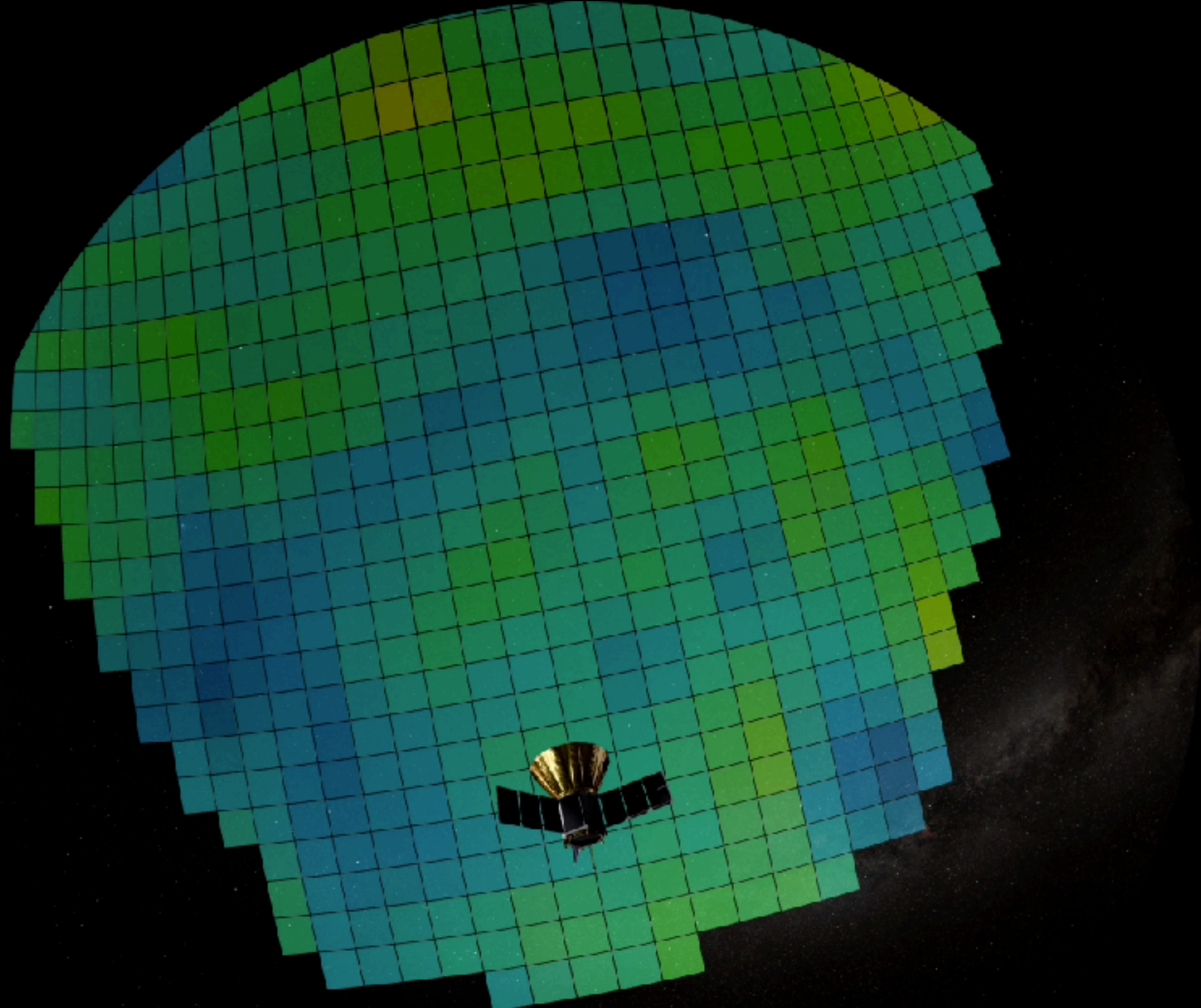
- WMAP was launched on June 30, 2001
- The WMAP mission ended after 9 years of operation



A Remarkable Story

- Observations of the cosmic microwave background and their interpretation taught us that **galaxies, stars, planets, and ourselves originated from tiny fluctuations in the early Universe**
- *But, what generated the initial fluctuations?*





Leading Idea

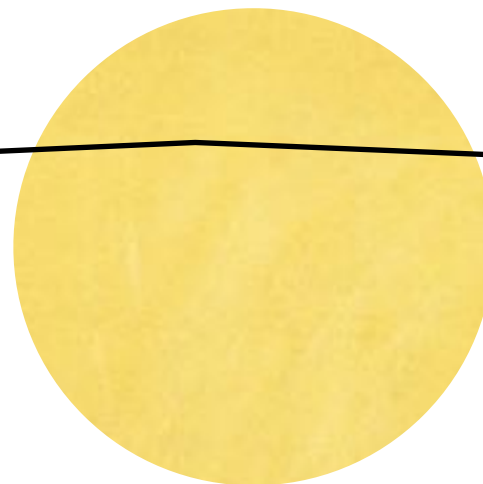
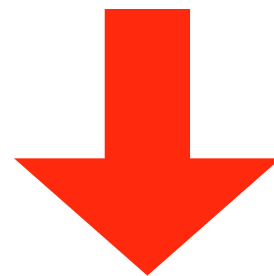
- Quantum mechanics at work in the early Universe
 - “*We all came from quantum fluctuations*”
- But, how did quantum fluctuations on the *microscopic* scales become *macroscopic* fluctuations over large distances?
- What is the **missing link** between small and large scales?

Cosmic Inflation

Quantum fluctuations on
microscopic scales



Inflation!



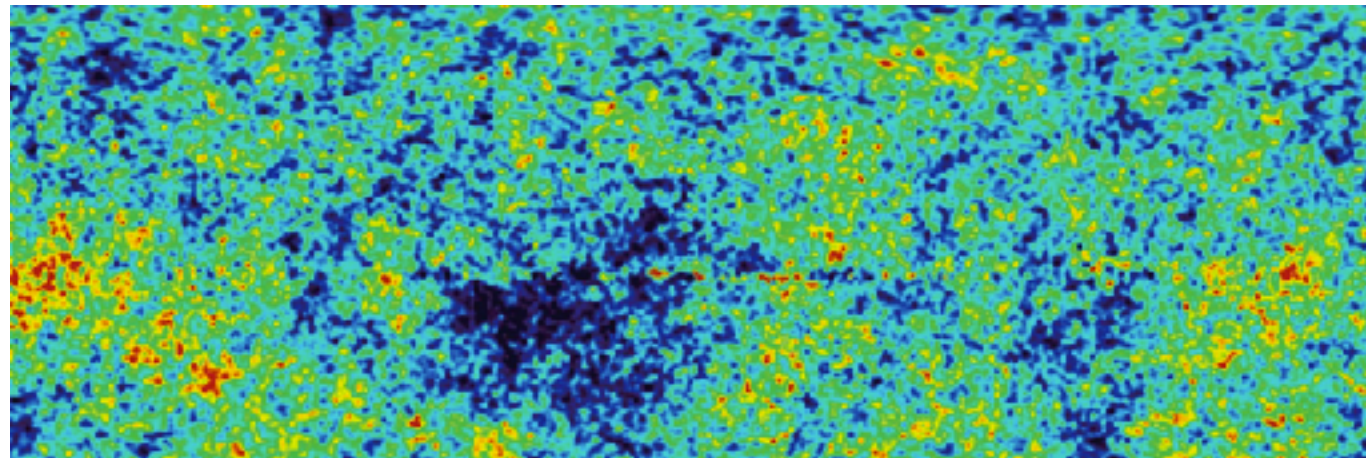
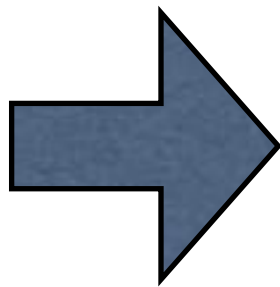
- Exponential expansion (inflation) stretches the wavelength of quantum fluctuations to cosmological scales

Key Predictions

 ζ

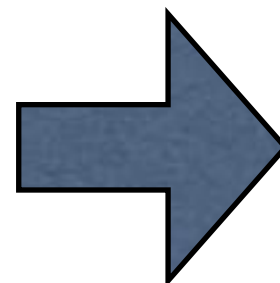
scalar
mode

- Fluctuations we observe today in CMB and the matter distribution originate from quantum fluctuations during inflation

 h_{ij}

tensor
mode

- There should also be *ultra long-wavelength* gravitational waves generated during inflation

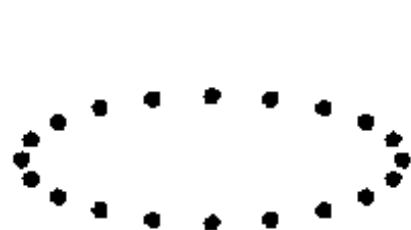


We measure distortions in space

- A distance between two points in space

$$d\ell^2 = a^2(t)[1 + 2\zeta(\mathbf{x}, t)][\delta_{ij} + h_{ij}(\mathbf{x}, t)]dx^i dx^j$$

- ζ : “curvature perturbation” (scalar mode)
 - Perturbation to the determinant of the spatial metric
- h_{ij} : “gravitational waves” (tensor mode)
 - Perturbation that does not alter the determinant



$$\sum_i h_{ii} = 0$$

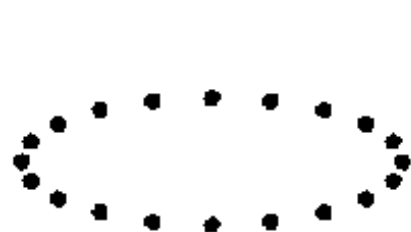
We measure distortions in space

- A distance between two points in space

$$d\ell^2 = \boxed{a^2(t)} [1 + 2\zeta(\mathbf{x}, t)] [\delta_{ij} + h_{ij}(\mathbf{x}, t)] dx^i dx^j$$

scale factor

- ζ : “curvature perturbation” (scalar mode)
 - Perturbation to the determinant of the spatial metric
- h_{ij} : “gravitational waves” (tensor mode)
 - Perturbation that does not alter the determinant



$$\sum_i h_{ii} = 0$$

Finding Inflation

- Inflation is the **accelerated**, quasi-exponential expansion. Defining the Hubble expansion rate as **$H(t)=d\ln(a)/dt$** , we must find

$$\frac{\ddot{a}}{a} = \dot{H} + H^2 > 0 \quad \longrightarrow \quad \epsilon \equiv -\frac{\dot{H}}{H^2} < 1$$

- For inflation to explain flatness of spatial geometry of our observable Universe, we need to have a **sustained** period of inflation. This implies $\epsilon=O(N^{-1})$ or smaller, where N is the number of e-folds of expansion counted from the end of inflation:

$$N \equiv \ln \frac{a_{\text{end}}}{a} = \int_t^{t_{\text{end}}} dt' H(t') \approx 50$$

Have we found inflation?

$$\epsilon \equiv -\frac{\dot{H}}{H^2}$$

- *Have we found $\epsilon \ll 1$?*
- To achieve this, we need to map out **H(t)**, and show that it does not change very much with time

Fluctuations are proportional to H

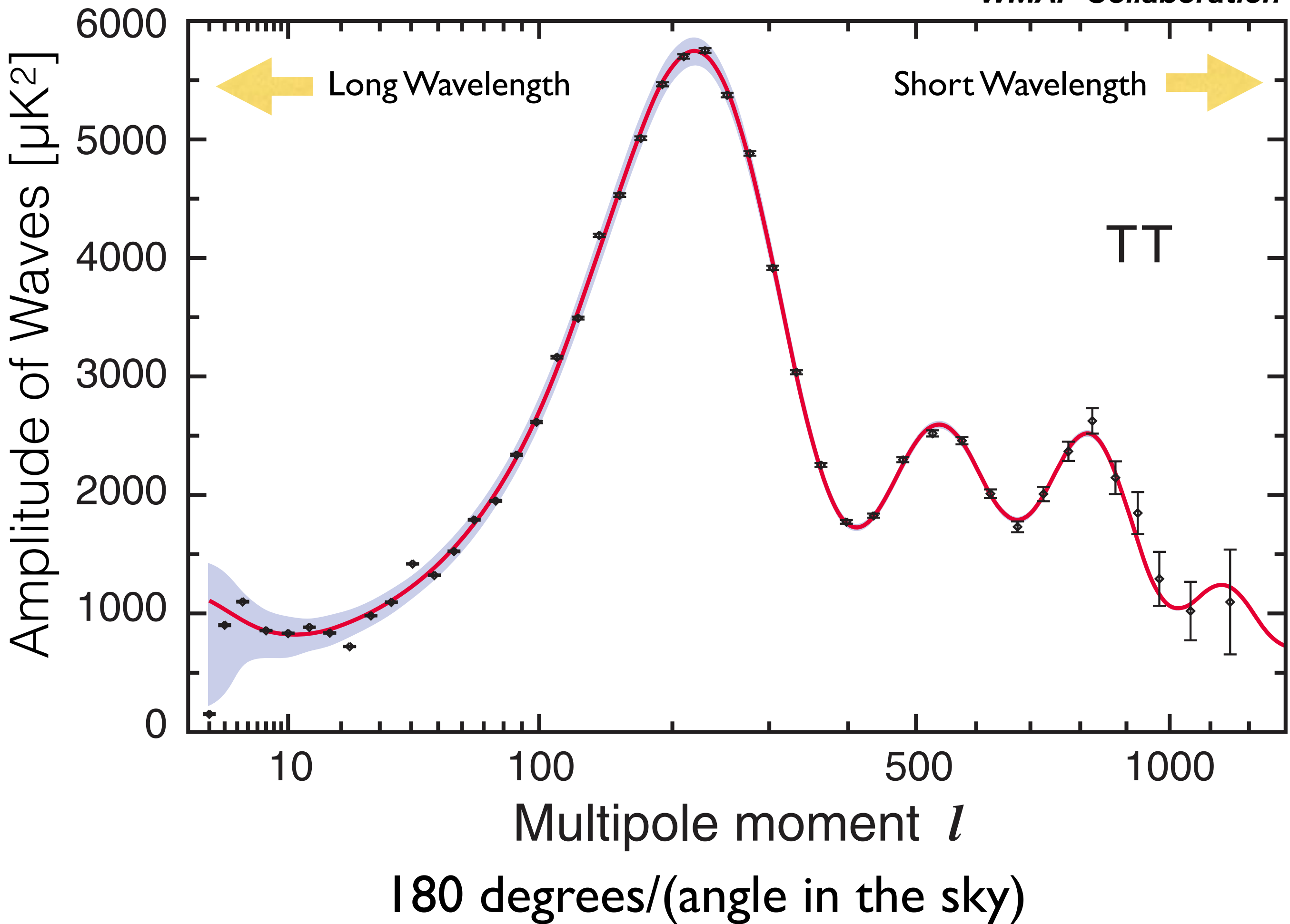
- Both scalar (ζ) and tensor (h_{ij}) perturbations are proportional to H
- Consequence of the uncertainty principle
 - [energy you can borrow] \sim [time you borrow] $^{-1} \sim H$
- **THE KEY:** The earlier the fluctuations are generated, the more its wavelength is stretched, and thus the bigger the angles they subtend in the sky. **We can map $H(t)$ by measuring CMB fluctuations over a wide range of angles**

Fluctuations are proportional to H

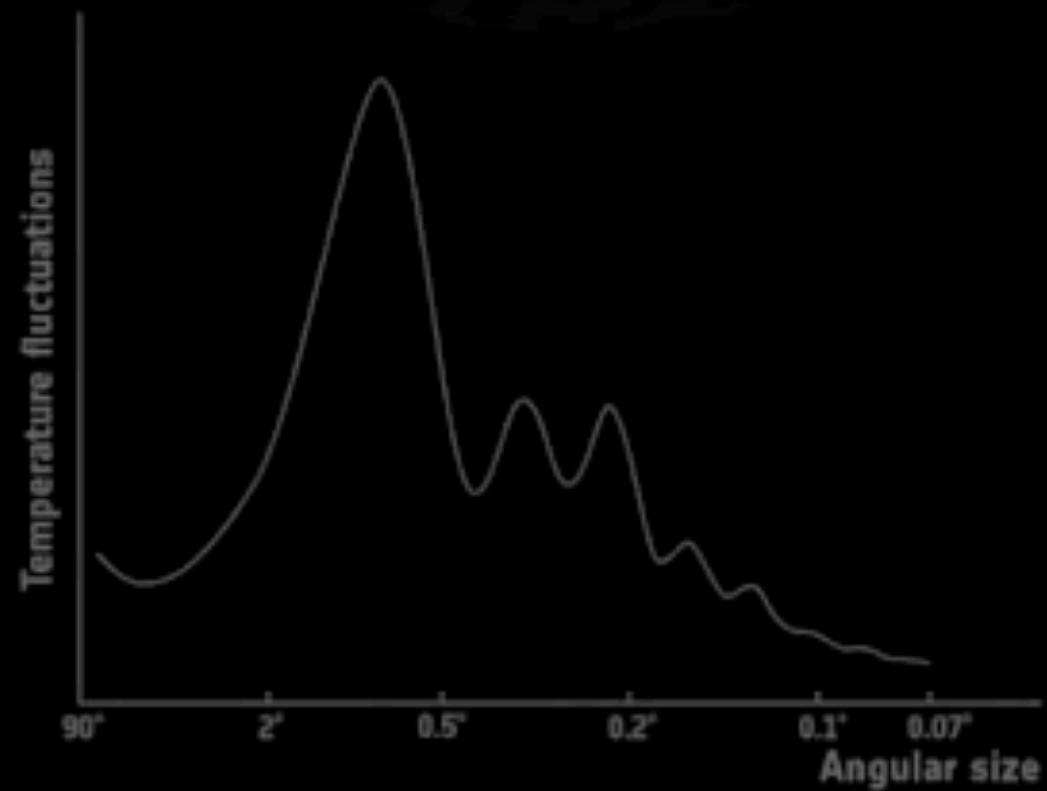
- We can map $H(t)$ by measuring CMB fluctuations over a wide range of angles
 1. We want to show that the amplitude of CMB fluctuations does not depend very much on angles (i.e., $\varepsilon \ll 1$)
 2. Moreover, since inflation must end, H would be a decreasing function of time. It would be fantastic to show that the amplitude of CMB fluctuations actually DOES depend on angles such that the small scale has *slightly* smaller power

Data Analysis

- Decompose temperature fluctuations in the sky into a set of waves with various wavelengths
- Make a diagram showing the strength of each wavelength



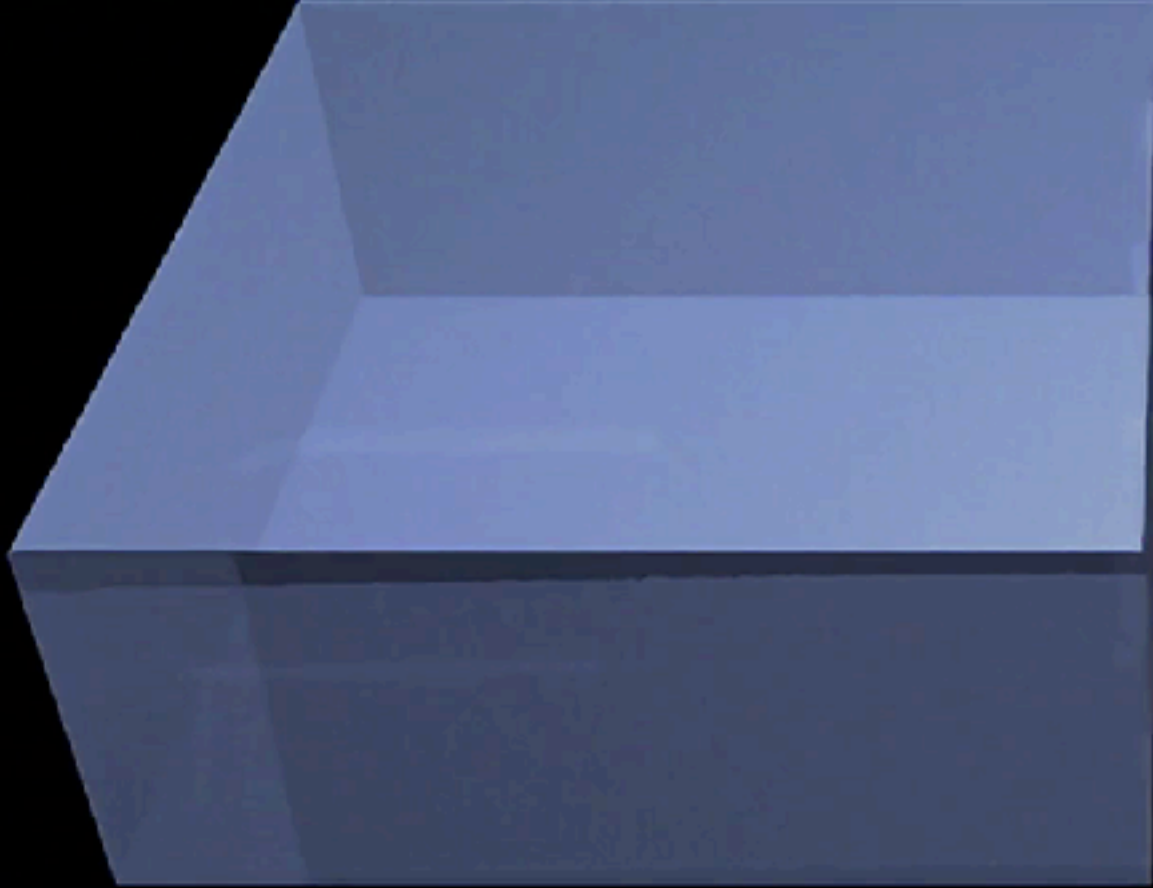
Power spectrum, explained





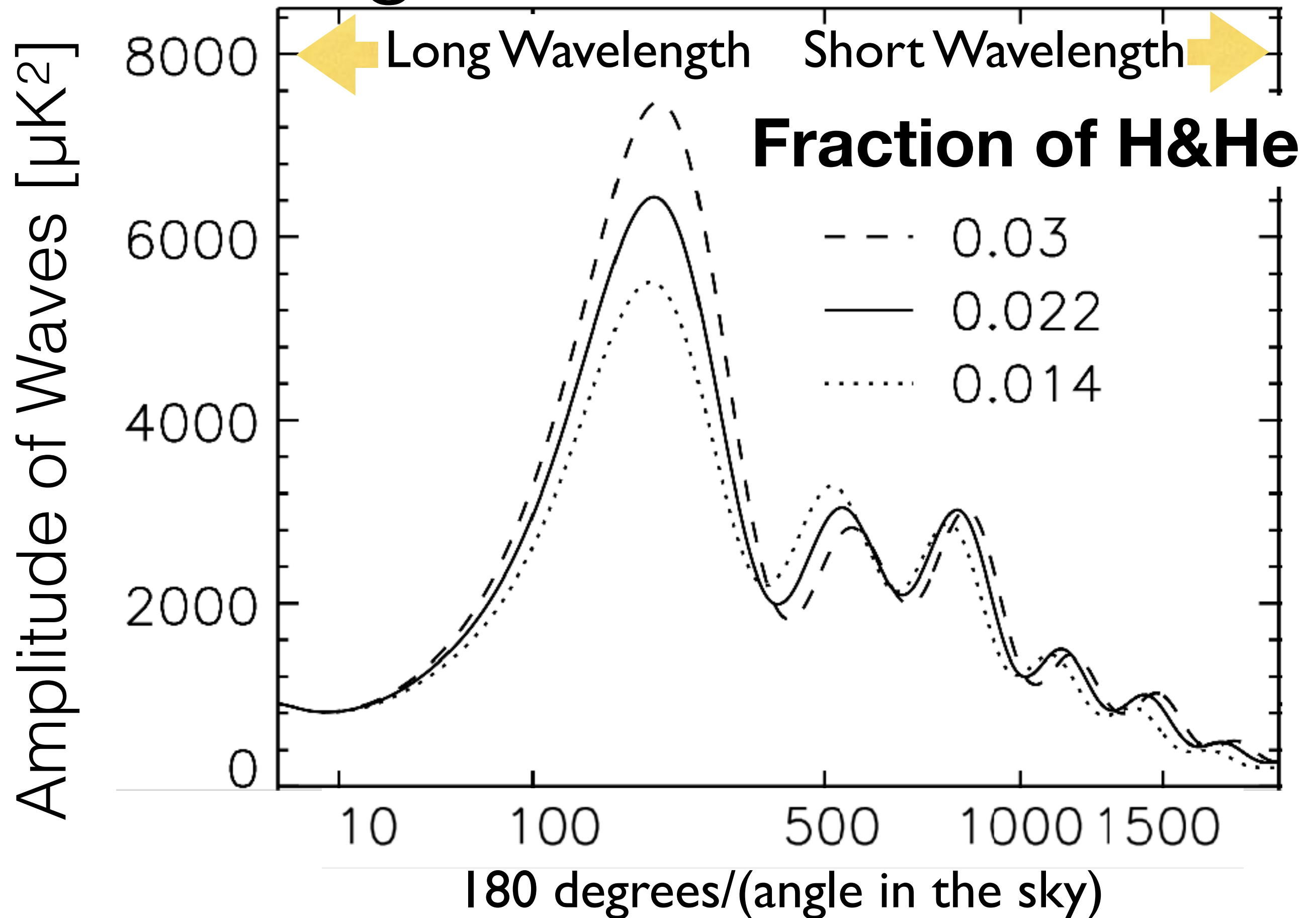
Kosmische Miso Suppe

- When matter and radiation were hotter than 3000 K, matter was completely ionised. The Universe was filled with plasma, which behaves just like a soup
- Think about a Miso soup (if you know what it is). Imagine throwing Tofus into a Miso soup, while changing the density of Miso
- And imagine watching how ripples are created and propagate throughout the soup

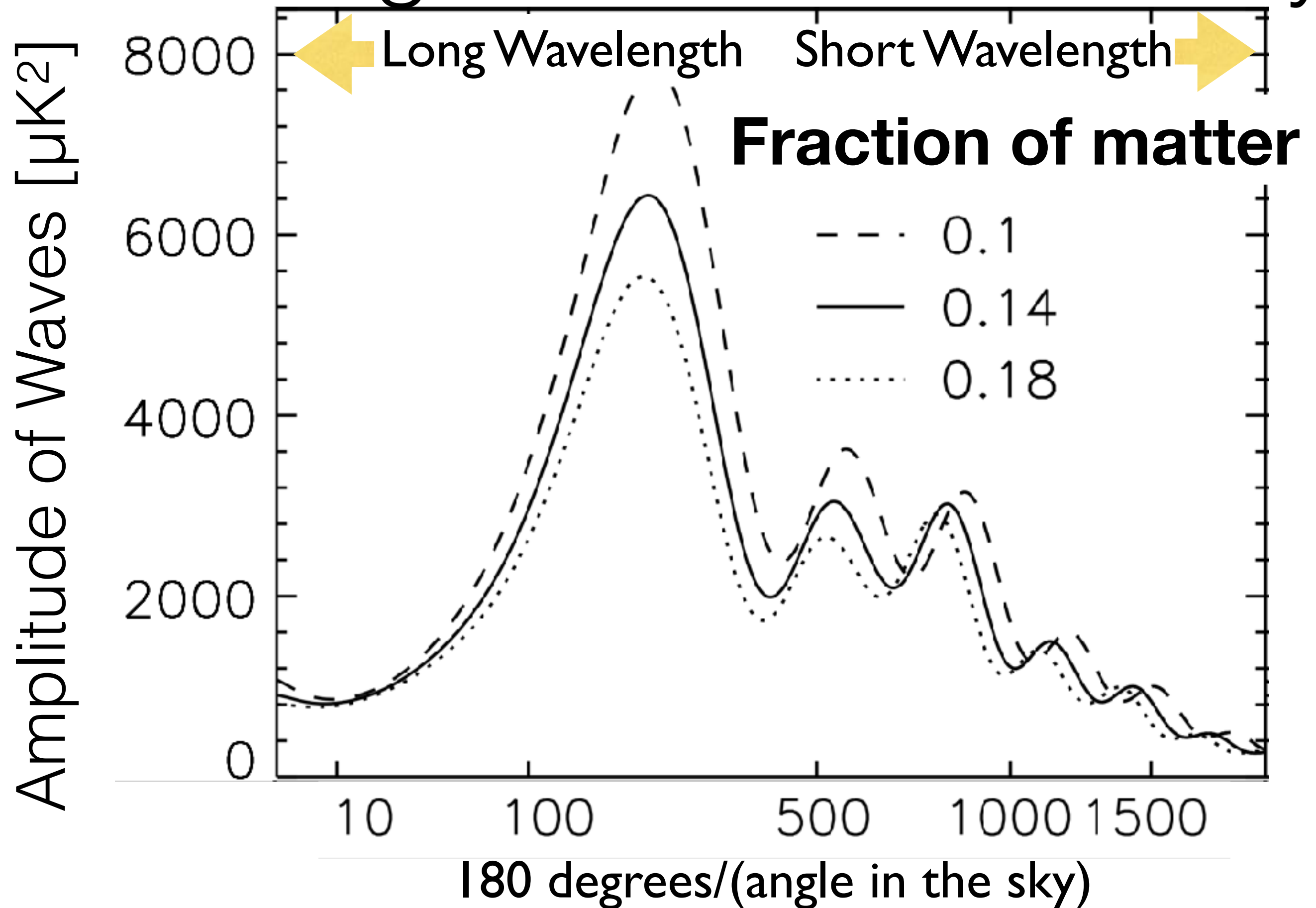


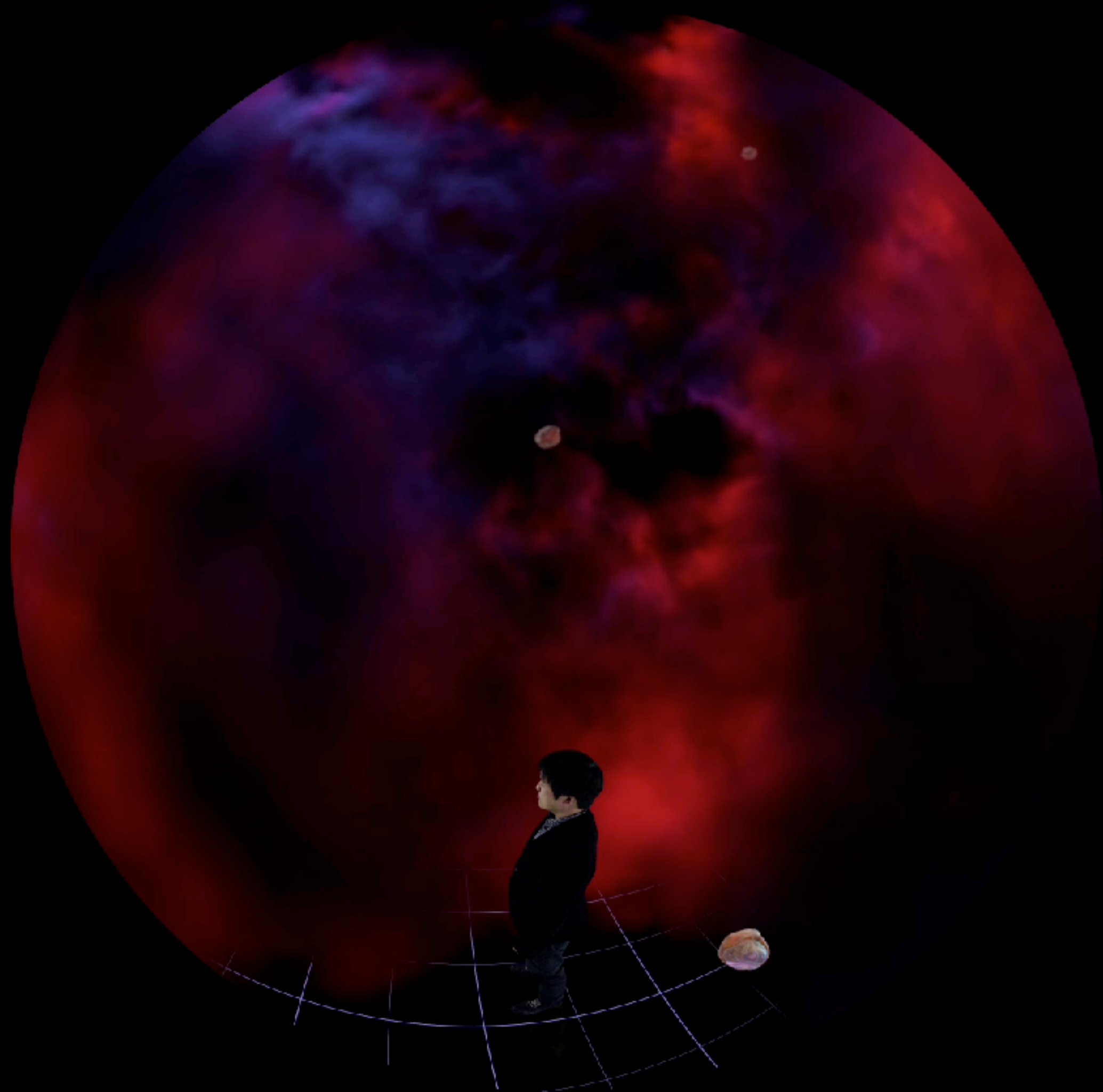


Measuring Abundance of H&He

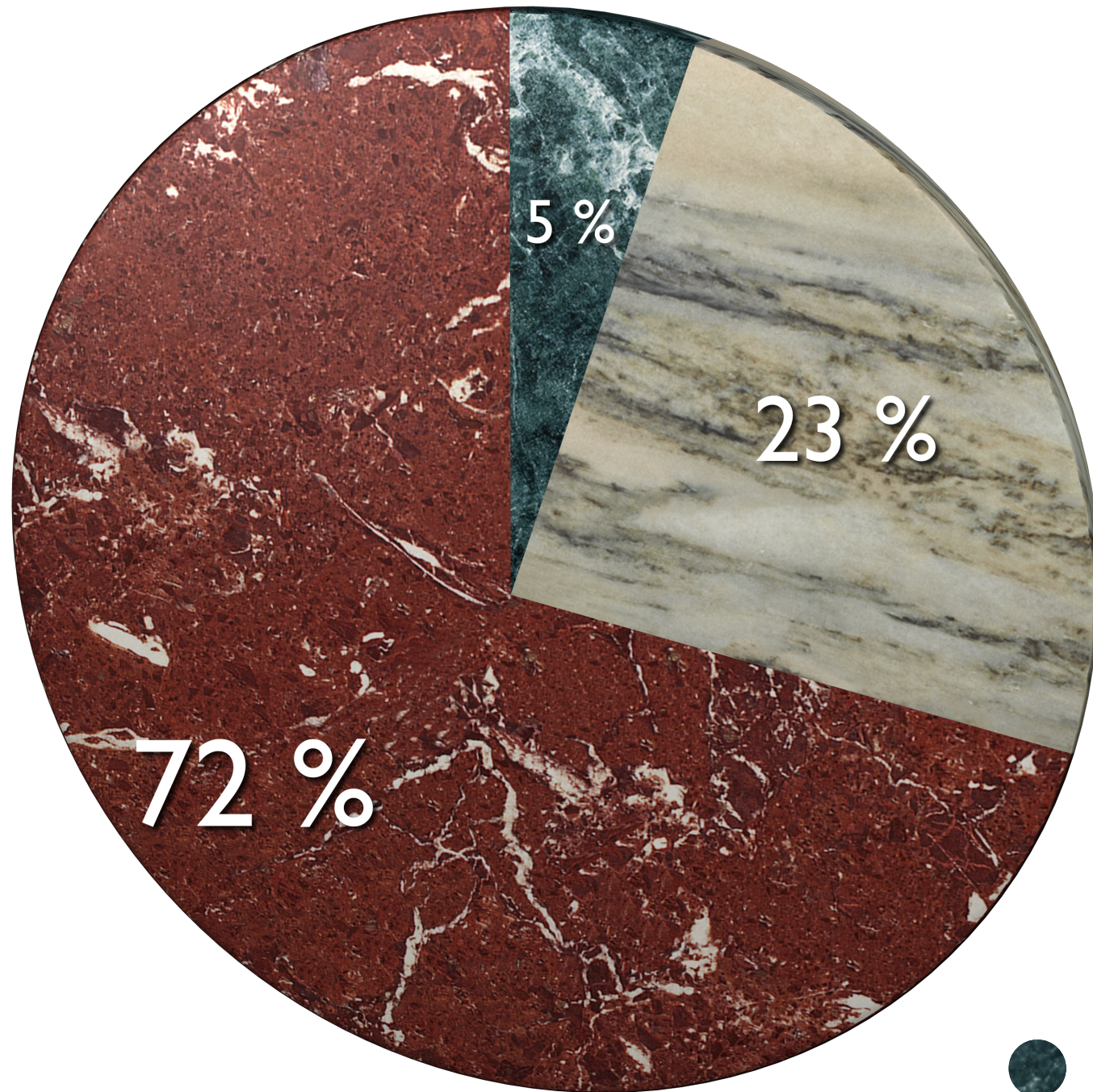


Measuring ***Total*** Matter Density





Cosmic Pie Chart

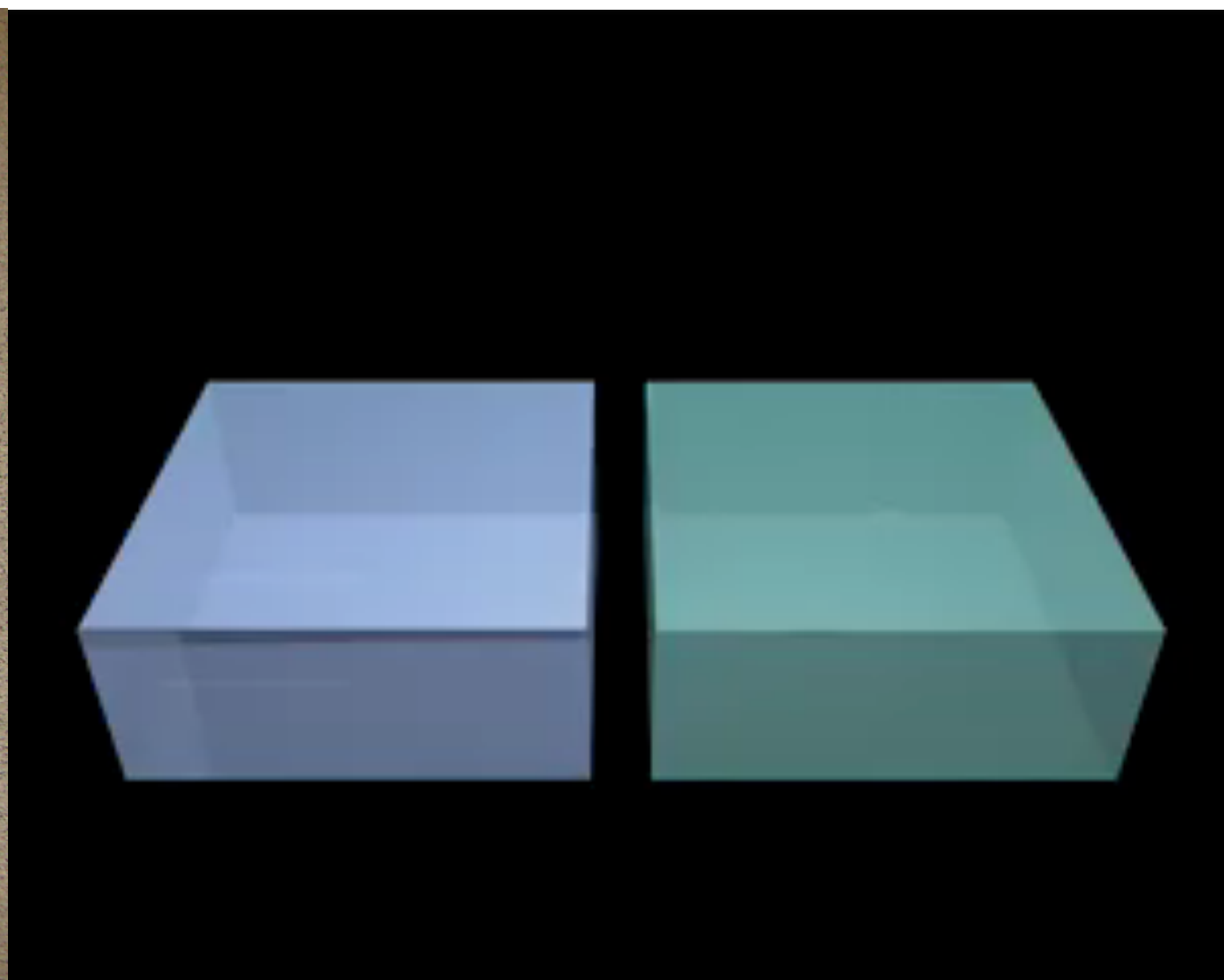


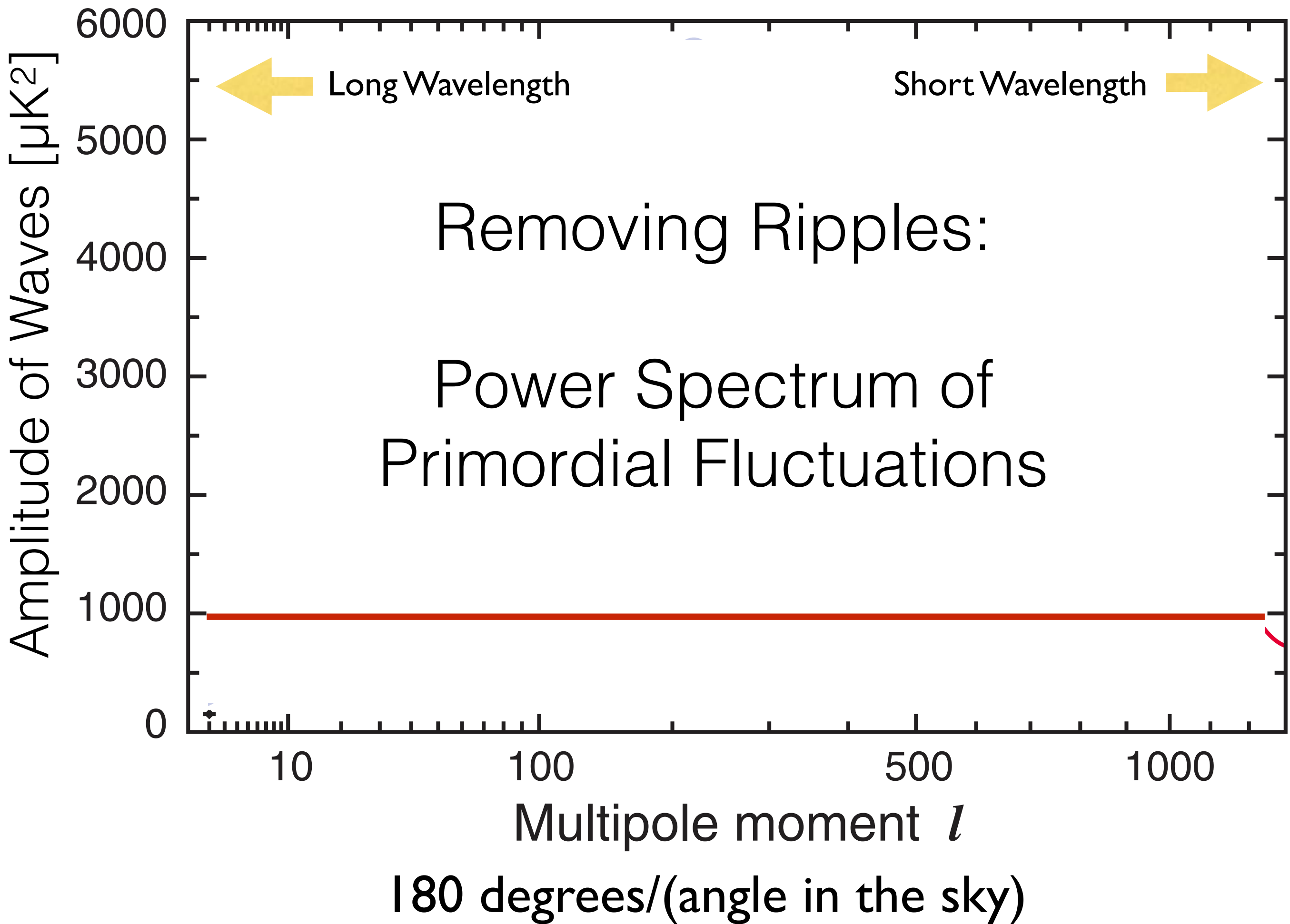
- WMAP determined the abundance of various components in the Universe
- As a result, **we came to realise that we do not understand 95% of our Universe...**

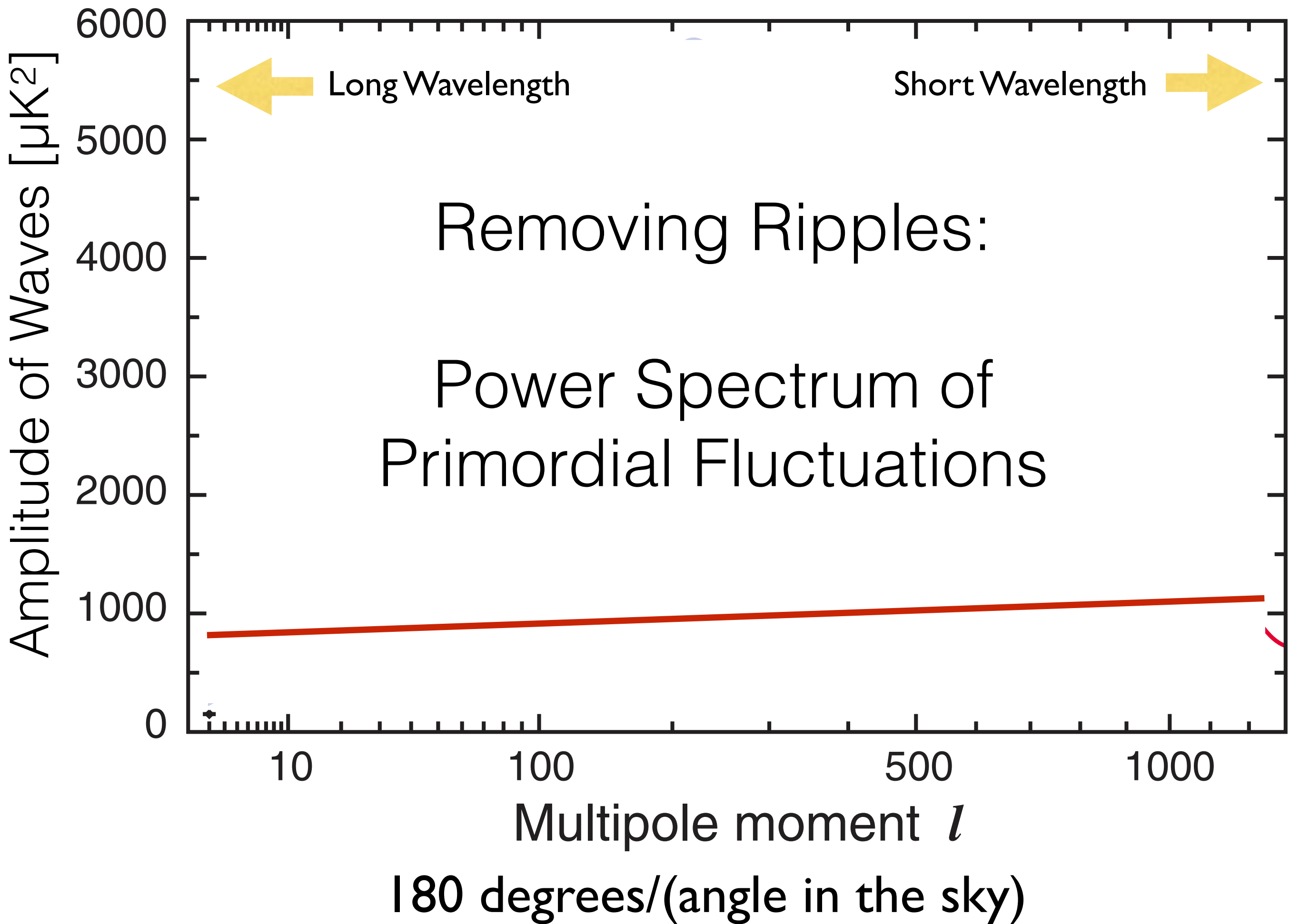
● H&He ● Dark Matter
● Dark Energy

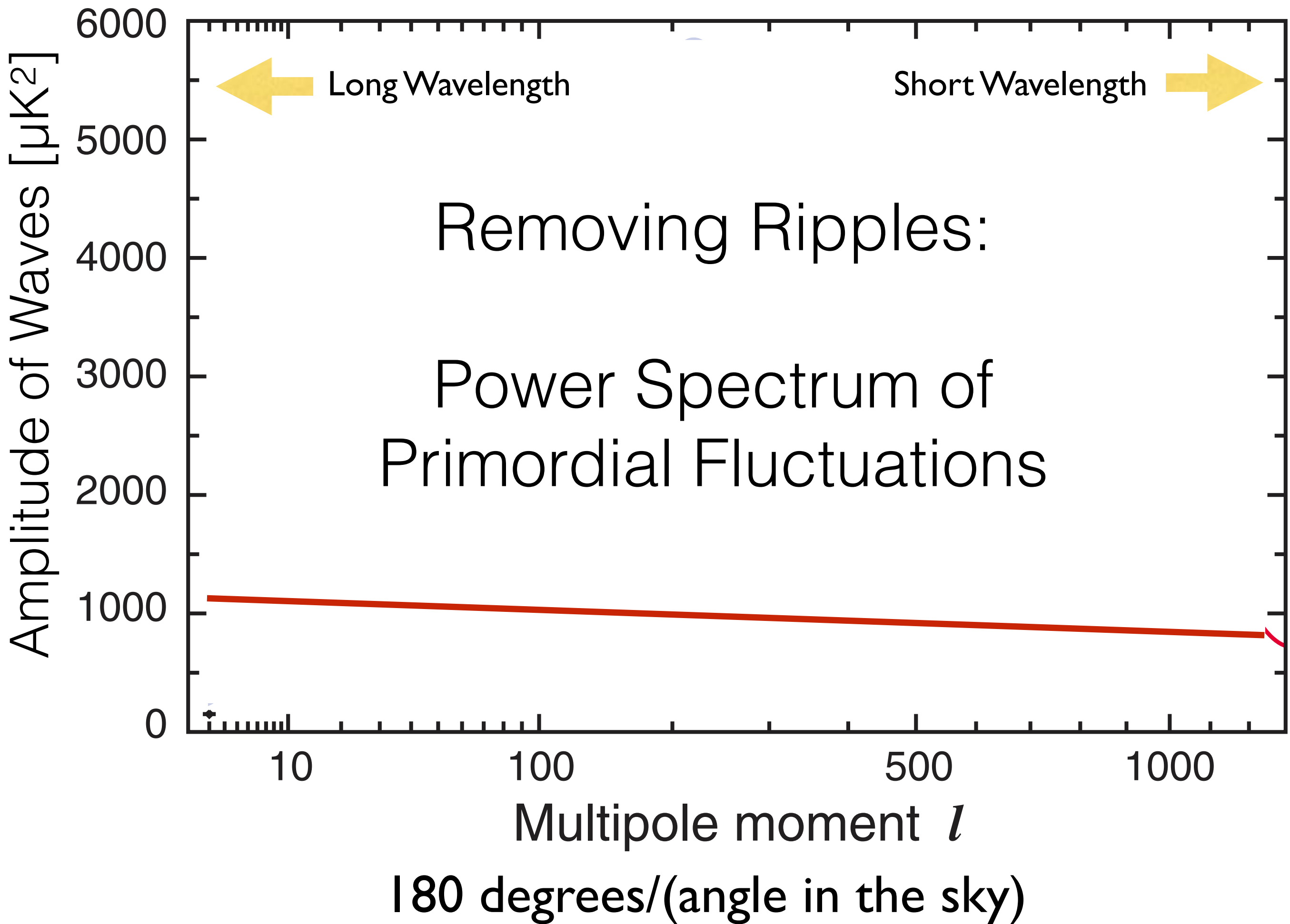
Origin of Fluctuations

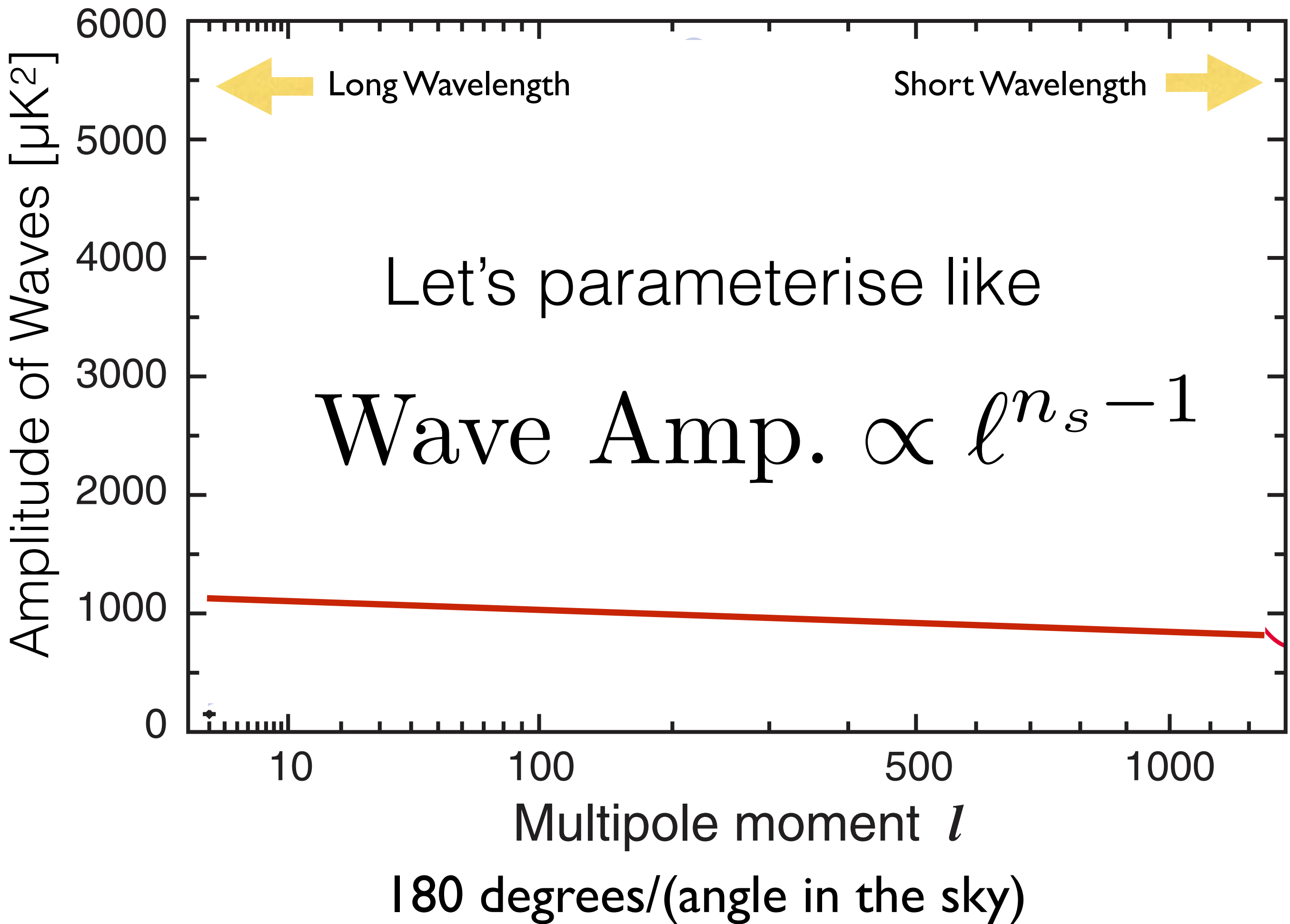
- Who dropped those Tofus into the cosmic Miso soup?

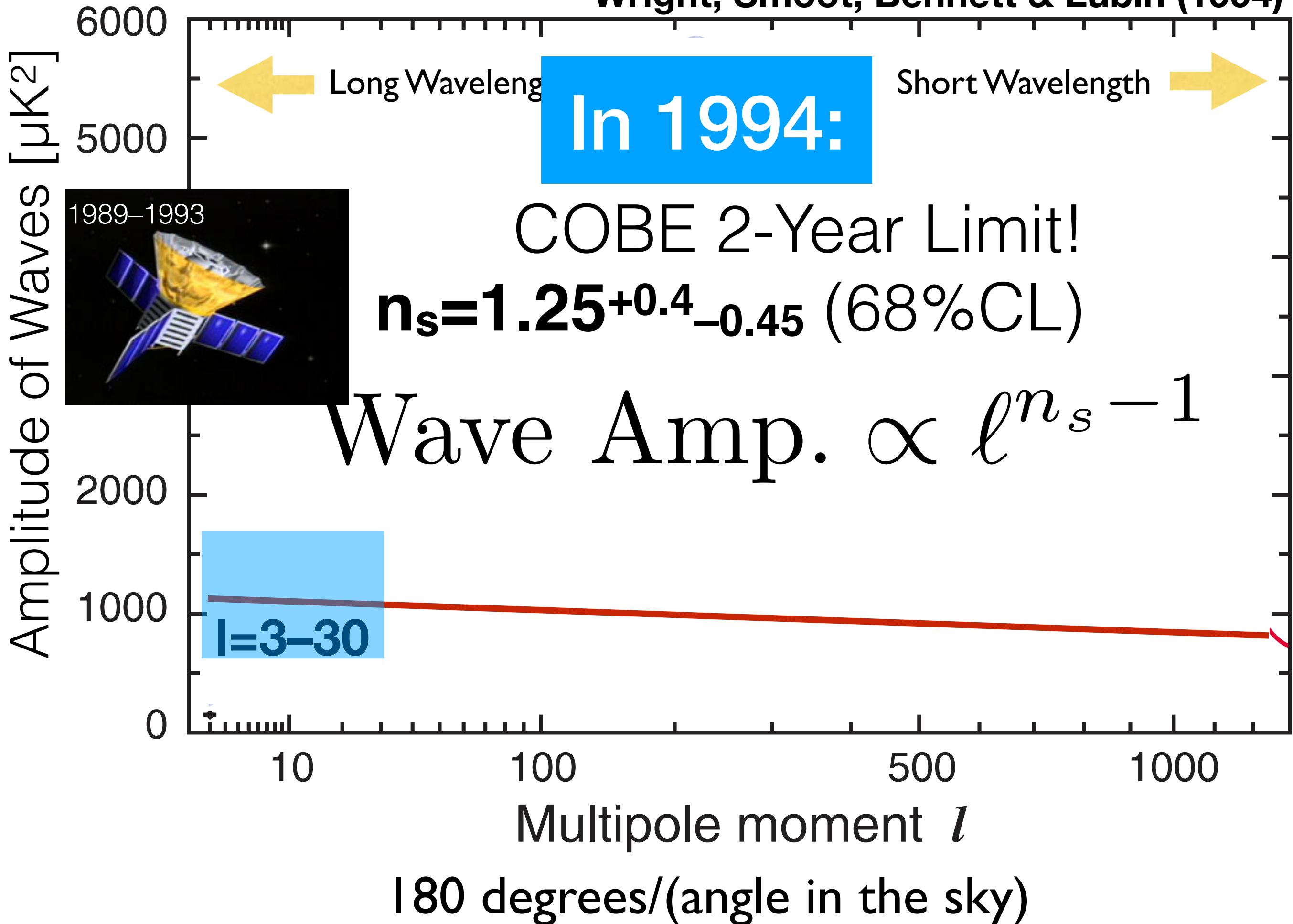


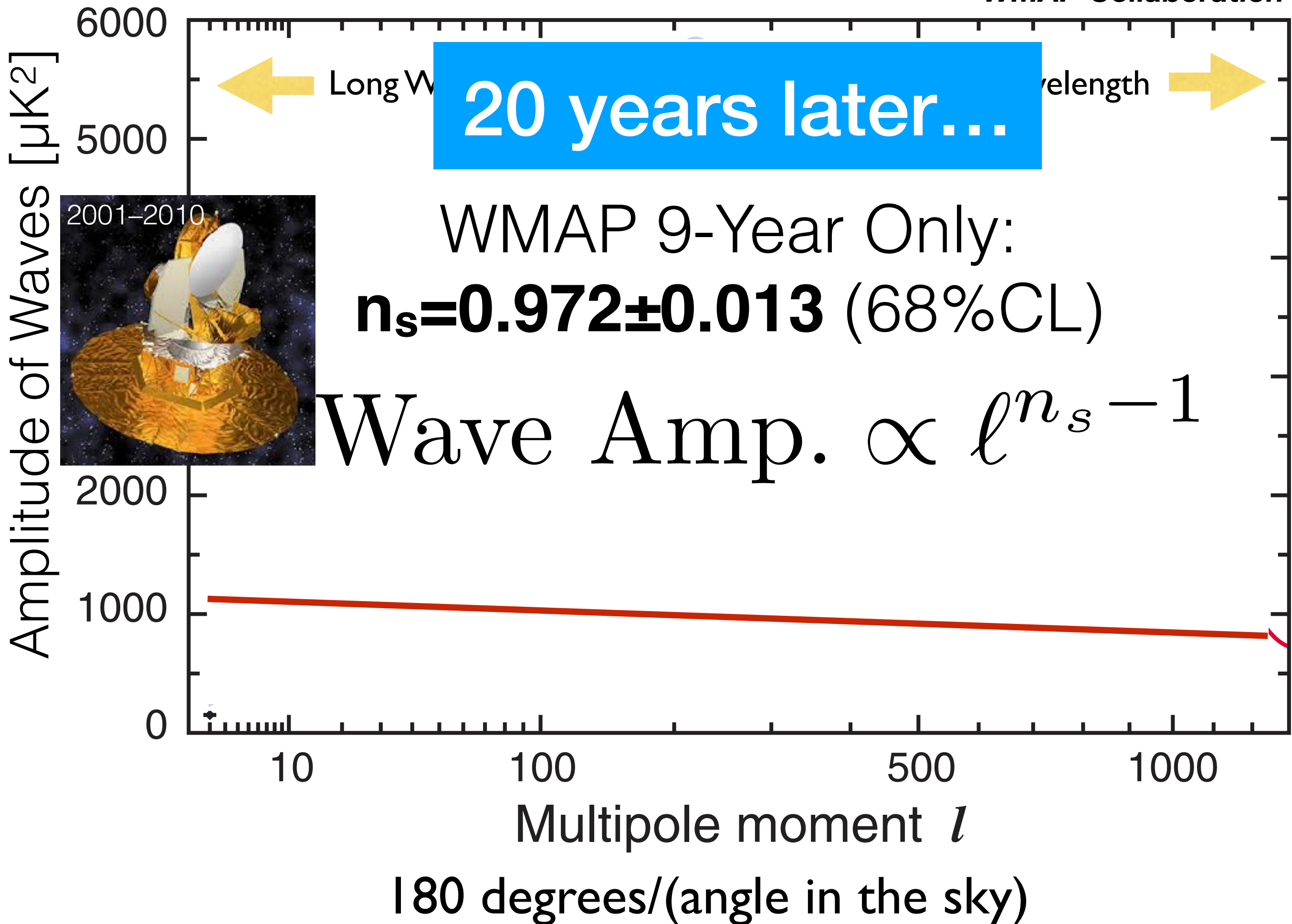












Angular scale

WMAP Collaboration

90°

2°

0.5°

0.2°

0.1°

Amplitude of $\Delta\kappa^2$

2001–2010

South Pole Telescope
[10-m in South Pole]

$$n_s = 0.965 \pm 0.010$$

Atacama Cosmology Telescope
[6-m in Chile]

100

10

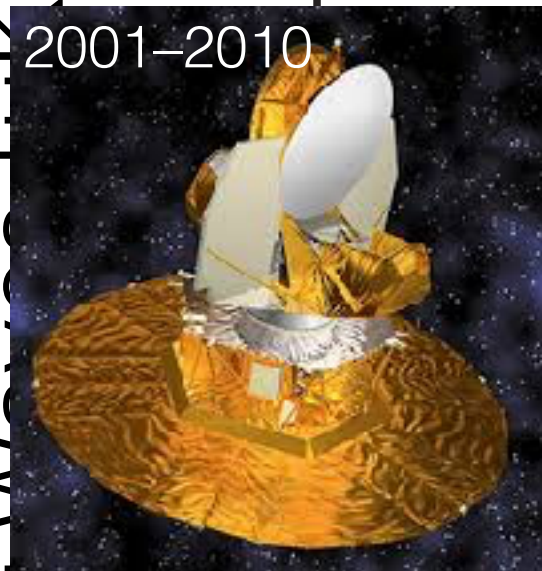
100

500

1000

2000

Multipole moment l



Angular scale

WMAP Collaboration

90°

2°

0.5°

0.2°

0.1°

Amplitude of $\Delta\kappa^2$

2001–2010

South Pole Telescope
[10-m in South Pole]

$$n_s = 0.961 \pm 0.008$$

~5 σ discovery of $n_s < 1$ from the
CMB data combined with the
distribution of galaxies

Atacama Cosmology Telescope
[6-m in Chile]

100

10

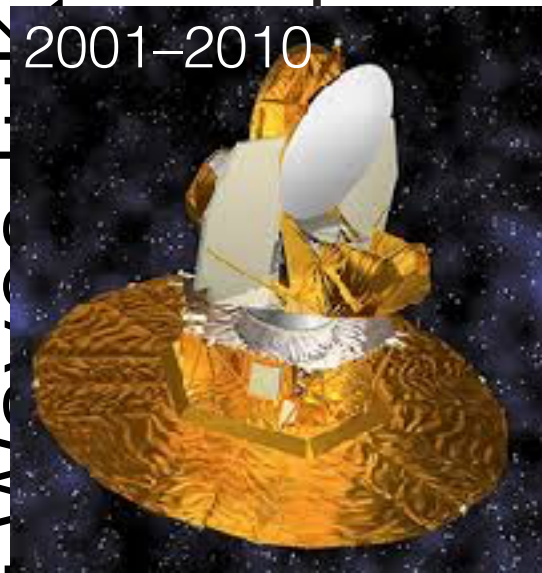
100

500

1000

2000

Multipole moment l



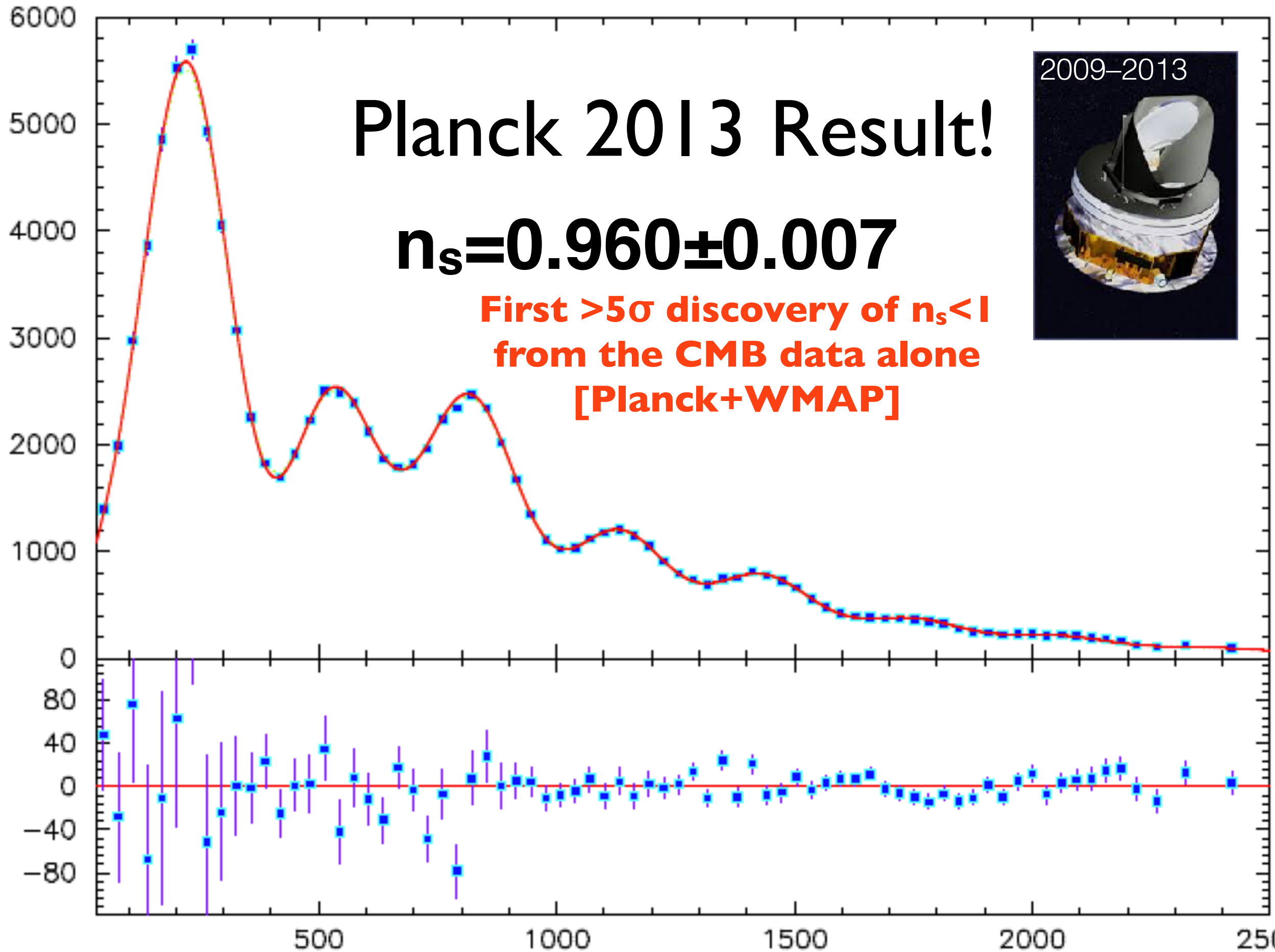
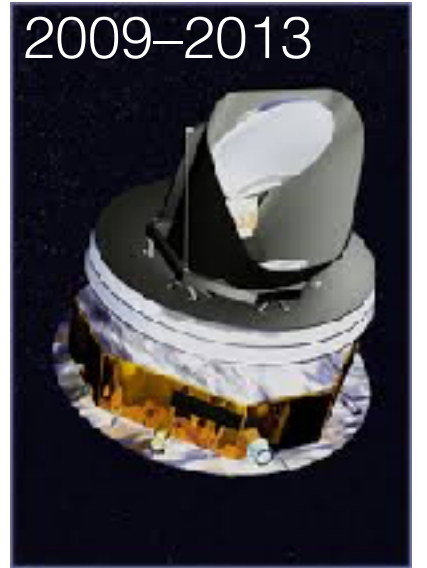
Residual Amplitude of Waves [μK^2]

Planck 2013 Result!

$$n_s = 0.960 \pm 0.007$$

**First $>5\sigma$ discovery of $n_s < 1$
from the CMB data alone
[Planck+WMAP]**

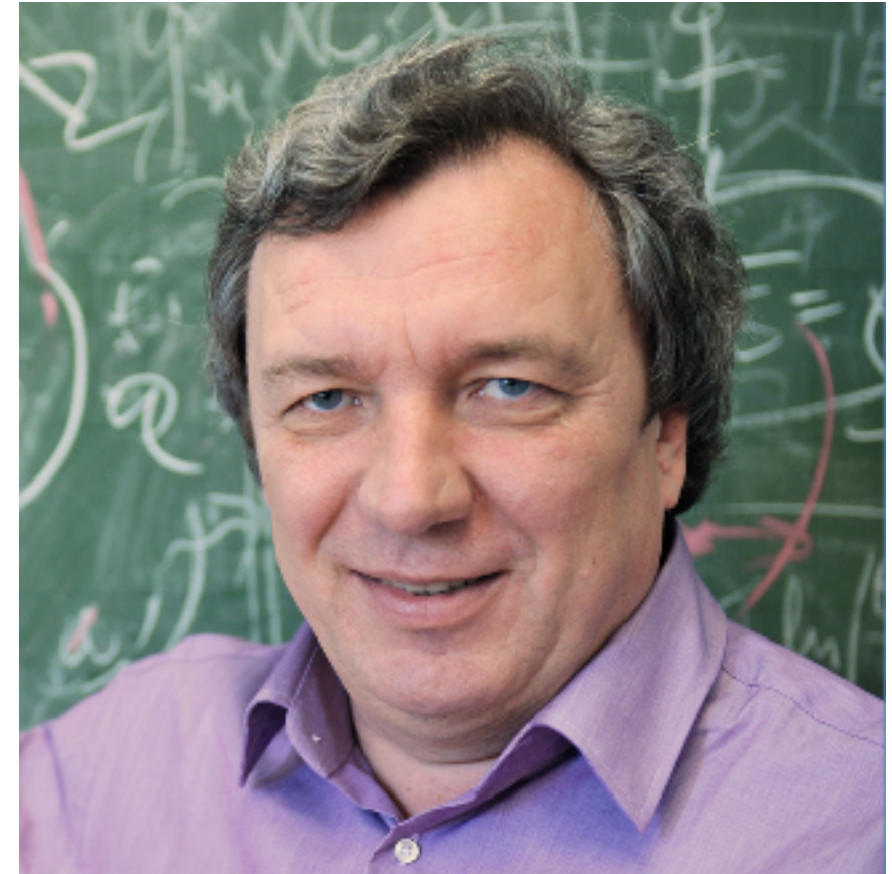
2009–2013



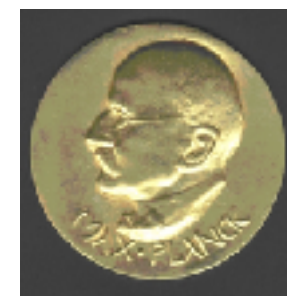
l 80 degrees/(angle in the sky)

Predicted in 1981. Finally discovered in 2013 by WMAP and Planck

- Inflation must end
- Inflation predicts $n_s \sim 1$, but not exactly equal to 1. Usually $n_s < 1$ is expected
- **The discovery of $n_s < 1$ has been the dream of cosmologists since 1992,** when the CMB anisotropy was first discovered and $n_s \sim 1(\pm 0.4)$ was indicated

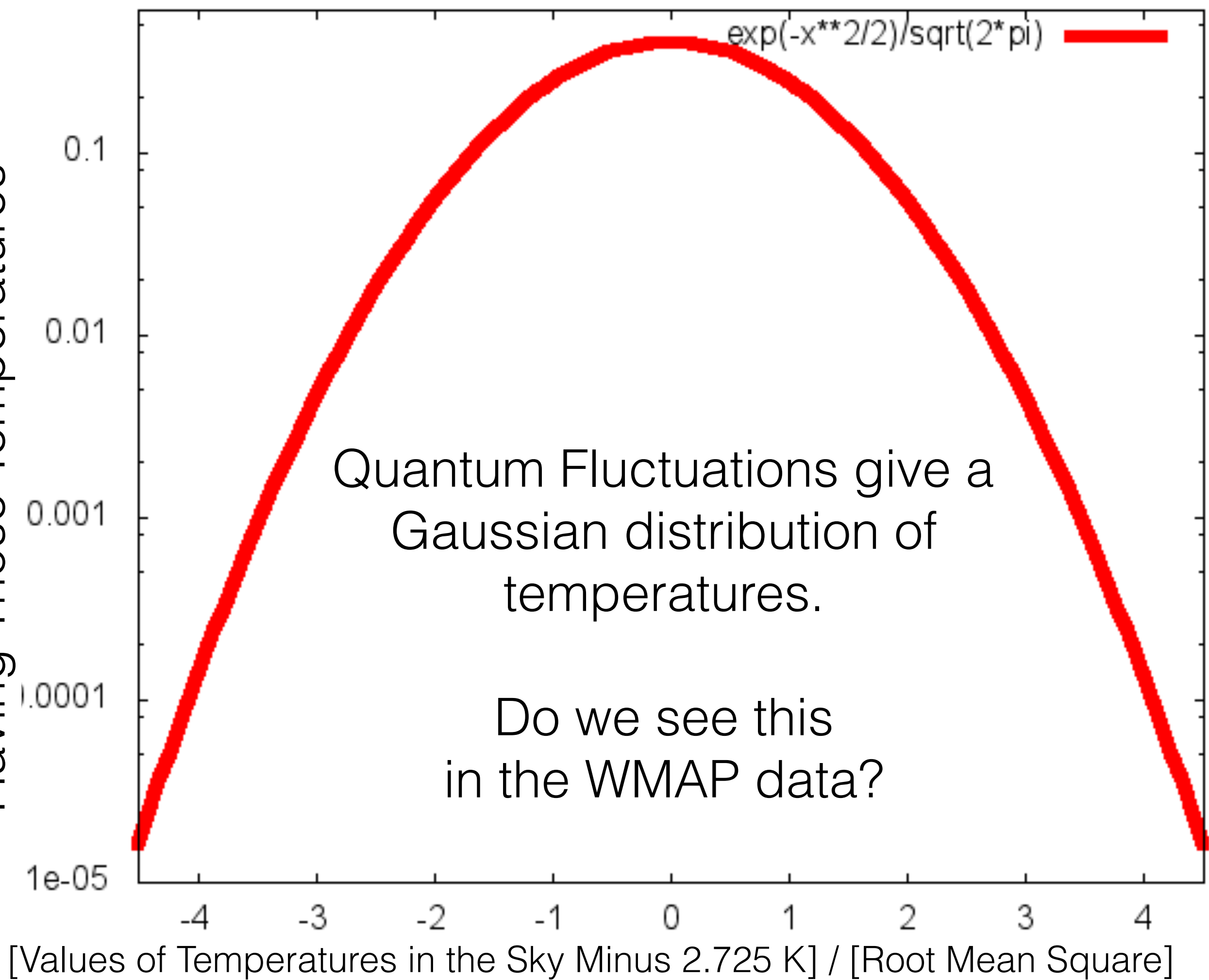


*Slava Mukhanov (LMU)
said in his 1981 paper
that n_s should be
less than 1*



He was awarded
Max Planck Medal in 2015

Fraction of the Number of Pixels
Having Those Temperatures



Fraction of the Number of Pixels
Having Those Temperatures

WMAP Collaboration

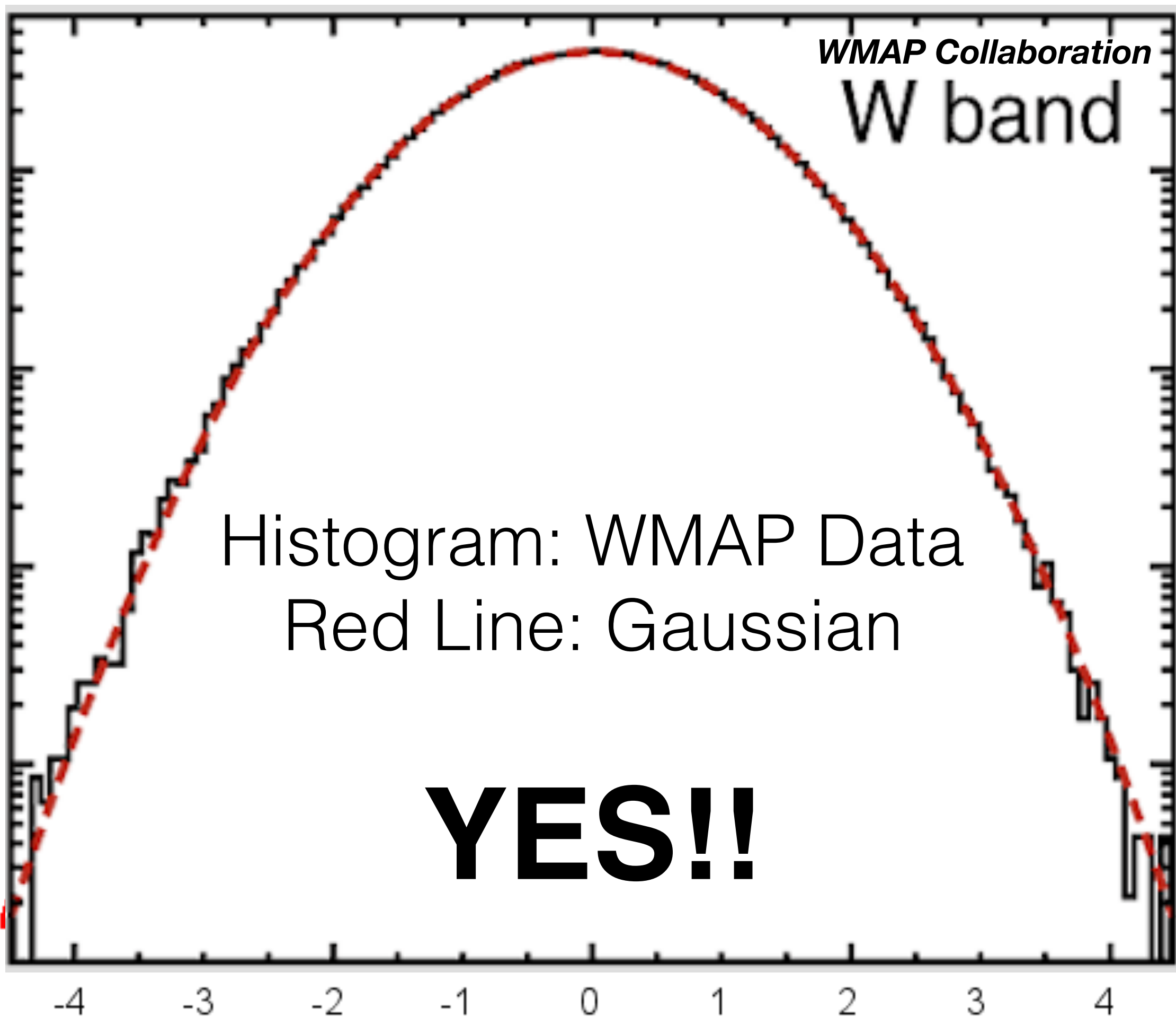
W band

0.1
0.01
0.001
0.0001
1e-05

Histogram: WMAP Data
Red Line: Gaussian

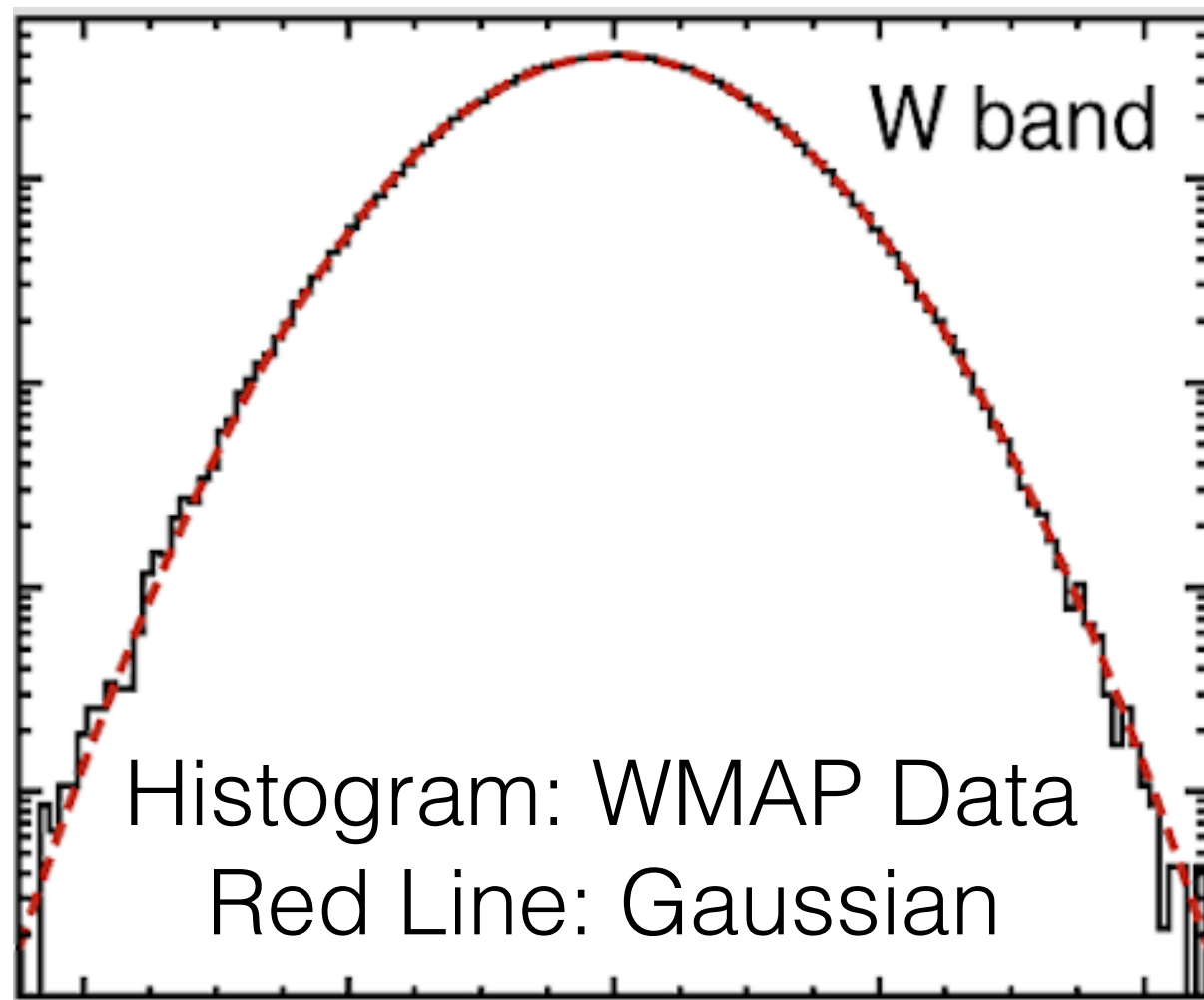
YES!!

[Values of Temperatures in the Sky Minus 2.725 K] / [Root Mean Square]



Testing Gaussianity

Fraction of the Number of Pixels
Having Those Temperatures



[Values of Temperatures in the Sky Minus
2.725 K]/ [Root Mean Square]

- Since a Gauss distribution is symmetric, it must yield a vanishing **3-point function**

$$\langle \delta T^3 \rangle \equiv \int_{-\infty}^{\infty} d\delta T \, P(\delta T) \delta T^3$$

- More specifically, we measure this by averaging the product of temperatures at three different locations in the sky

$$\langle \delta T(\hat{n}_1) \delta T(\hat{n}_2) \delta T(\hat{n}_3) \rangle$$

Lack of non-Gaussianity

- The WMAP data show that the distribution of temperature fluctuations of CMB is very precisely Gaussian
 - with an upper bound on a deviation of **0.2%** (95%CL)

$$\zeta(\mathbf{x}) = \zeta_{\text{gaus}}(\mathbf{x}) + \frac{3}{5} f_{\text{NL}} \zeta_{\text{gaus}}^2(\mathbf{x}) \text{ with } f_{\text{NL}} = 37 \pm 20 \text{ (68\% CL)}$$

WMAP 9-year Result

- The Planck data improved the upper bound by an order of magnitude: deviation is **<0.03%** (95%CL)

$$f_{\text{NL}} = 0.8 \pm 5.0 \text{ (68\% CL)}$$

Planck 2015 Result

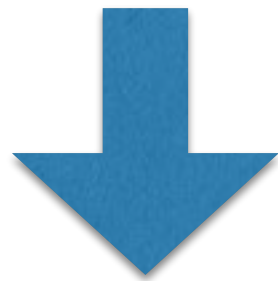
So, have we found inflation?

- Single-field slow-roll inflation looks remarkably good:
 - **Super-horizon fluctuation**
 - **Adiabaticity**
 - **Gaussianity**
 - **$n_s < 1$**
- What more do we want? **Gravitational waves**. Why?
 - Because the “*extraordinary claim requires extraordinary evidence*”

Measuring GW

- GW changes distances between two points

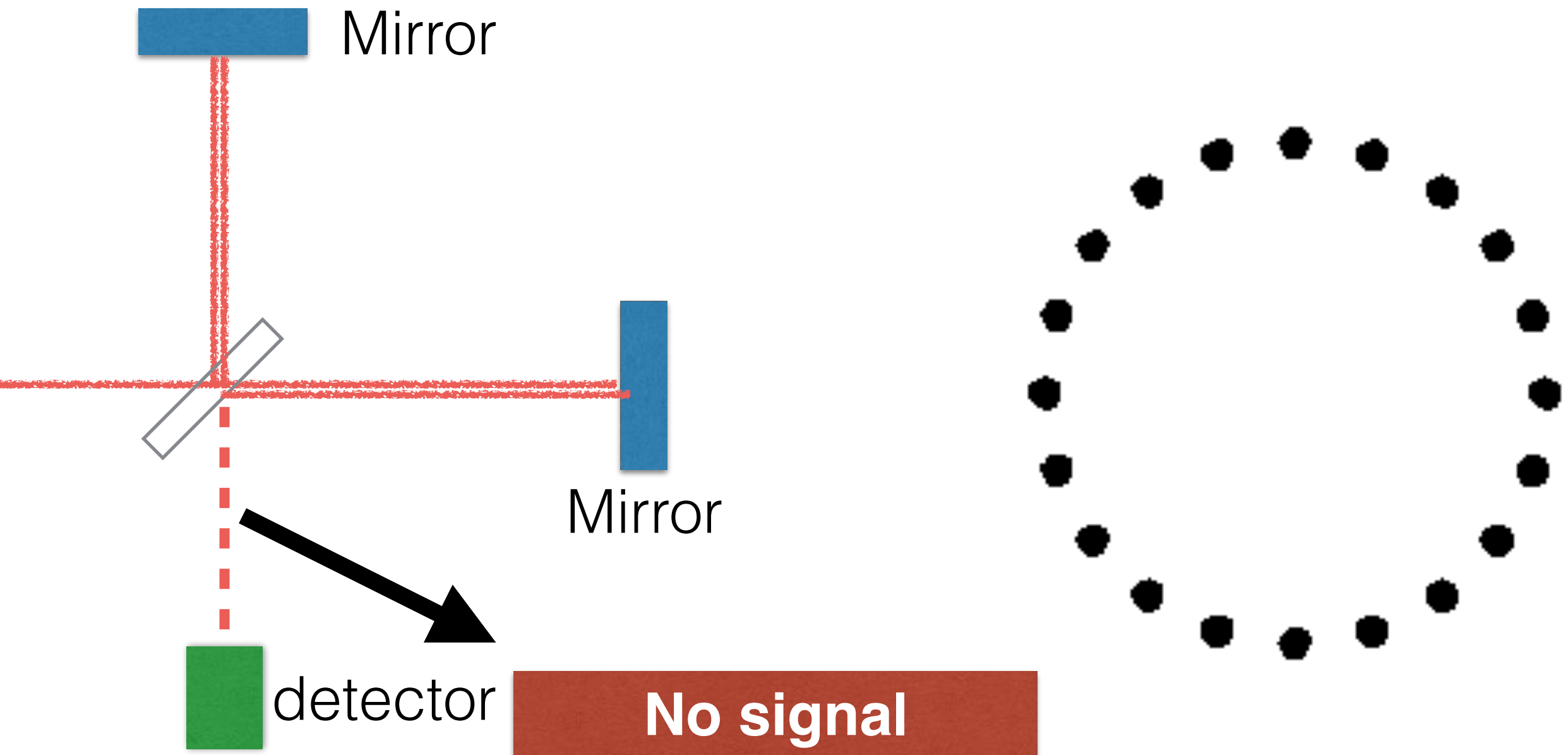
$$d\ell^2 = d\mathbf{x}^2 = \sum_{ij} \delta_{ij} dx^i dx^j$$



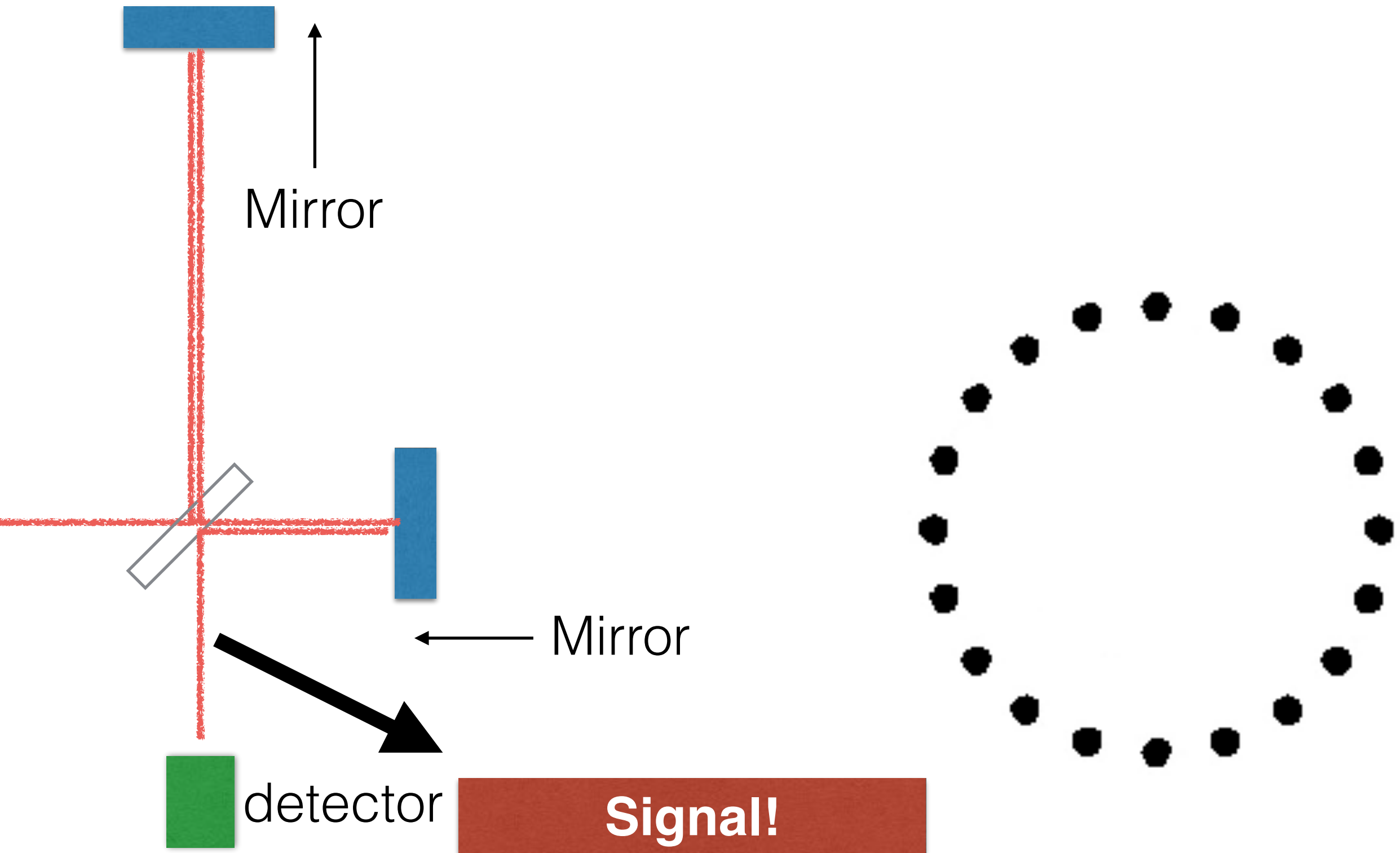
$$d\ell^2 = \sum_{ij} (\delta_{ij} + \textcolor{red}{h_{ij}}) dx^i dx^j$$



Laser Interferometer



Laser Interferometer



LIGO detected GW from a binary blackholes, with the wavelength of thousands of kilometres

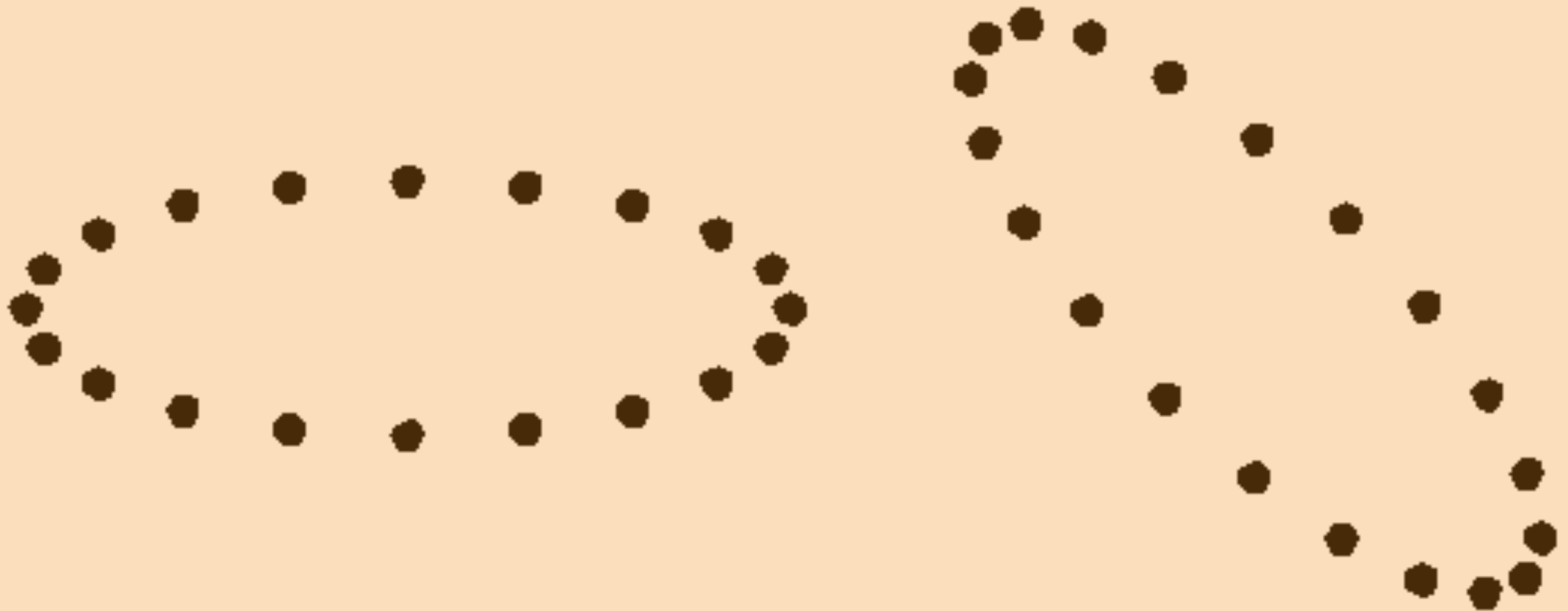
But, the primordial GW affecting the CMB has a wavelength of **billions of light-years!!** How do we find it?

Detecting GW by CMB

Isotropic electro-magnetic fields

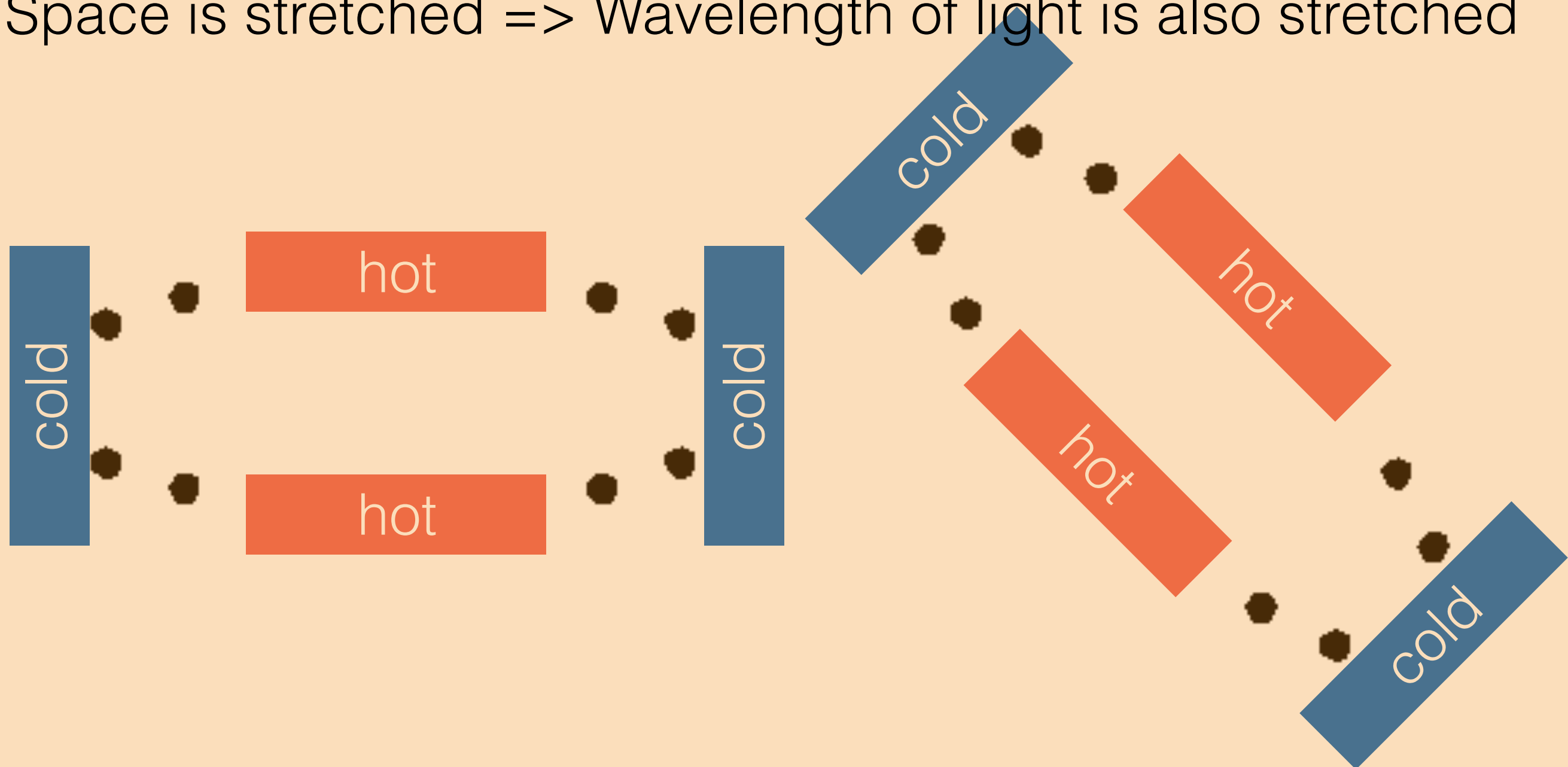
Detecting GW by CMB

GW propagating in isotropic electro-magnetic fields



Detecting GW by CMB

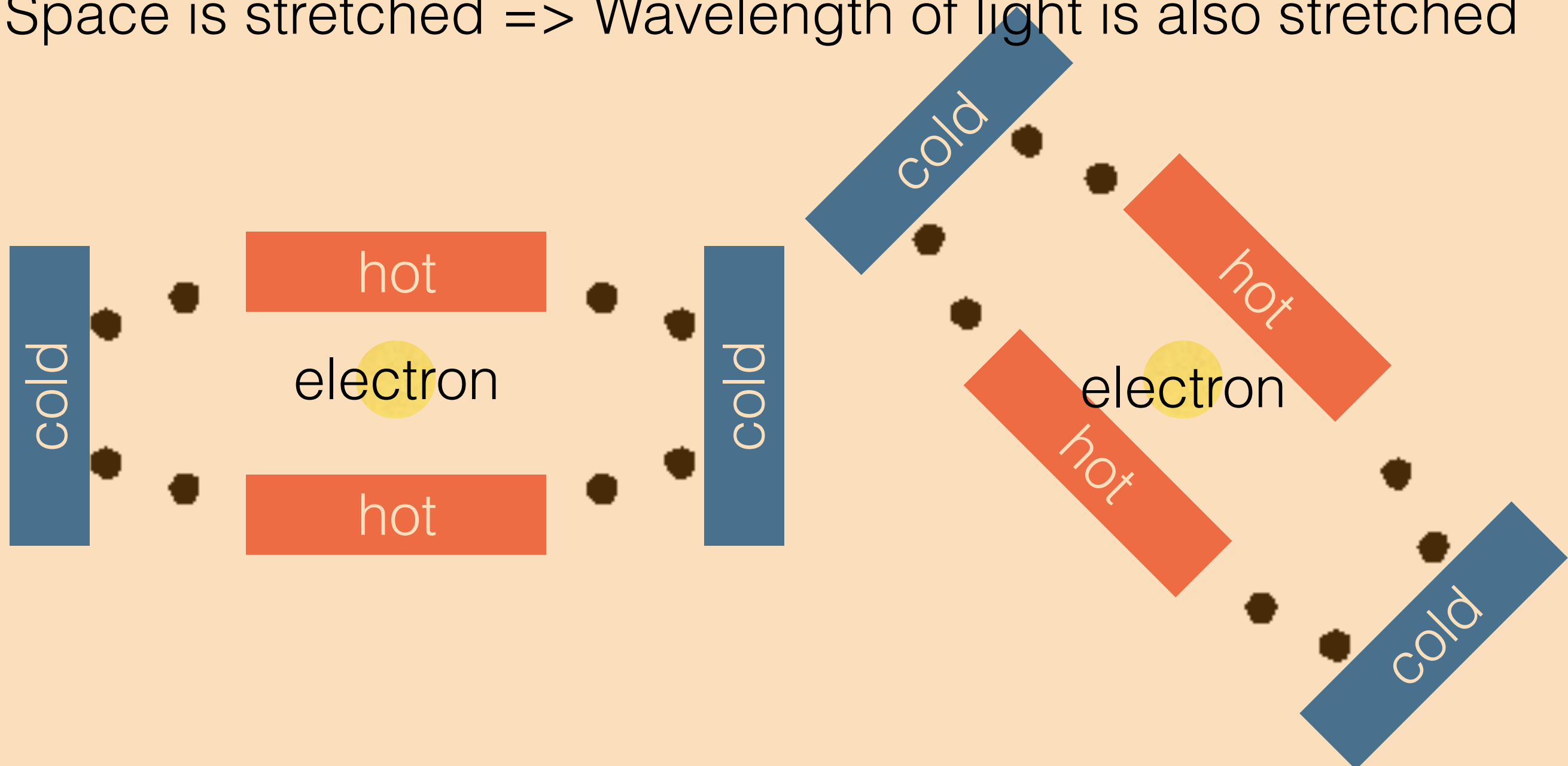
Space is stretched => Wavelength of light is also stretched



Detecting GW by CMB

Polarisation

Space is stretched => Wavelength of light is also stretched



Detecting GW by CMB

Polarisation

Space is stretched => Wavelength of light is also stretched

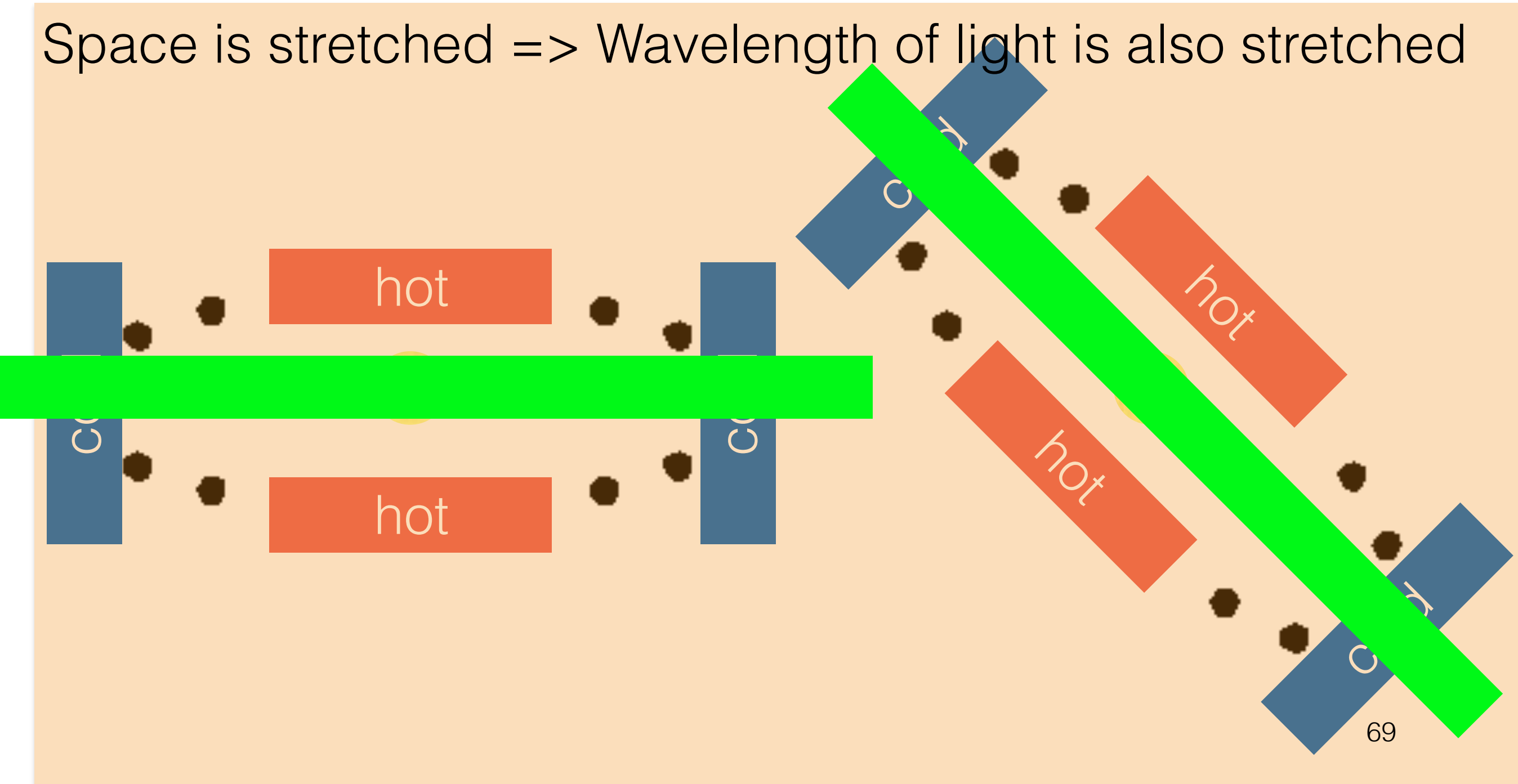


Photo Credit: TALEX



horizontally polarised

Photo Credit: TALEX

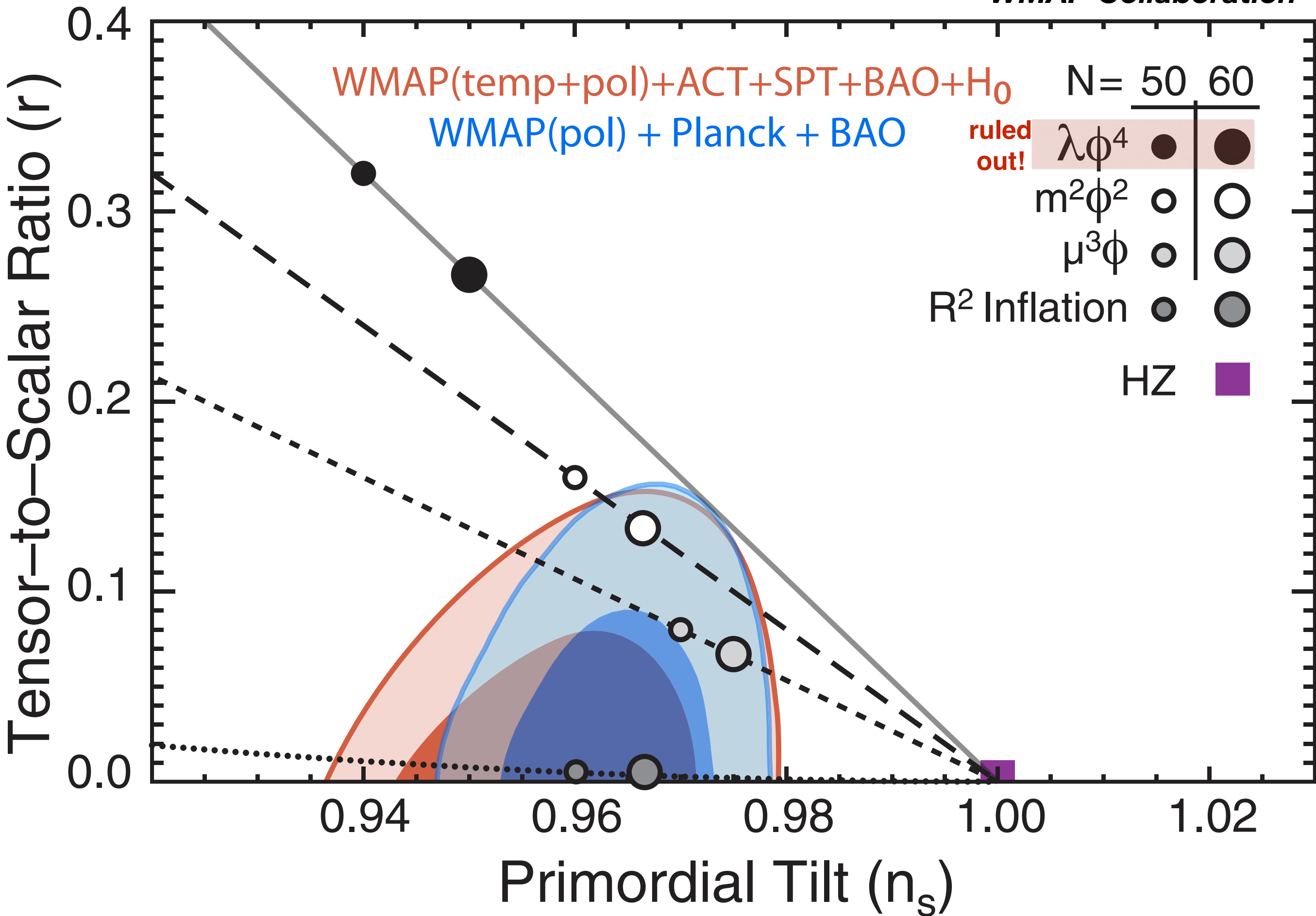


Tensor-to-scalar Ratio

$$r \equiv \frac{\langle h_{ij} h^{ij} \rangle}{\langle \zeta^2 \rangle}$$

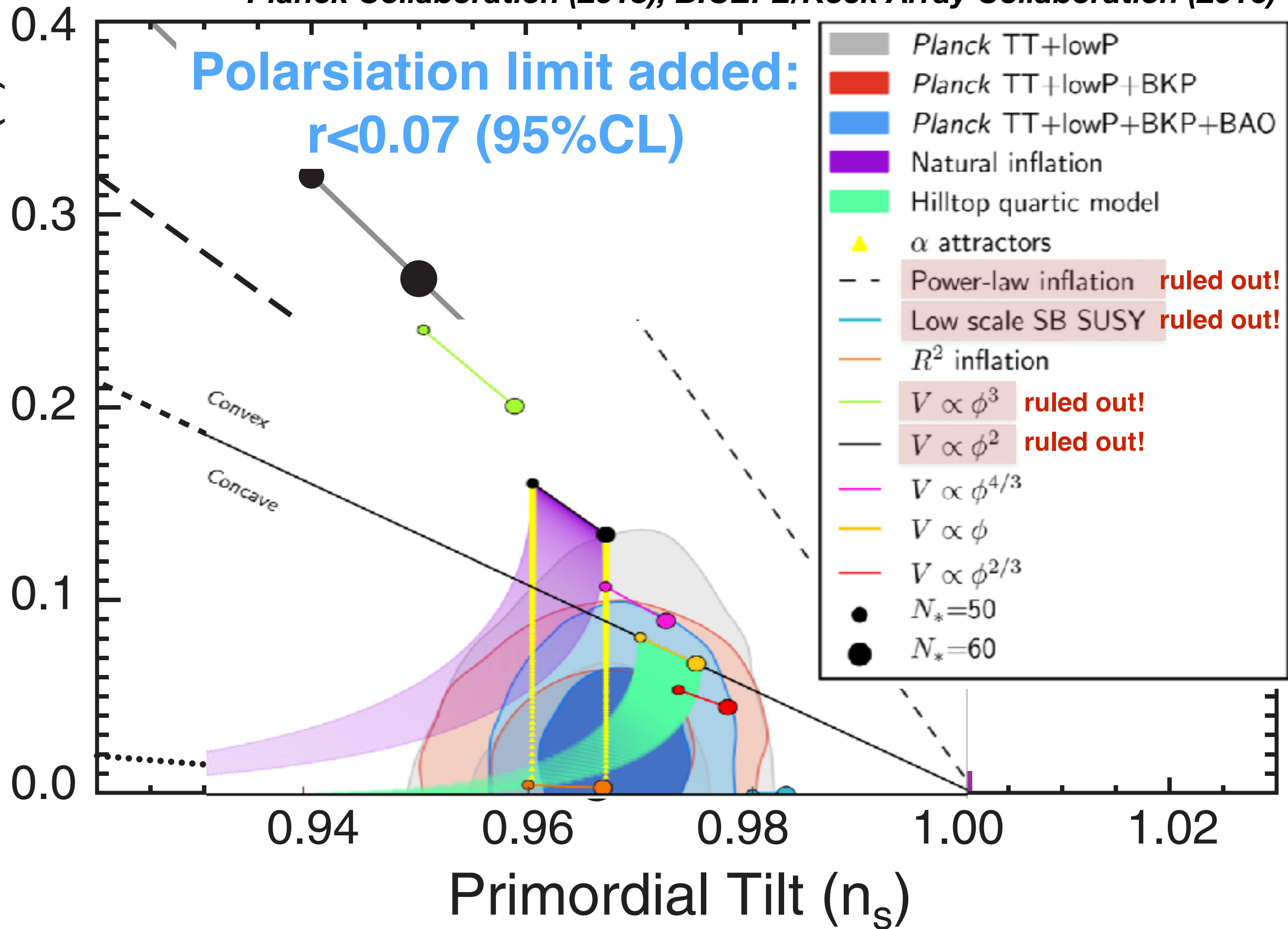
- We really want to find this! The current upper bound is **$r < 0.07$** (95%CL)

BICEP2/Keck Array Collaboration (2016)



Tensor-to-Scalar Ratio (r)

Polarisation limit added:
 $r < 0.07$ (95%CL)

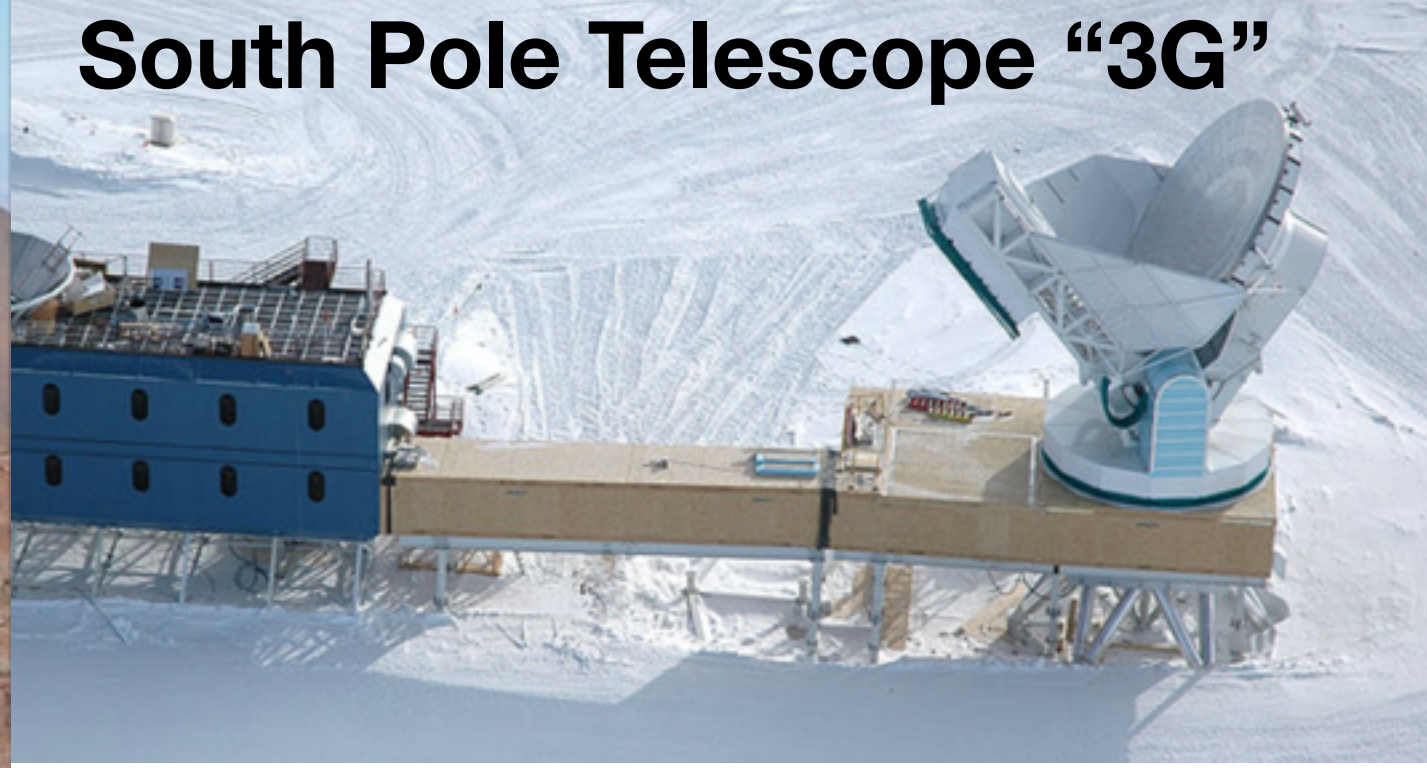


What comes next?

Advanced Atacama Cosmology Telescope

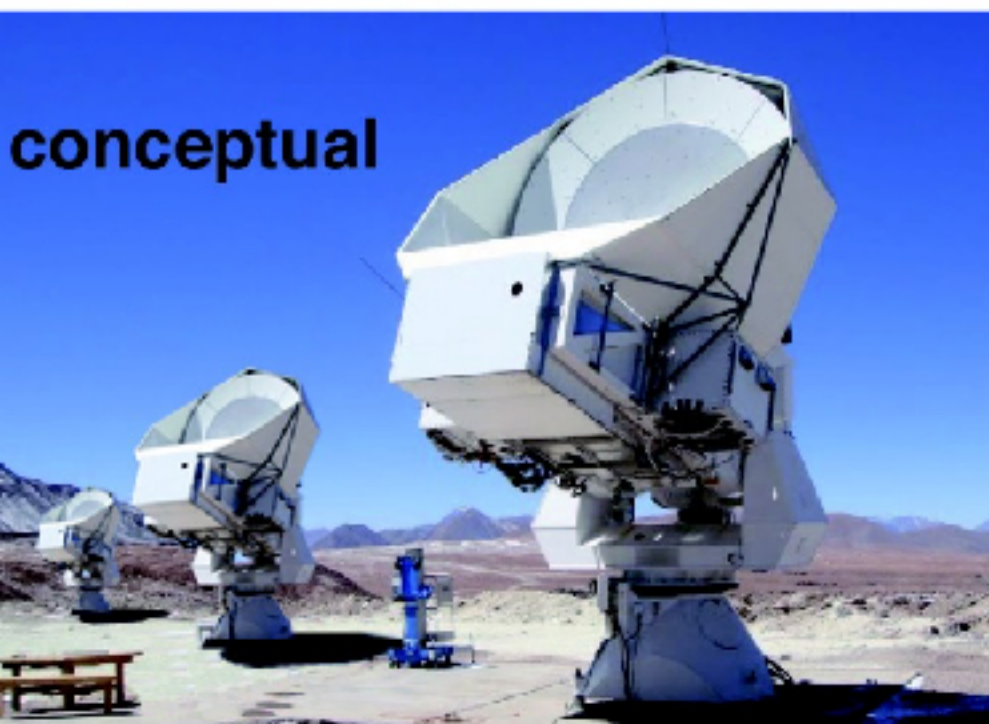


South Pole Telescope “3G”



What comes next?

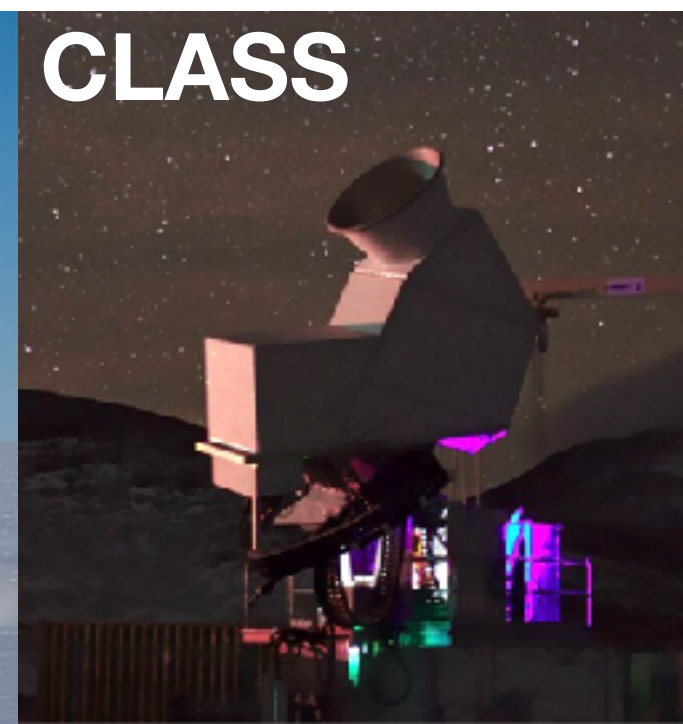
The Simons Array



BICEP/Keck Array



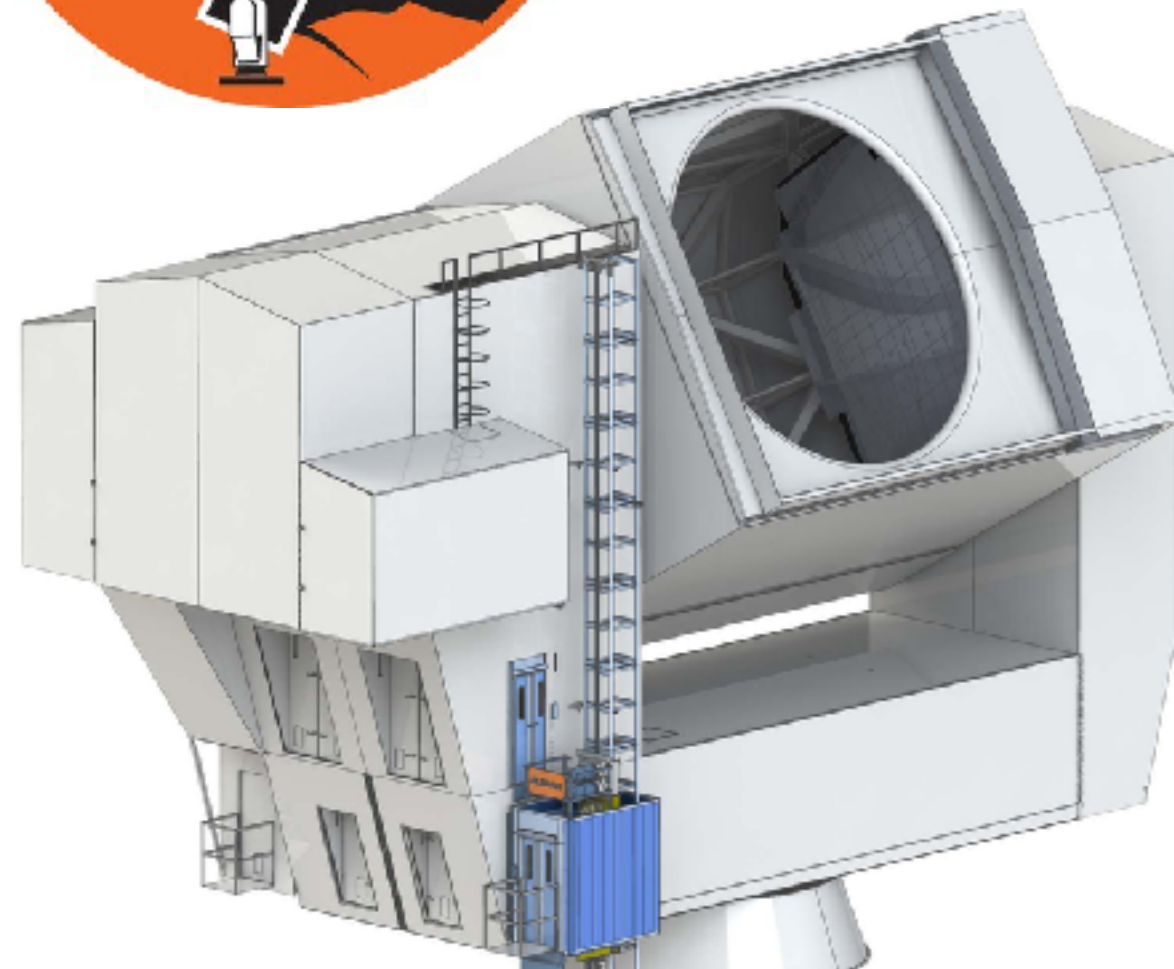
CLASS

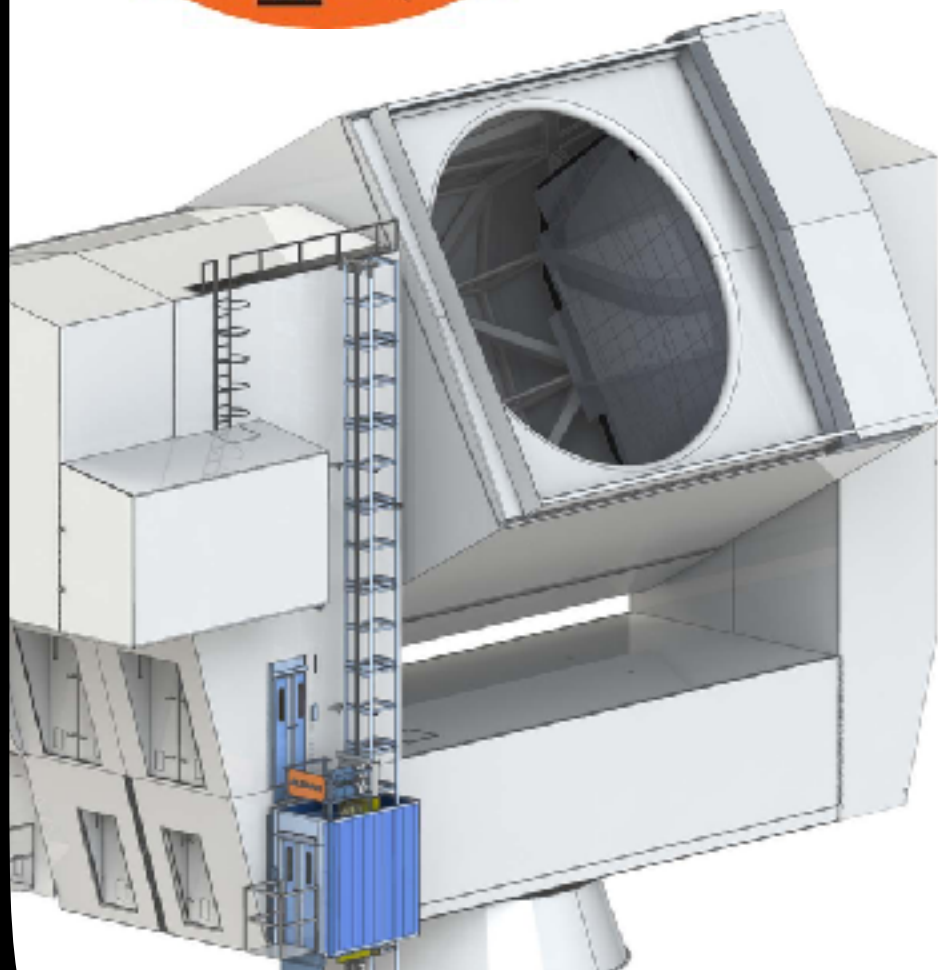
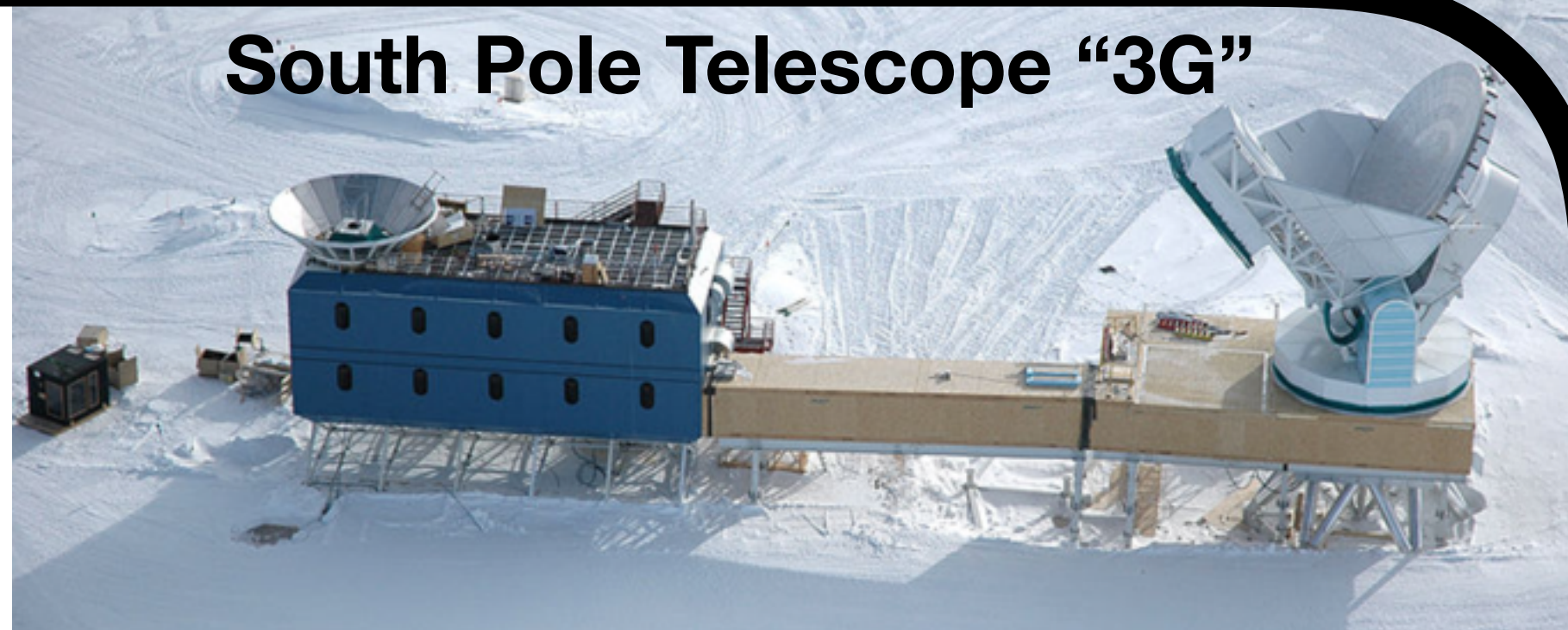


Advanced Atacama Cosmology Telescope

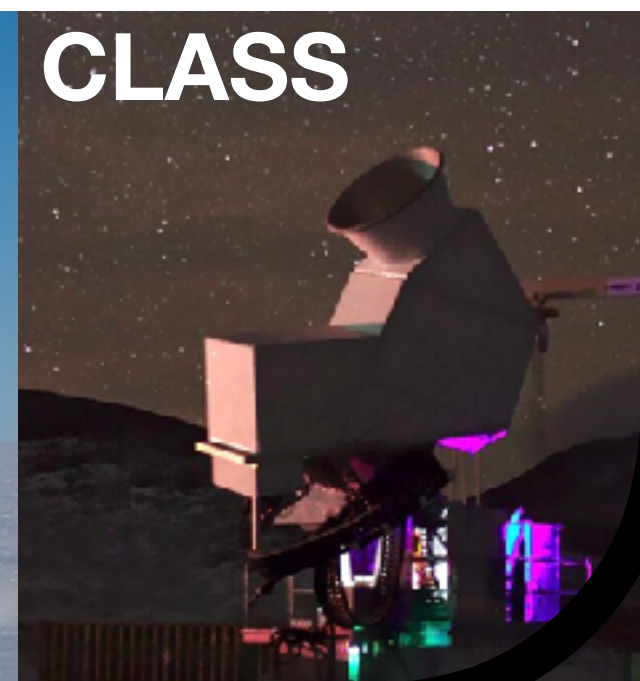


The Simons Array





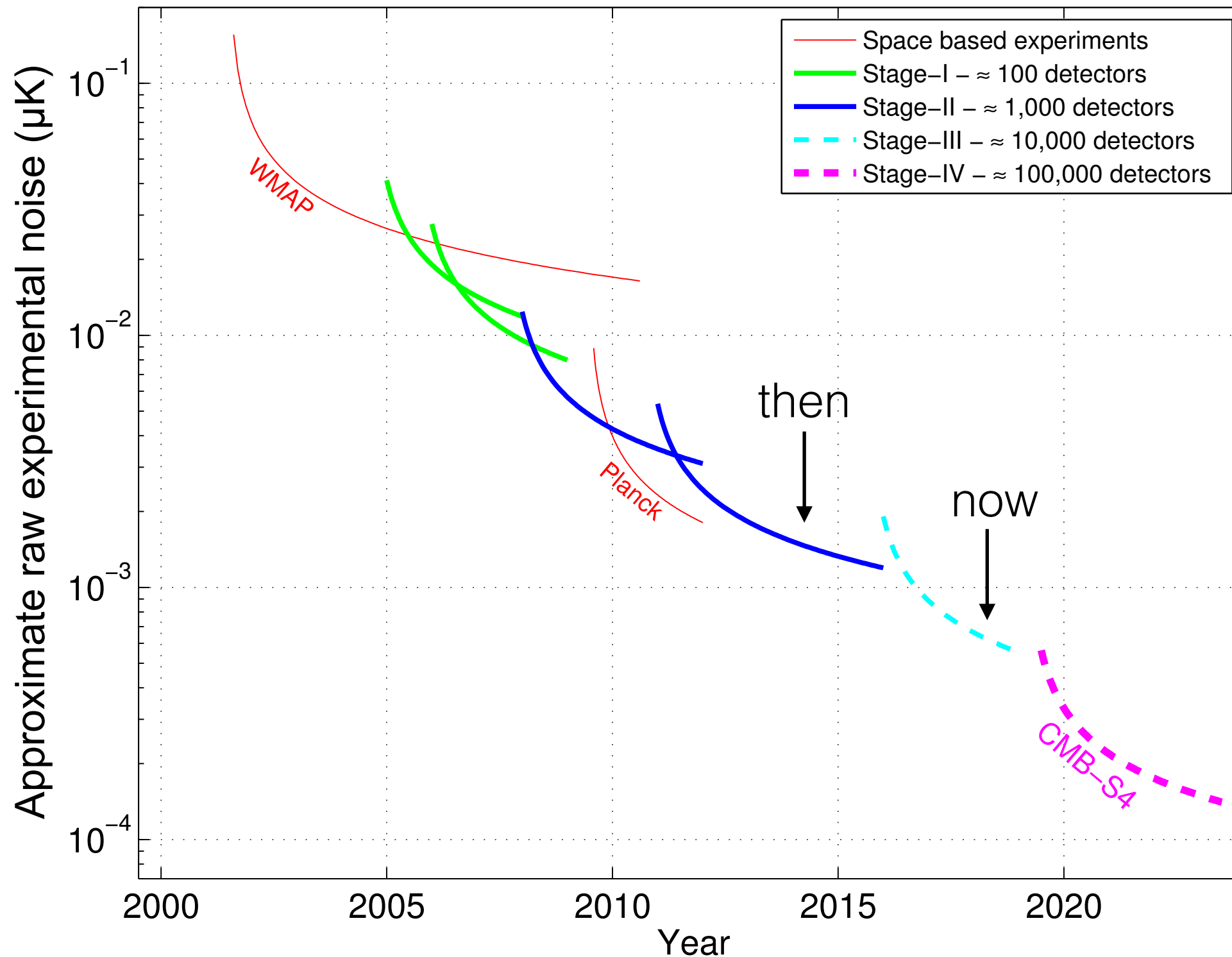
CMB-S4(?)



CMB-S4

Next Generation CMB Experiment

CMB Stages



The Biggest Enemy: Polarised Dust Emission

- The upcoming data will **NOT** be limited by statistics, but by systematic effects such as the Galactic contamination
- **Solution**: Observe the sky at multiple frequencies, especially at high frequencies (>300 GHz)
- This is challenging, unless we have a superb, high-altitude site with low water vapour
- CCAT-p!

March 17, 2014

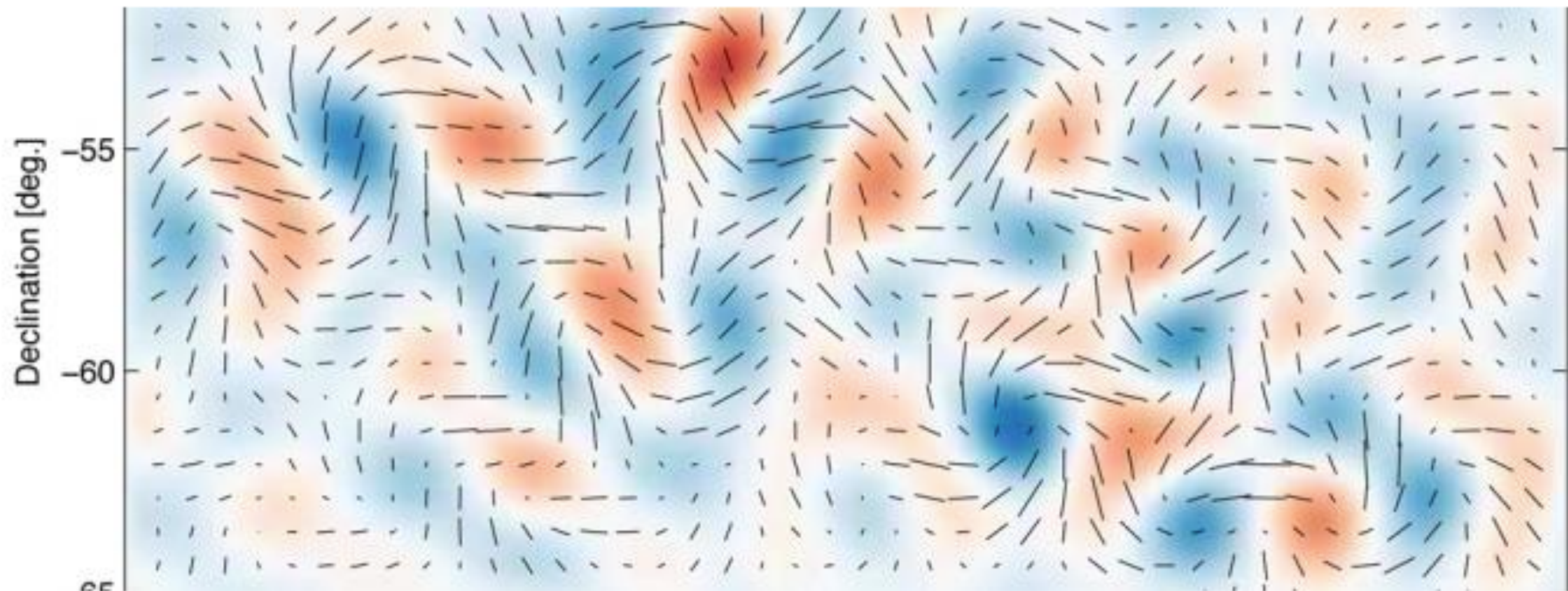
BICEP2's announcement



First Direct Evidence of Cosmic Inflation

Release No.: 2014-05

For Release: Monday, March 17, 2014 - 10:45am



Cambridge, MA - Almost 14 billion years ago, the universe we inhabit burst into existence in an extraordinary event that initiated the Big Bang. In the first fleeting fraction of a second, the universe expanded exponentially, stretching far beyond the view of our best telescopes. All this, of course, was just theory.

SPACE & COSMOS

The New York Times

Space Ripples Reveal Big Bang's Smoking Gun

By DENNIS OVERBYE MARCH 17, 2014

BBC

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17 March 2014 Last updated at 14:46 GMT

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Cosmic inflation: 'Spectacular' discovery hailed

By Jonathan Amos

Science correspondent, BBC News



Cambridge, MA - Almost 14 billion years ago, the event that initiated the Big Bang. In the far beyond the view of our best tel

Süddeutsche.de

Wissen

Politik Panorama Kultur Wirtschaft Sport München Bayern Digital Auto Reise Video

Home > Wissen > Urknall > Urknall - Gravitationswellen belegen inflationäres Universum

Süddeutsche.de als Startseite einrichten

17. März 2014, 17:34 Gravitationswellen

Signale aus der Geburtsstunde des Universums

Von Patrick Illinger

January 30, 2015

Joint Analysis of BICEP2 data and Planck data

Speck of Interstellar Dust Obscures Glimpse of Big Bang

By DENNIS OVERBYE JAN. 30, 2015

BBC

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30 January 2015 Last updated at 20:54 GMT



Cosmic inflation: New study says BICEP claim was wrong

By Jonathan Amos
Science correspondent, BBC News

Süddeutsche.de

Wissen

Politik Panorama Kultur Wirtschaft Sport München Bayern Digital Auto Reise Video

Home > Wissen > Kosmologie - Urknall-Forscher gestehen Irrtum ein

[Süddeutsche.de als Startseite einrichten](#)

Hir

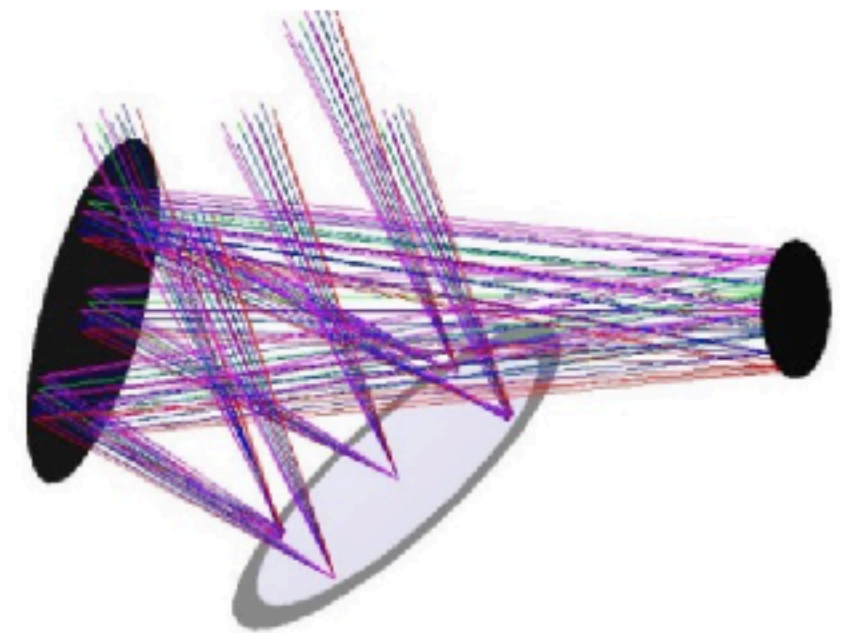
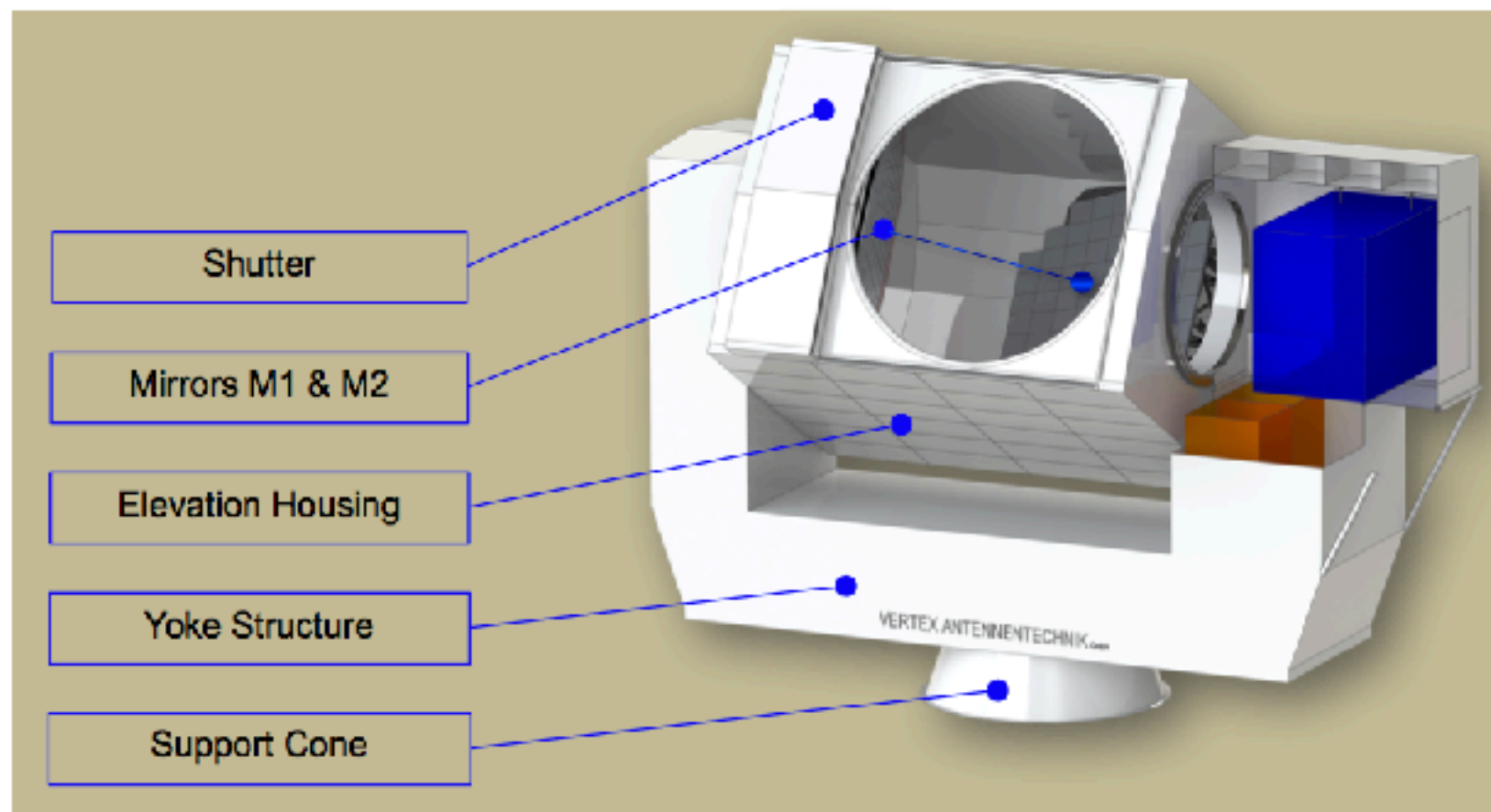
1. Februar 2015, 22:19 Kosmologie

Urknall-Forscher gestehen Irrtum ein

Von Marlene Weiß

What is CCAT-p?

CCAT-prime is a high surface accuracy /
throughput 6 m submm (0.3-3mm) telescope



Cornell U. + German consortium + Canadian consortium + ...

Where is CCAT-p?

Cerro Chajnantor at 5600 m w/ TAO



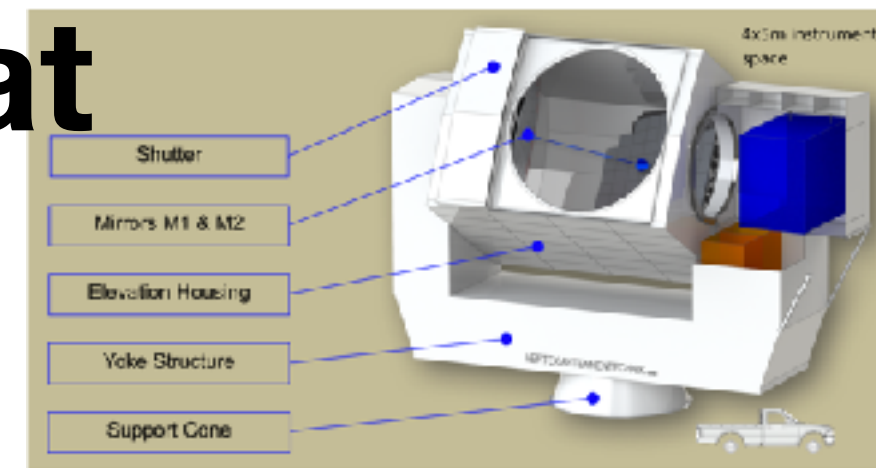
A Game Changer

- **CCAT-p**: 6-m, **Cross-dragone** design, on Cerro Chajnantor (5600 m)

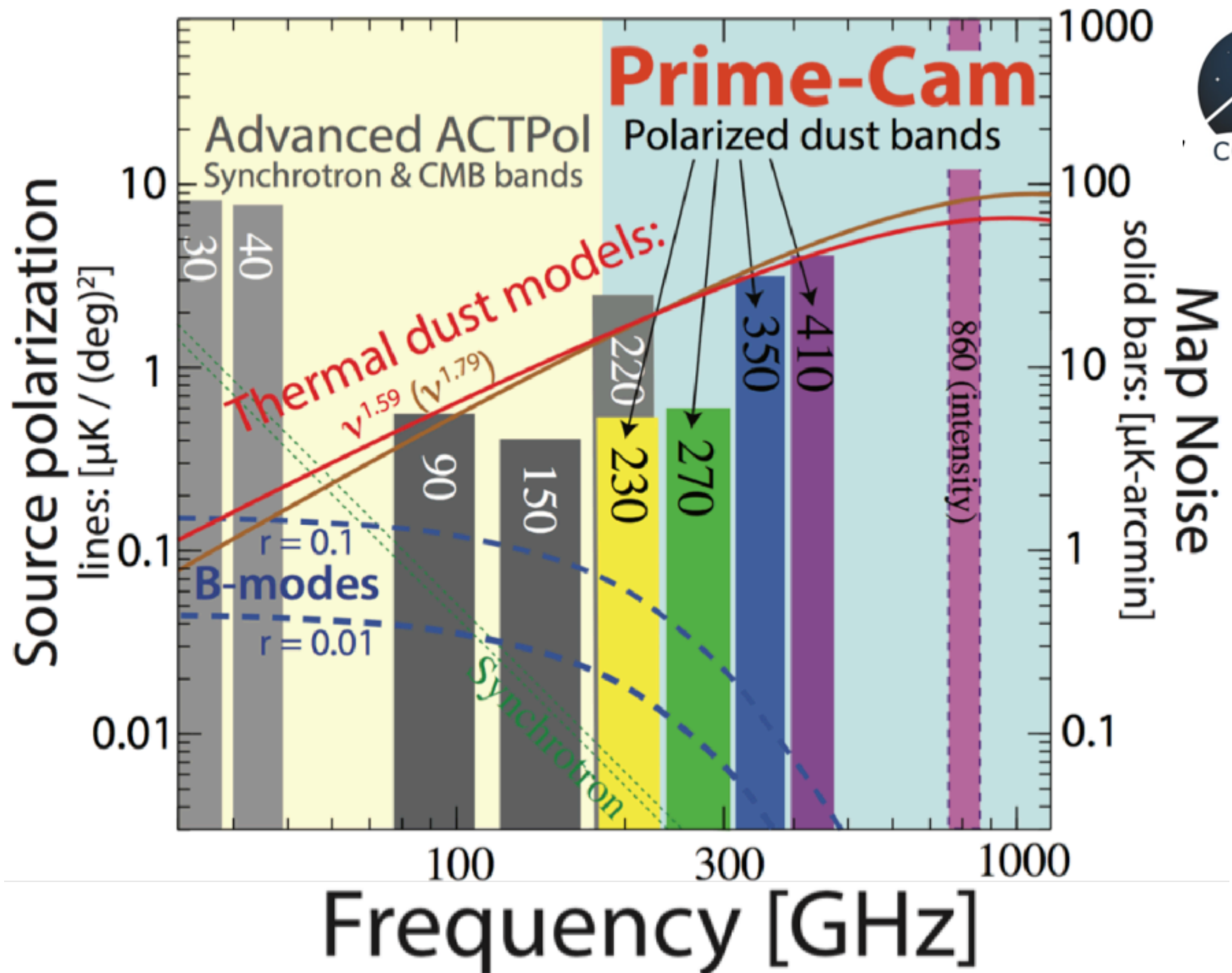
- **Germany makes great telescopes!**

CCAT-prime

designed and built by Vertex Antennentechnik GmbH, Duisburg

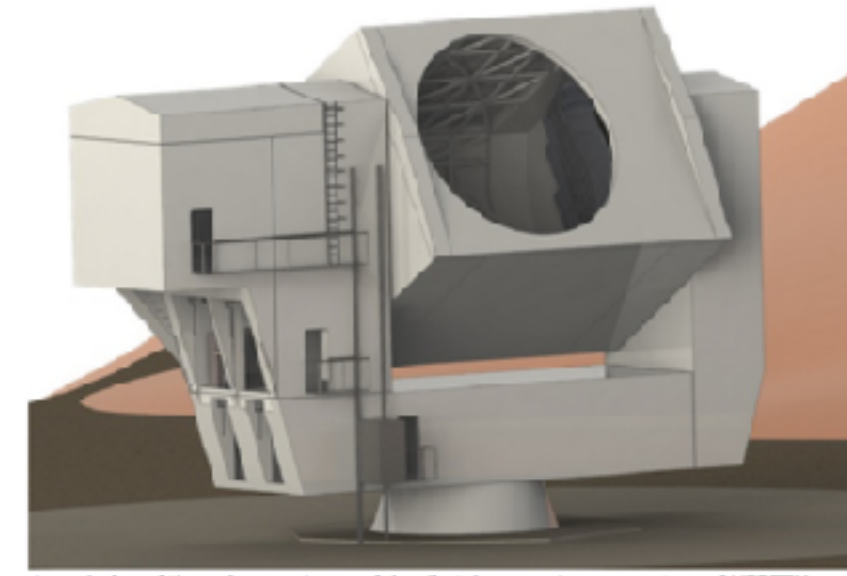
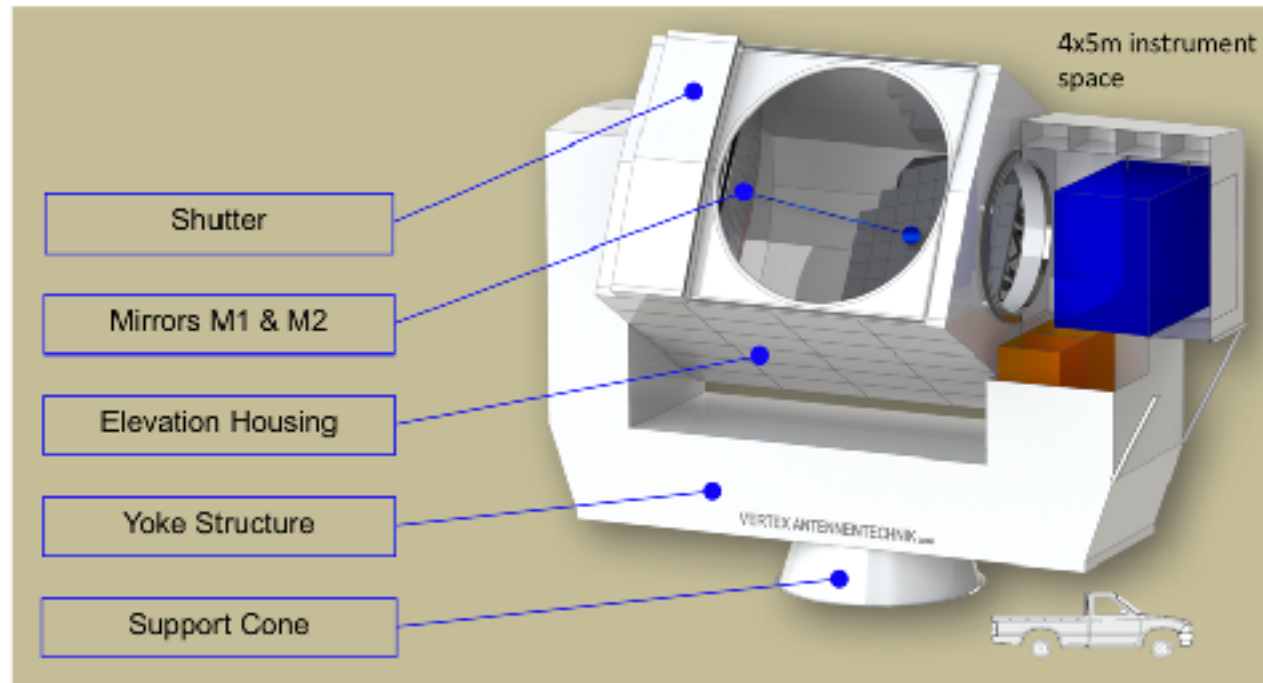


- Design study completed, and the contract has been signed by “VERTEX Antennentechnik GmbH”
 - CCAT-p is a great opportunity for Germany to make significant contributions towards the CMB S-4 landscape (both US and Europe) by providing telescope designs and the “lessons learned” with prototypes.



CCAT-prime

designed and built by Vertex Antennentechnik GmbH, Duisburg



A rendering of the unique and powerful radio telescope. Image courtesy of VERTEX ANTENNENTECHNIK.

Simons Observatory (USA)

in collaboration

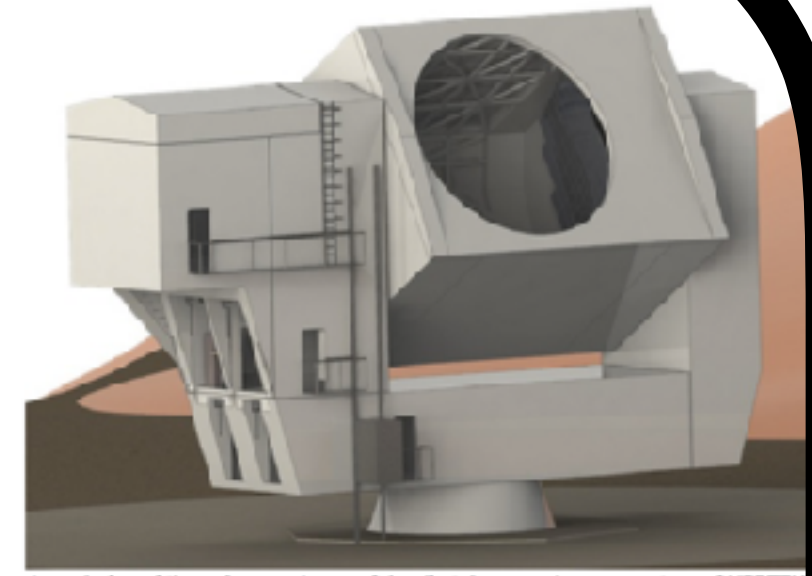
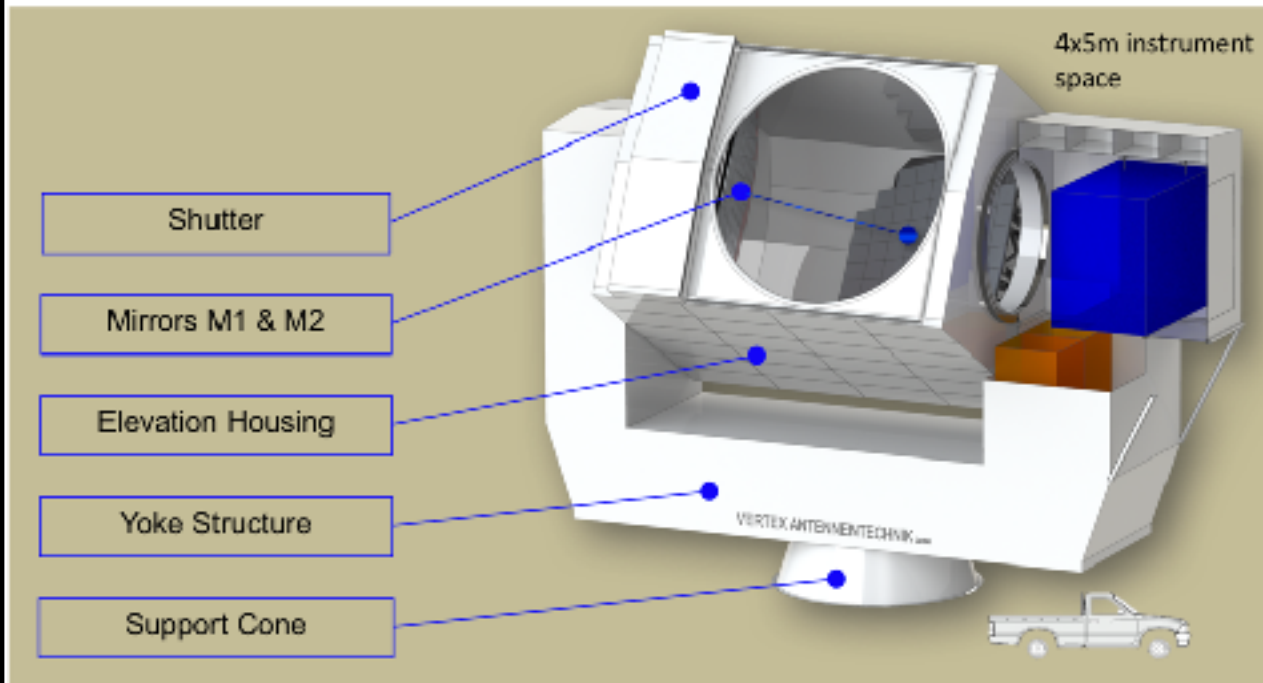


South Pole?

This could be “CMB-S4”

CCAT-prime

designed and built by Vertex Antennentechnik GmbH, Duisburg



A rendering of the unique and powerful radio telescope. Image courtesy of VERTEX ANTENNENTECHNIK.

**Simons Observatory
(USA)**

in collaboration



South Pole?

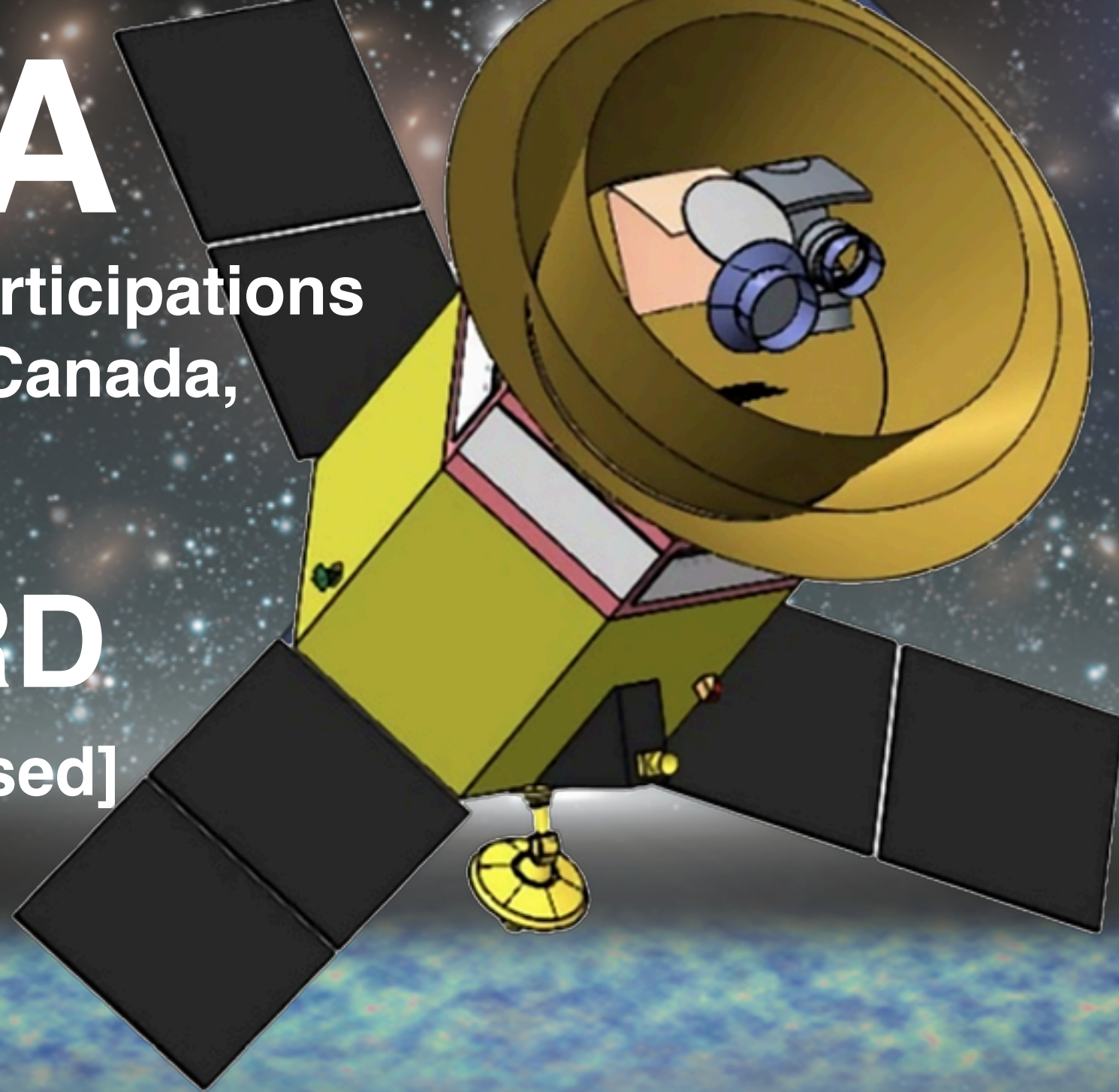
**To have even more
frequency coverage...**

JAXA

+ possible participations
from USA, Canada,
Europe

LiteBIRD

2027– [proposed]



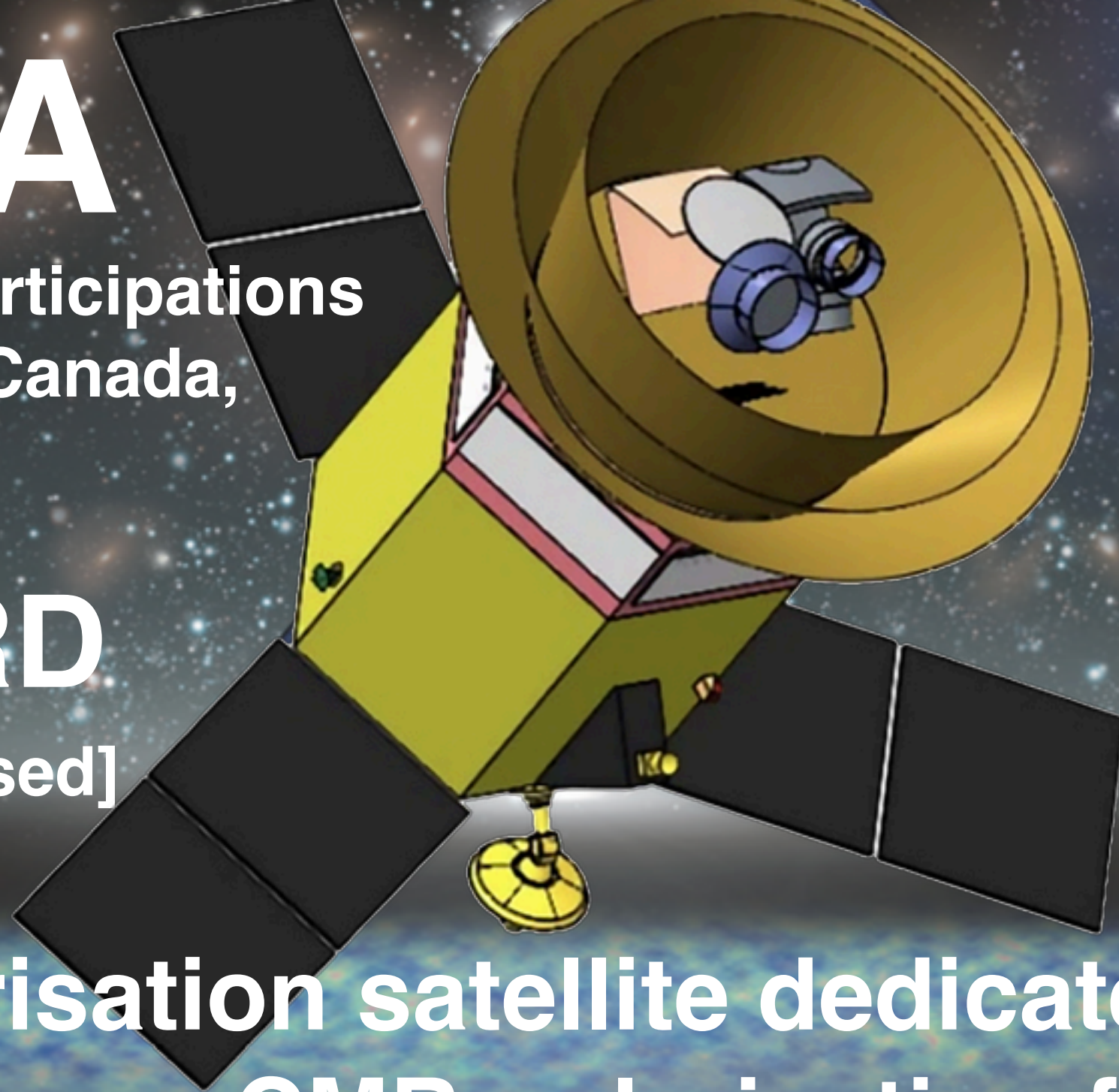
Target: $\delta r < 0.001$ (68%CL)

JAXA

+ possible participations
from USA, Canada,
Europe

LiteBIRD

2027– [proposed]



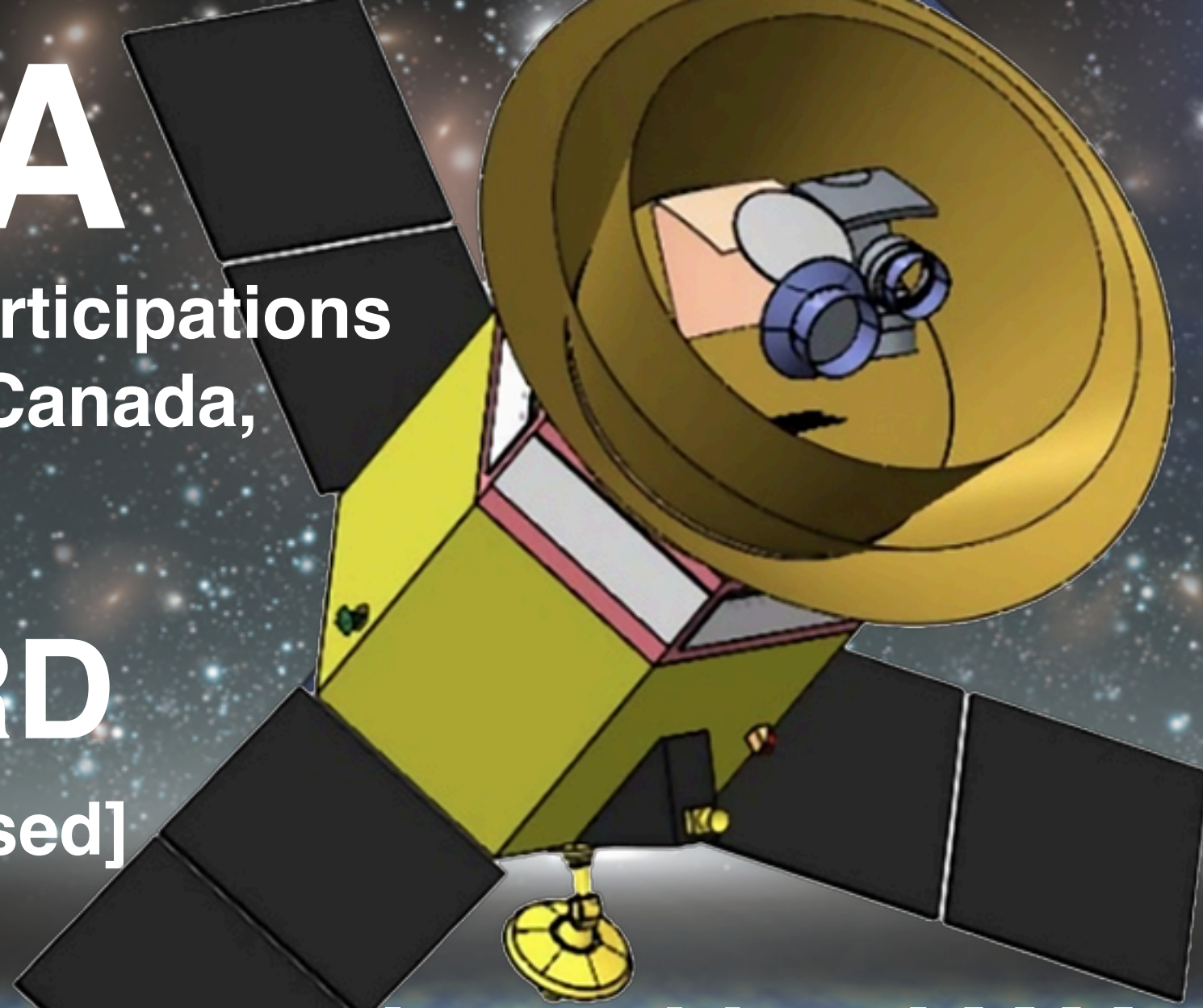
**Polarisation satellite dedicated to
measure CMB polarisation from
primordial GW, with a few thousand
super-conducting detectors in space**

JAXA

+ possible participations
from USA, Canada,
Europe

LiteBIRD

2027– [proposed]

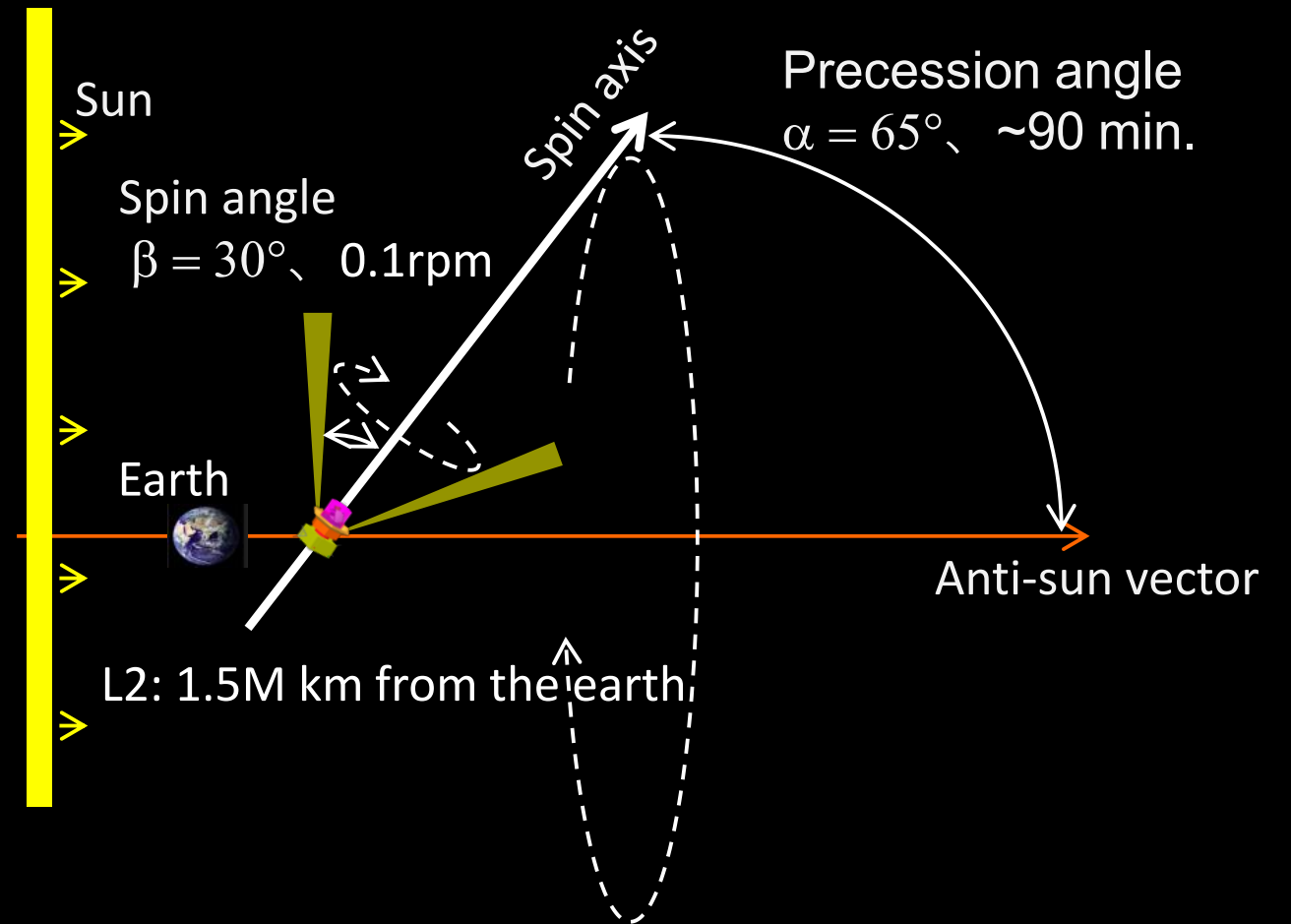


Down-selected by JAXA as
one of the two missions
competing for a launch in mid 2020's

Observation Strategy

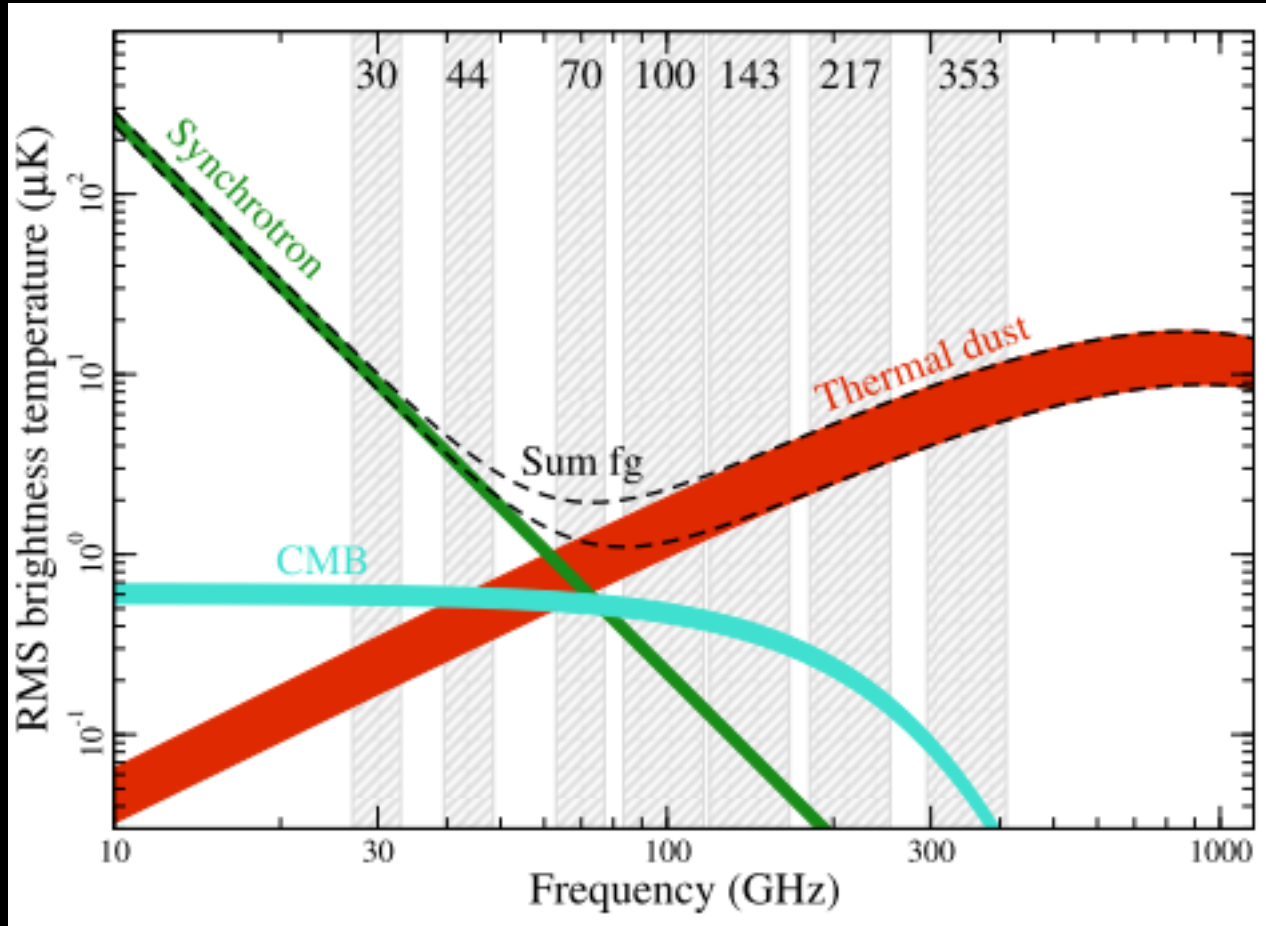


JAXA H3 Launch Vehicle (JAXA)

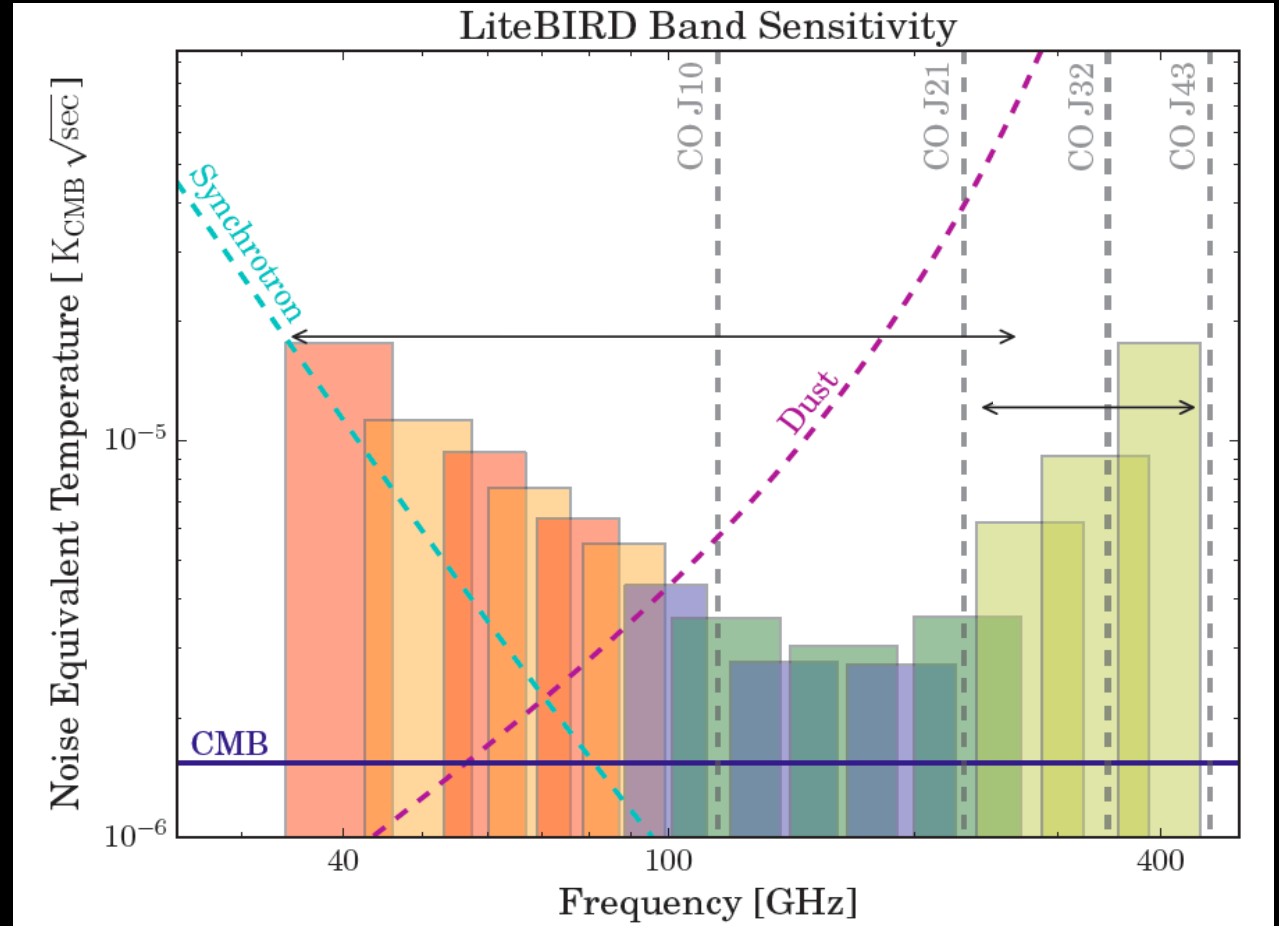


- Launch vehicle: **JAXA H3**
- Observation location: Second Lagrangian point (**L2**)
- Scan strategy: **Spin and precession, full sky**
- Observation duration: **3-years**
- Proposed launch date: **Mid 2020's**

Foreground Removal



Polarized galactic emission (Planck X)

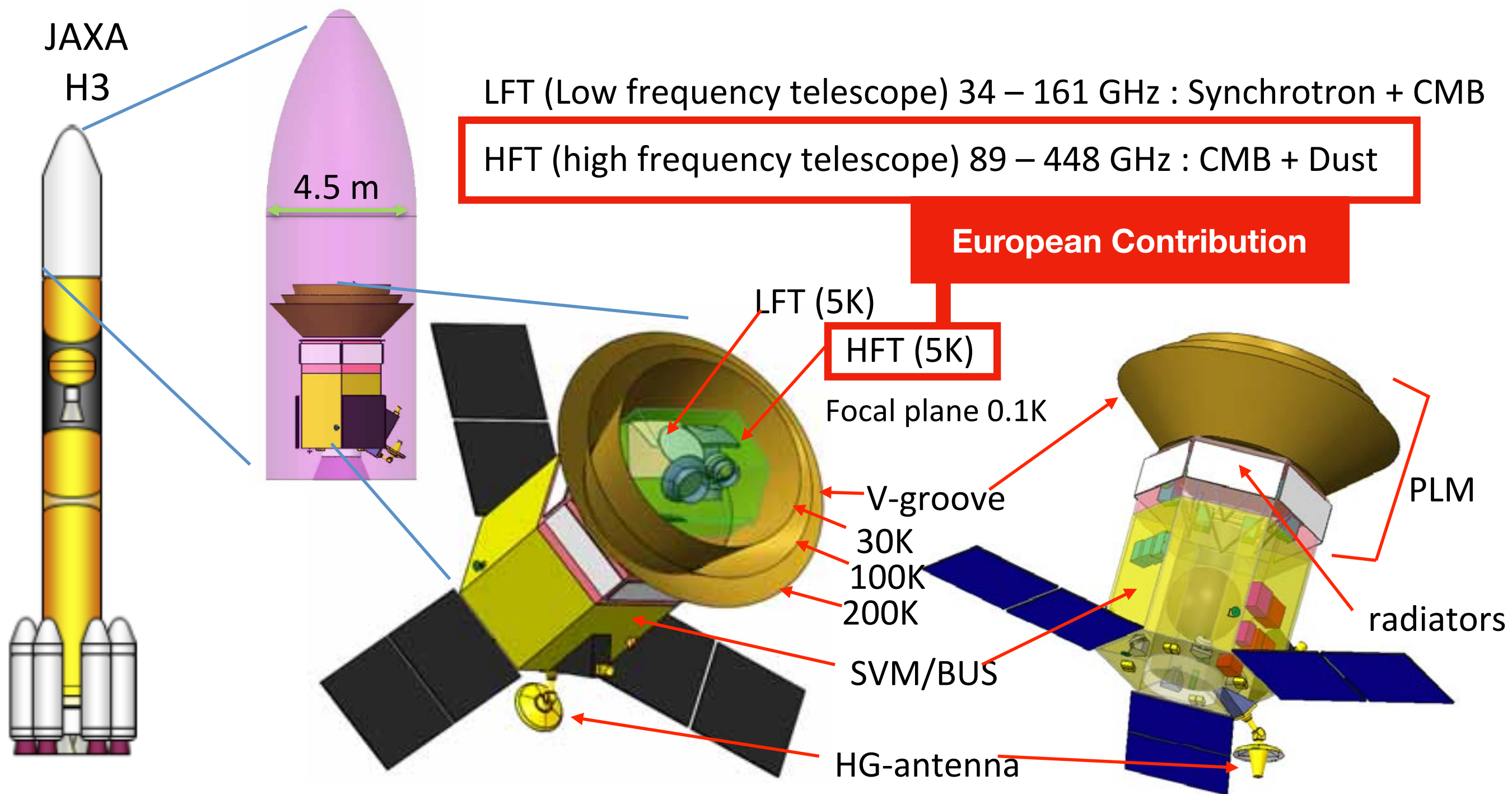
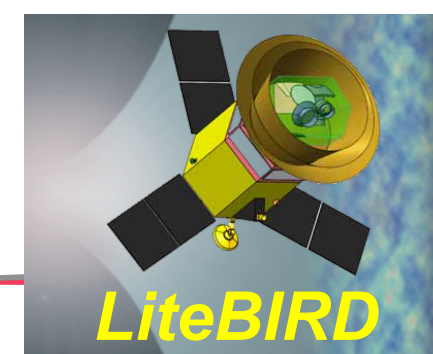


LiteBIRD: 15 frequency bands

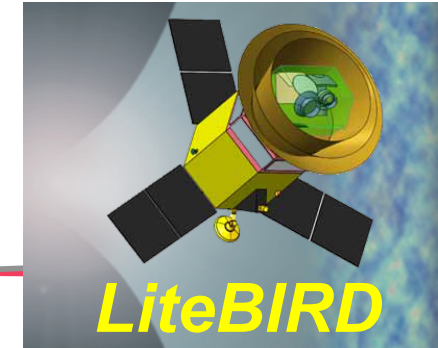
- Polarized foregrounds
 - Synchrotron radiation and thermal emission from inter-galactic dust
 - Characterize and remove foregrounds
 - 15 frequency bands between 40 GHz - 400 GHz
 - Split between Low Frequency Telescope (LFT) and High Frequency Telescope (HFT)
 - LFT: 40 GHz – 235 GHz
 - HFT: 280 GHz – 400 GHz
- Slide courtesy Toki Suzuki (Berkeley)

Slide courtesy Toki Suzuki (Berkeley)

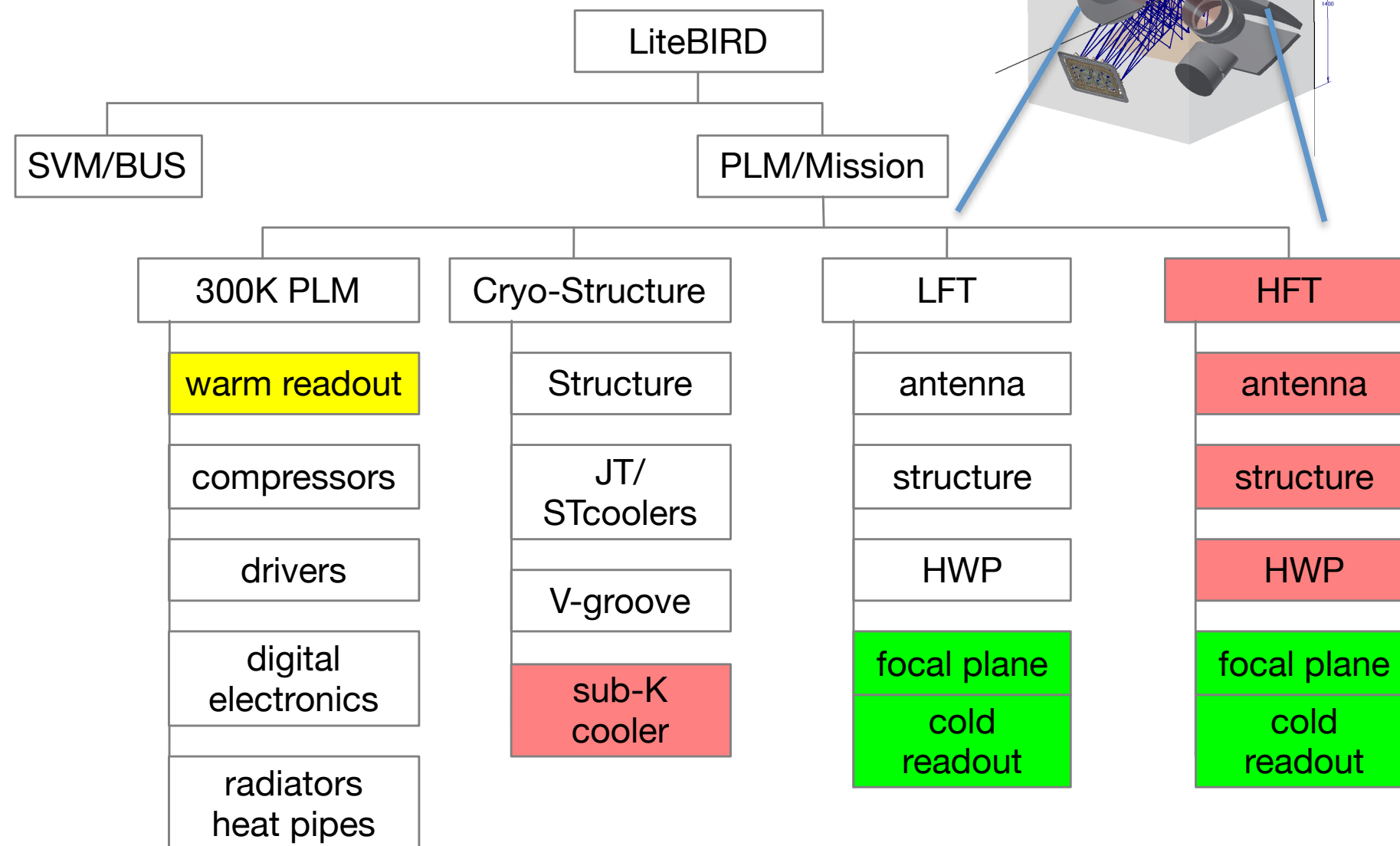
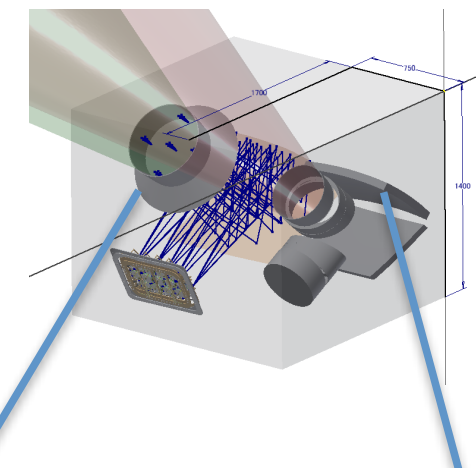
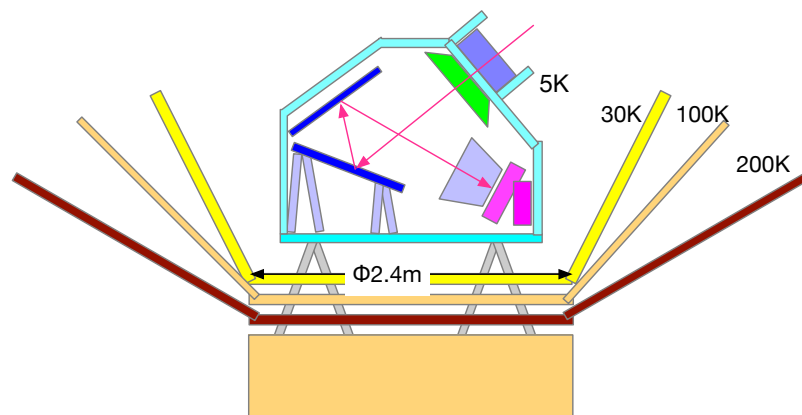
LiteBIRD Spacecraft



LiteBIRD product tree



LFT 34 – 161 GHz
HFT 89 – 448 GHz

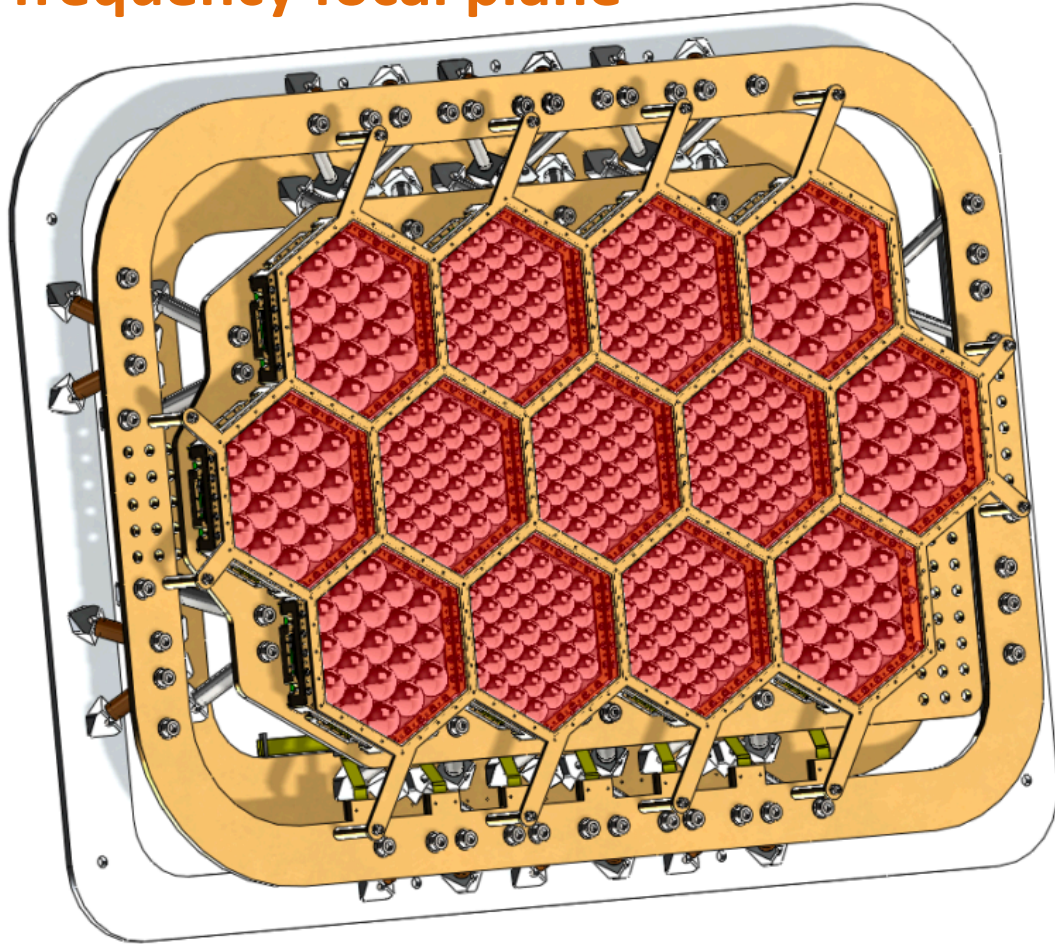


Summary

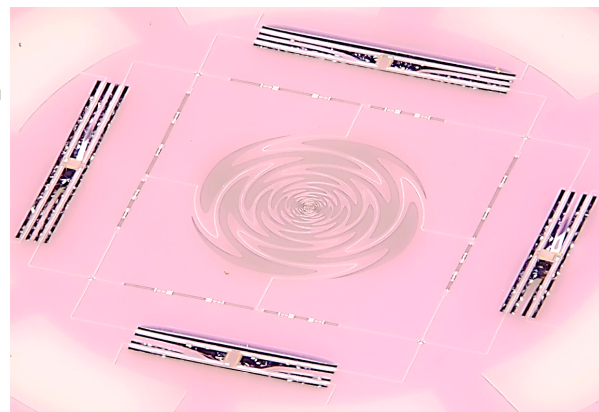
- Inflation looks good: all the CMB data support it
- **Next frontier**: Using CMB polarisation to find GWs from inflation. **Definitive evidence for inflation!**
- With CCAT-p we can remove the dust polarisation to reach $r \sim 10^{-2}$ **reliably**, i.e., 10 times better than the current bound
- With LiteBIRD we plan to reach $r \sim 10^{-3}$, i.e., 100 times better than the current bound

LFT and HFT focal plane units using TES

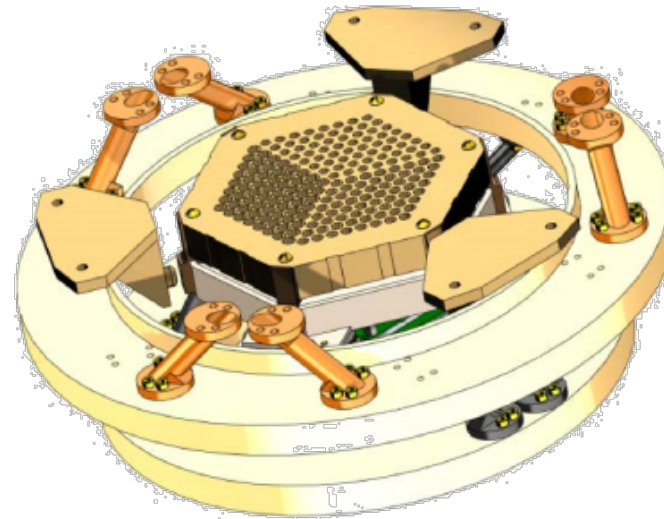
Low frequency focal plane



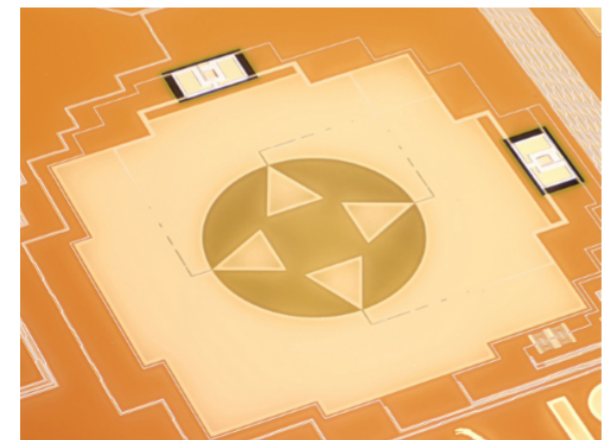
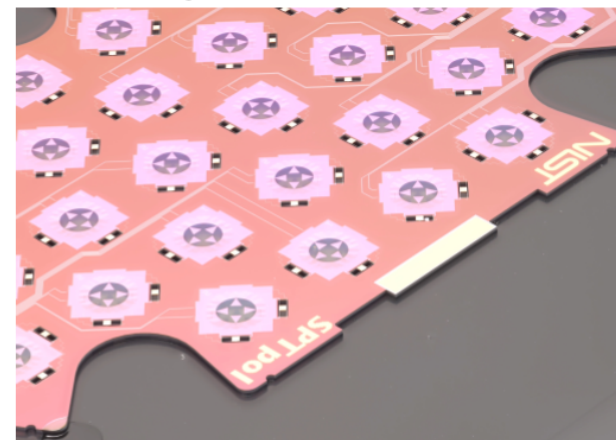
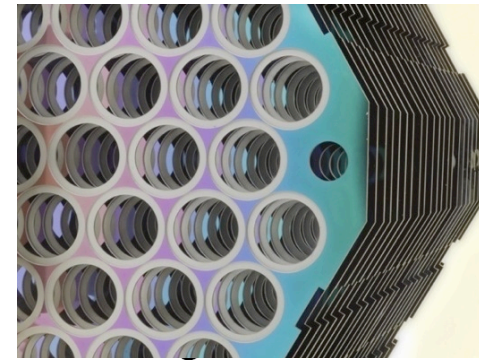
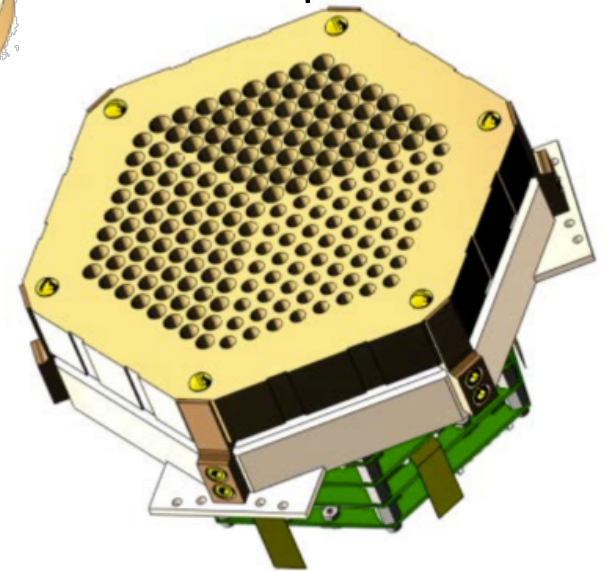
Three colors per pixel with a lenslet coupling.



High frequency focal plane



Each color per feed, and three colors within one focal plane.



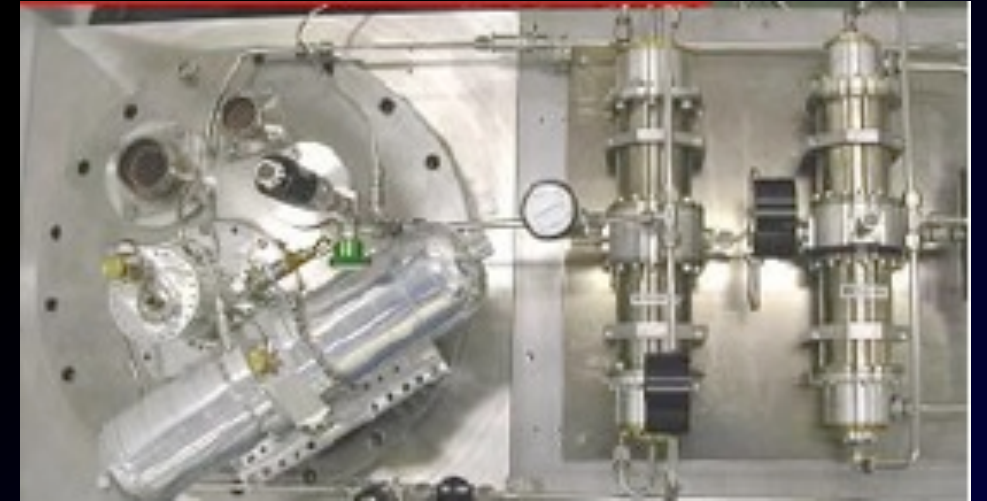
- The current baseline design uses a single ADR to cool the both focal planes.
- The LF focal plane has ** TESs and the HF focal plane has ** TESs.
- The TES is read by SQUID together with the readout electronics is based on the digital frequency multiplexing system.
- The effect of the cosmic ray is evaluated by building a model. The irradiation test is in plan.

Slide courtesy Tomo Matsumura (Kavli IPMU)

Cooling system

Cryogenics

- Warm launch
- 3 years of observations
- 4 K for the mission instruments (optical system)
- 100 mK for the focal plane



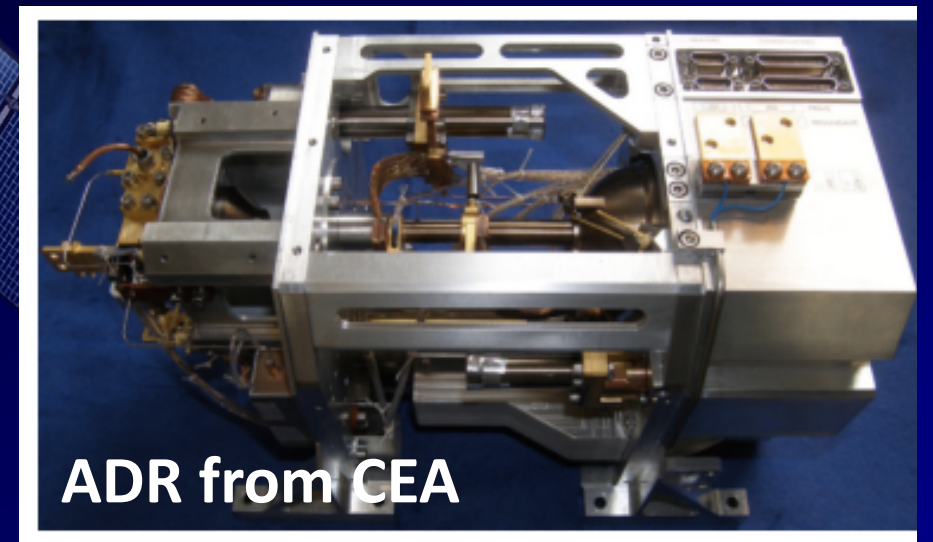
SHI/JAXA

Mechanical cooler

- The 2-stage Stirling cooler and 4K-JT cooler from the heritage of the JAXA satellites, **Akari** (Astro-F), **JEM-SMILES** and **Astro-H**.
- The 1K-JT provides the 1.7 K interface to the sub-Kelvin stage.

Sub-Kelvin cooler

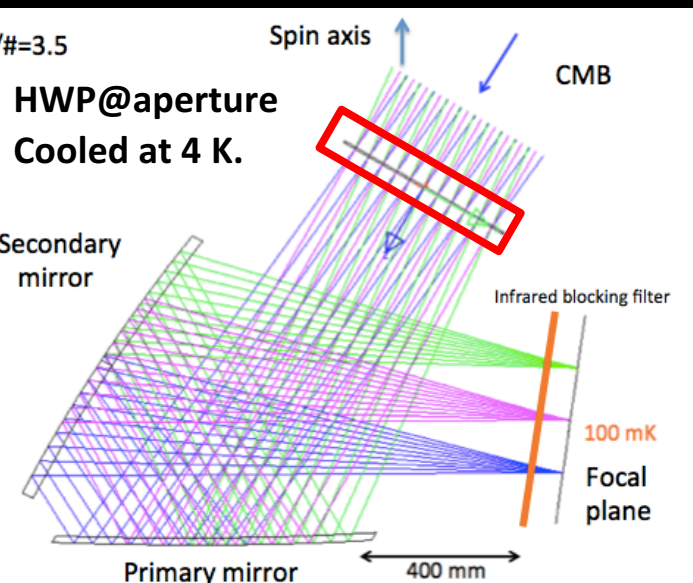
- ADR has a high-TRL and extensive development toward **Astro-H**, **SPICA**, and **Athena**.
- Closed dilution with the Planck heritage is also under development.



ADR from CEA

Slide courtesy Tomo Matsumura (Kavli IPMU)

Polarization modulator



- Due to our focus on the primordial signal at low ℓ , we employ the continuously rotating achromatic half-wave plate (HWP).
- The HWP modulator suffices mitigating the $1/f$ noise and the differential systematics.

Broadband coverage

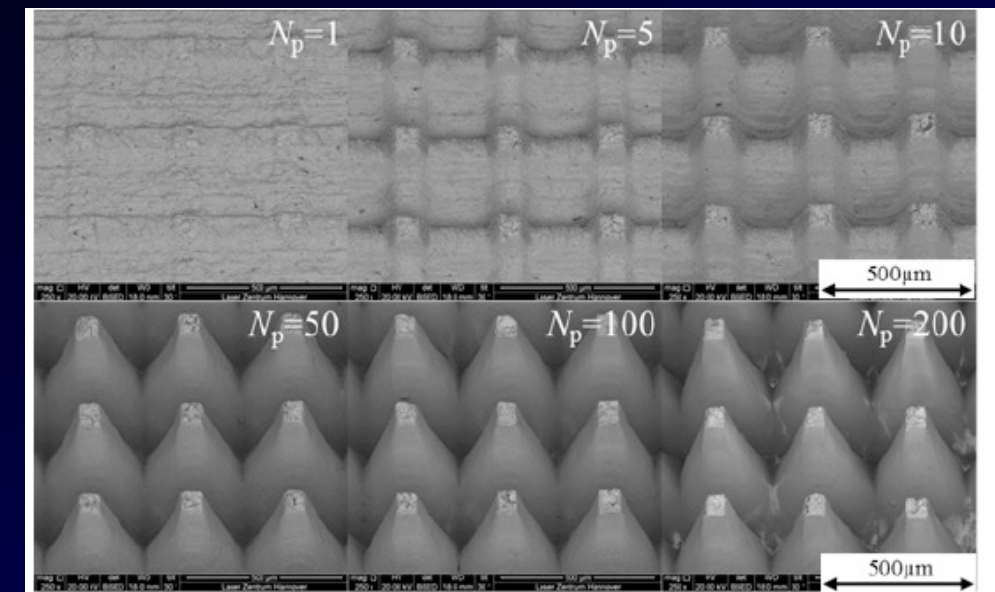
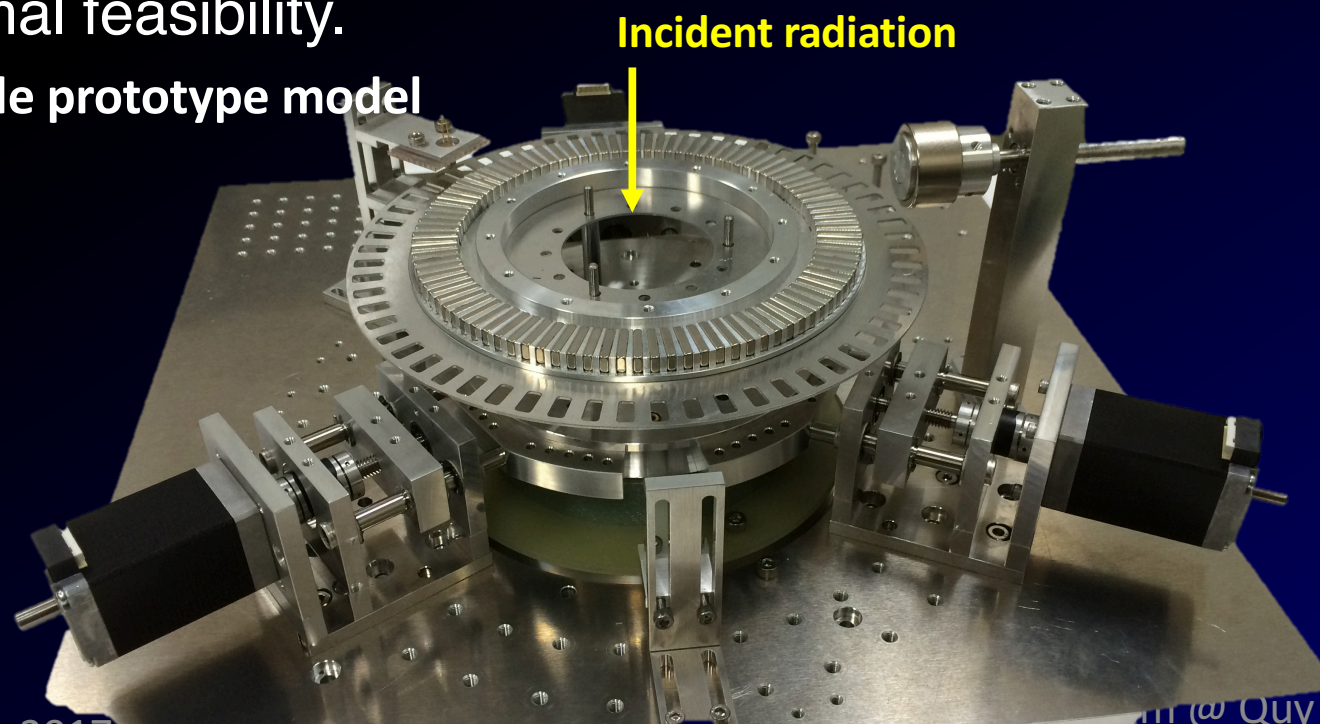
- The broadband coverage is done by the sub-wavelength anti-reflection structure.
- The broadband modulation efficiency is achieved by using 9-layer achromatic HWP.

ote: we also employ the polarization modulator for HFT.

Rotational mechanism

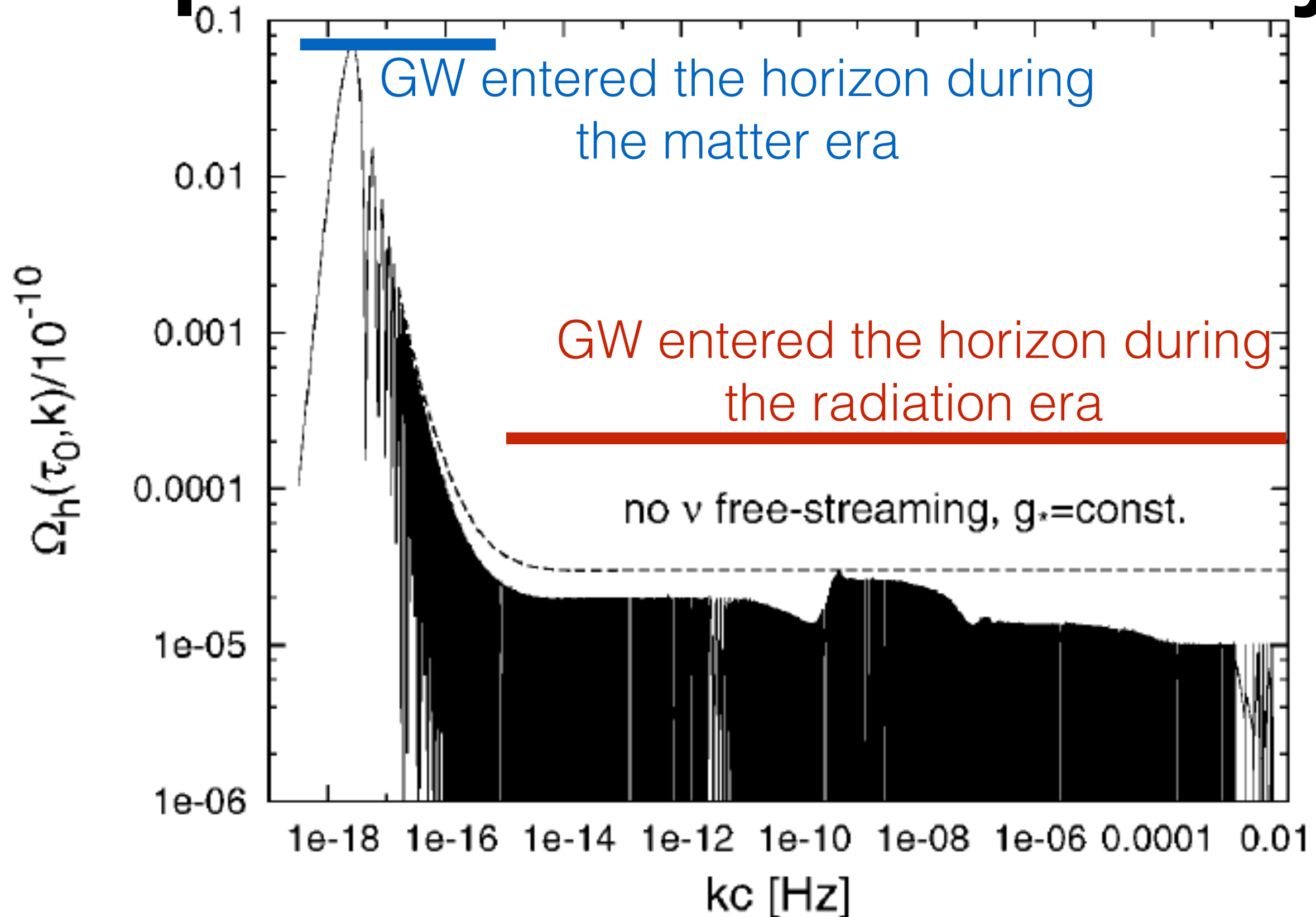
The continuous rotation is achieved by employing the superconducting magnetic bearing. This system has a heritage from EBEX. The prototype system has built and test the kinetic and thermal feasibility.

The 1/9 scale prototype model

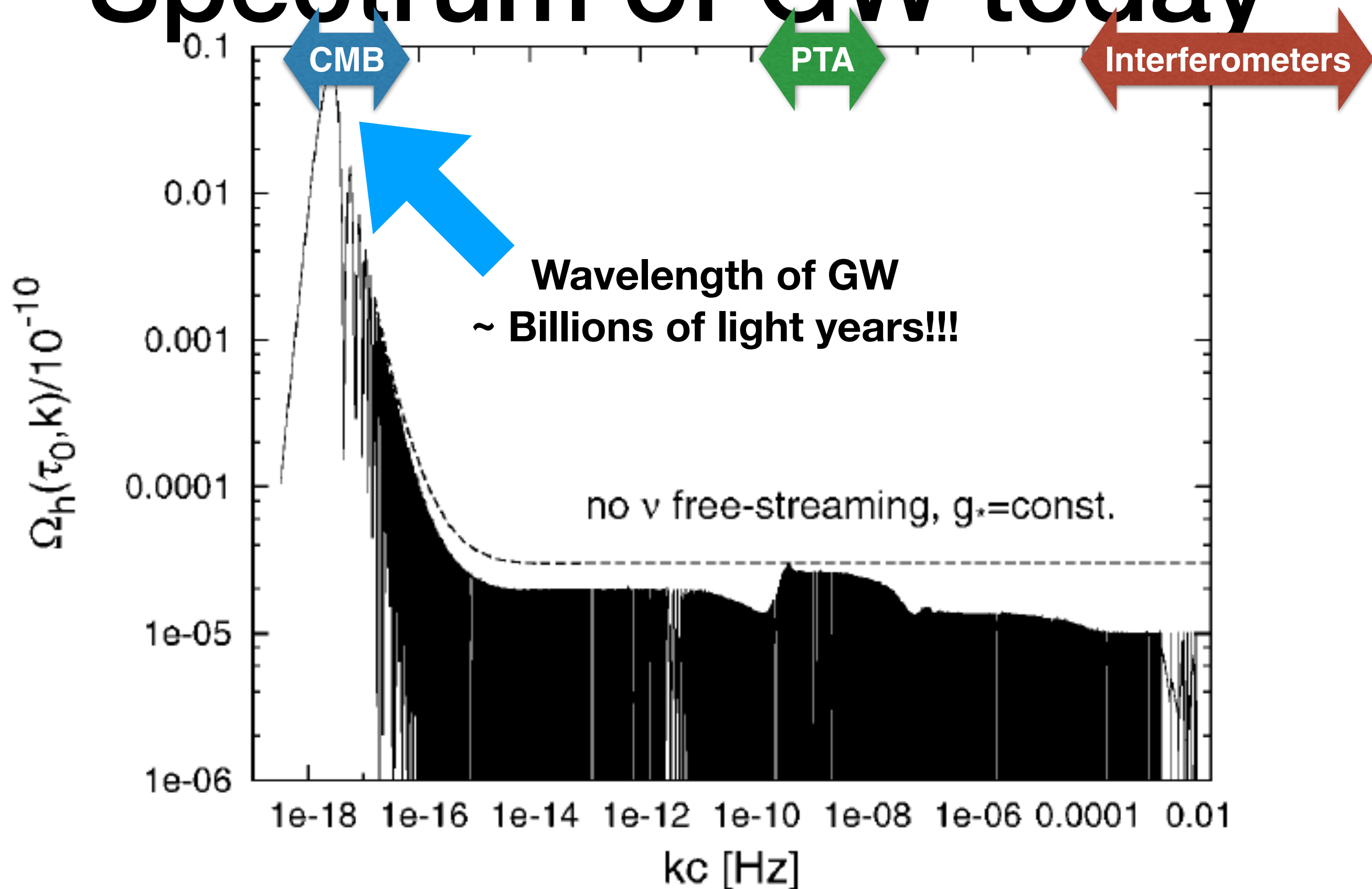


The proton irradiation test is conducted to key components, including sapphire, YBCO, and magnets. We have not found the no-go results. And the further test is in progress.

Theoretical energy density Spectrum of GW today



Theoretical energy density Spectrum of GW today



Finding Signatures of Gravitational Waves in the CMB

- **Next frontier in the CMB research**
 1. Find evidence for nearly scale-invariant gravitational waves
 2. Once found, test Gaussianity to make sure (or not!) that the signal comes from the vacuum fluctuation in spacetime
 3. Constrain inflation models

Are GWs from vacuum fluctuation in spacetime, or from sources?

$$\square h_{ij} = -16\pi G \pi_{ij}$$

- **Homogeneous solution:** “GWs from vacuum fluctuation”
- **Inhomogeneous solution:** “GWs from sources”
 - Scalar and vector fields cannot source tensor fluctuations at linear order (possible at non-linear level)
 - SU(2) gauge field can!

Maleknejad & Sheikh-Jabbari (2013); Dimastrogiovanni & Peloso (2013);
Adshead, Martinec & Wyman (2013); Obata & Soda (2016); ...

Important Message

$$\square h_{ij} = -16\pi G \pi_{ij}$$

- Do not take it for granted if someone told you that detection of the primordial gravitational waves would be a signature of “quantum gravity”!
- Only the homogeneous solution corresponds to the vacuum tensor metric perturbation. **There is no *a priori* reason to neglect an inhomogeneous solution!**
- Contrary, we have several examples in which detectable B-modes are generated by **sources** [U(1) and SU(2)]

Experimental Strategy

Commonly Assumed So Far

1. Detect CMB polarisation in multiple frequencies, to make sure that it is from the CMB (i.e., Planck spectrum)
2. Check for scale invariance: Consistent with a scale invariant spectrum?
 - Yes => Announce discovery of the vacuum fluctuation in spacetime
 - No => WTF?

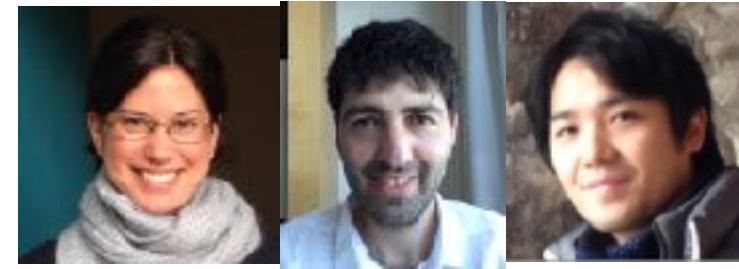
New Experimental Strategy: New Standard!

1. Detect CMB polarisation in multiple frequencies, to make sure that it is from the CMB (i.e., Planck spectrum)
 2. Consistent with a scale invariant spectrum?
 3. Parity violating correlations consistent with zero?
 4. Consistent with Gaussianity?
- If, and **ONLY IF** Yes to **all** => Announce discovery of the vacuum fluctuation in spacetime

If not, you may have just discovered new physics during inflation!

2. Consistent with a scale invariant spectrum?
 3. Parity violating correlations consistent with zero?
 4. Consistent with Gaussianity?
- If, and **ONLY IF** Yes to **all** => Announce discovery of the vacuum fluctuation in spacetime

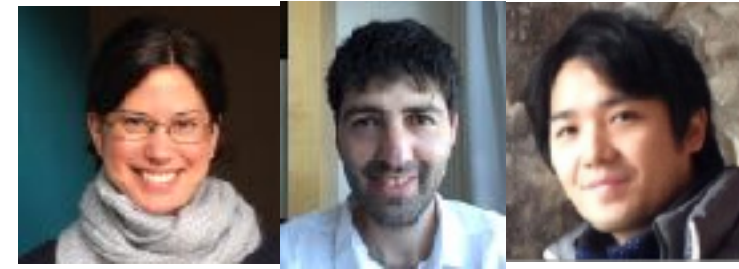
GW from Axion-SU(2) Dynamics



$$\mathcal{L} = \mathcal{L}_{GR} + \mathcal{L}_\phi + \mathcal{L}_\chi - \frac{1}{4} F_{\mu\nu}^a F^{a\mu\nu} + \frac{\lambda \chi}{4f} F_{\mu\nu}^a \tilde{F}^{a\mu\nu}$$

- ϕ : inflaton field => Just provides quasi-de Sitter background
- χ : pseudo-scalar “axion” field. Spectator field (i.e., negligible energy density compared to the inflaton)
- Field strength of an SU(2) field A_ν^a :

$$F_{\mu\nu}^a \equiv \partial_\mu A_\nu^a - \partial_\nu A_\mu^a - g\epsilon^{abc} A_\mu^b A_\nu^c$$



Background and Perturbation

- In an inflating background, the SU(2) field has a background solution:

$$A_i^a = [\text{scale factor}] \times Q \times \delta_i^a$$

$$Q \equiv (-f \partial_\chi U / 3g\lambda H)^{1/3}$$

U: axion potential

- Perturbations contain a tensor mode (as well as S&V)

$$\delta A_i^a = t_{ai} + \dots$$

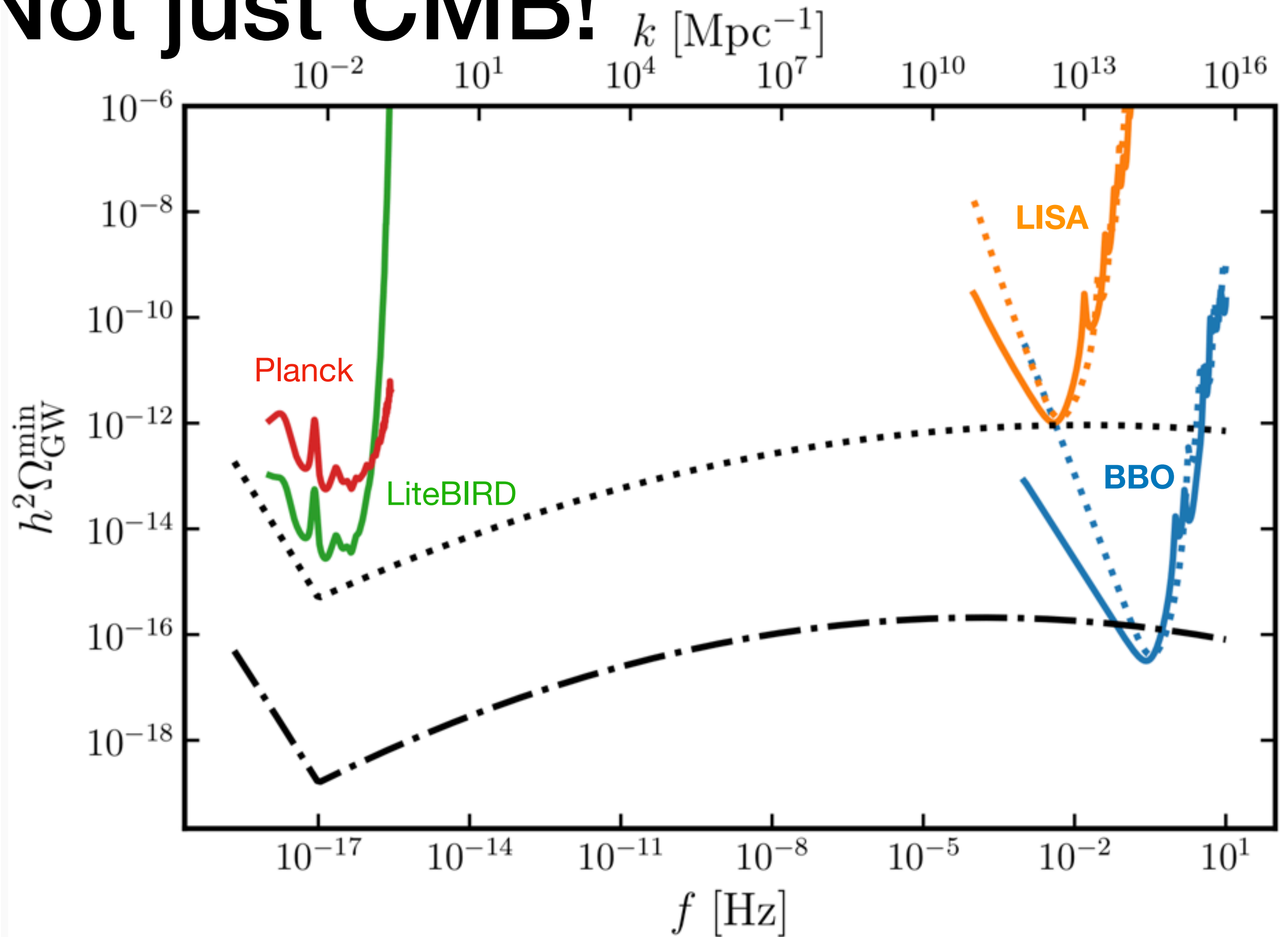
$$t_{ii} = \partial_a t_{ai} = \partial_i t_{ai} = 0$$

Scenario

- The $SU(2)$ field contains tensor, vector, and scalar components
- The tensor components are amplified strongly by a coupling to the axion field
- But, only one helicity is amplified \Rightarrow GW is **chiral**
(well-known result)
- Brand-new result: **GWs sourced by this mechanism are strongly non-Gaussian!**

Agrawal, Fujita & EK (2017)

Not just CMB!



Large bispectrum in GW from SU(2) fields



Aniket Agrawal
(MPA)

$$\frac{B_h^{RRR}(k, k, k)}{P_h^2(k)} \approx \frac{25}{\Omega_A}$$



Tomo Fujita
(Kyoto)

$$\langle \hat{h}_R(\mathbf{k}_1) \hat{h}_R(\mathbf{k}_2) \hat{h}_R(\mathbf{k}_3) \rangle = (2\pi)^3 \delta \left(\sum_{i=1}^3 \mathbf{k}_i \right) B_h^{RRR}(k_1, k_2, k_3)$$

- $\Omega_A \ll 1$ is the energy density fraction of the gauge field
- **B_h/P_h^2 is of order unity for the vacuum contribution**
[Maldacena (2003); Maldacena & Pimentel (2011)]
- ***Gaussianity offers a powerful test of whether the detected GW comes from the vacuum or sources***

NG generated at the tree level

$$L_3^{(i)} = c^{(i)} \left[\epsilon^{abc} t_{ai} t_{bj} \left(\partial_i t_{cj} - \frac{m_Q^2 + 1}{3m_Q \tau} \epsilon^{ijk} t_{ck} \right) \right.$$

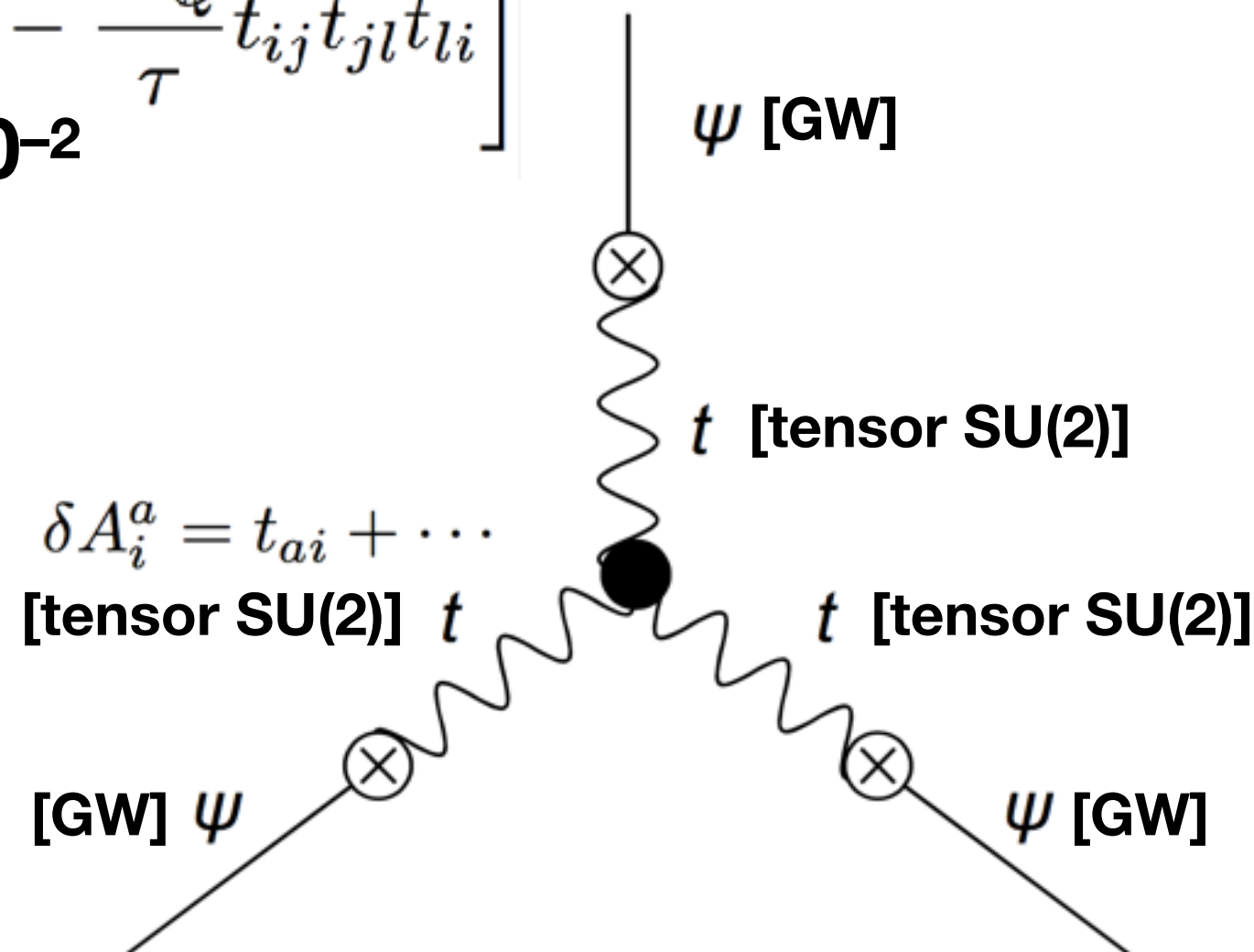
$$\left. - \frac{m_Q}{\tau} t_{ij} t_{jl} t_{li} \right]$$

$$c^{(i)} = g = m_Q^2 H / \sqrt{\epsilon_B} M_{\text{Pl}} \sim \mathbf{10^{-2}}$$

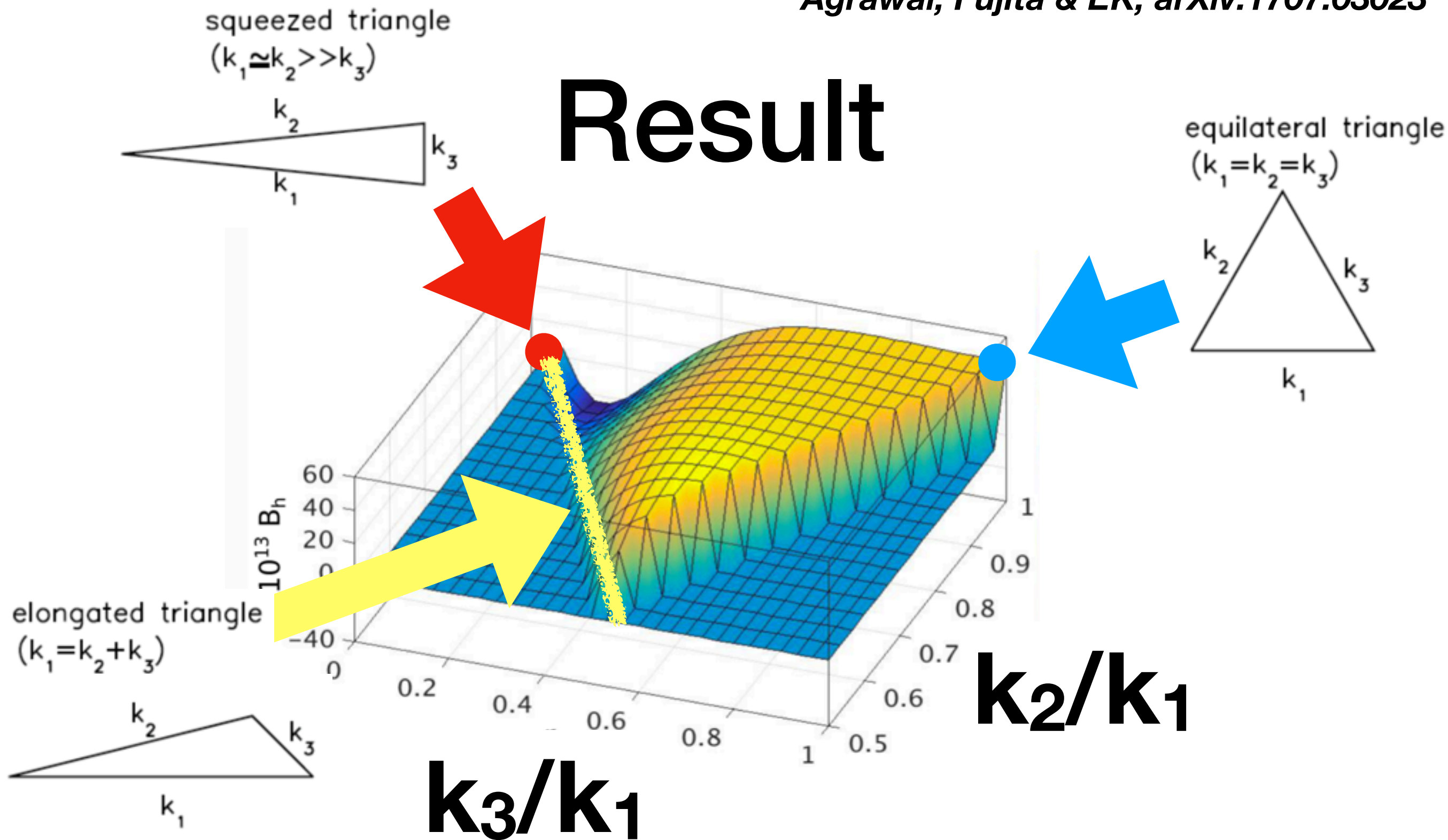
$$\epsilon_B \equiv \frac{g^2 Q^4}{H^2 M_{\text{Pl}}^2} \simeq \frac{2\Omega_A}{1 + m_Q^{-2}} \ll 1$$

$$m_Q \equiv gQ/H \quad [\mathbf{m_Q \sim a\ few}]$$

- This diagram generates second-order equation of motion for GW



Result



- This shape is similar to, but not exactly the same as, what was used by the Planck team to look for tensor bispectrum

Current Limit on Tensor NG

- The Planck team reported a limit on the tensor bispectrum in the following form:

$$f_{\text{NL}}^{\text{tens}} \equiv \frac{B_h^{+++}(k, k, k)}{F_{\text{scalar}}^{\text{equil.}}(k, k, k)}$$

- The denominator is the **scalar** equilateral bispectrum template, giving $F_{\text{scalar}}^{\text{equil.}}(k, k, k) = (18/5)P_{\text{scalar}}^2(k)$
- The current 68%CL constraint is $f_{\text{NL}}^{\text{tens}} = 400 \pm 1500$

SU(2), confronted

- The SU(2) model of Dimastrogiovanni et al. predicts:

$$f_{\text{NL}}^{\text{tens}} \approx \frac{125}{18\sqrt{2}} \frac{r^2}{\epsilon_B} \approx 2.5 \frac{r^2}{\Omega_A}$$

- The current 68%CL constraint is $f_{\text{NL}}^{\text{tens}} = 400 \pm 1500$
 - This is already constraining!

LiteBIRD would nail it!

