

# Mapping Hot Gas in the Universe using the Sunyaev-Zeldovich Effect

Eiichiro Komatsu (Max-Planck-Institut für Astrophysik)  
OKC Cosmology and Gravity Seminar, Oskar Klein Centre,  
February 15, 2017

# This presentation is based primarily upon...



1. **T. Kitayama** et al., “*The Sunyaev-Zeldovich effect at 5”: RXJ1347.5–1145 imaged by ALMA*”, PASJ, 68, 88 (2016), arXiv:1607.08833

**Data**



2. **K. Dolag**, EK & R.A. Sunyaev, “*SZ effects in the Magneticum Pathfinder Simulation: Comparison with Planck, SPT, and SCT results*”, MNRAS, 463, 1797 (2016), arXiv:1509.05134

**Sim**

*[I probably do not have time to cover this]*



3. **X. Shi** & EK, “*Analytical model for non-thermal pressure in galaxy clusters*”, MNRAS 442, 521 (2014), arXiv:1401.7657

**Model**



# Where is a galaxy cluster?

Subaru image of RXJ1347-1145 (Medezinski et al. 2010)  
<http://wise-obs.tau.ac.il/~elinor/clusters>



# Where is a galaxy cluster?



Subaru image of RXJ1347-1145 (Medezinski et al. 2010)  
<http://wise-obs.tau.ac.il/~elinor/clusters>



# Subaru

Subaru image of RXJ1347-1145 (Medezinski et al. 2010)  
<http://wise-obs.tau.ac.il/~elinor/clusters>

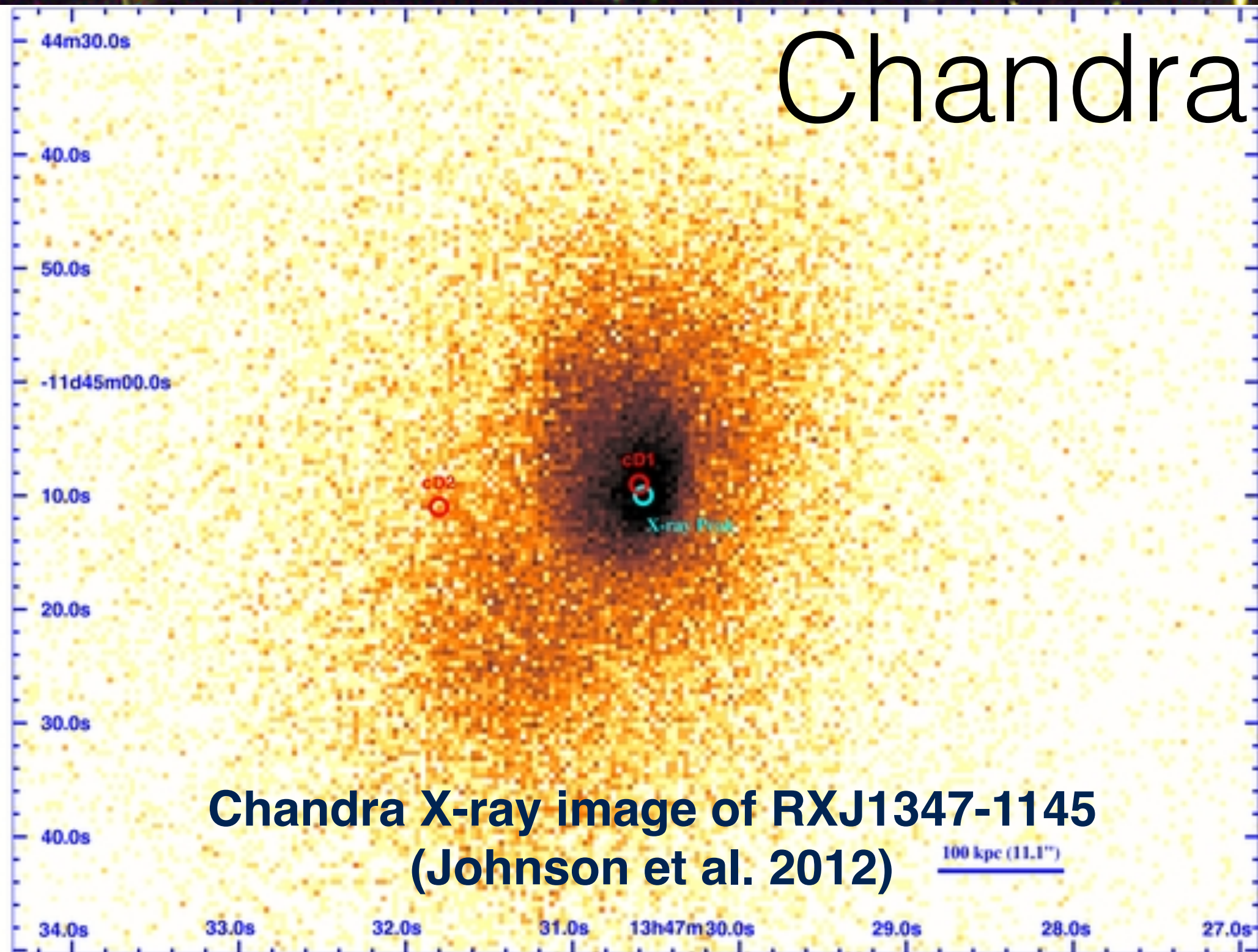


# Hubble

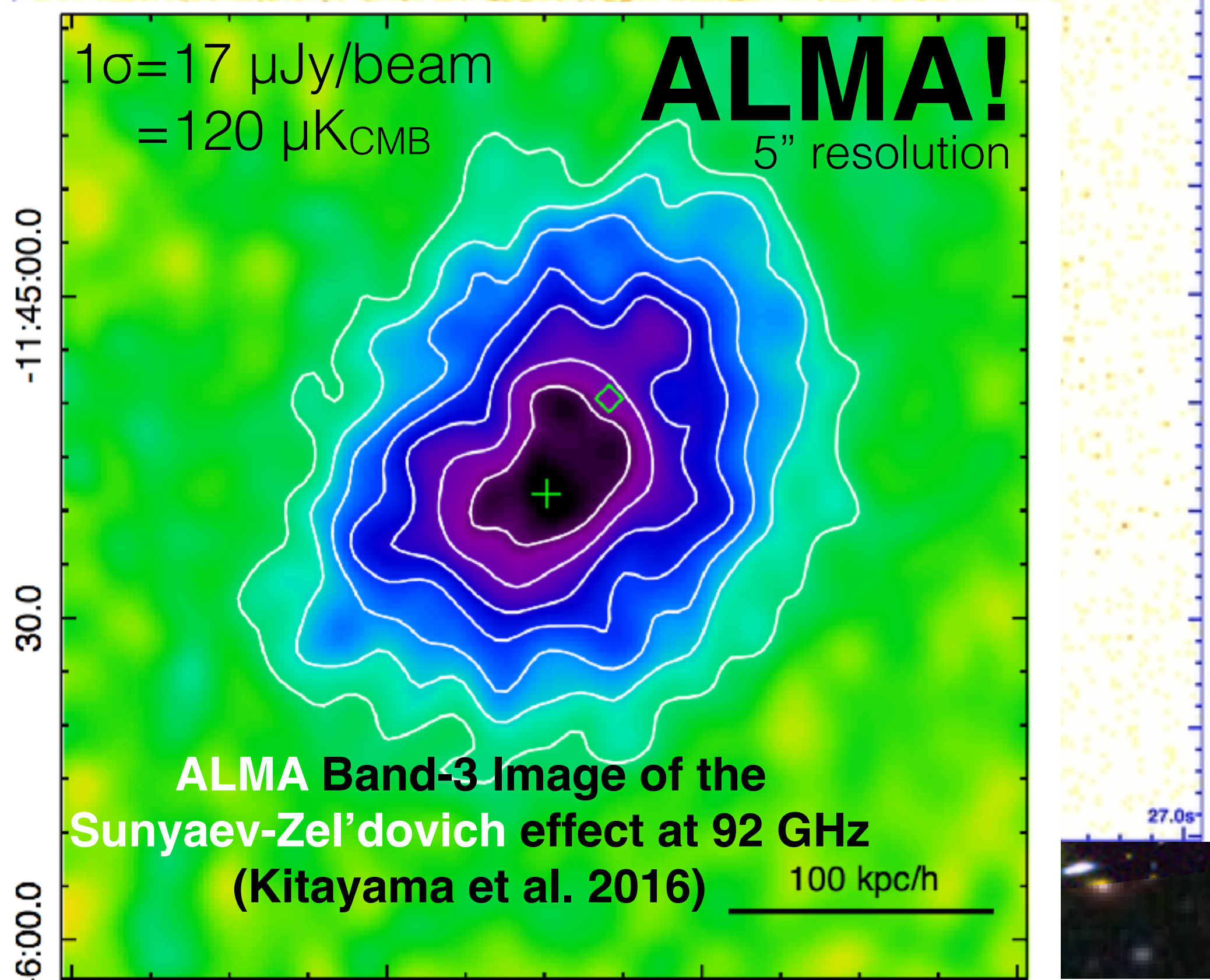
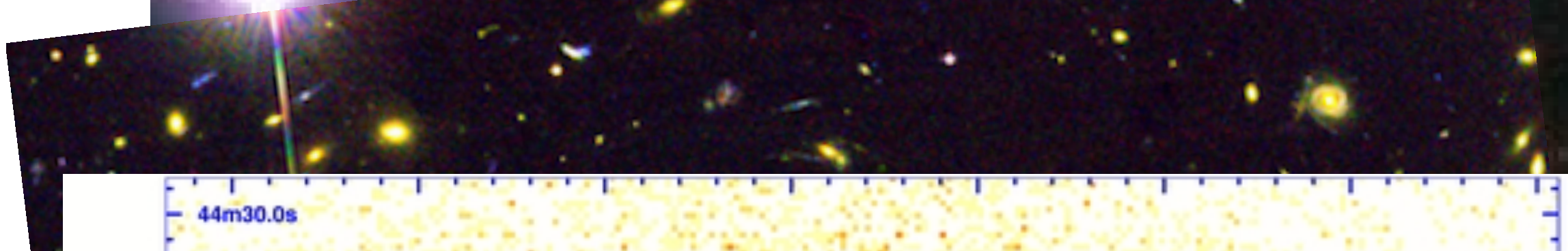
Hubble image of RXJ1347-1145 (Bradac et al. 2008)



# Chandra







$1\sigma = 17 \mu\text{Jy/beam}$   
 $= 120 \mu\text{K}_{\text{CMB}}$

**ALMA!**  
5" resolution

**ALMA Band-3 Image of the  
Sunyaev-Zel'dovich effect at 92 GHz  
(Kitayama et al. 2016)**

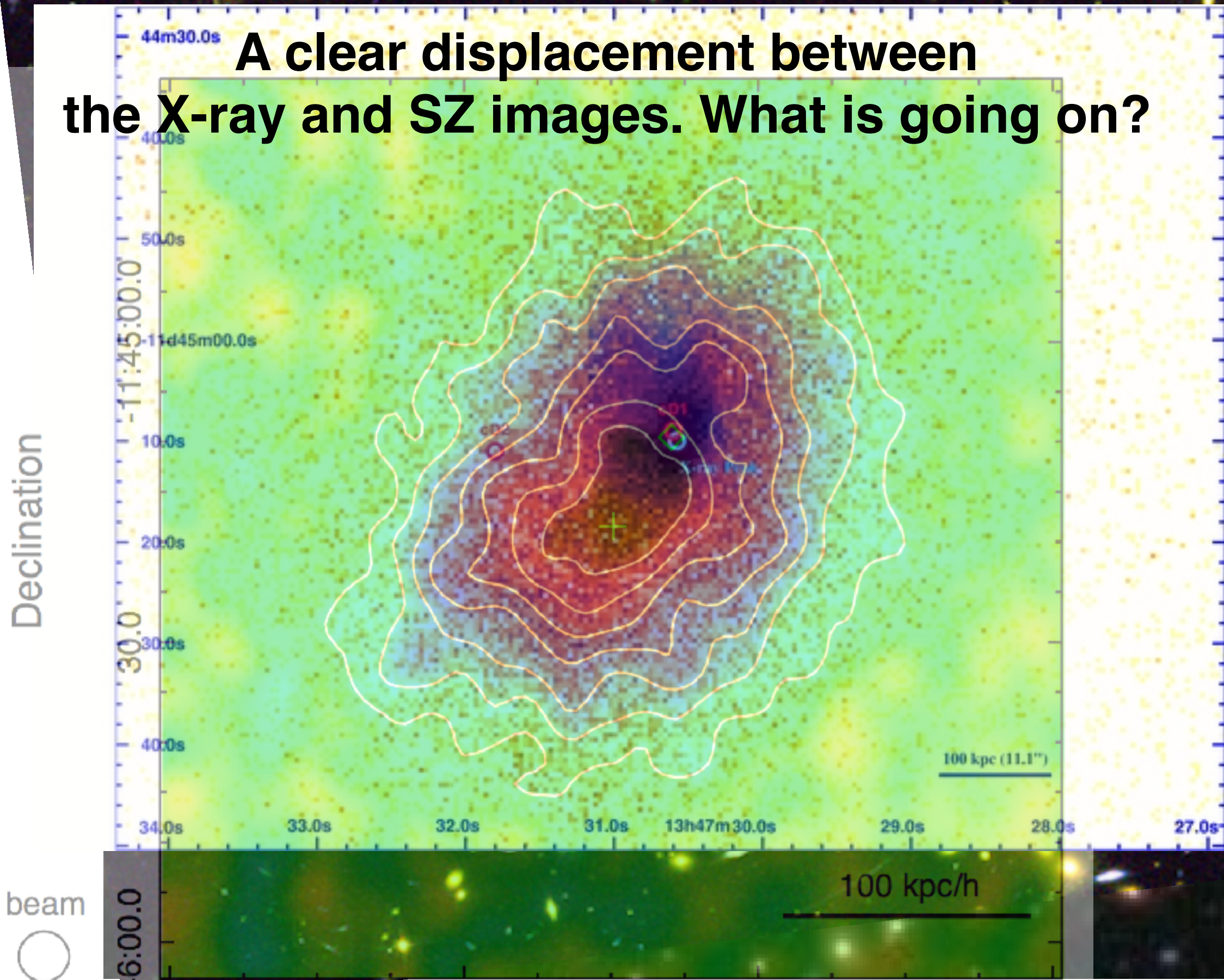
100 kpc/h

beam

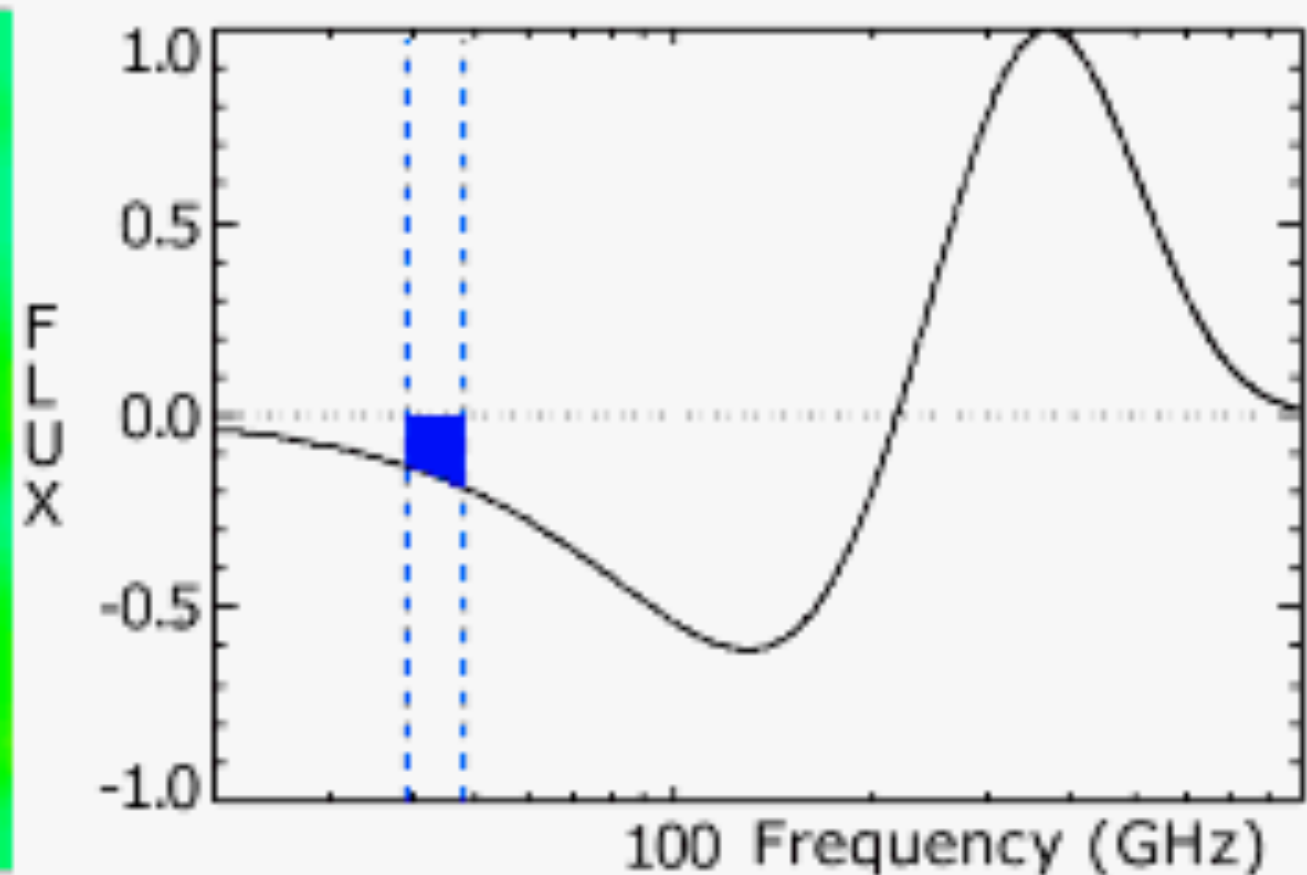
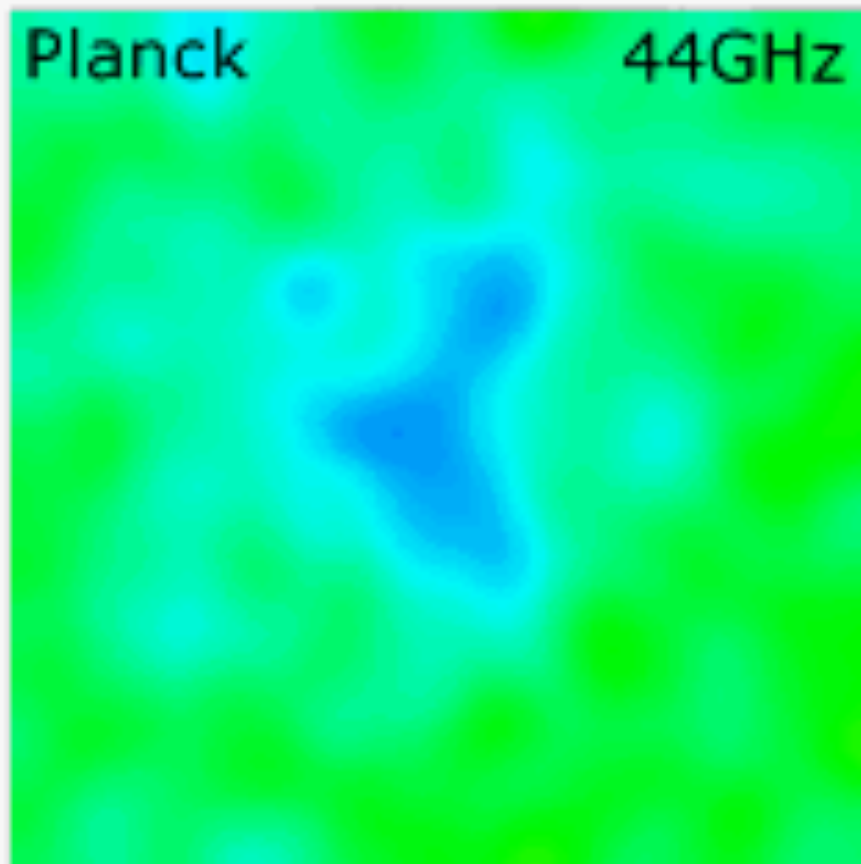
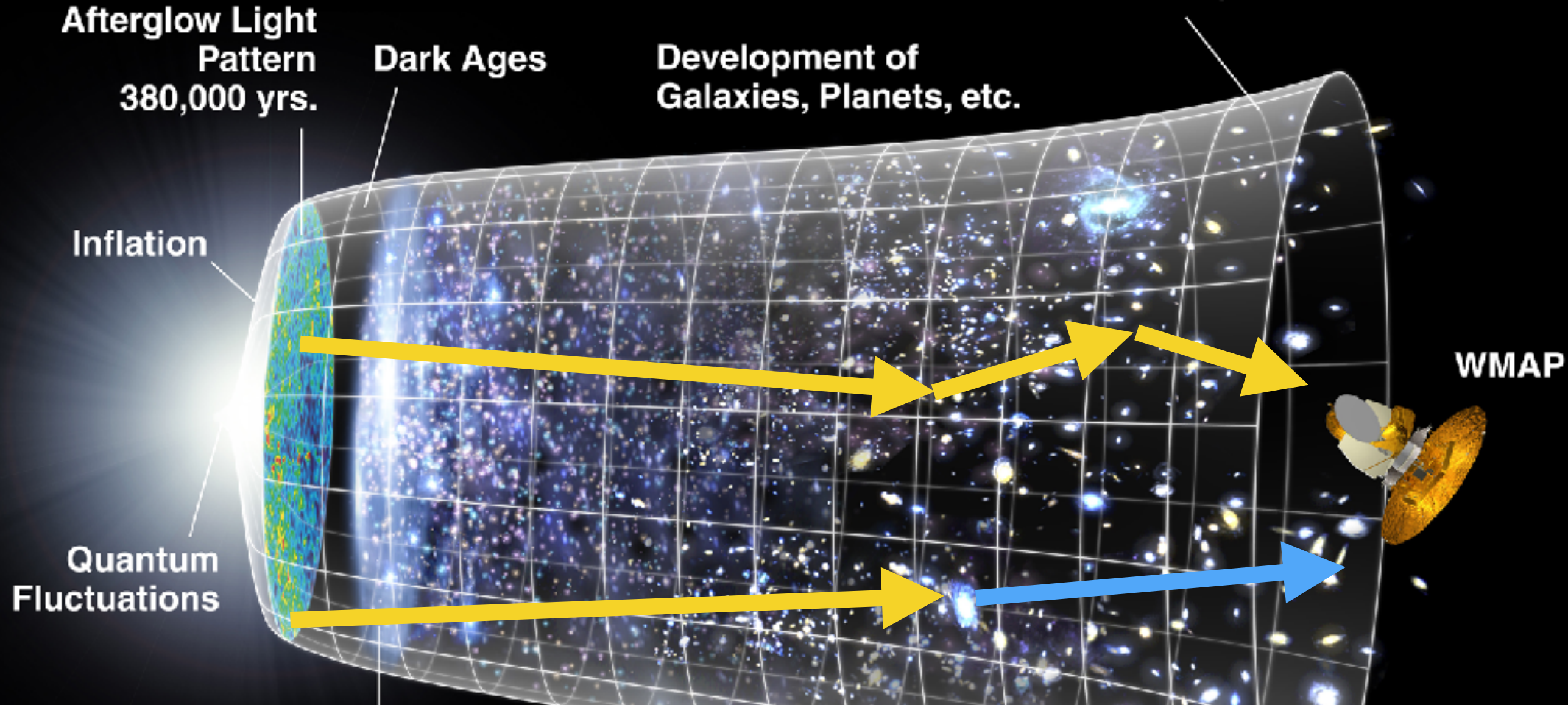




**A clear displacement between  
the X-ray and SZ images. What is going on?**



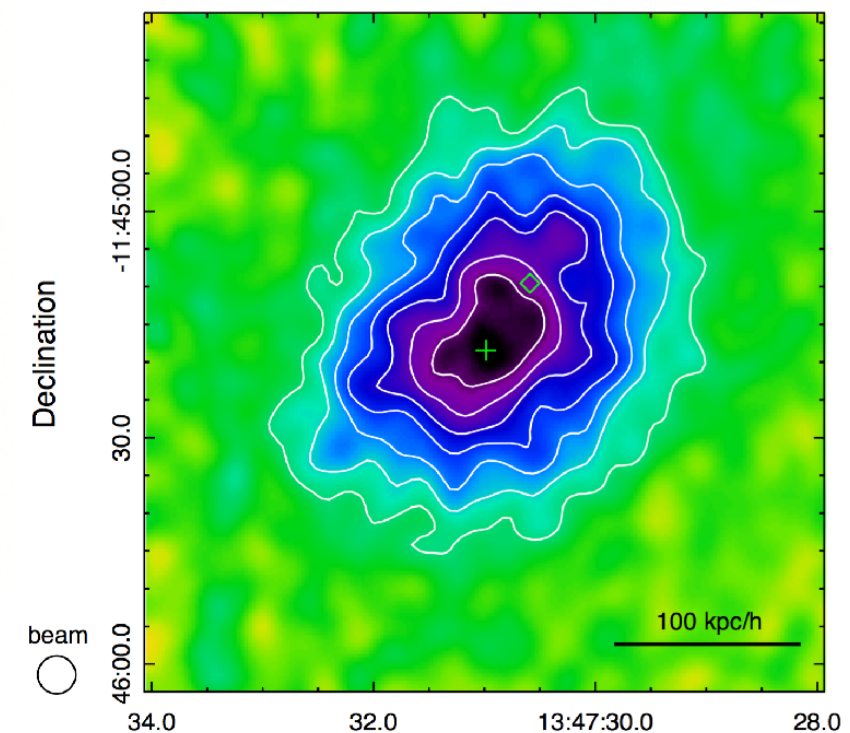
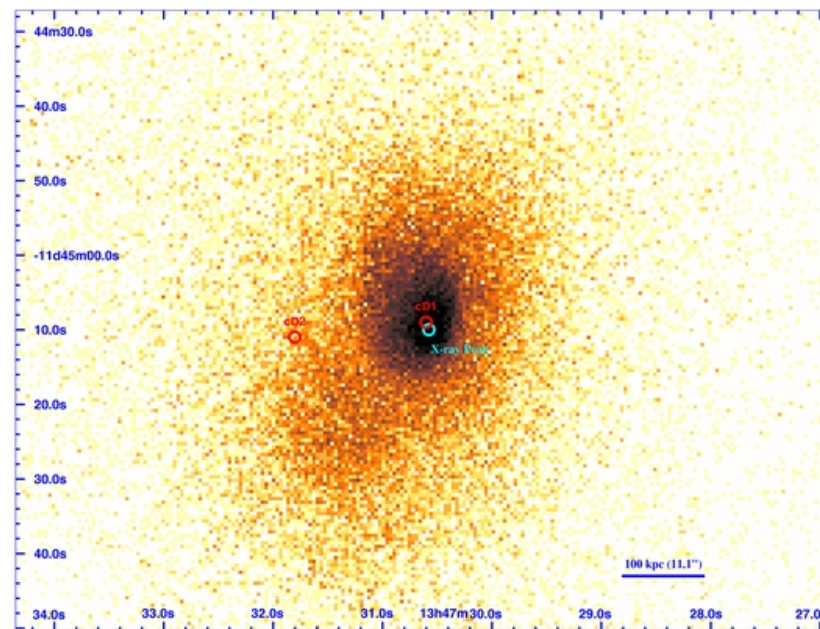






# Multi-wavelength Data

$$I_X = \int dl \, n_e^2 \Lambda(T_X) \quad I_{SZ} = g_\nu \frac{\sigma_T k_B}{m_e c^2} \int dl \, n_e T_e$$



## Optical:

- $10^{2-3}$  galaxies
- velocity dispersion
- gravitational lensing

## X-ray:

- hot gas ( $10^7-8$  K)
- spectroscopic  $T_X$
- Intensity  $\sim n_e^2 L$

## SZ [microwave]:

- hot gas ( $10^7-8$  K)
- electron pressure
- Intensity  $\sim n_e T_e L$



# A Story about RXJ1347–1145

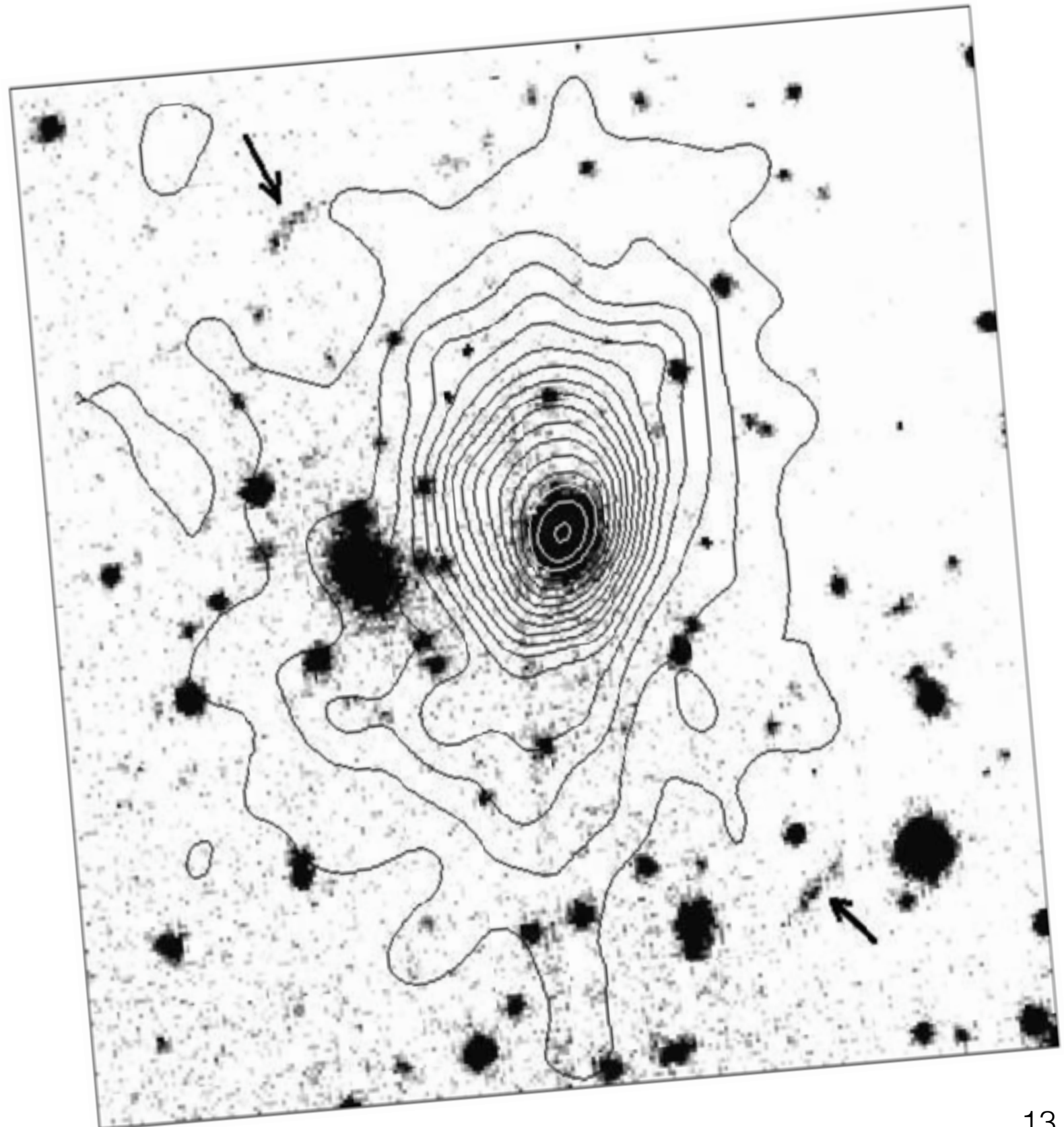
- Let me tell you a little story about this particular cluster, which **highlights the unique power of the SZ data to study cluster astrophysics**
- A massive cluster with  $10^{15} M_{\text{sun}}$  at  $z=0.45$ 
  - *The most X-ray luminous galaxy cluster found in the ROSAT All Sky Survey*
- Very compact, “cool core” cluster



# 1997

ROSAT/HRI image  
[Schindler et al.]  
5" resolution

- 0.1–2.4 keV
- Looked pretty “spherical”
- Thought to be a typical, relaxed, cooling-flow cluster





# 2001

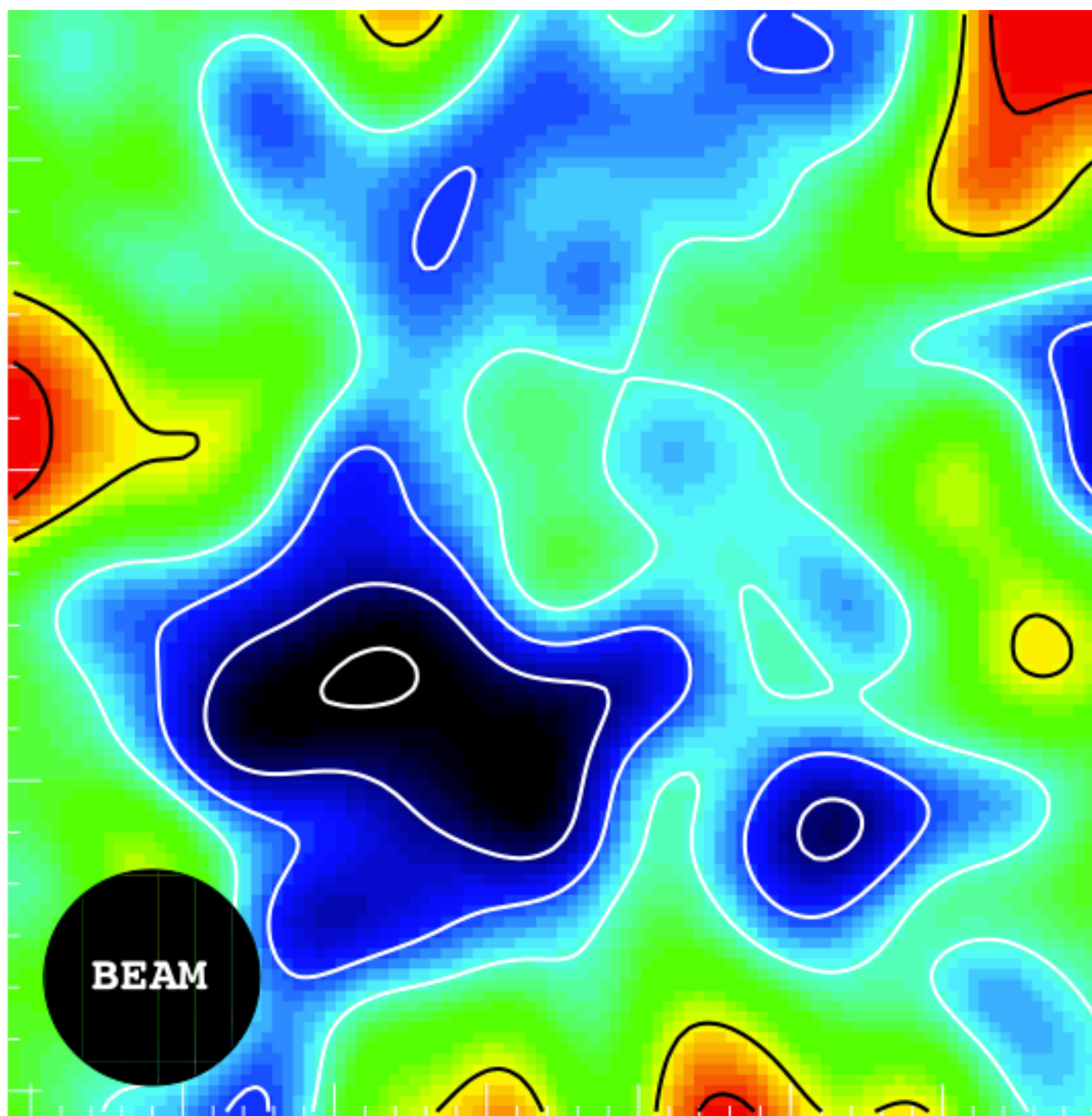
SZ w/ Nobeyama  
[Komatsu et al.]  
12" resolution

-11:45:00

- The highest angular resolution SZ mapping at that time
- (The record holder for a decade)
- **A surprise!**

30

46:00





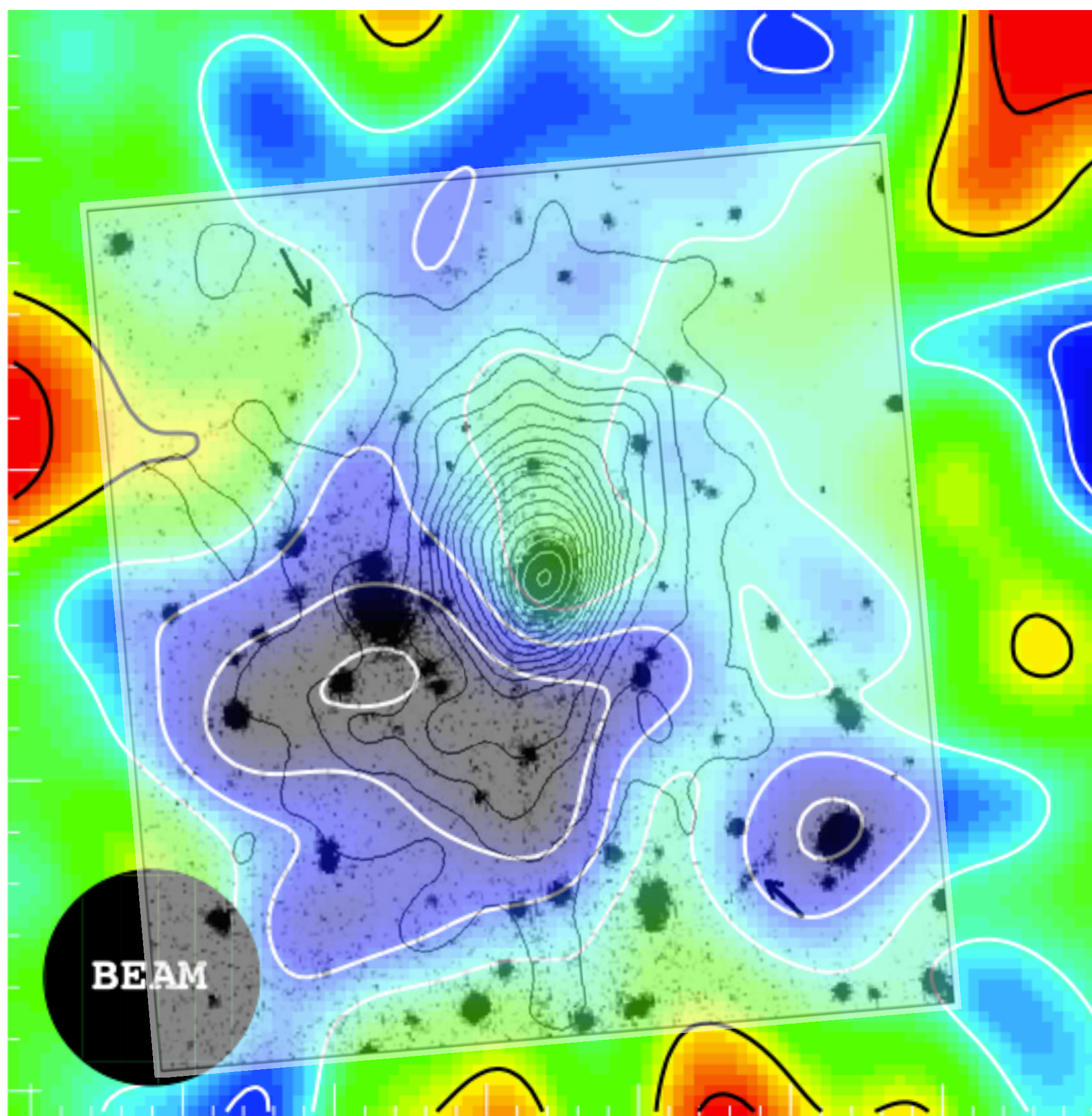
# 2001<sub>44:30</sub>

SZ w/ Nobeyama  
[Komatsu et al.]  
12" resolution

<sub>-11:45:00</sub>

- The highest angular resolution SZ mapping at that time
- (The record holder for a decade)
- **A surprise!**

<sub>46:00</sub>

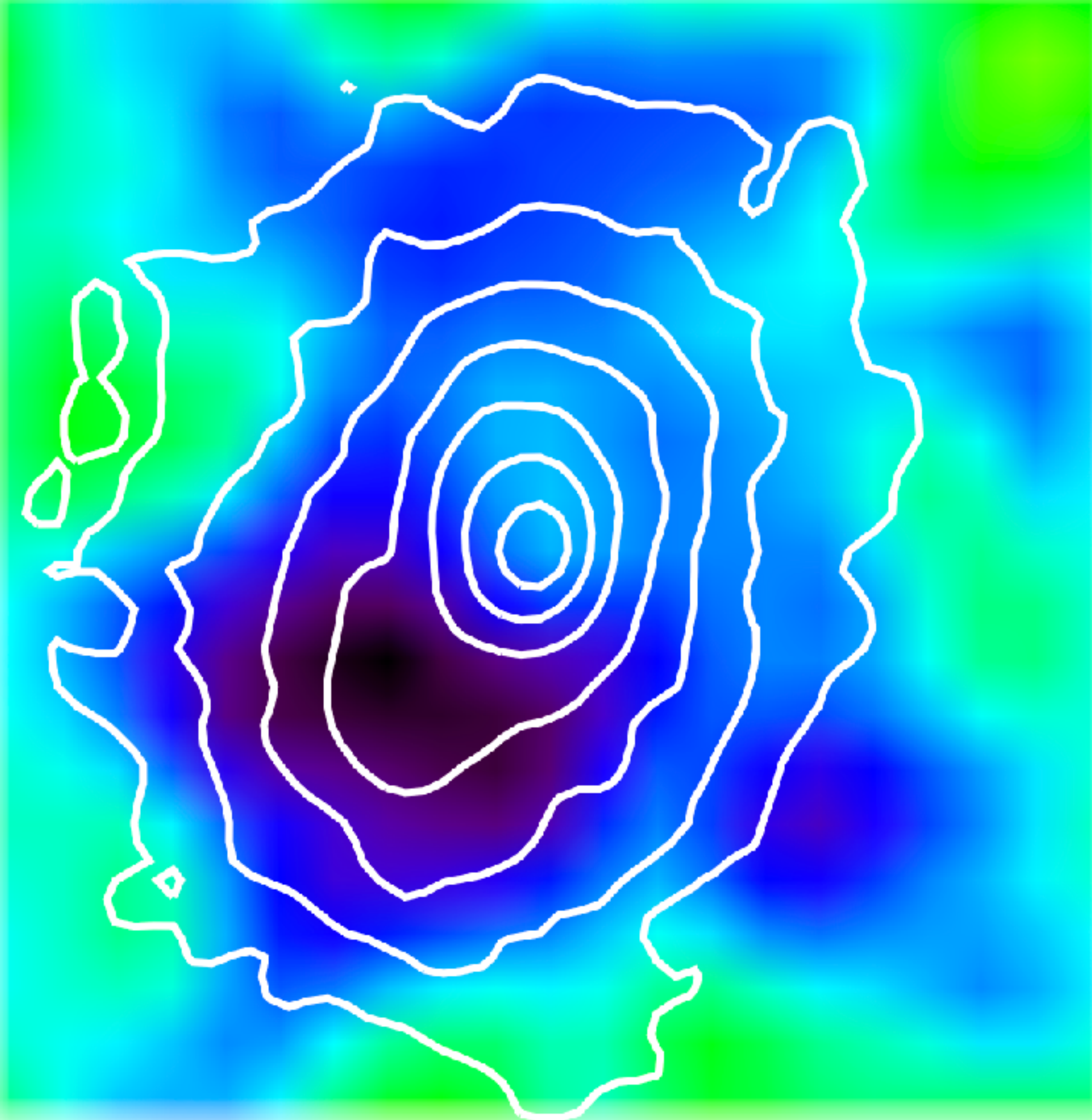




# 2002

X-ray w/ Chandra  
[Allen et al.]

- 0.5–7 keV
- An excess X-ray emission found at the location of the SZ excess
- A hot gas, missed by ROSAT due to the lack of sensitivity at high energies!





# A lesson learned

- X-ray observations are band-limited
  - They are not usually not sensitive to very hot gas with temperature  $>10(1+z)$  keV
- SZ observations are **not** band-limited
  - They are in principle sensitive to arbitrarily high temperatures (more precisely, pressure)
- SZ data probe electron pressure: a good probe of shock-heated gas due to mergers
  - *RXJ1347–1145 was thought to be a relaxed cluster. Our Nobeyama data challenged it, and now it is accepted that this cluster is a merging system!*

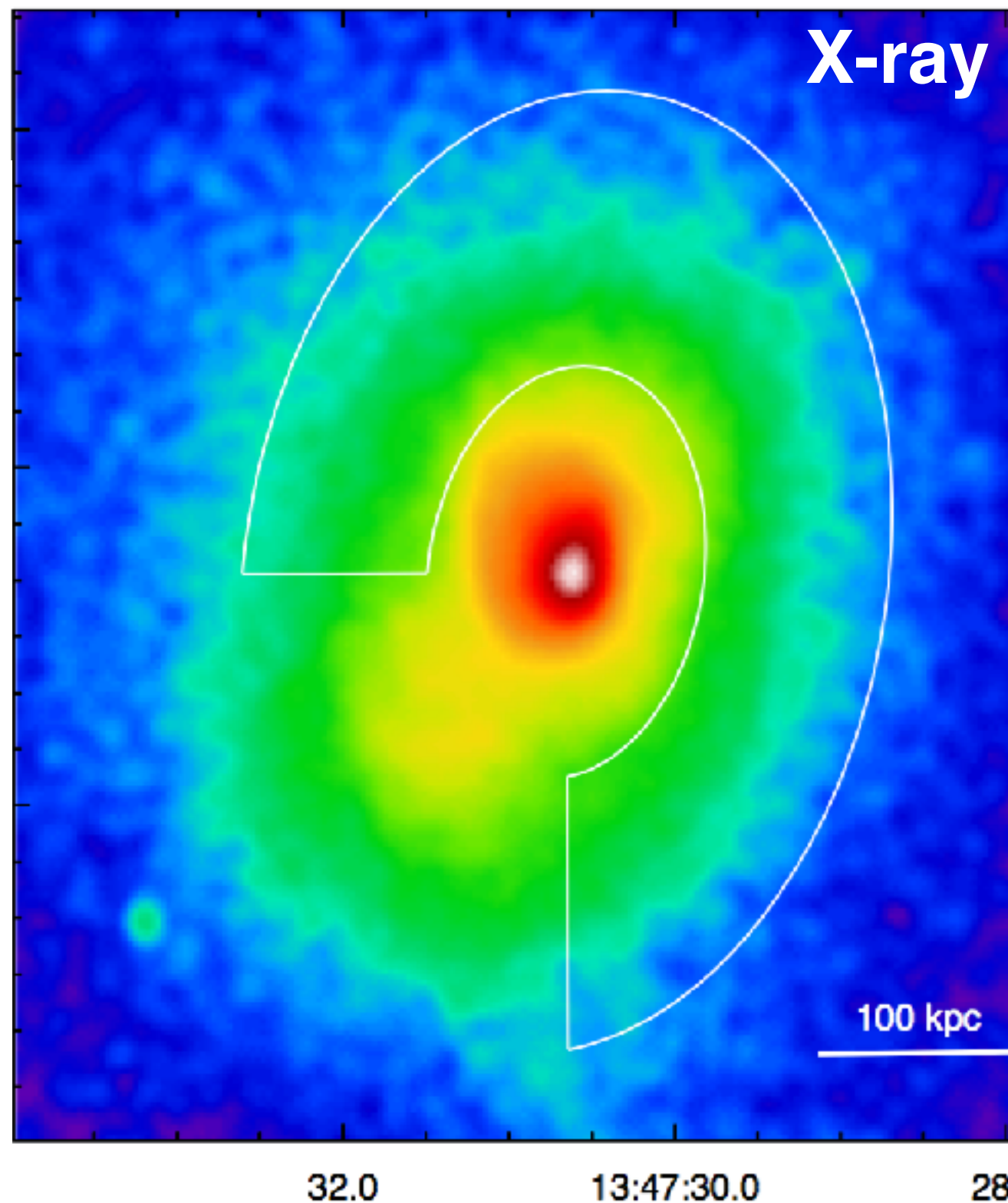
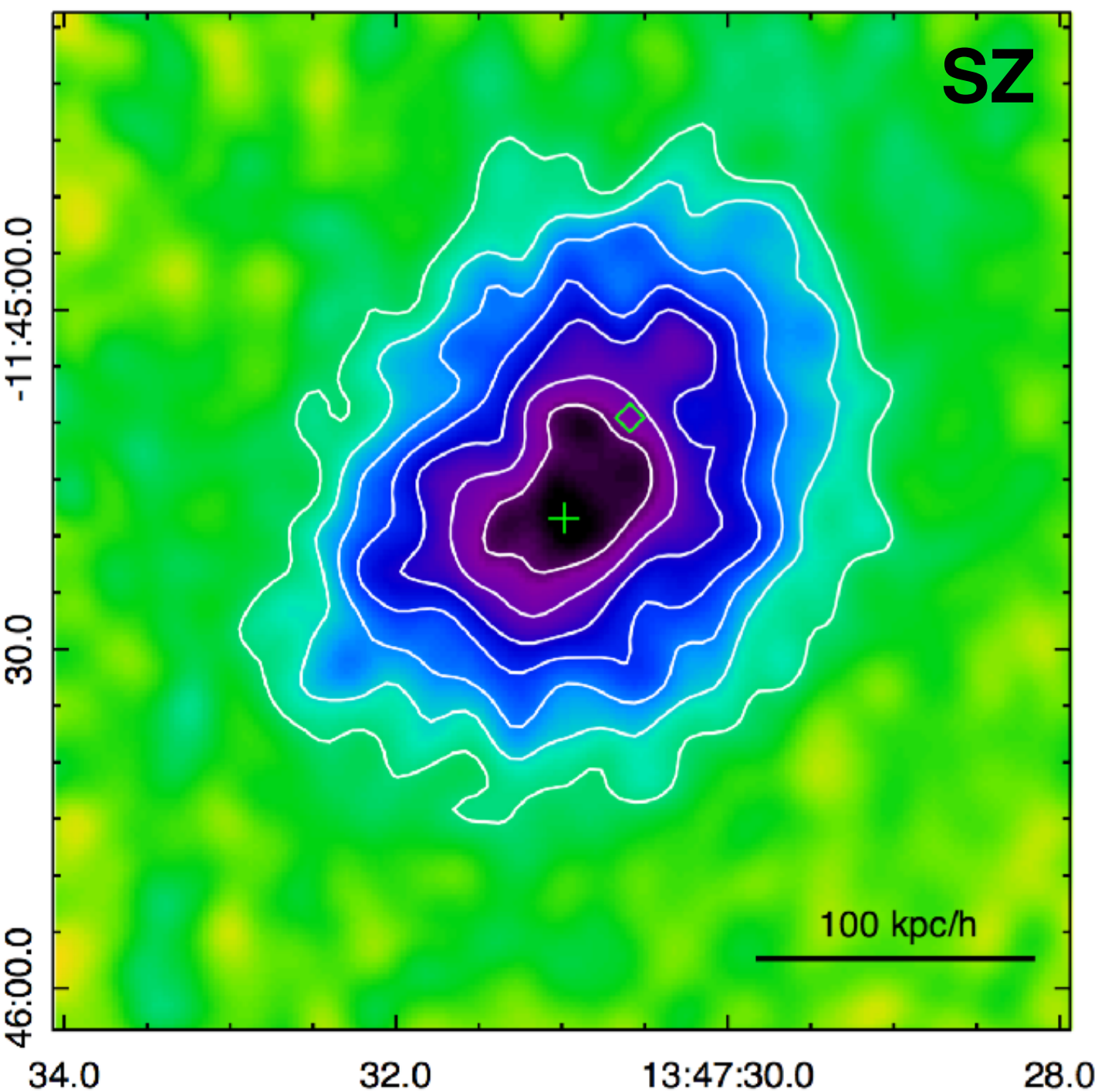


# We have ALMA. Now what?

- What is a new science we can do with such high resolution, high sensitivity measurements?
- Finding shocks and hot clumps is fun, but can we do something new and more quantitative?
- One example: **Pressure fluctuations**



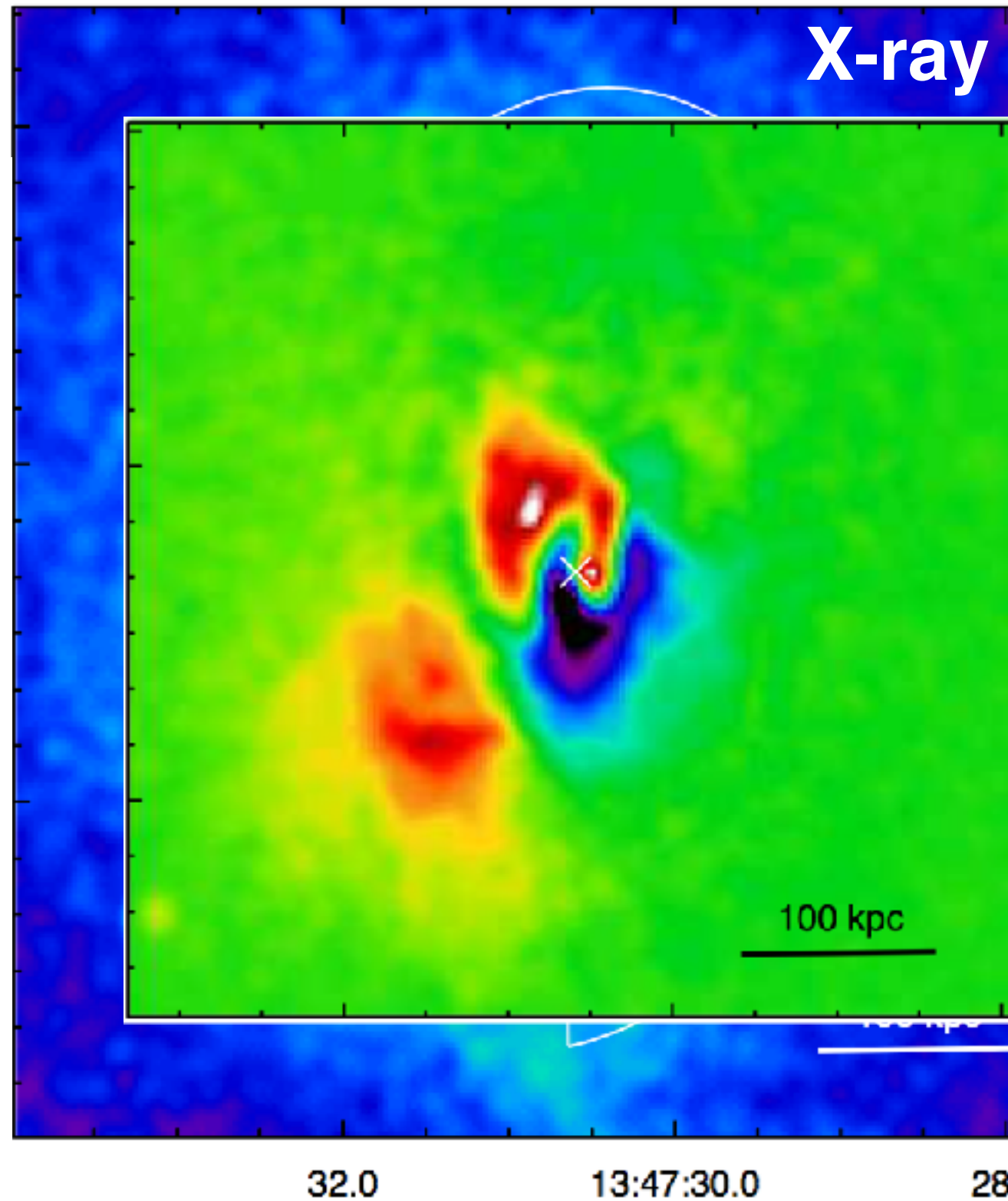
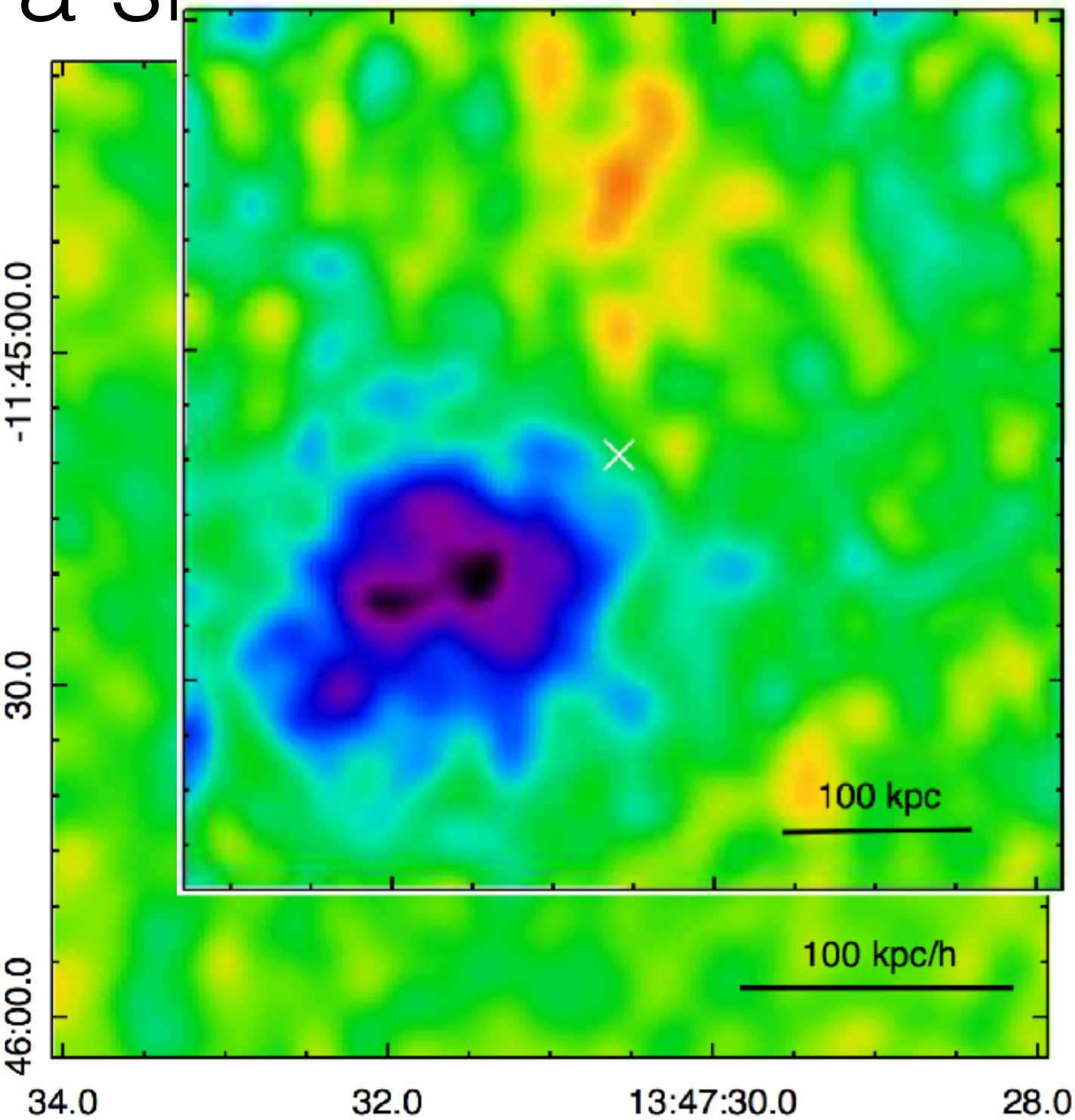
Let's subtract  
a smooth component



Right ascension



Let's subtract  
a smooth component



Right ascension

Let's subtract

a smooth component

X-ray

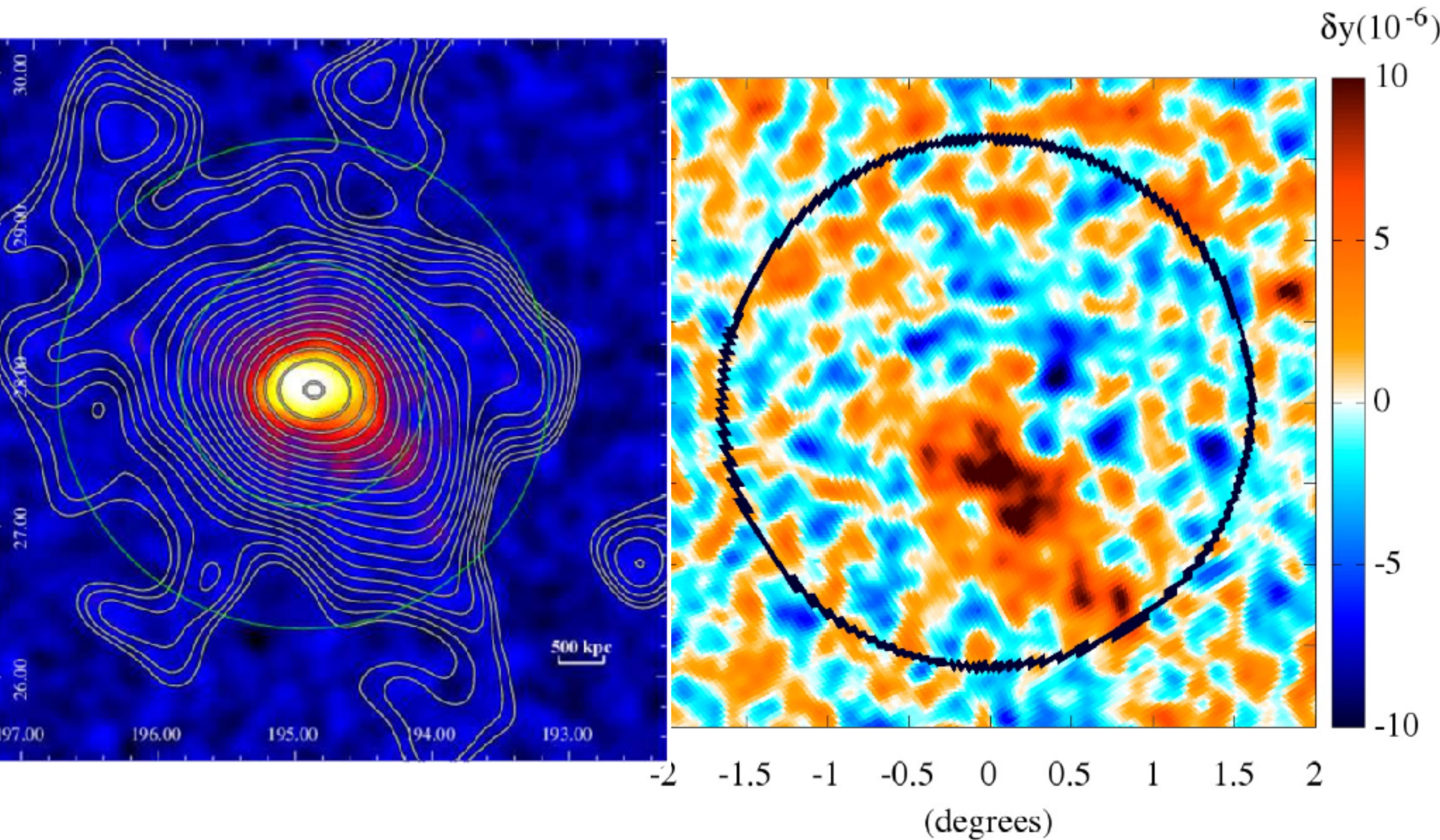
**Gas density is stirred  
("sloshed"), but no change in  
pressure! Not sound waves**

**=> Unique measurements of the  
effective equation of state of  
density fluctuations**

**Right ascension**



# Coma

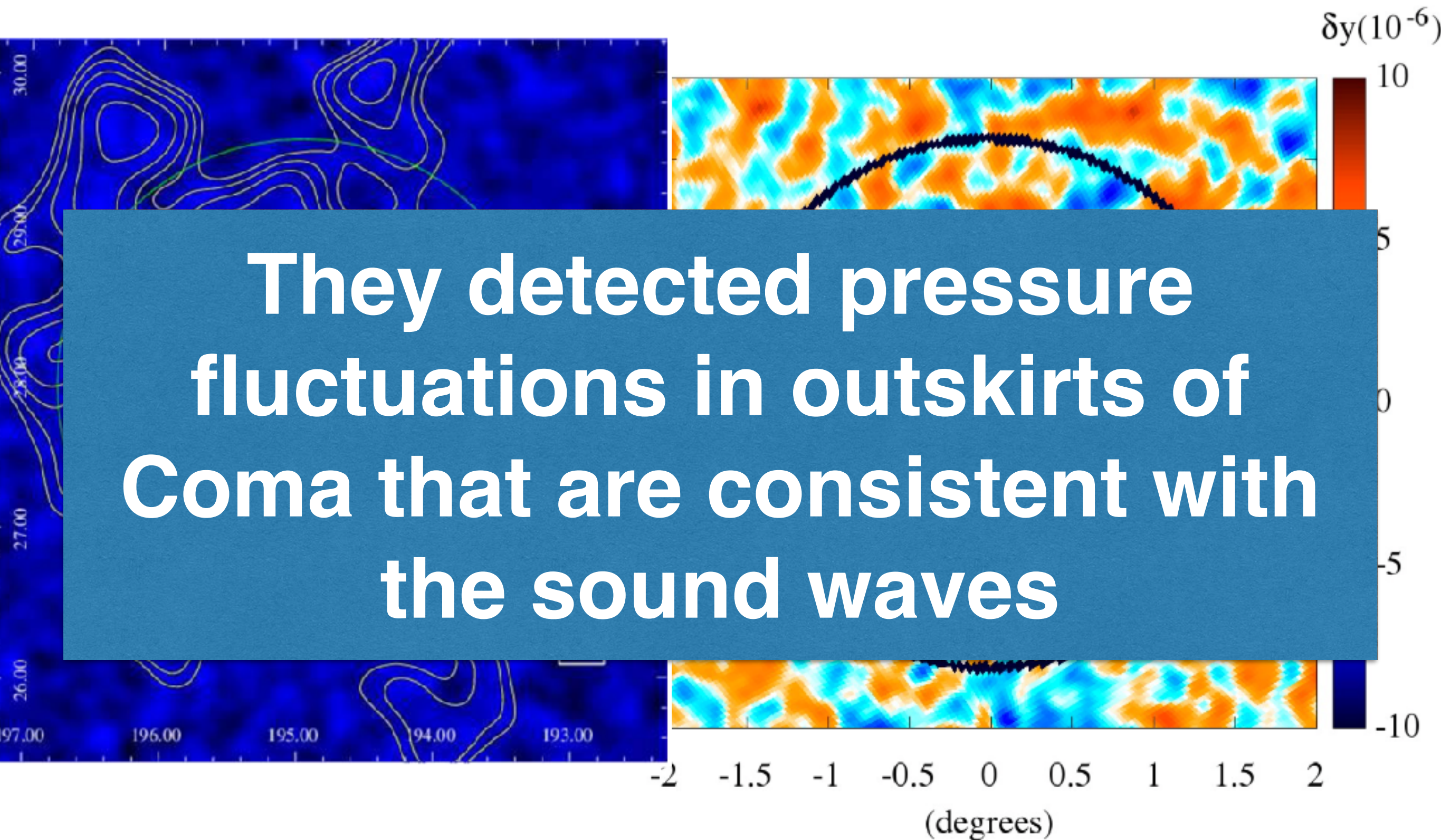


Planck Collaboration (2013)

*R. Khatri & M. Gaspari (2016)*



# Coma





# A Picture

- In the outskirts of a galaxy cluster, mass still accretes, creating weak shocks ( $M \sim \text{a few}$ )
  - The effective equation of state of pressure fluctuations is adiabatic
- In the core of a cluster, gas is just pushed around by sloshing, buoyancy, etc, without changing pressure
  - The effective equation of state of pressure fluctuations is isobaric
- This kind of study has been done by “pressure” estimated from X-ray data (Churazov et al. 2012; 2016; many others), but we can finally do this with **real** pressure from high-resolution SZ data!

# Secondary Anisotropies: Structure Formation seen in the CMB

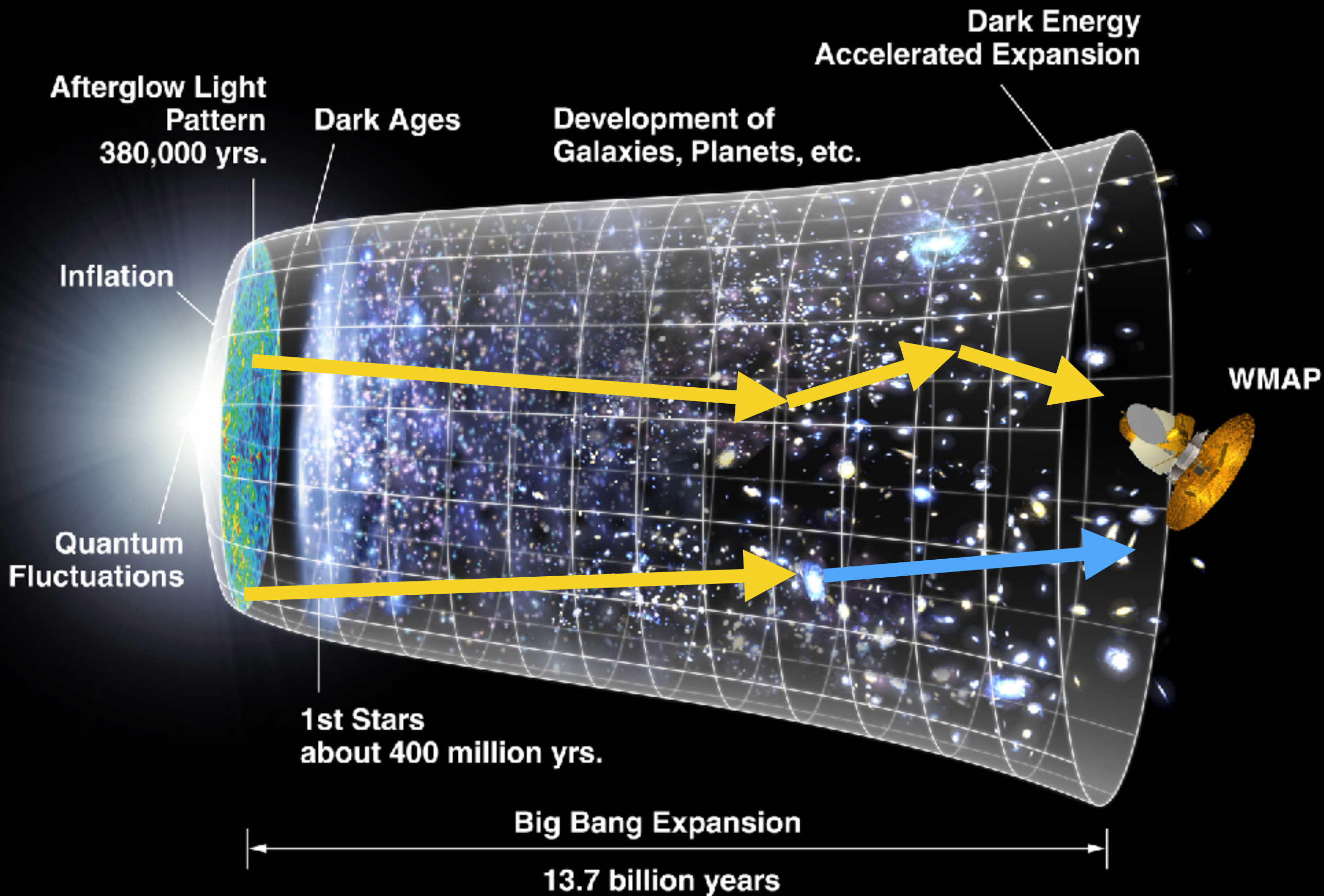
## Gravitational Lensing

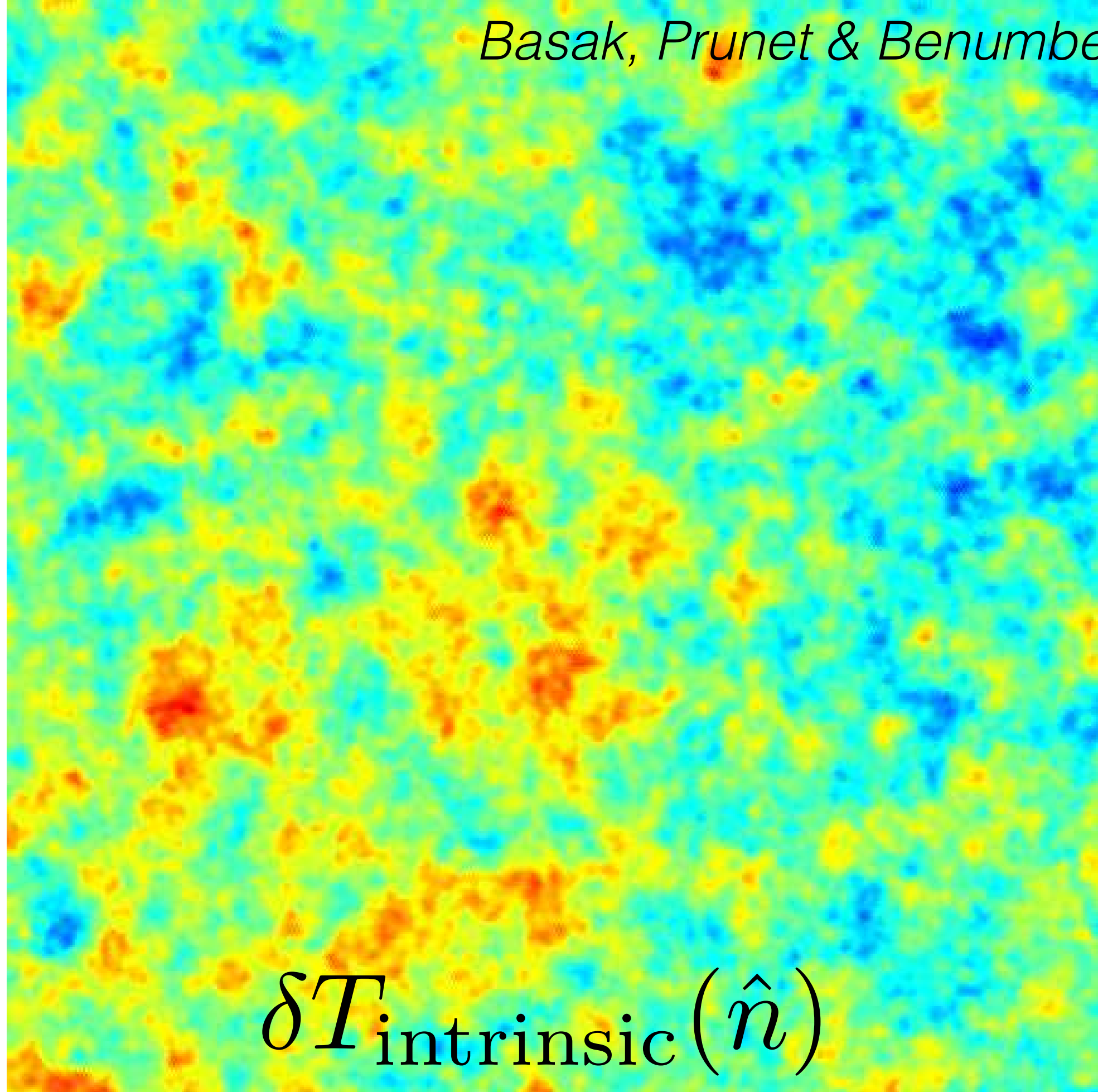
- Matter bends light of the CMB

## Sunyaev-Zel'dovich Effect

- Electrons in hot, collapsed gas up-scatter low-energy CMB photons, distorting the black-body spectrum of the CMB
- Both have been measured, providing the key insights into how the structures grew out of initial conditions.  
**Initial conditions to structure formation**, using the CMB data only!

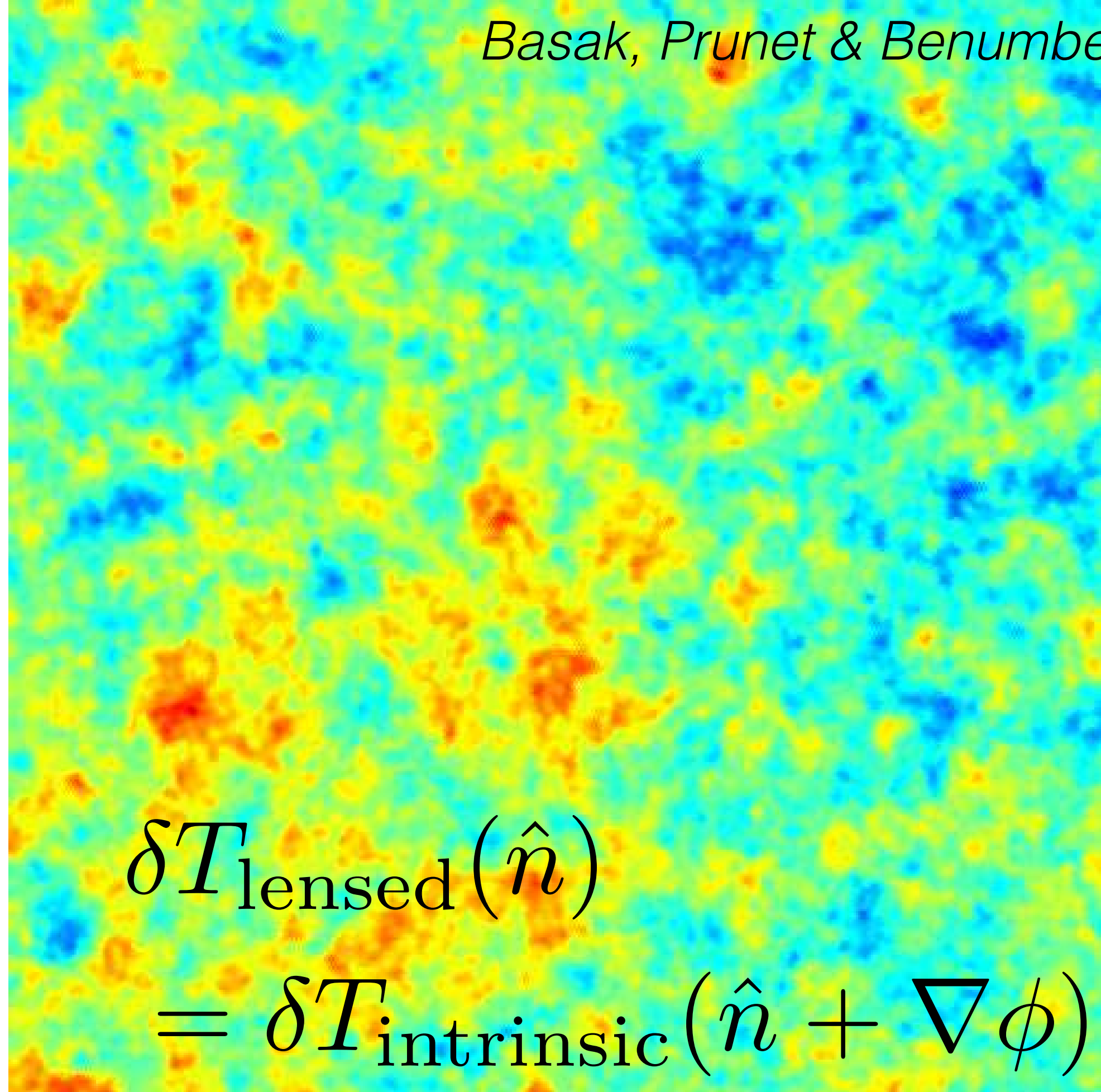




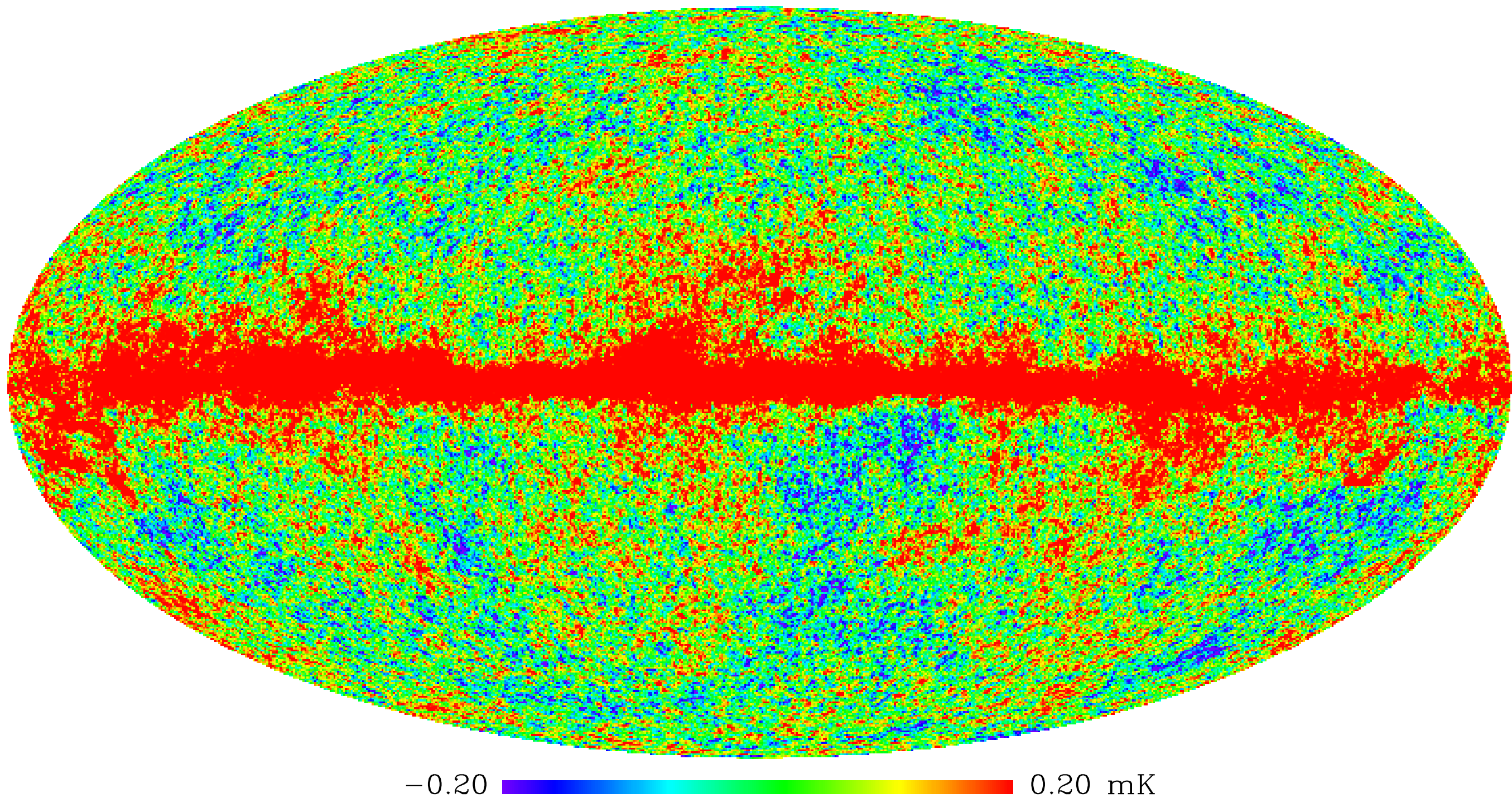


−605 605  $\mu\text{K}$





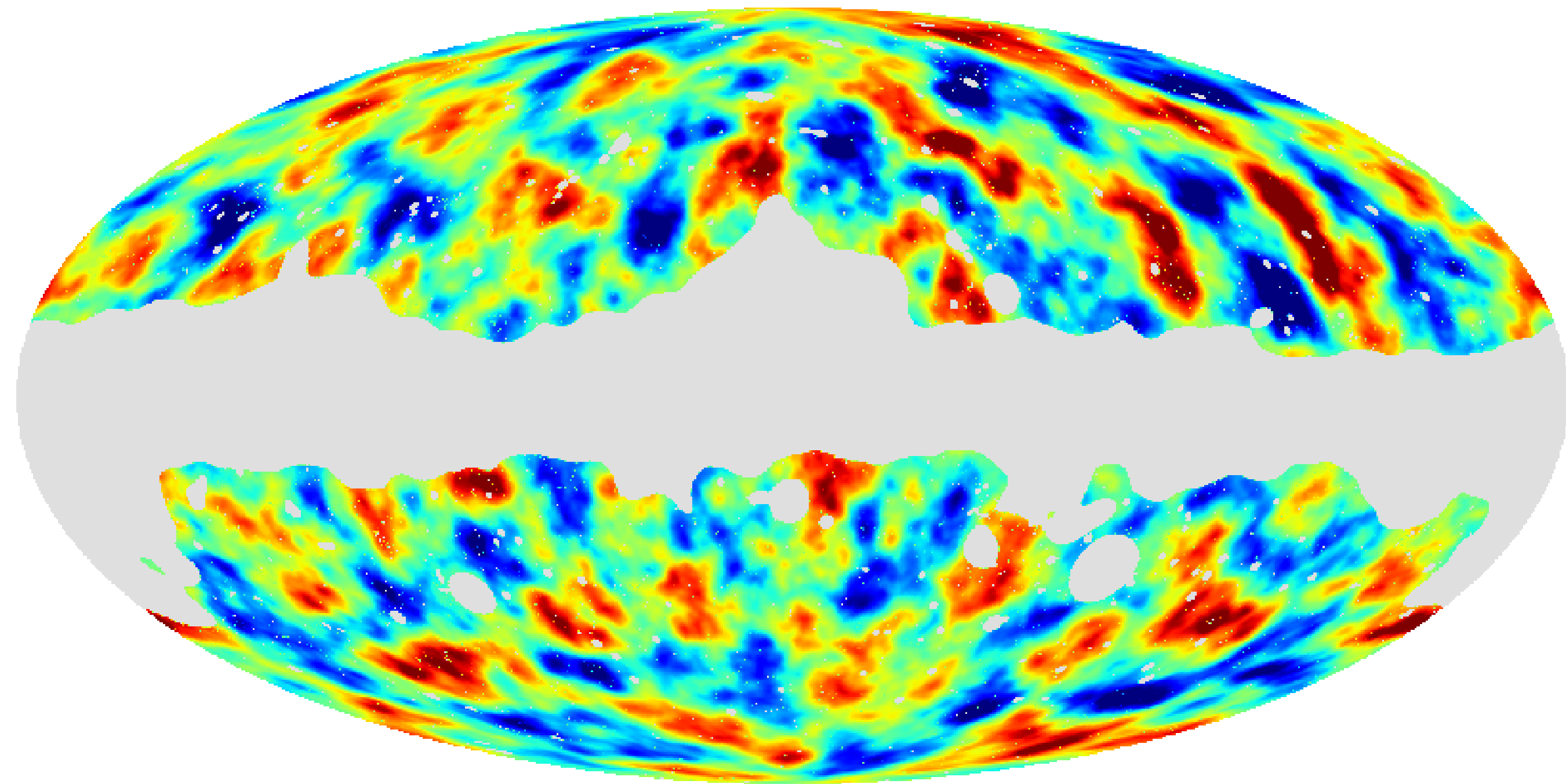
Planck 29–Month Map [100 GHz]



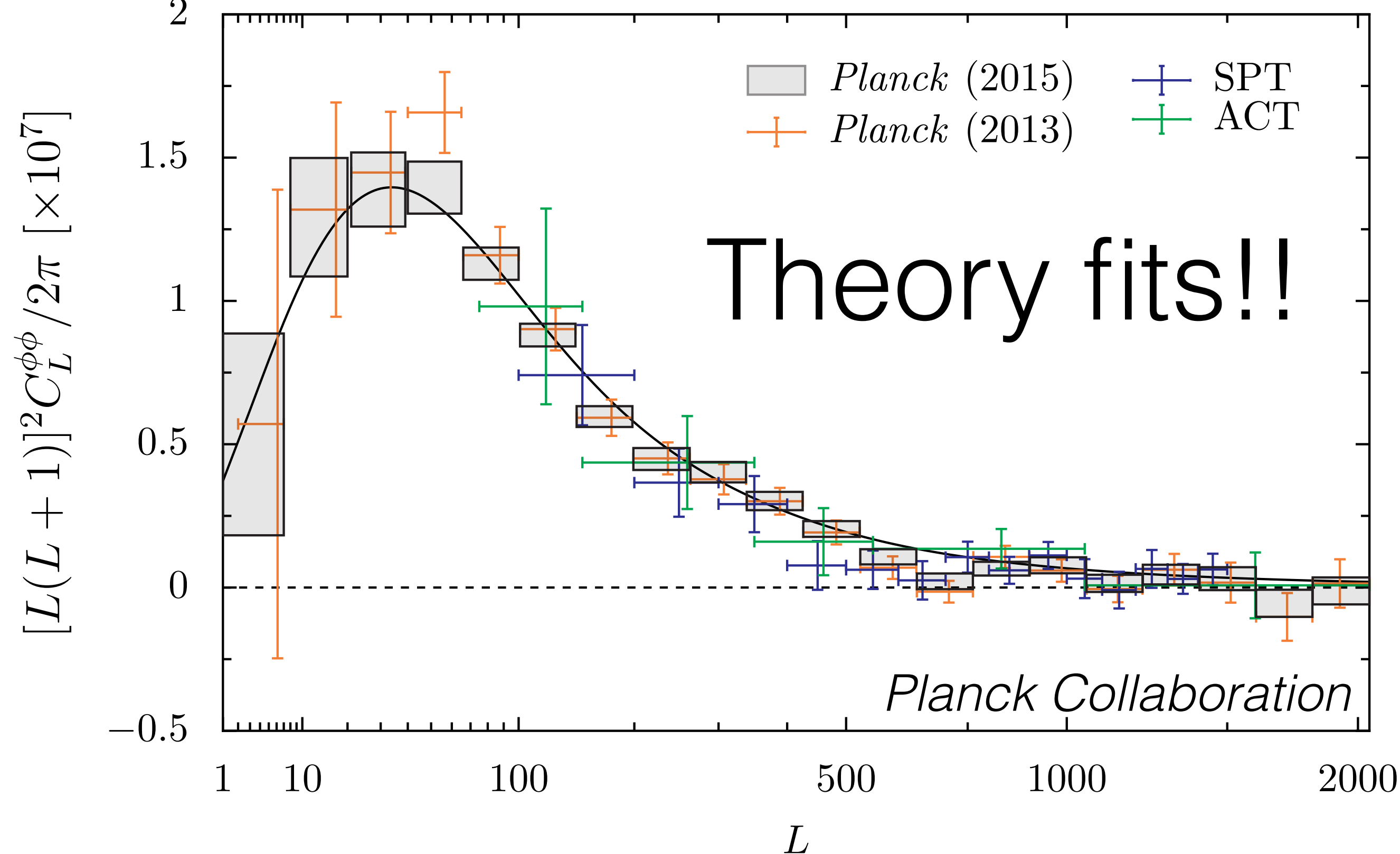
−0.20 0.20 mK

**From full-sky temperature maps to...**





**A full-sky lensing potential map!**



**...and our knowledge of the matter distribution improves**

$$\Omega_m = 0.315 \pm 0.013$$

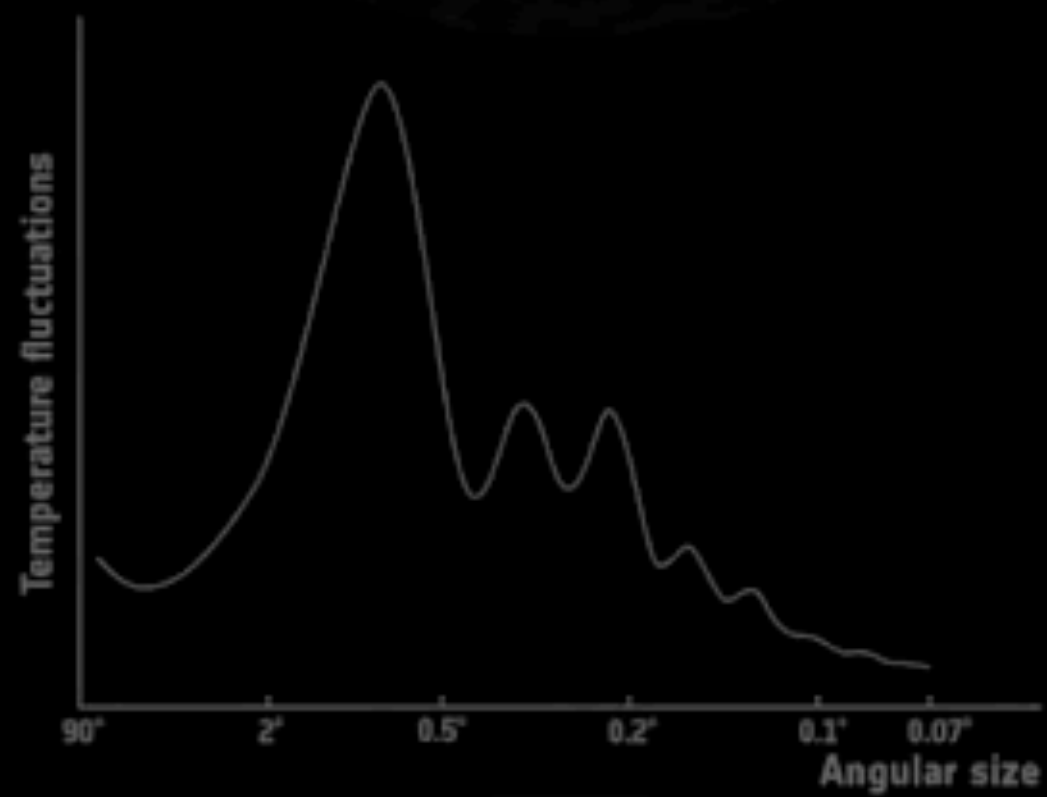
$$\sigma_8 = 0.829 \pm 0.014$$

Adding the  
lensing info

$$\Omega_m = 0.308 \pm 0.012$$

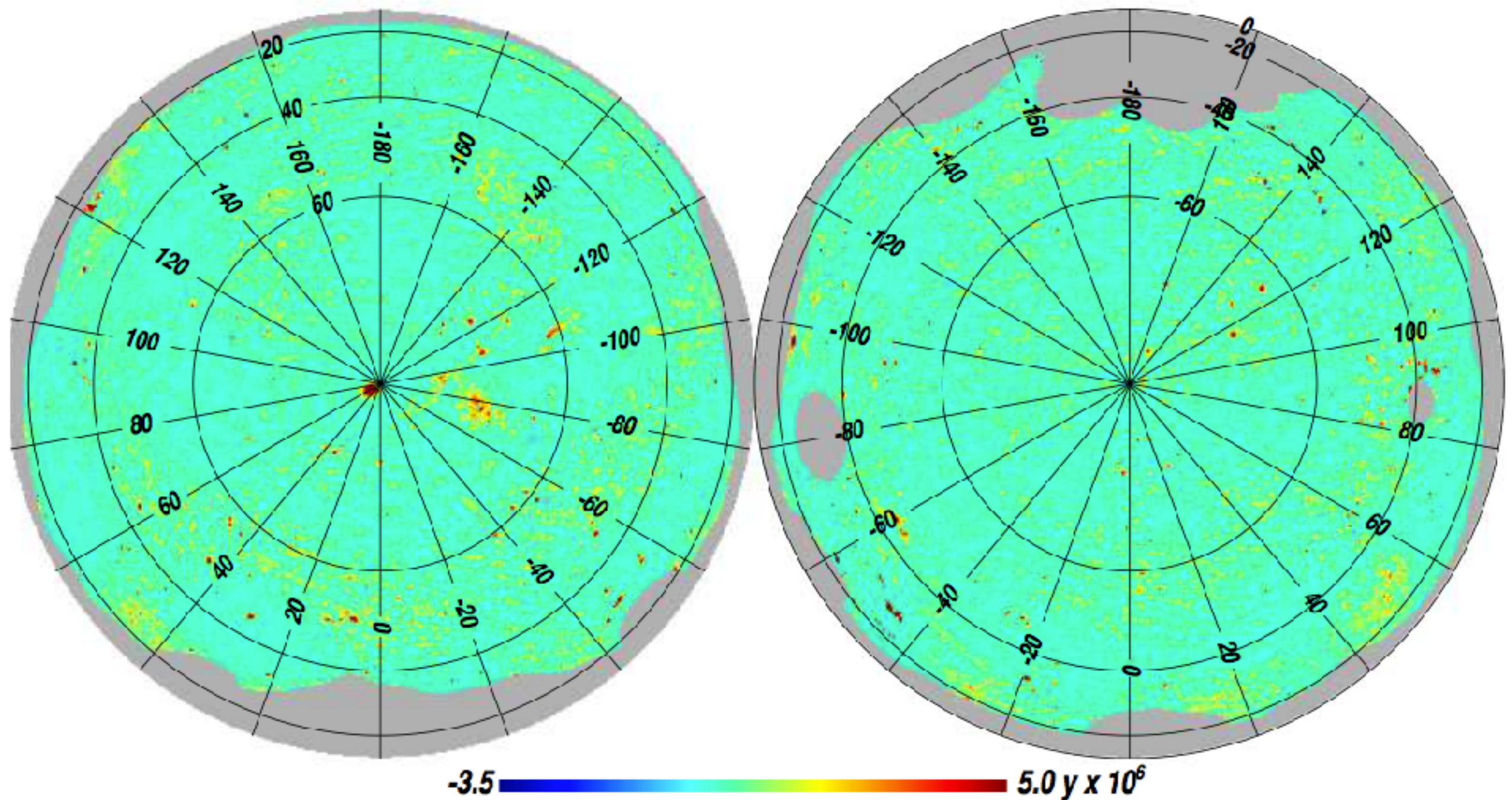
$$\sigma_8 = 0.8149 \pm 0.0093$$





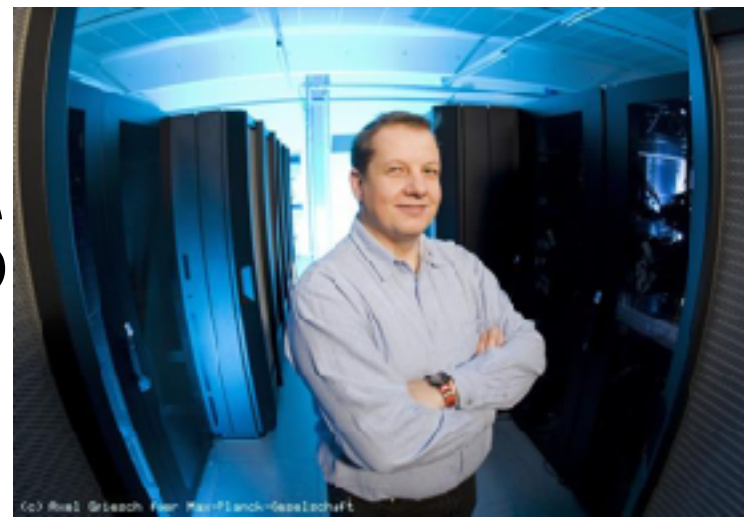
# Full-sky Thermal Pressure Map

North Galactic Pole *MILCA tSZ map* South Galactic Pole





# We can simulate this



Klaus Dolag (MPA/LMU)

**arXiv:1509.05134** [accepted for publication in MNRAS]

## **SZ effects in the Magneticum Pathfinder Simulation: Comparison with the Planck, SPT, and ACT results**

**K. Dolag<sup>1,2\*</sup>, E. Komatsu<sup>2,3</sup> and R. Sunyaev<sup>2,4</sup>**

<sup>1</sup> *University Observatory Munich, Scheinerstr. 1, 81679 Munich, Germany*

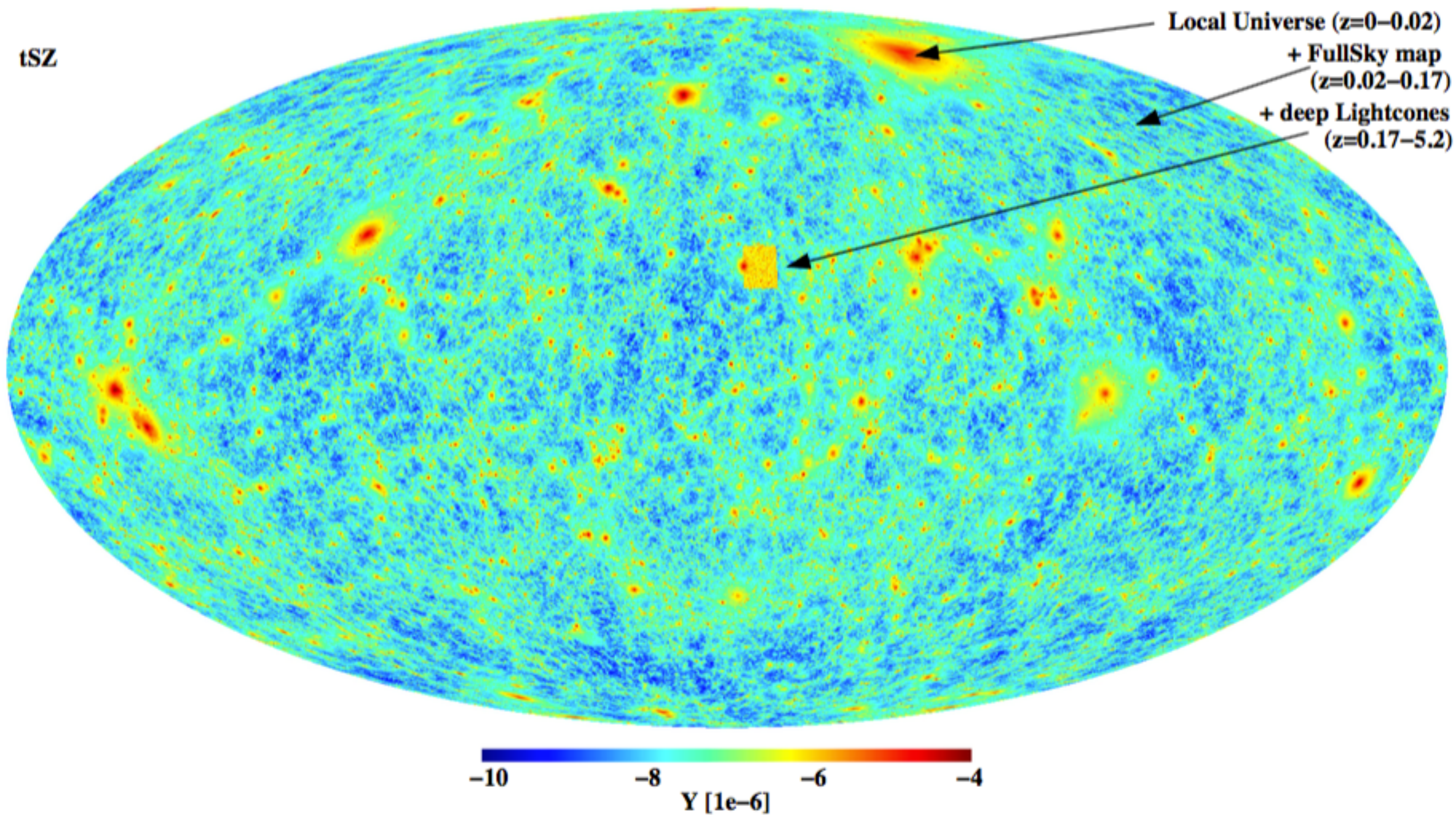
<sup>2</sup> *Max-Planck-Institut für Astrophysik, Karl-Schwarzschild Strasse 1, 85748 Garching, Germany*

<sup>3</sup> *Kavli Institute for the Physics and Mathematics of the Universe (Kavli IPMU, WPI), Todai Institutes for Advanced Study, the University of Tokyo, Kashiwa 277-8583, Japan*

<sup>4</sup> *Space Research Institute (IKI), Russian Academy of Sciences, Profsoyuznaya str. 84/32, Moscow, 117997 Russia*

- Volume:  $(896 \text{ Mpc}/h)^3$
- Cosmological hydro (P-GADGET3) with star formation and AGN feed back
- $2 \times 1526^3$  particles ( $m_{\text{DM}}=7.5 \times 10^8 \text{ M}_{\text{sun}}/h$ )





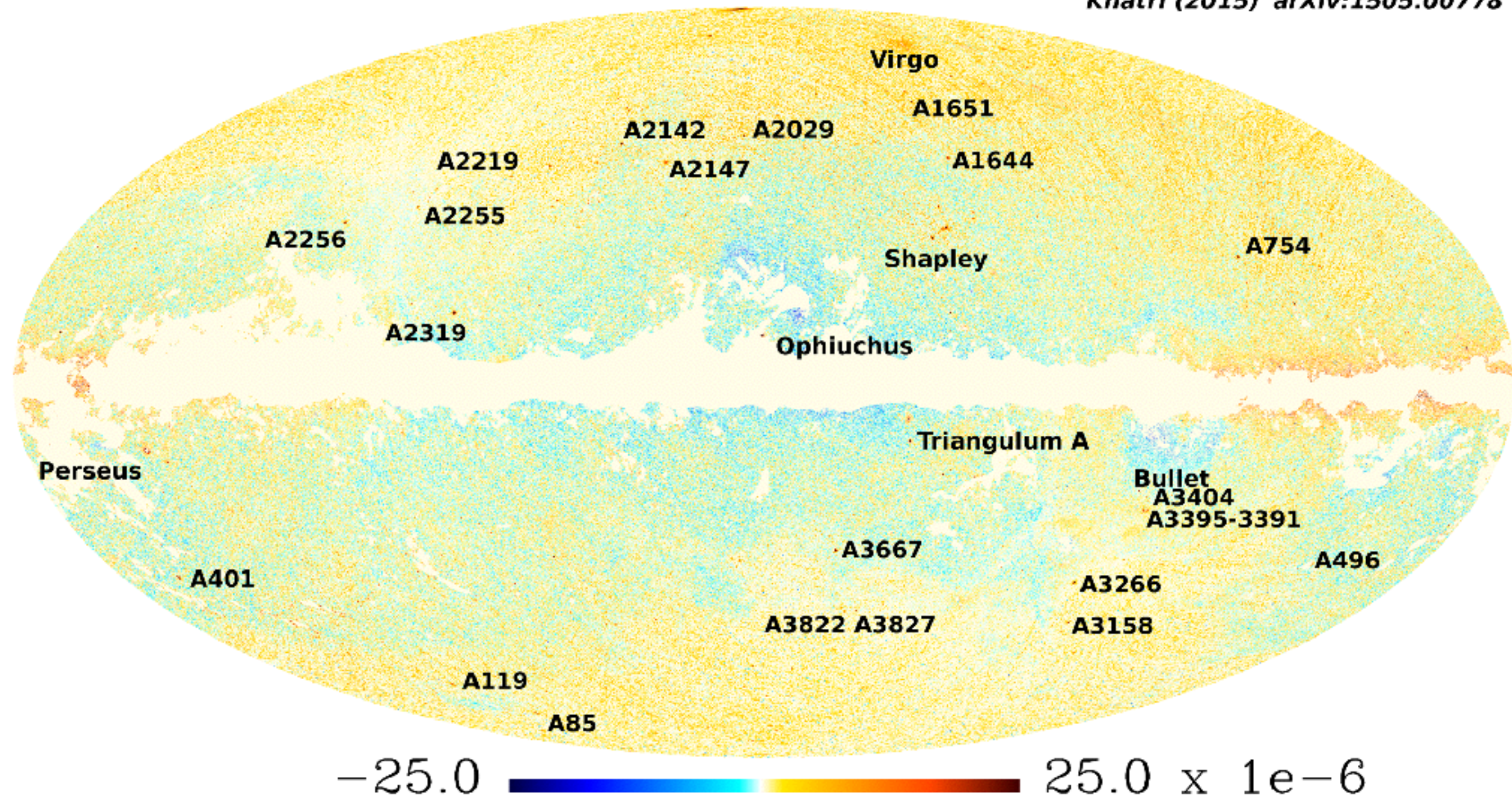
$$Y_{\text{tSZ}}(\boldsymbol{\theta}) = \frac{k_B \sigma_T}{m_e c^2} \int dl n_e(\boldsymbol{\theta}, l) T(\boldsymbol{\theta}, l)$$



# y-distortion map, 10 arcmin

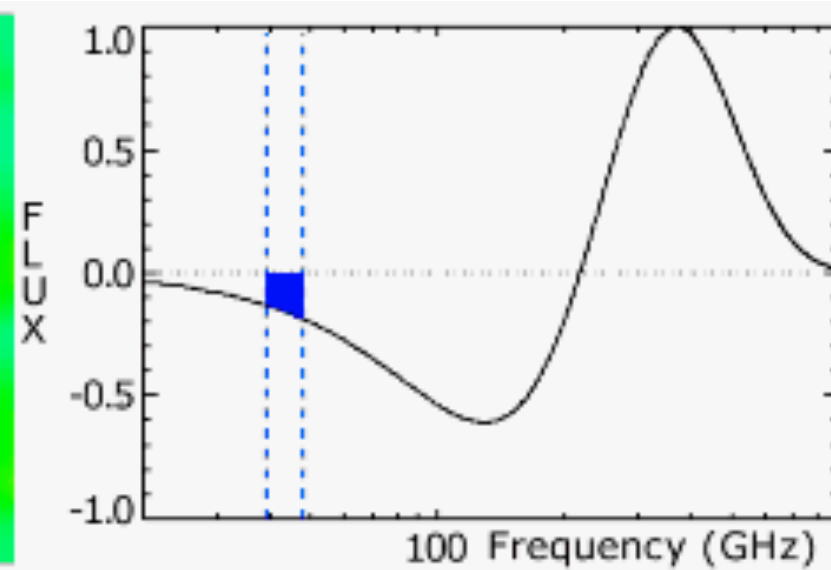
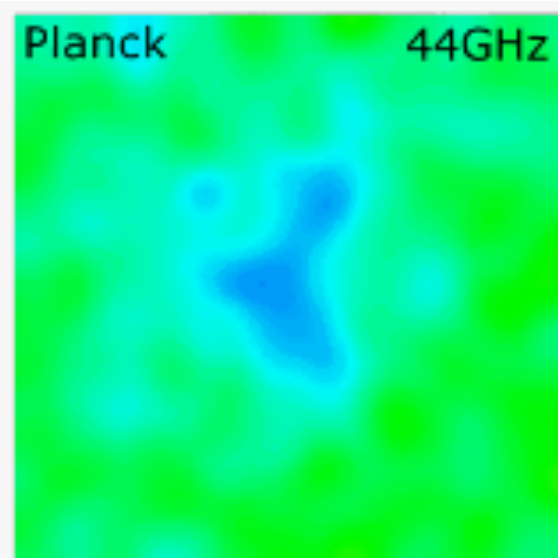
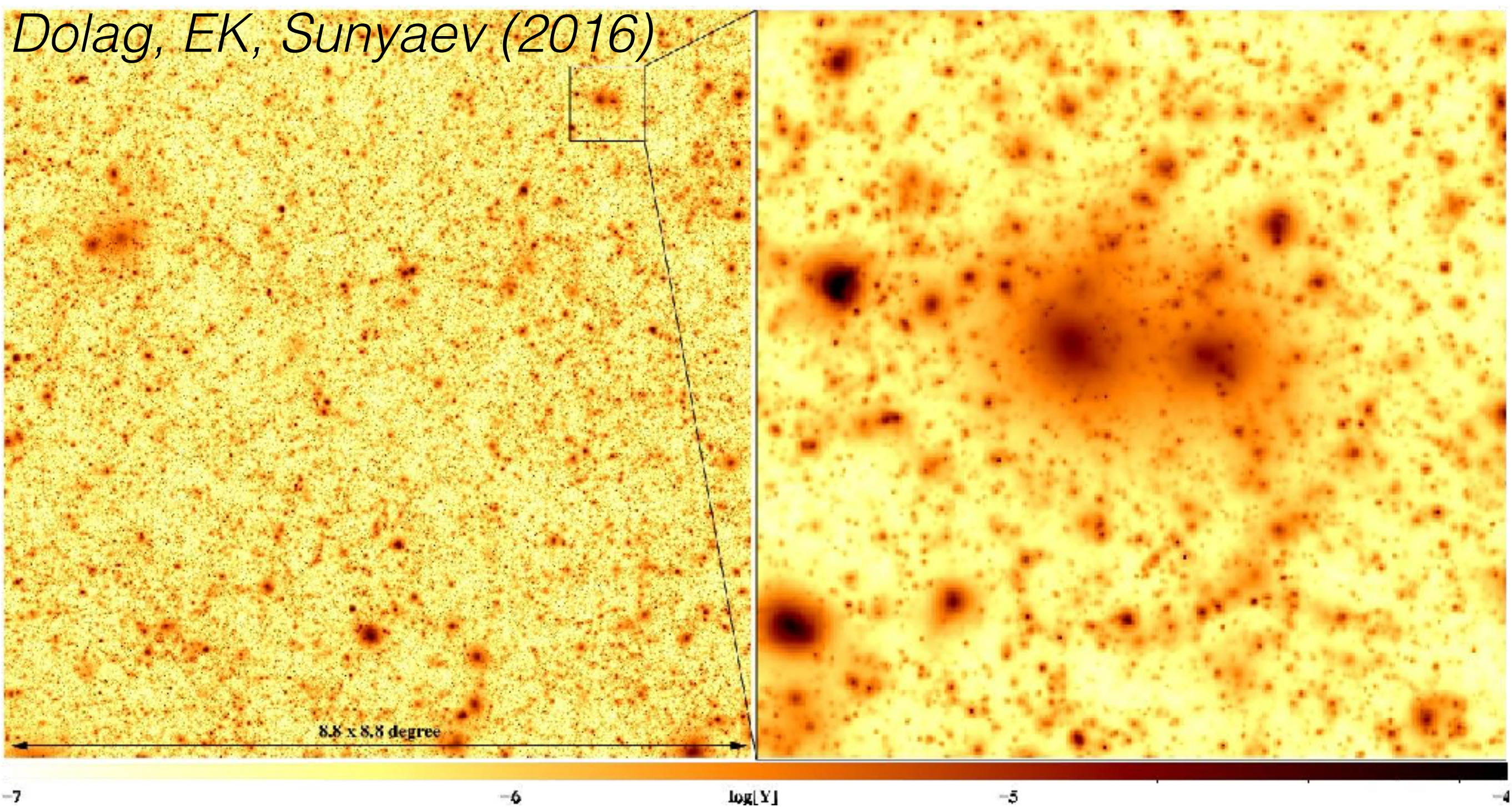
Coma

*Khatri (2015) arXiv:1505.00778*

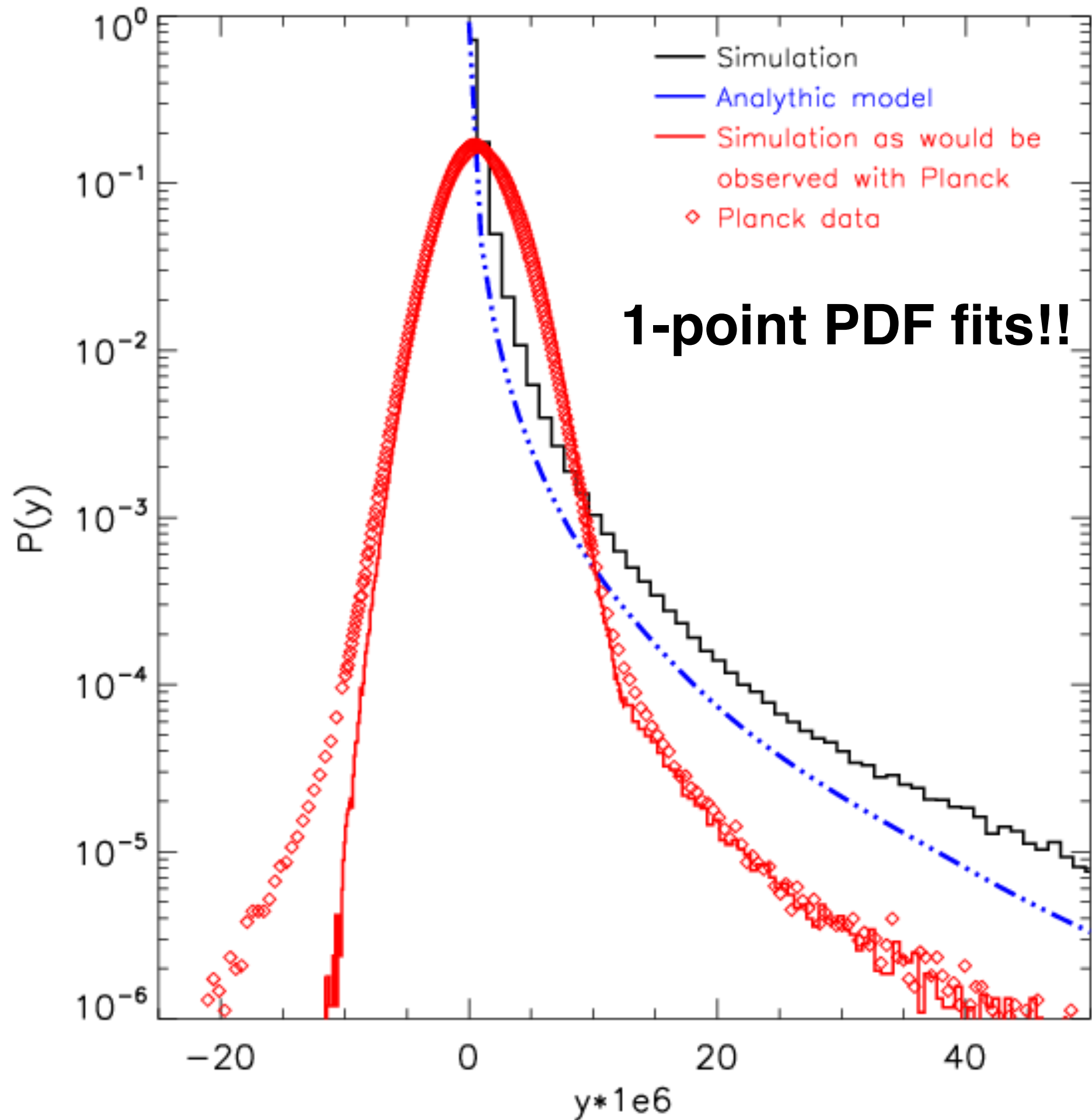


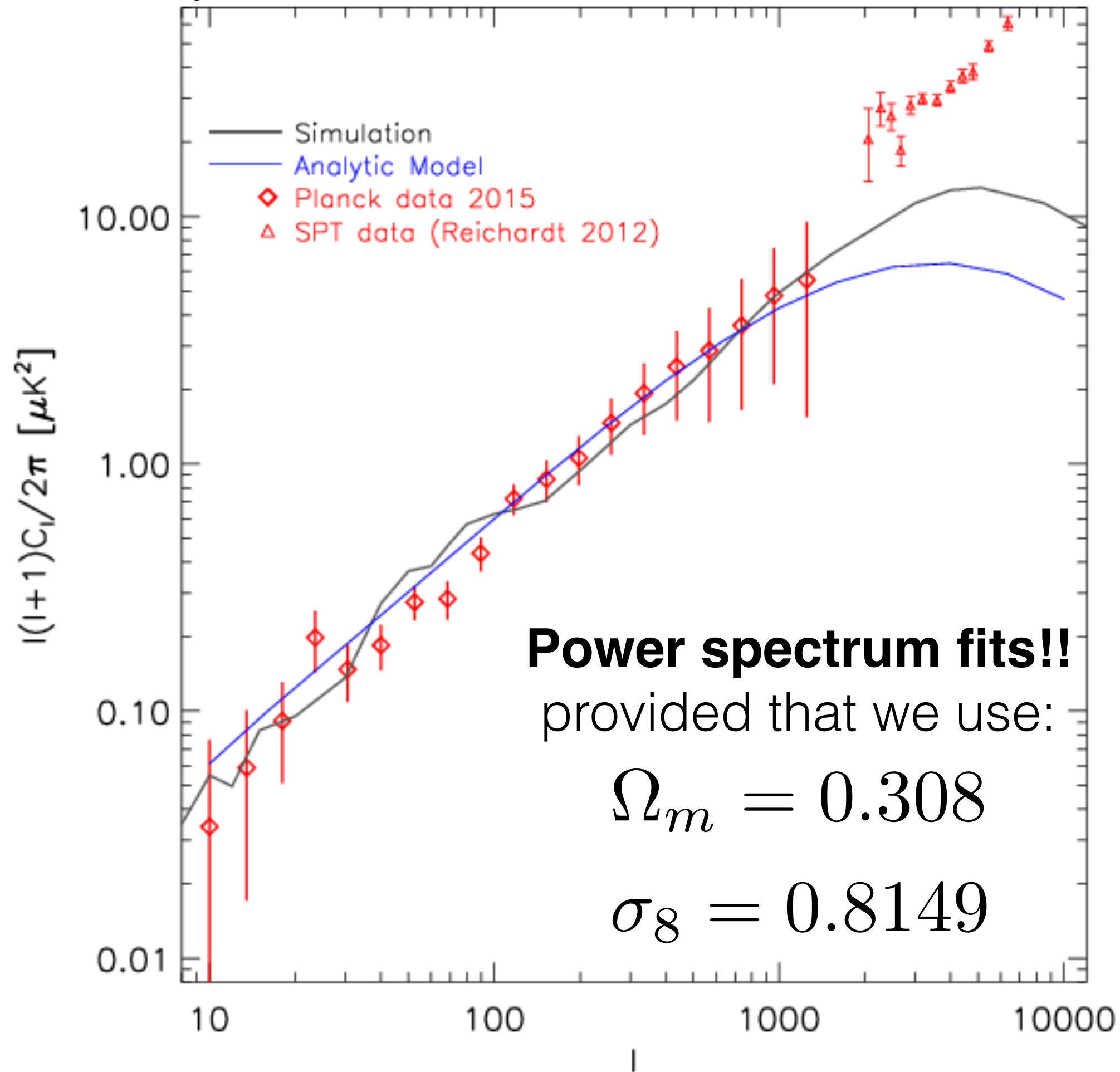
- “The local universe simulation” reproduces the observed structures pretty well





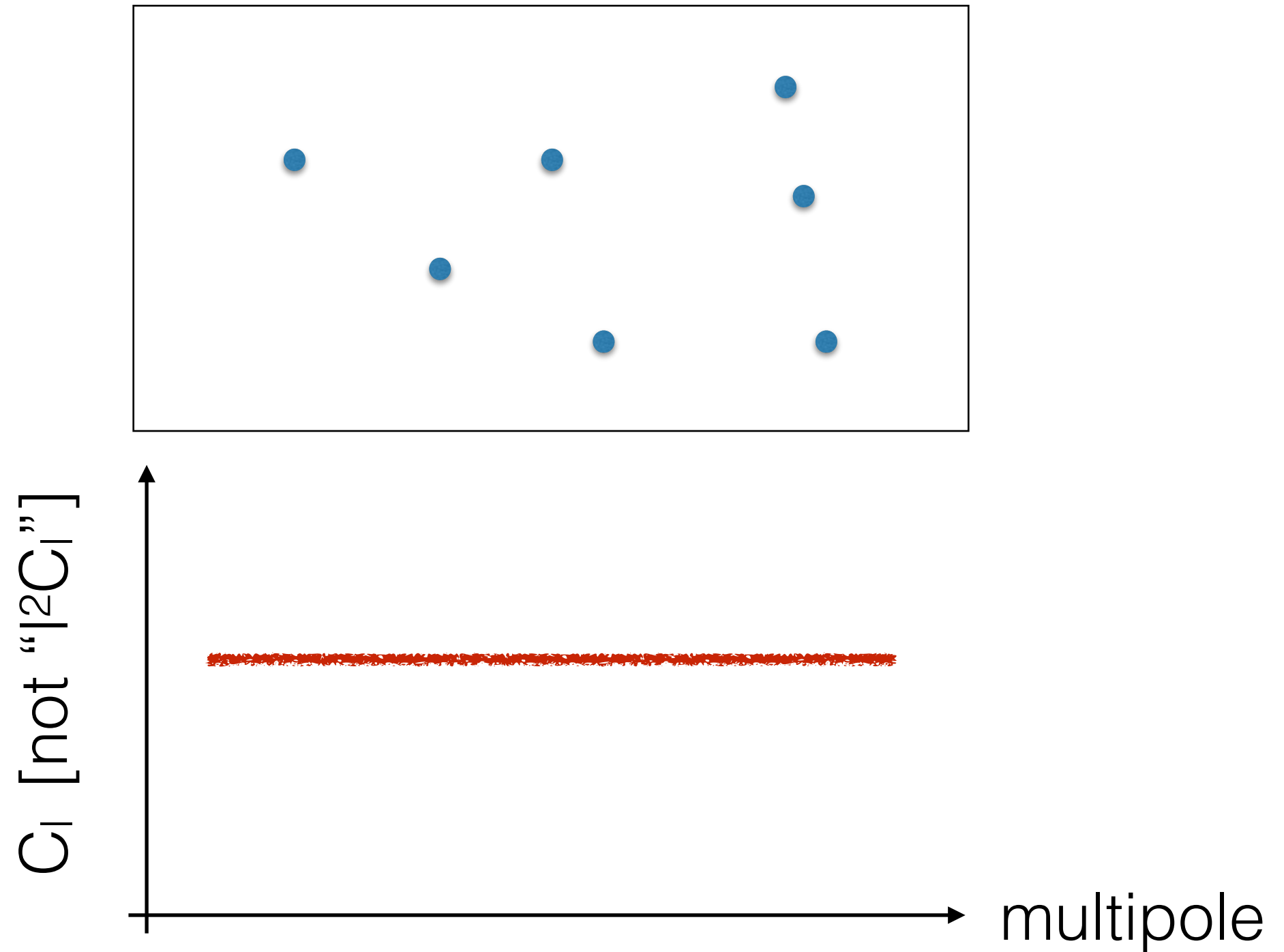






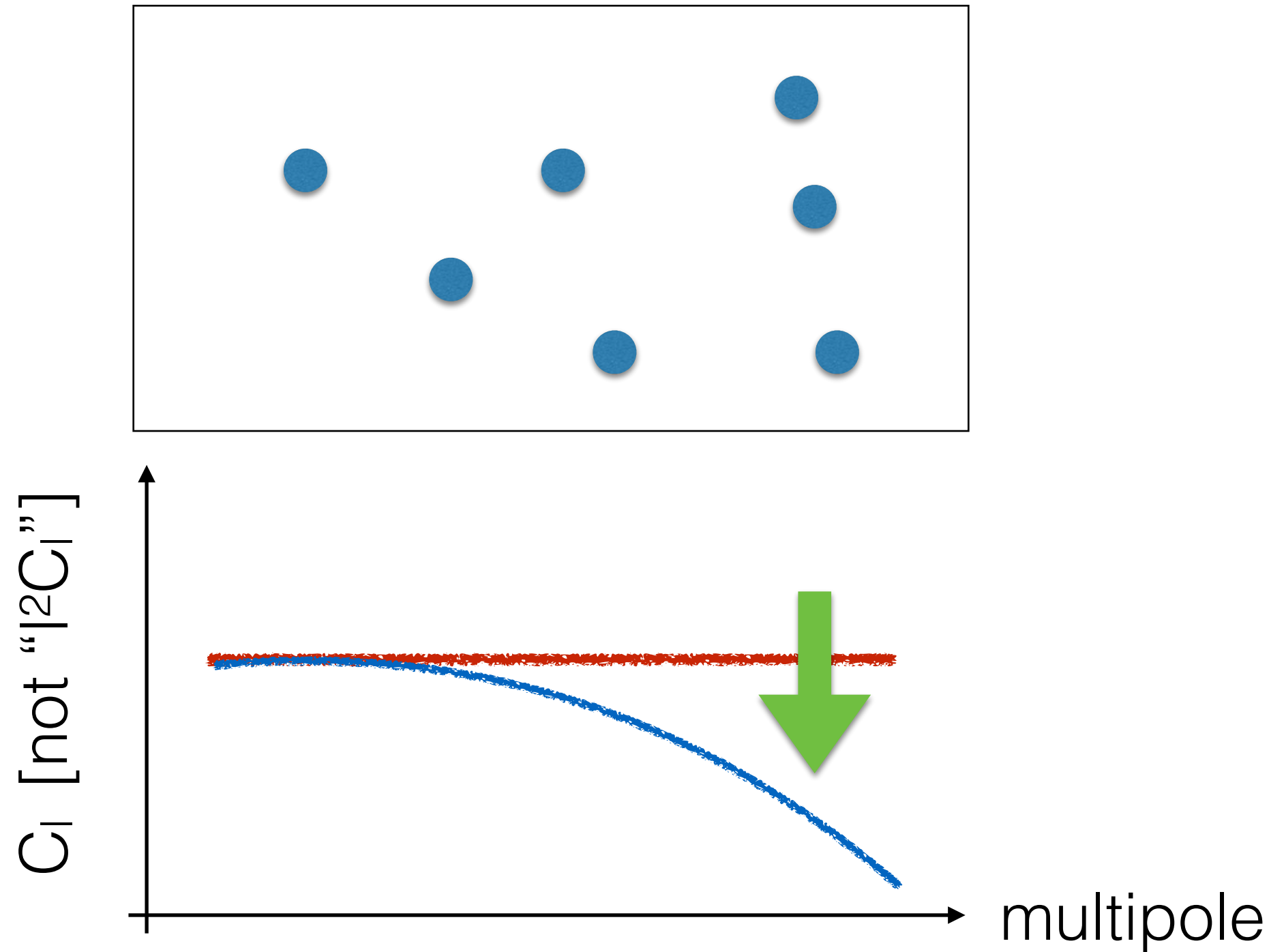


# Simple Interpretation



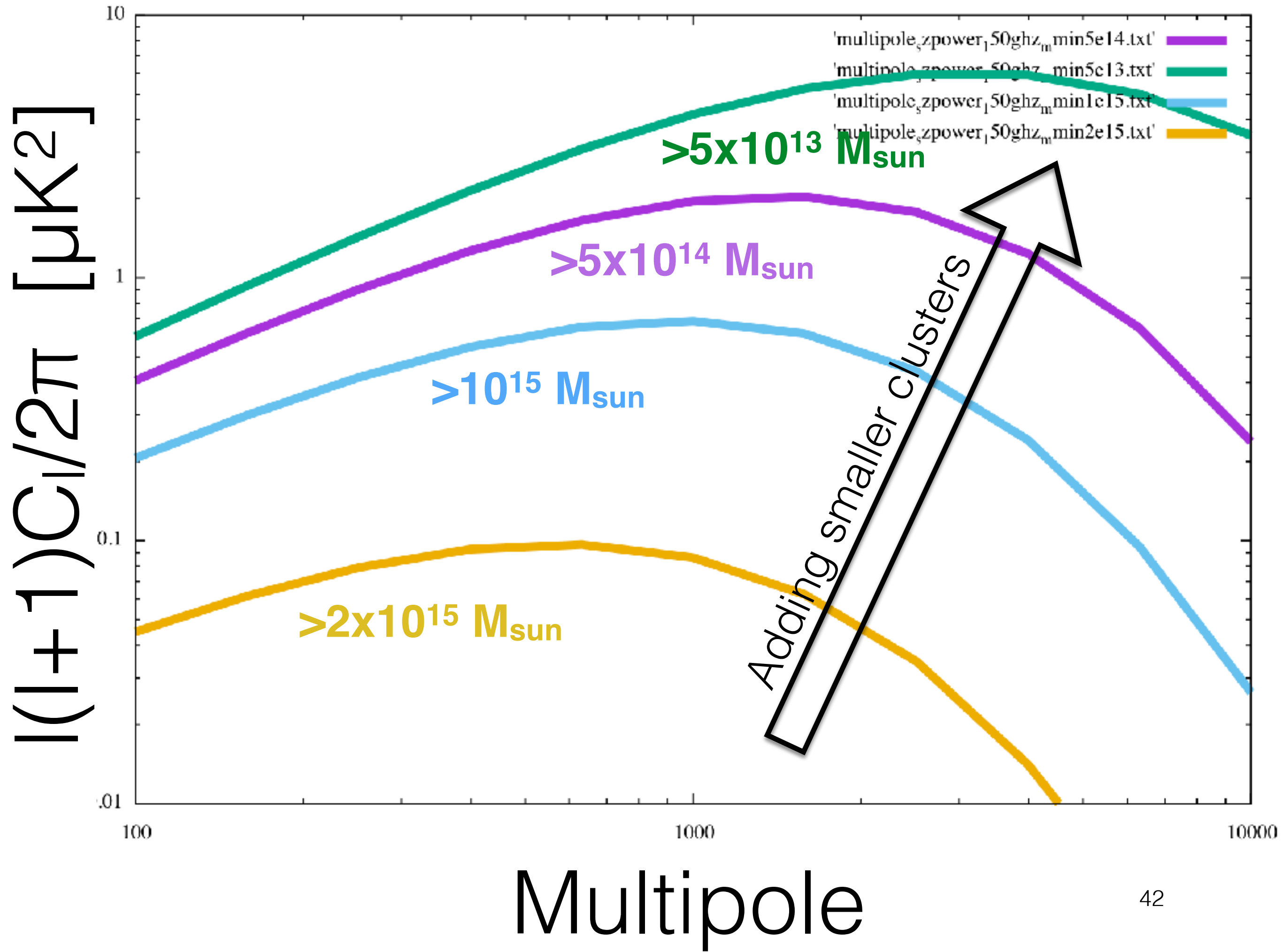
- Randomly-distributed point sources  
= Poisson spectrum =  $\sum_i (\text{flux}_i)^2 / 4\pi$

# Simple Interpretation



- Extended sources = the power spectrum reflects intensity profiles





# Simple Formula

$$C_\ell = \int dz \frac{dV}{dz} \int dM \frac{dn}{dM} |y_\ell(M, z)|^2$$

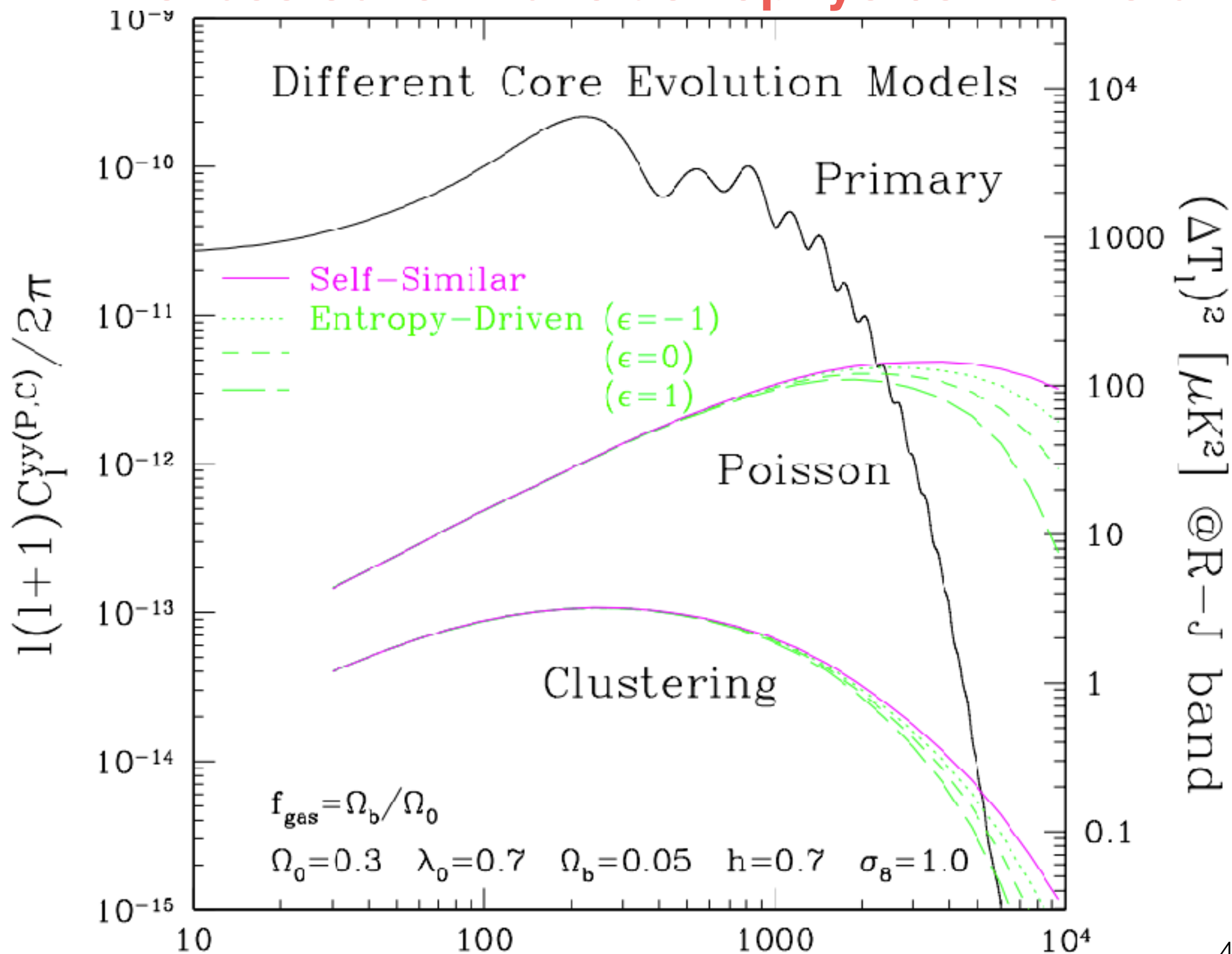
2d Fourier transform  
of pressure

- $y_l$  with small  $l$  just gives the total thermal pressure,  $MT \sim M^{5/3}$
- Heavily weighted by massive clusters
- The mass function,  $dn/dM$ , is sensitive to the amplitude of fluctuations,  $\sigma_8$

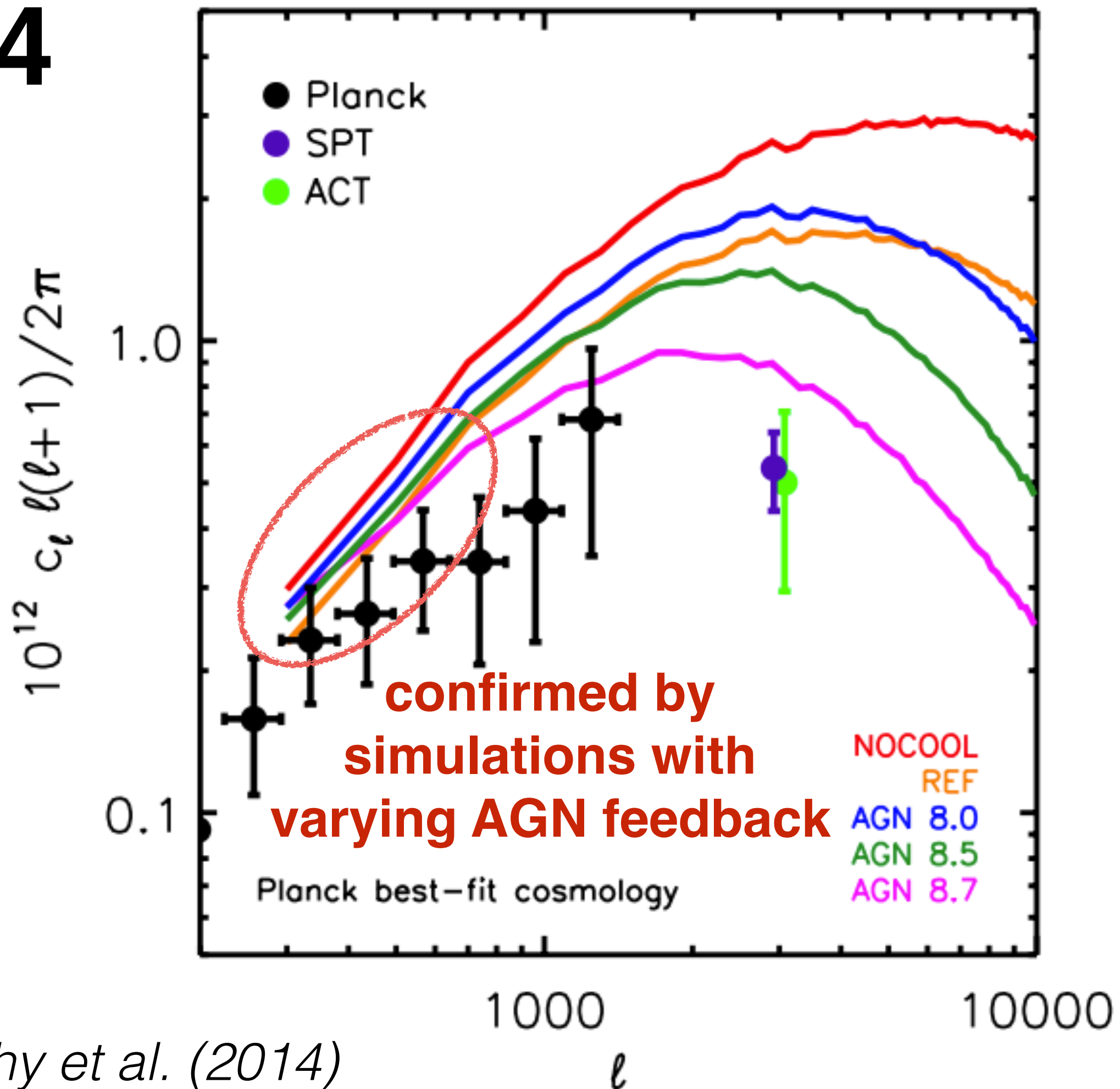


# 1999

## Degree-scale SZ power spectrum is less sensitive to astrophysics in cluster cores



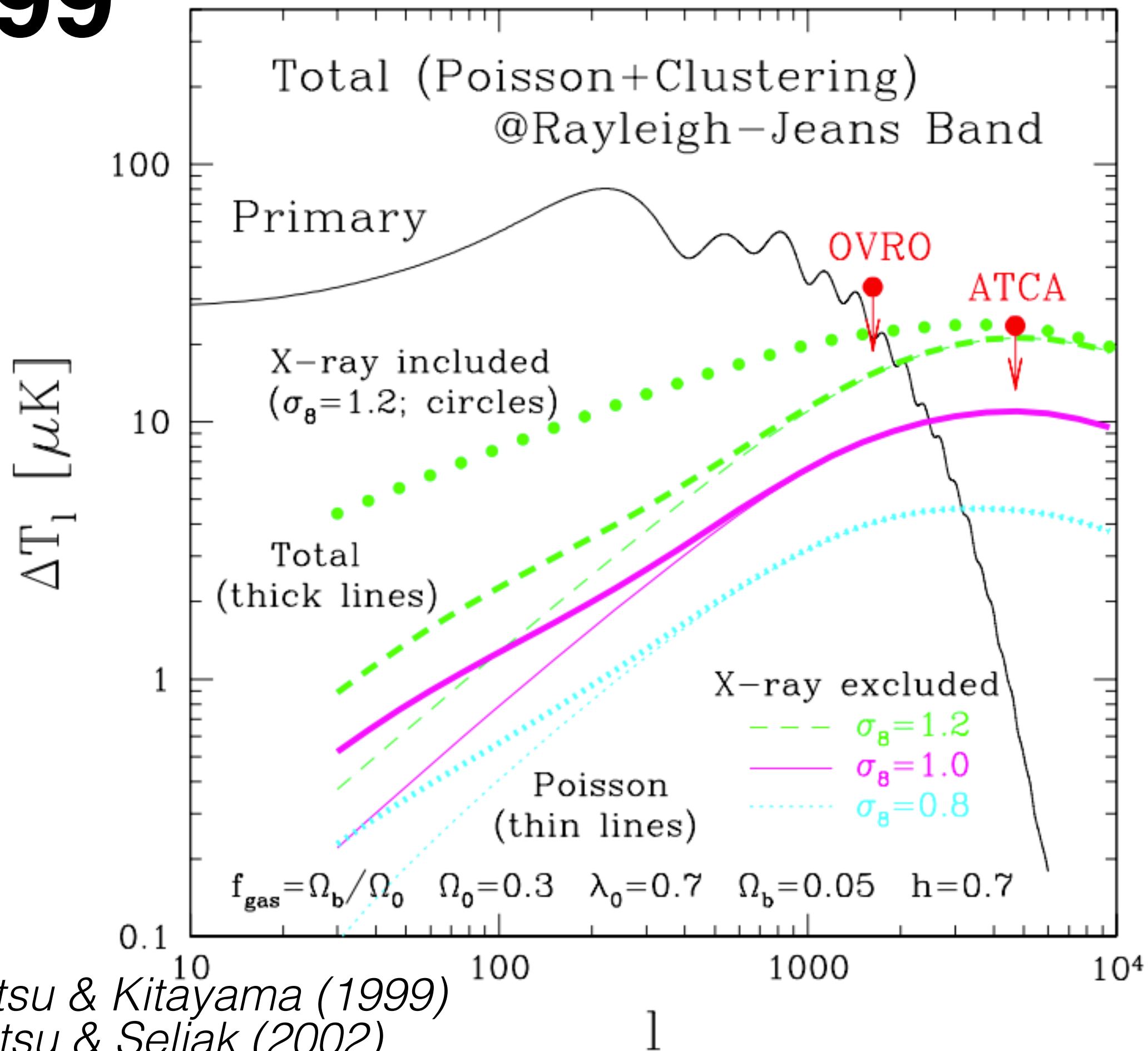
# 2014





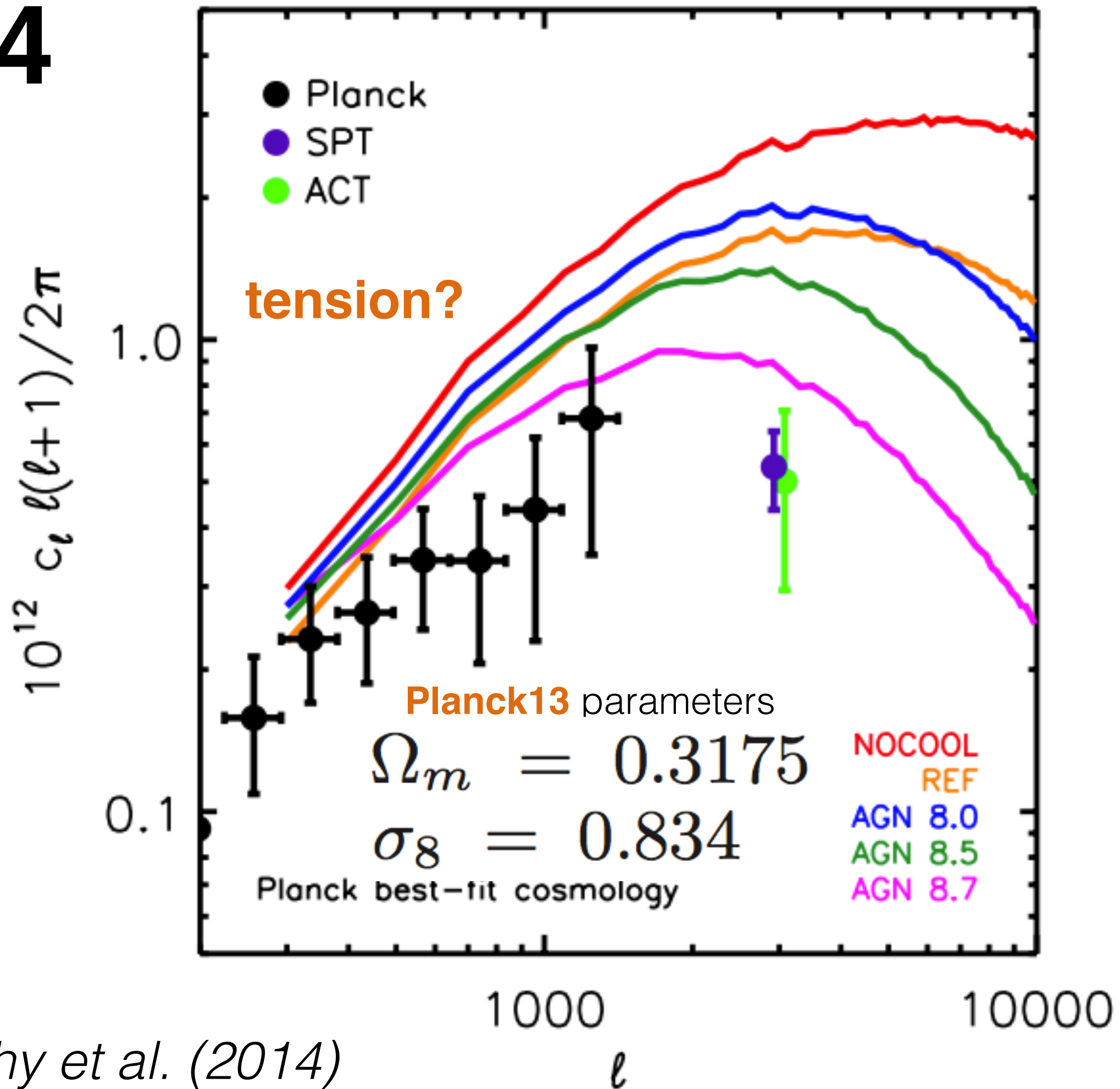
# 1999

It is very sensitive to the amplitude of fluctuations



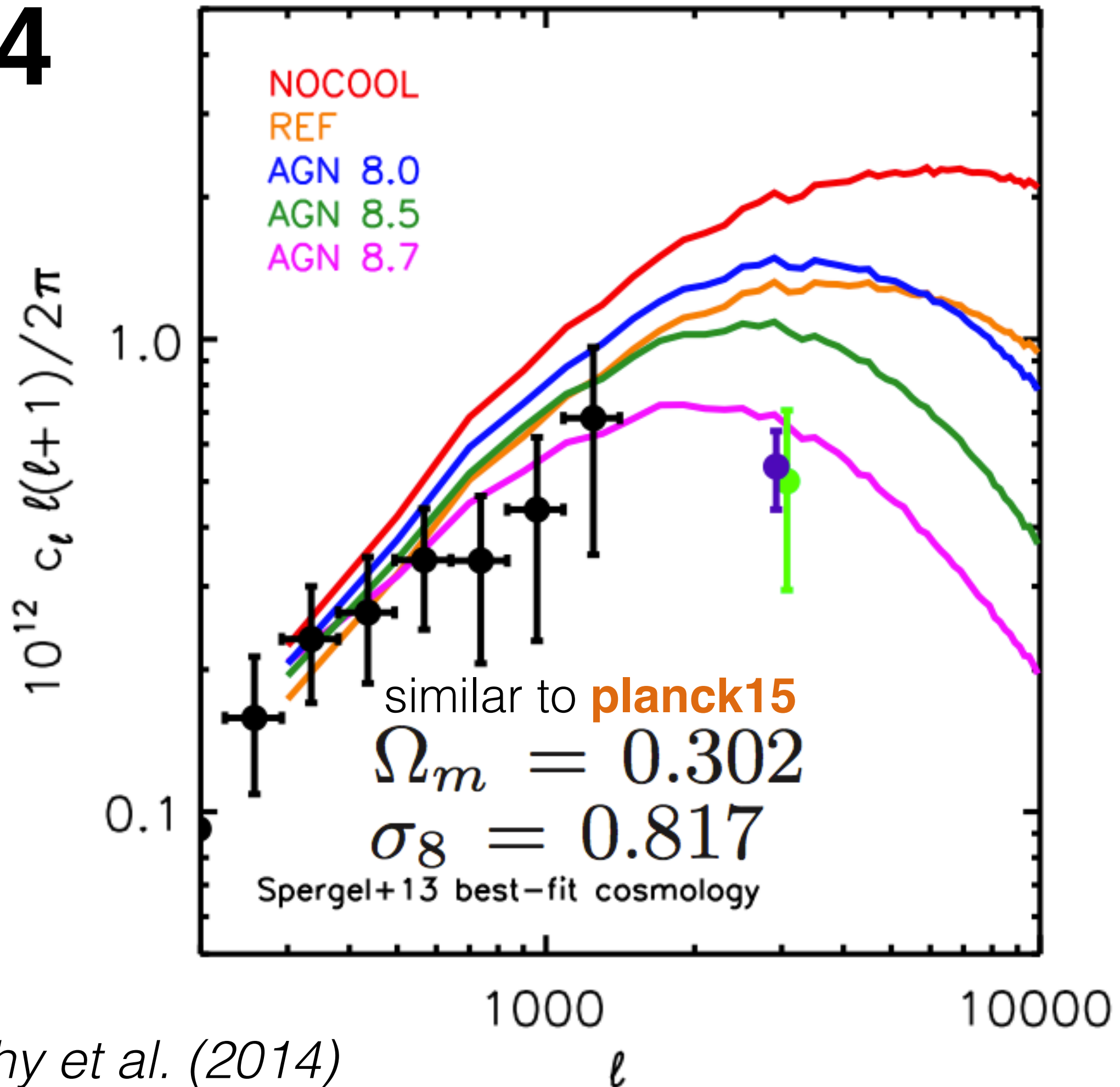
Komatsu & Kitayama (1999)  
 Komatsu & Seljak (2002)

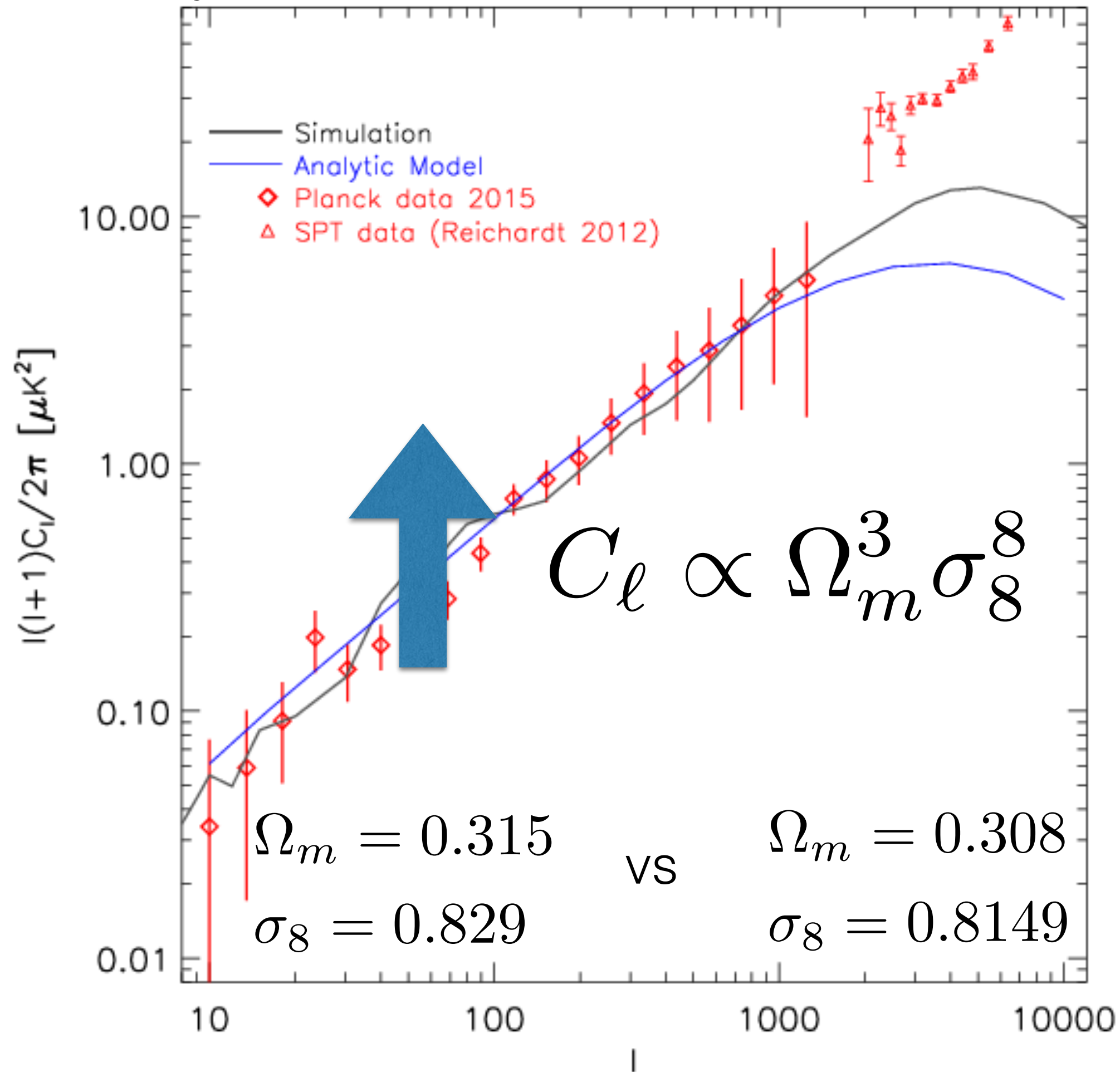
# 2014



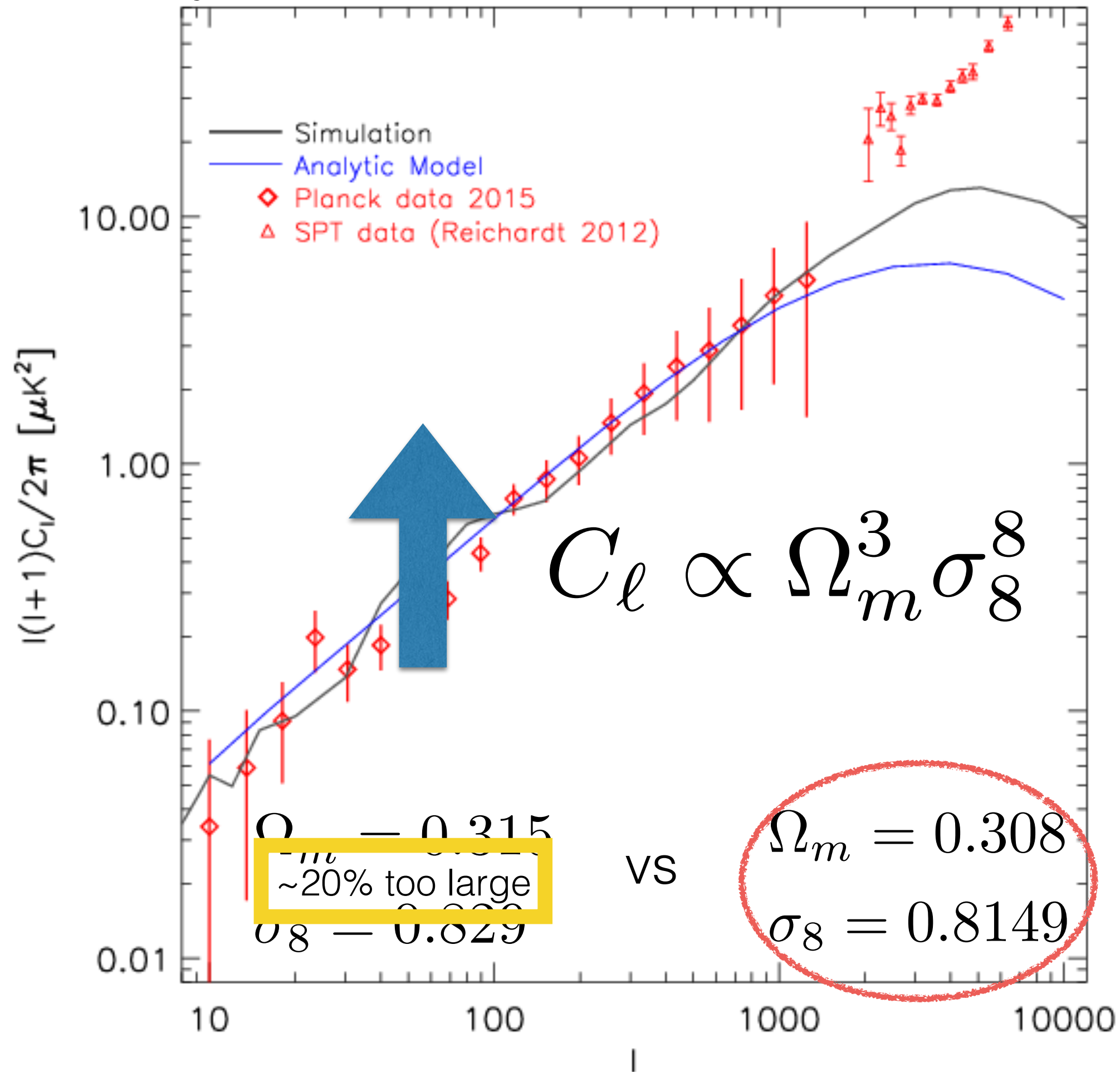


# 2014









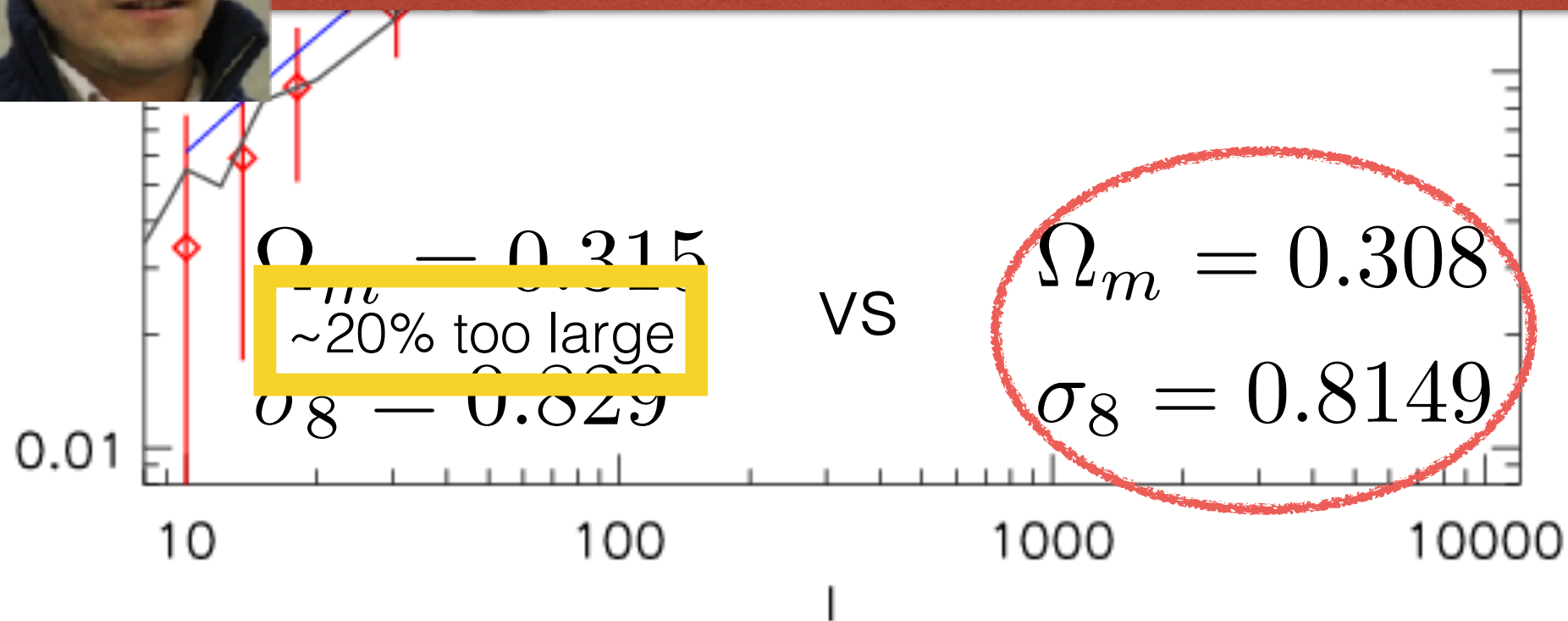
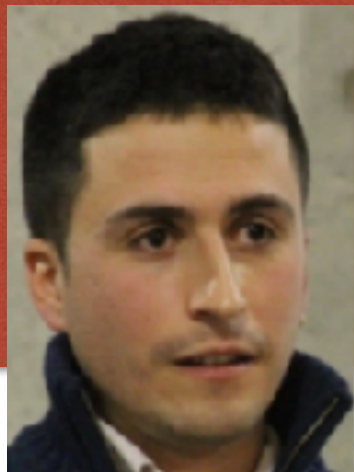


**But, it needs a proper Markov Chain parameter exploration.**

**Almost done**

(Bolliet, et al, in prep)

$l(l+1)C_l/2\pi$  [ $\mu K^2$ ]





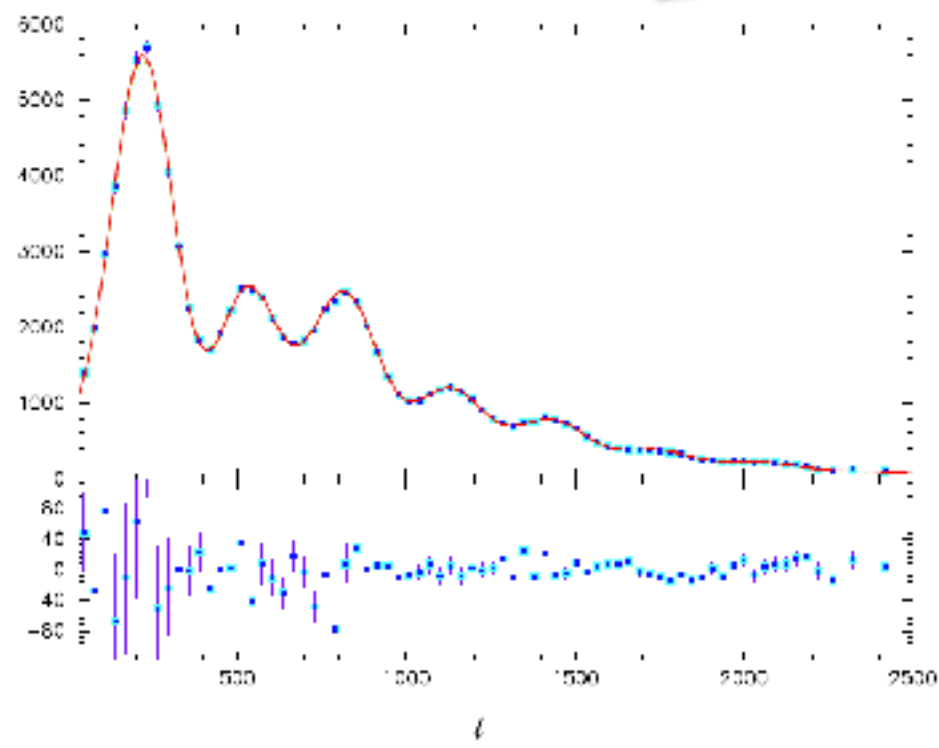
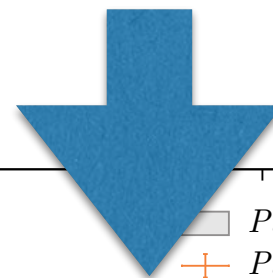
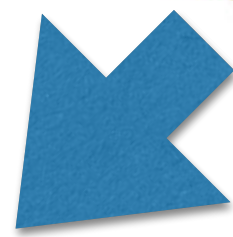
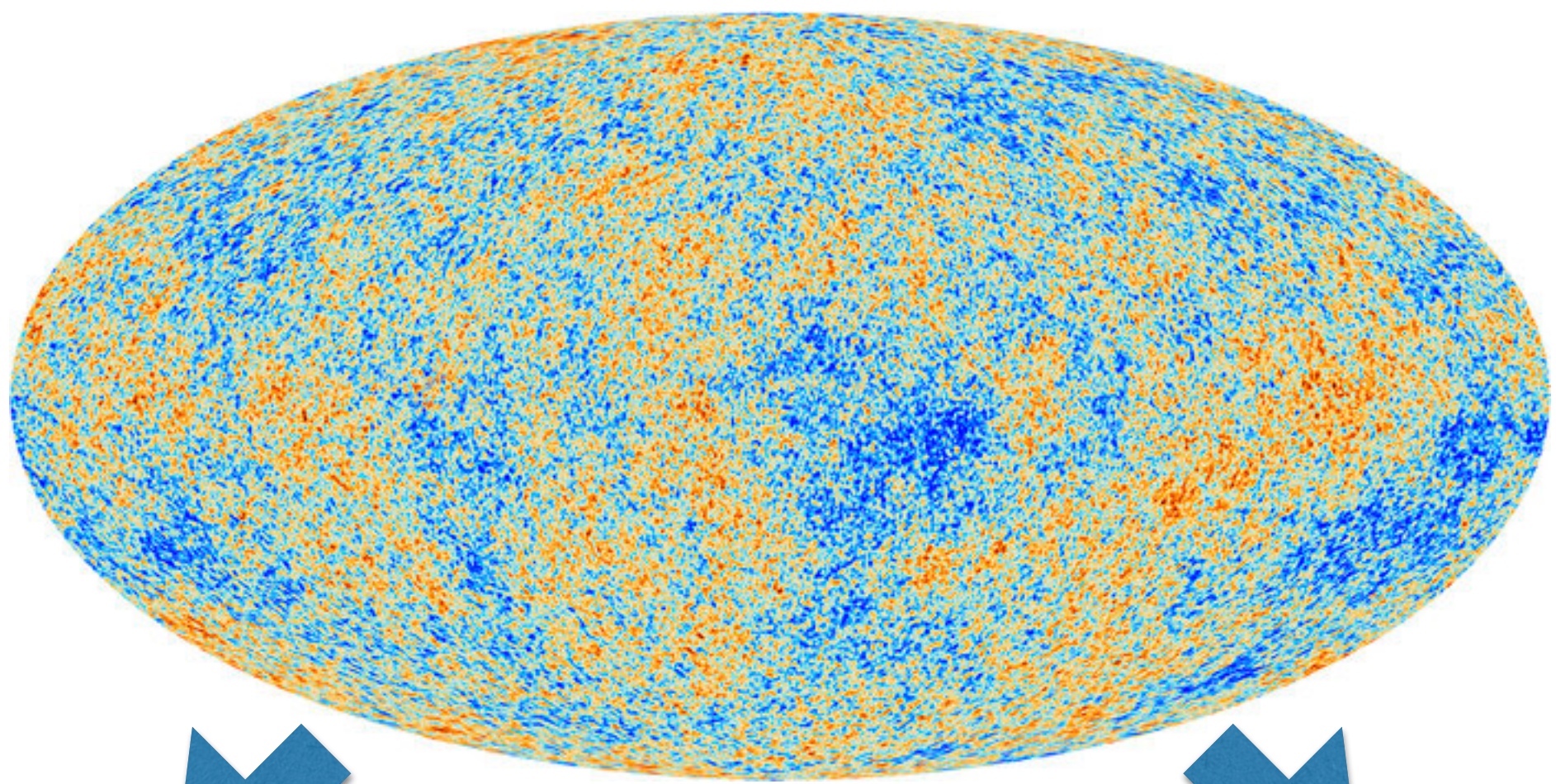
# Codes (CRL)

<http://wwwmpa.mpa-garching.mpg.de/~komatsu/crl/>

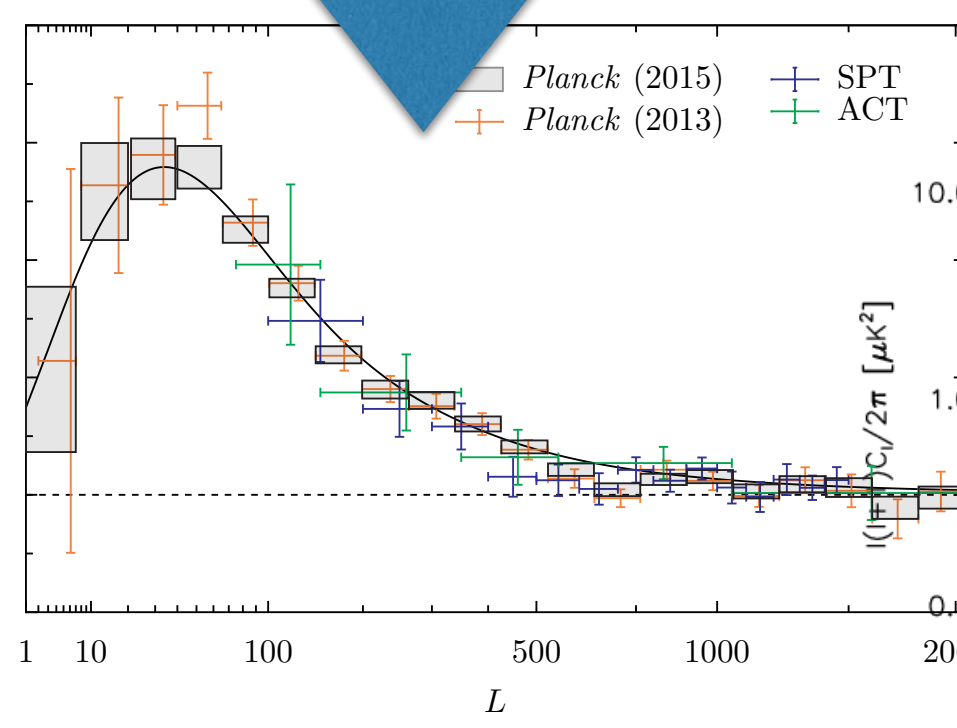
## Clusters of Galaxies

- ▶ **Converting Virial Mass to Overdensity Mass**
- ▶ **Gas Pressure and Sunyaev-Zel'dovich Effect Profiles (Arnaud et al.)**
- ▶ **Fourier Transform of the Sunyaev-Zel'dovich Effect Profile (Arnaud et al.)**
- ▶ **Power Spectrum of the Sunyaev-Zel'dovich Effect (Arnaud et al.)**
- ▶ **Gas Pressure and Sunyaev-Zel'dovich Effect Profiles (Komatsu-Seljak)**
- ▶ **Fourier Transform of the Sunyaev-Zel'dovich Effect Profile (Komatsu-Seljak)**
- ▶ **Power Spectrum of the Sunyaev-Zel'dovich Effect (Komatsu-Seljak)**
- ▶ **Power Spectrum of the Sunyaev-Zel'dovich Effect (Self-similar Arnaud et al., as in Shaw et al. 2010)**
- ▶ **Gas Pressure and Sunyaev-Zel'dovich Effect Profiles (Planck 2013)**
- ▶ **Power Spectrum of the Sunyaev-Zel'dovich Effect (Planck profile and parameters, as in Dolag et al. 2015)**
- ▶ **Mean Compton Y (Planck profile and parameters, as in Dolag et al. 2015)**
- ▶ **Gas Pressure and Sunyaev-Zel'dovich Effect Profiles (Battaglia et al.)**
- ▶ **Mean Compton Y (Battaglia et al. profile and WMAP9 parameters, as in Hill et al. 2015)**
- ▶ **Bin-Integrated PDF of Compton Y (Planck profile and Magneticum parameters, as in Dolag et al. 2015)**
- ▶ **Electron density, X-ray temperature, and electron pressure profiles of Vikhlinin's low-z sample**

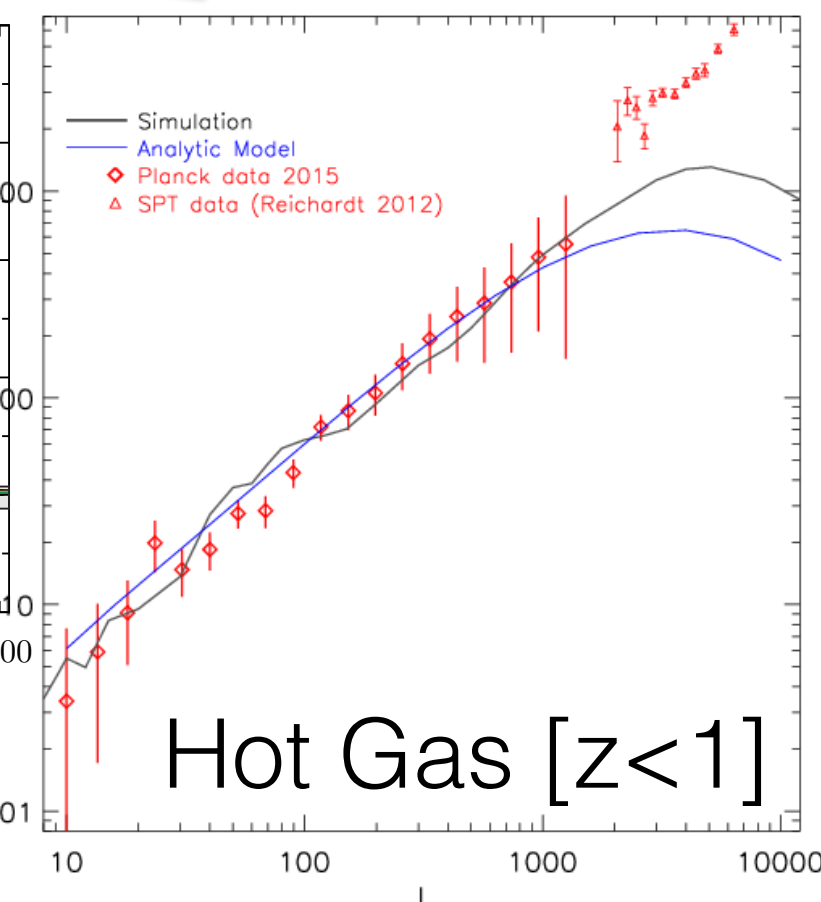




Initial Condition

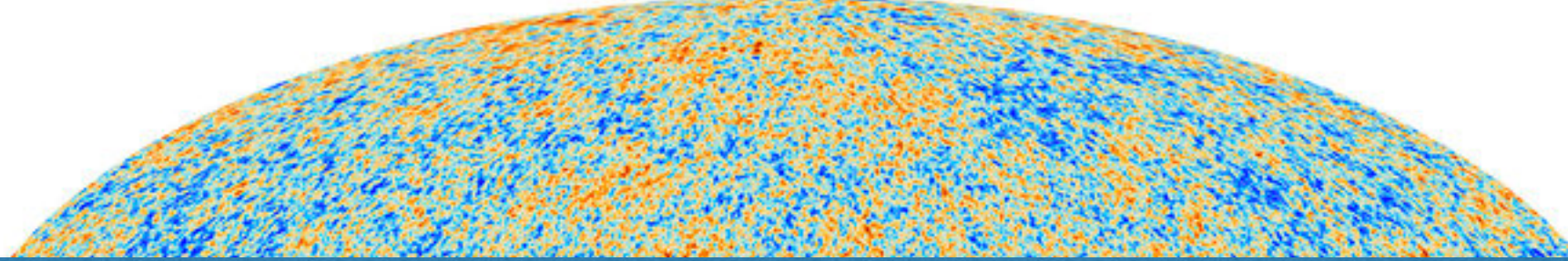


Dark Matter [ $z \sim 2$ ]



Hot Gas [ $z < 1$ ]





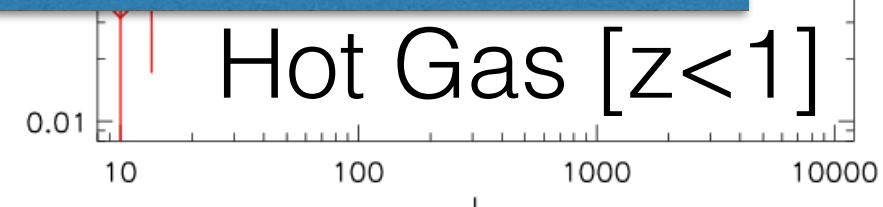
**Standard  $\Lambda$ CDM Model**, starting with  
**inflation** producing adiabatic,  
Gaussian, isotropic,  $n_s < 1$  primordial  
fluctuations fit all the data from the  
**initial condition to structure  
formation!**

These results are all solely based on the  
microwave background data



Initial Condition

Dark Matter [ $z \sim 2$ ]



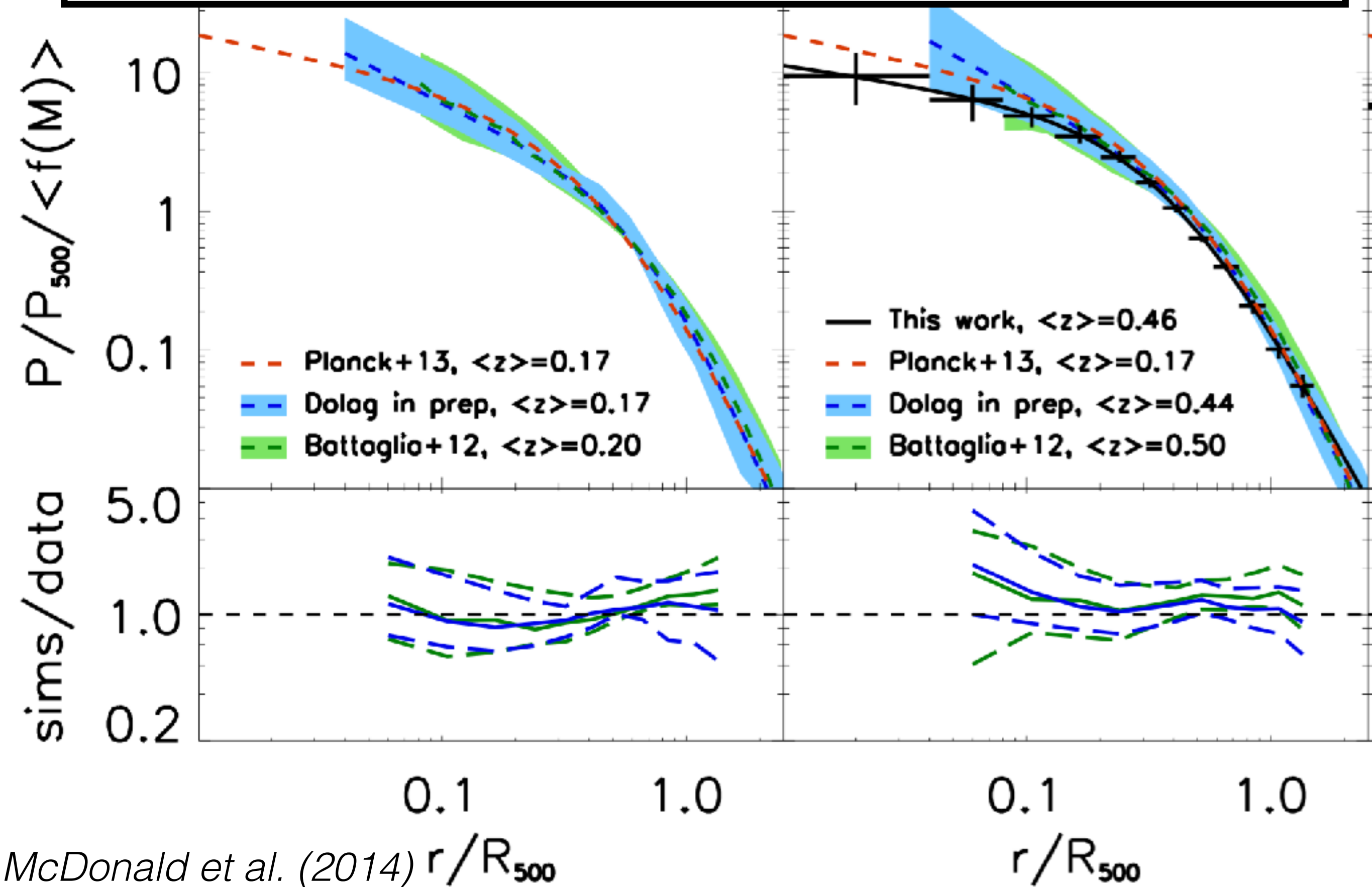
# Toward more satisfaction

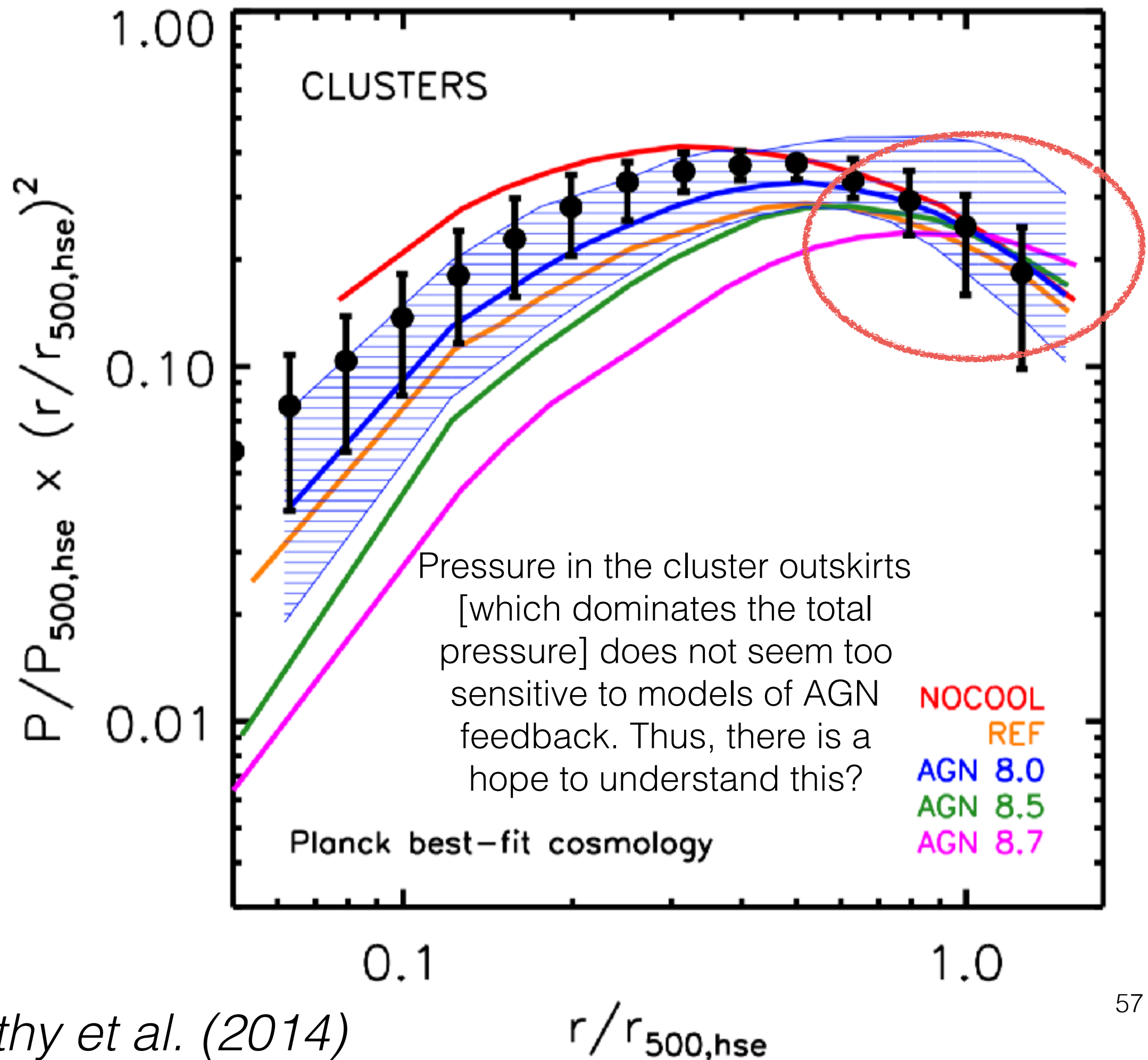
$$C_\ell = \int dz \frac{dV}{dz} \int dM \frac{dn}{dM} |y_\ell(M, z)|^2$$

- The key ingredient of the power spectrum is a profile of **thermal pressure of electrons**
- We can simulate this... but, it would be great to understand it physically before trusting our results on  $\sigma_8$  from the SZ power spectrum on large scales



The pressure profiles in Dolag's simulations agree well with those measured by Planck







# Hydrostatic Equilibrium

$$\frac{1}{\rho_{\text{gas}}(r)} \frac{\partial P_{\text{gas}}(r)}{\partial r} = - \frac{GM(< r)}{r^2}$$

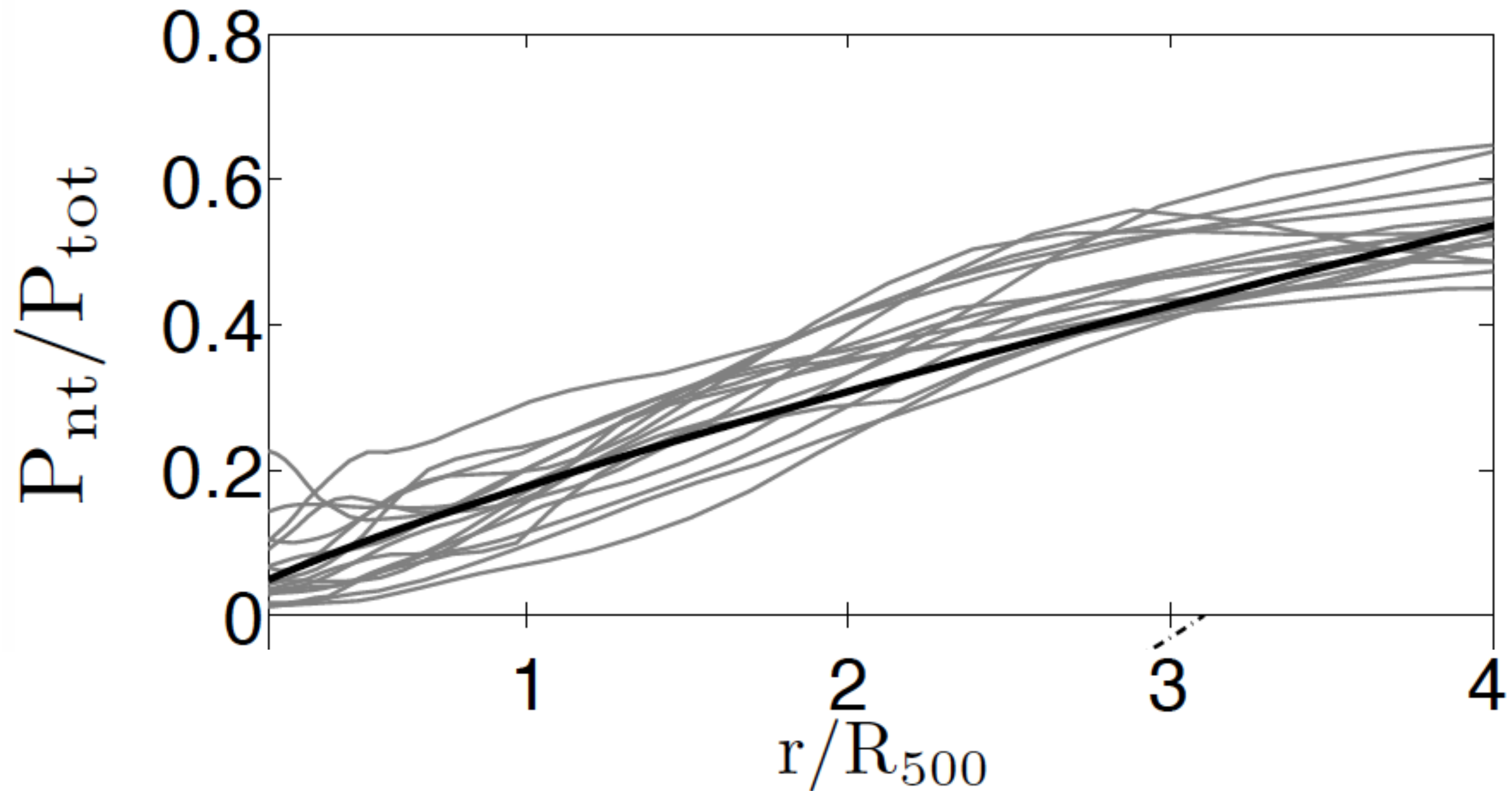
- We now know a lot about the matter distribution in galaxy clusters (i.e., NFW profile)
- **Why can't we just compute the gas pressure by balancing it against gravity of an NFW profile?**
- **We can.** But, **it will give you the total pressure, rather than thermal pressure**

# Non-thermal Pressure

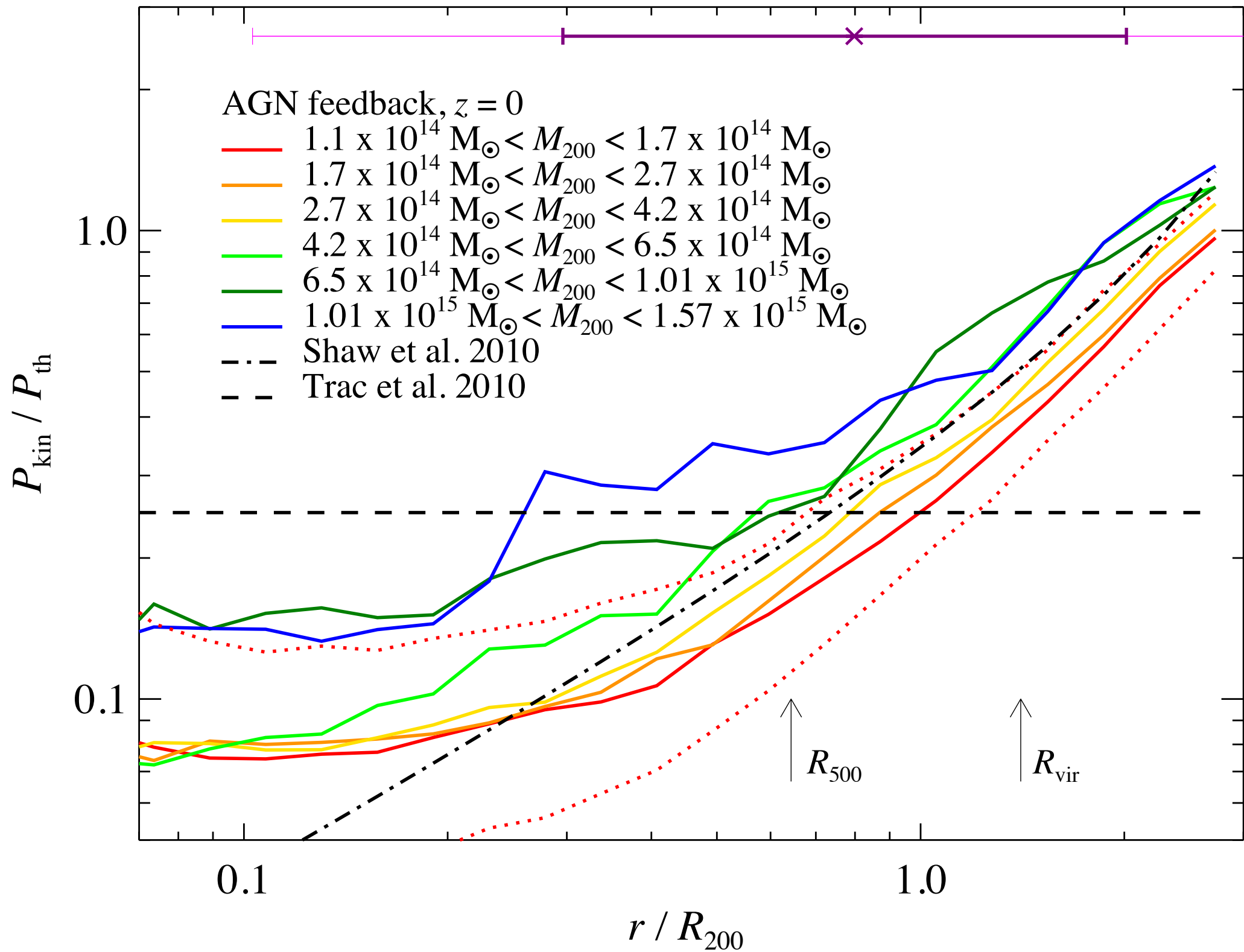
- The HSE equation  $\frac{1}{\rho_{\text{gas}}(r)} \frac{\partial P_{\text{gas}}(r)}{\partial r} = - \frac{GM(< r)}{r^2}$ 
  - includes the total pressure; however, not all kinetic energy of in-falling gas is thermalised
  - There is evidence that there is significant **non-thermal pressure support** coming from bulk motion of gas (e.g., turbulence)
- Therefore, the correct equation to use would be

$$\frac{1}{\rho_{\text{gas}}(r)} \frac{\partial [P_{\text{th}}(r) + P_{\text{non-th}}(r)]}{\partial r} = - \frac{GM(< r)}{r^2}$$



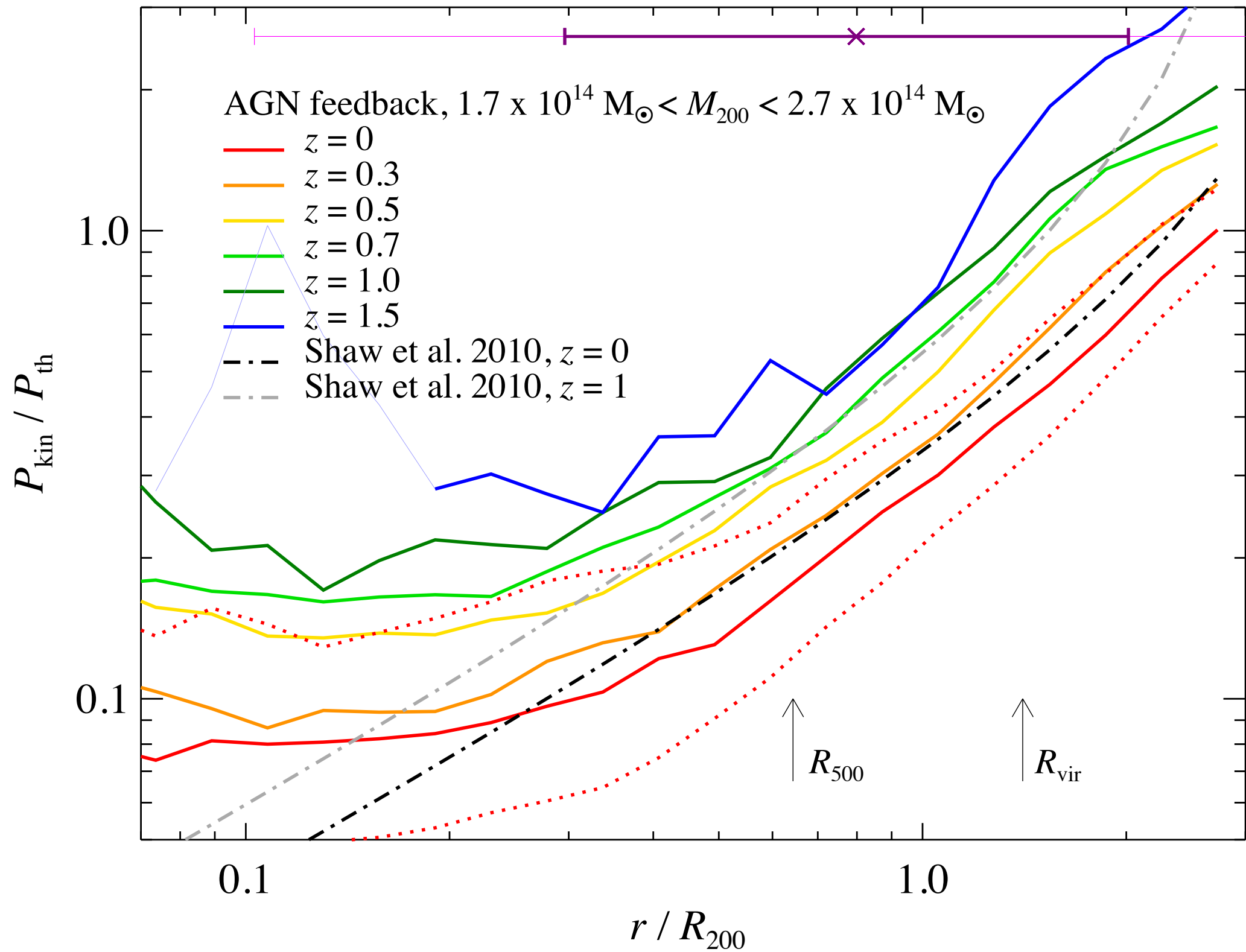


- Simulations by Shaw et al. show that the non-thermal pressure [by bulk motion of gas] divided by the total pressure increases toward large radii. But why?



- Battaglia et al.'s simulations show that the ratio increases for larger masses, and...





- ...increases for larger redshifts. But why?

# Analytical Model for Non-Thermal Pressure

- **Basic idea 1:** non-thermal motion of gas in clusters is sourced by the mass growth of clusters [via mergers and mass accretion] with efficiency  $\eta$
- **Basic idea 2:** induced non-thermal motion decays and thermalises in a dynamical time scale
- Putting these ideas into a differential equation:

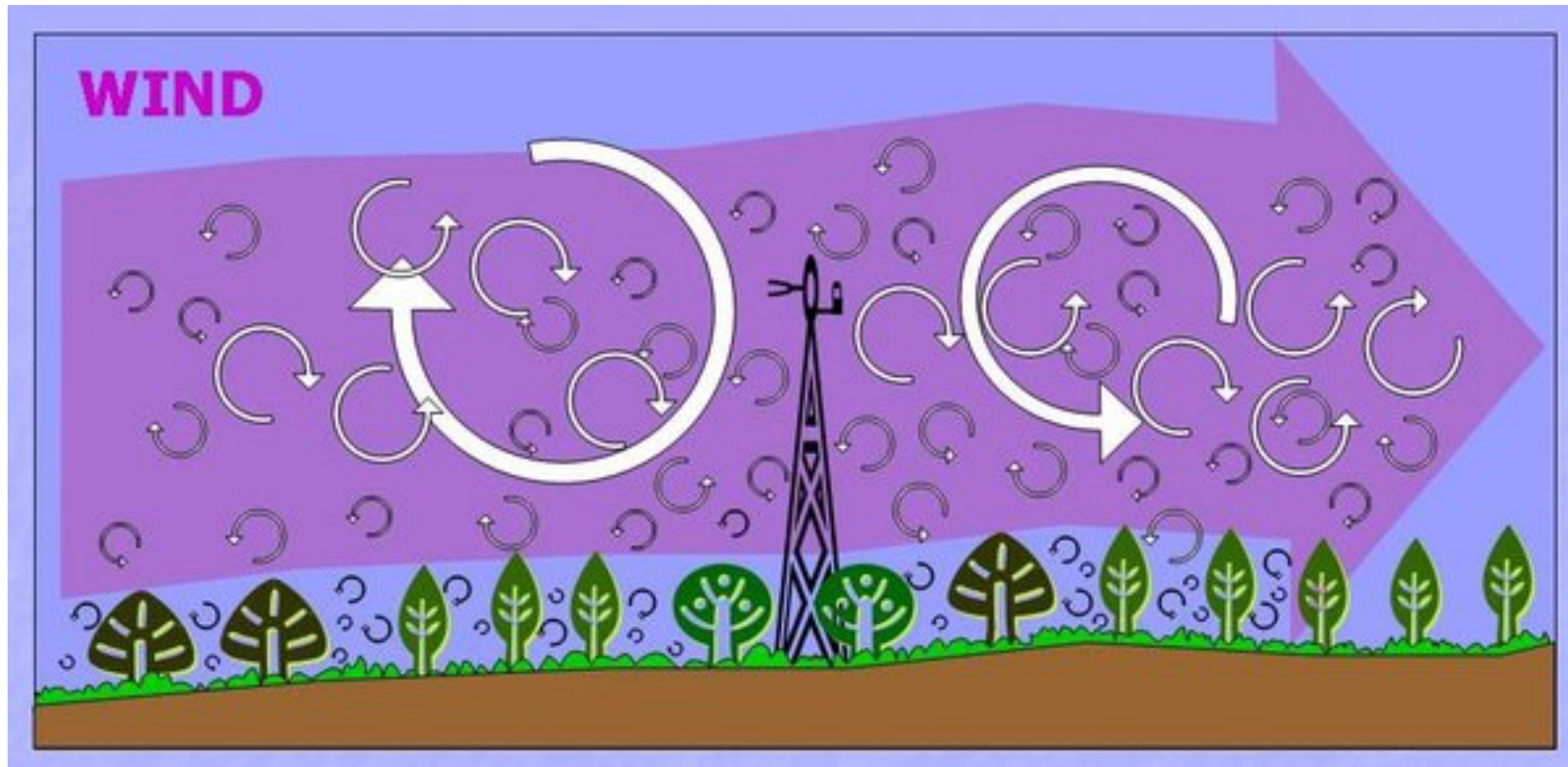
$$\frac{d\sigma_{\text{nth}}^2}{dt} = -\frac{\sigma_{\text{nth}}^2}{t_d} + \eta \frac{d\sigma_{\text{tot}}^2}{dt}$$

$$[\sigma^2 = P/\rho_{\text{gas}}]$$

*Shi & Komatsu (2014)*

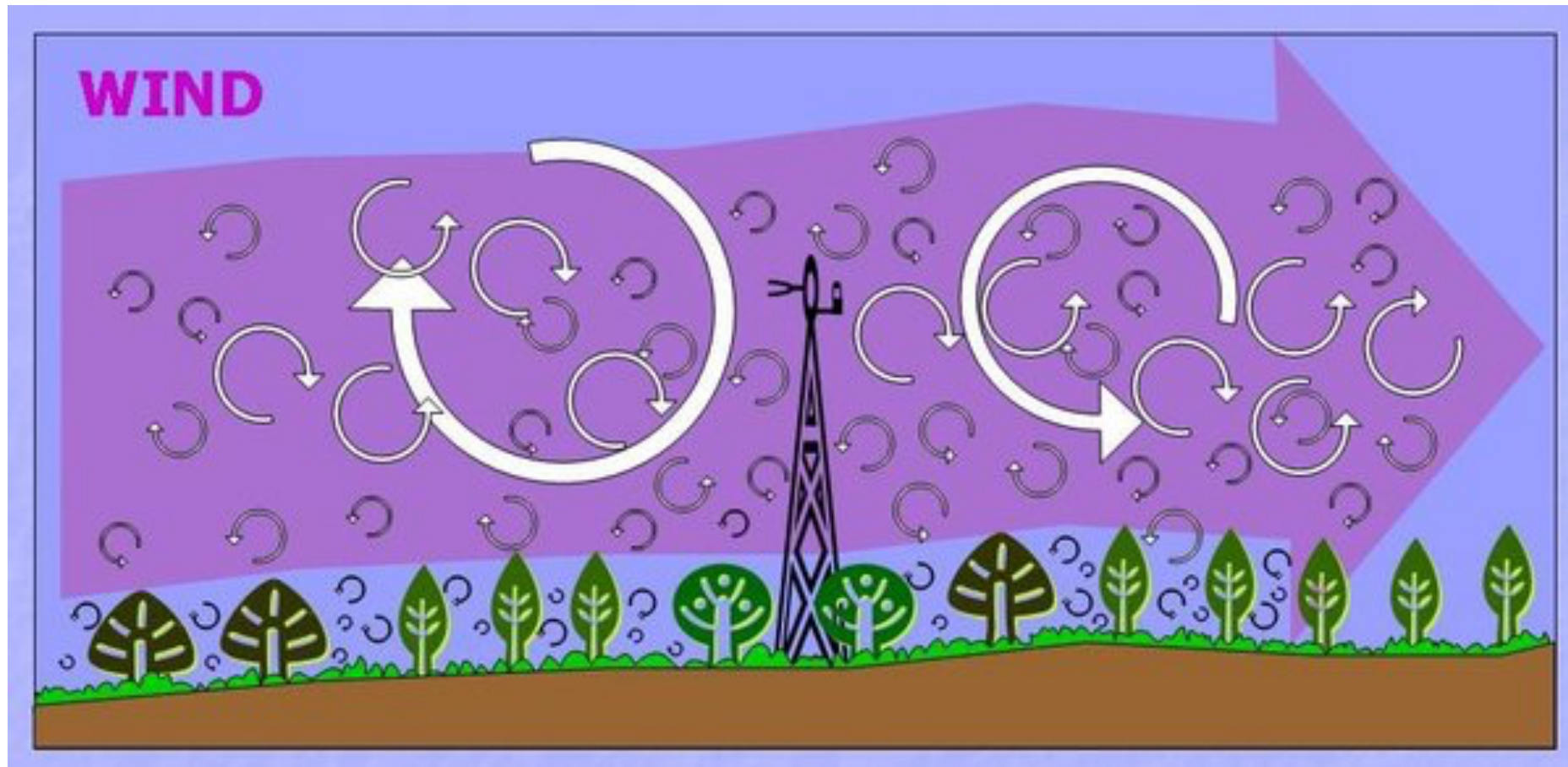


# Finding the decay time, $t_d$



- Think of non-thermal motion as turbulence
- Turbulence consists of “eddies” with different sizes

# Finding the decay time, $t_d$



- Largest eddies carry the largest energy
- Large eddies are unstable. They break up into smaller eddies, and transfer energy from large-scales to small-scales



# Finding the decay time, $t_d$

- Assumption: the size of the largest eddies at a radius  $r$  from the centre of a cluster is proportional to  $r$
- Typical peculiar velocity of turbulence is

$$v(r) = r\Omega(r) = \sqrt{\frac{GM(< r)}{r}}$$

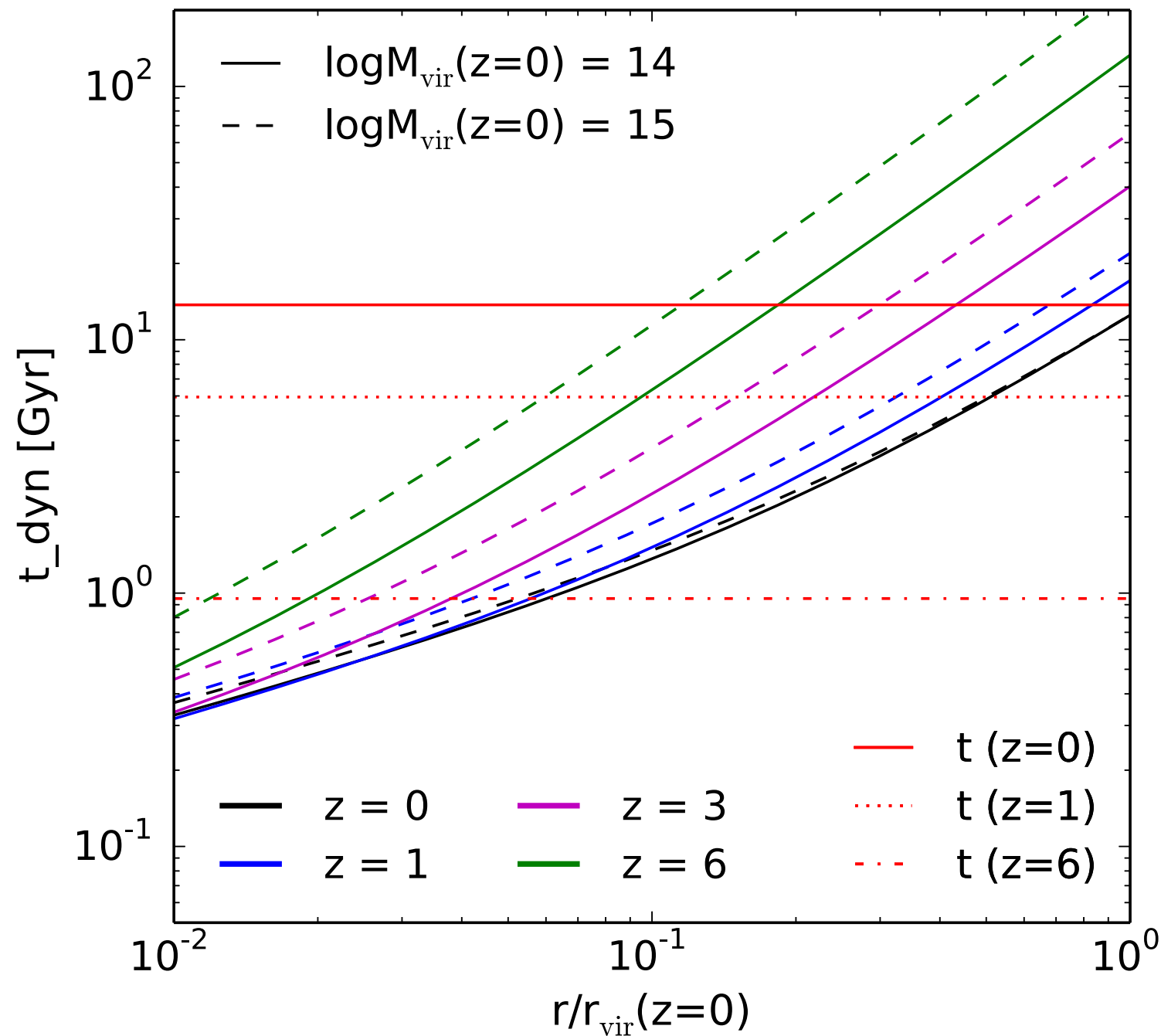
- Breaking up of eddies occurs at the time scale of

$$t_d \approx \frac{2\pi}{\Omega(r)} \equiv t_{\text{dynamical}}$$

- We thus write:

$$t_d \equiv \frac{\beta}{2} t_{\text{dynamical}}$$

# Dynamical Time



- Dynamical time increases toward large radii. **Non-thermal motion decays into heat faster in the inner region**



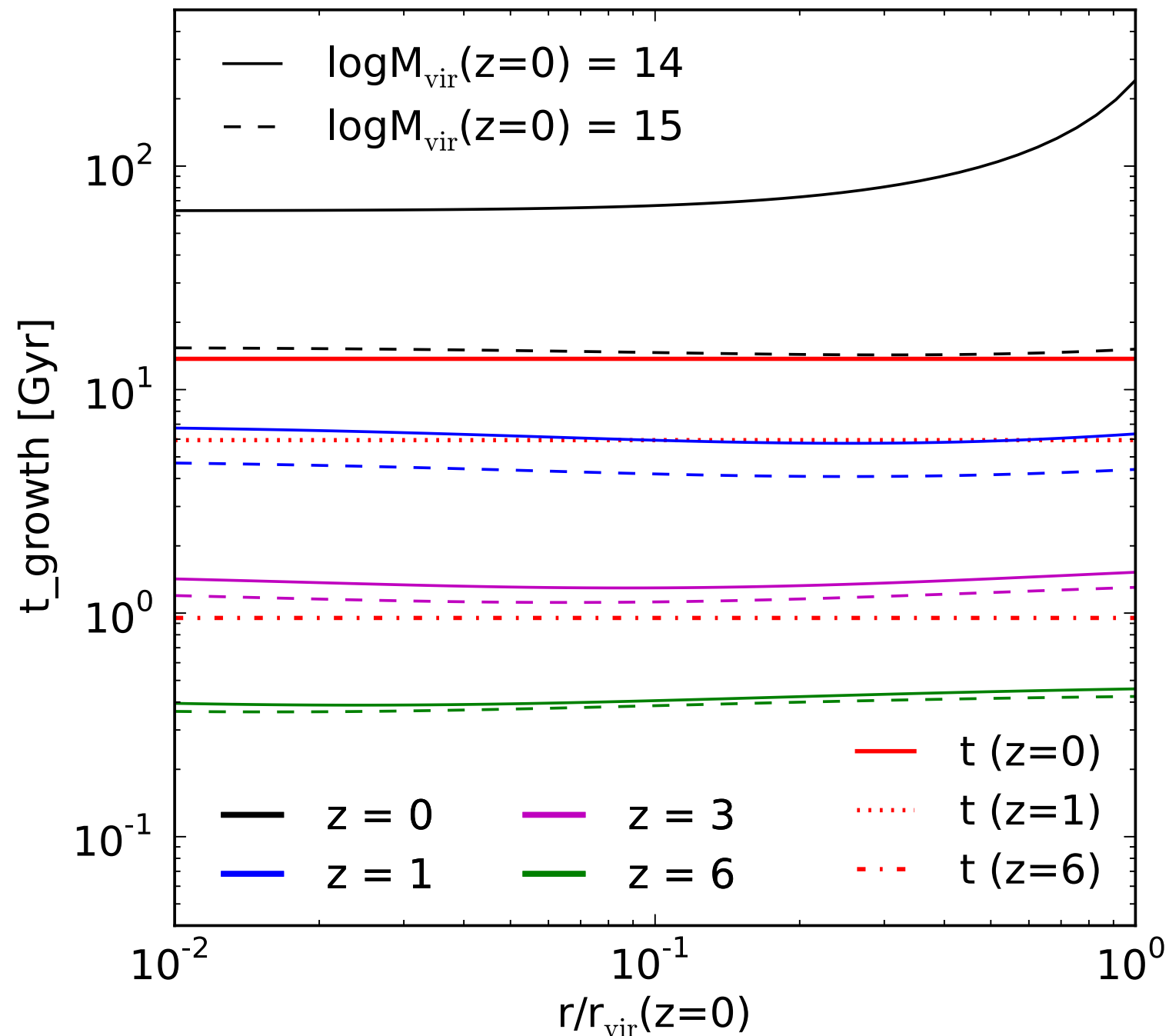
# Source term

$$\frac{d\sigma_{\text{nth}}^2}{dt} = -\frac{\sigma_{\text{nth}}^2}{t_d} + \eta \frac{d\sigma_{\text{tot}}^2}{dt}$$

- Define the “growth time” as

$$t_{\text{growth}} \equiv \sigma_{\text{tot}}^2 \left( \frac{d\sigma_{\text{tot}}^2}{dt} \right)^{-1}$$

# Growth Time

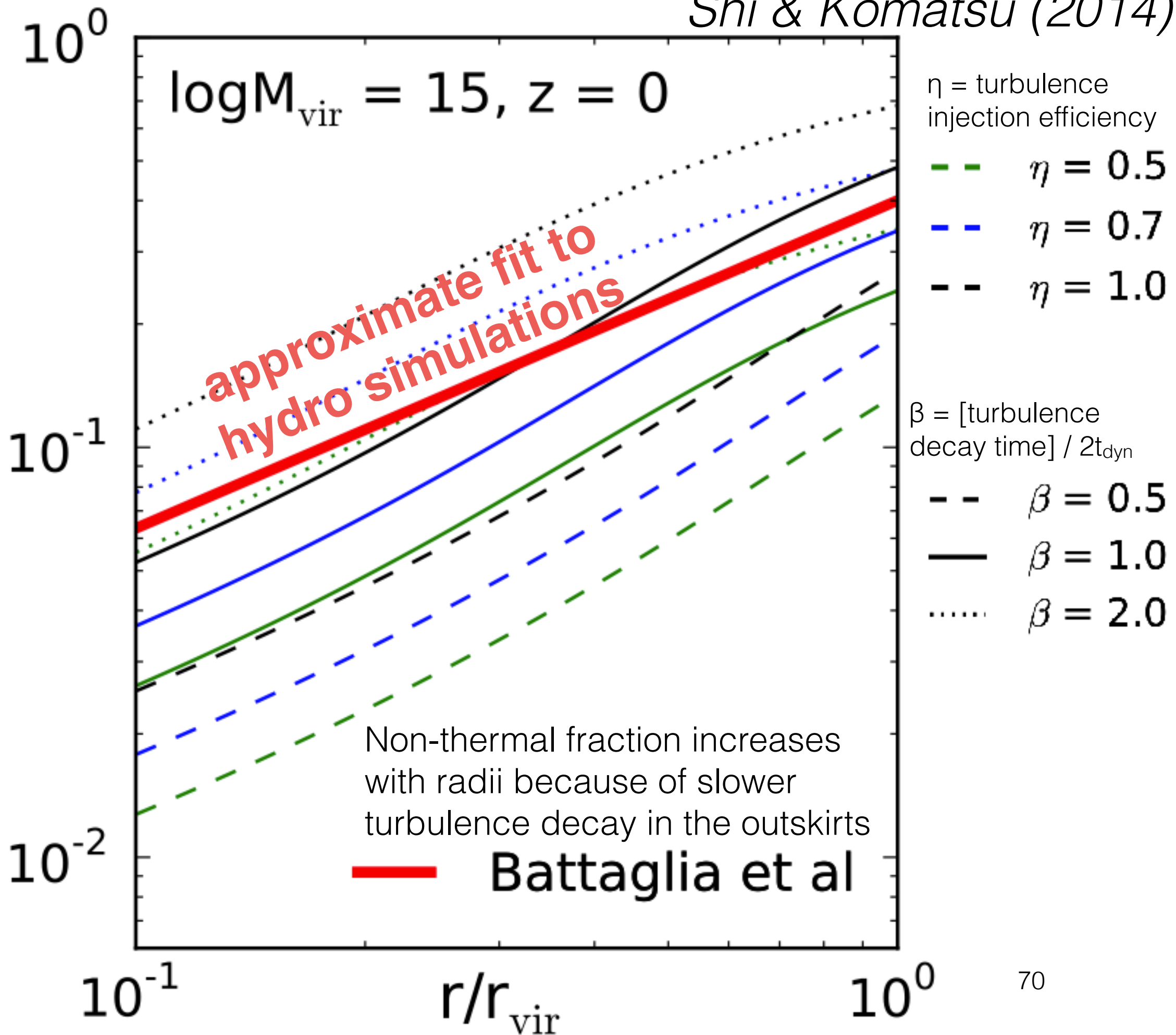


- Growth time increases toward lower redshifts and smaller masses. **Non-thermal motion is injected more efficiently at high redshifts and for large-mass halos**



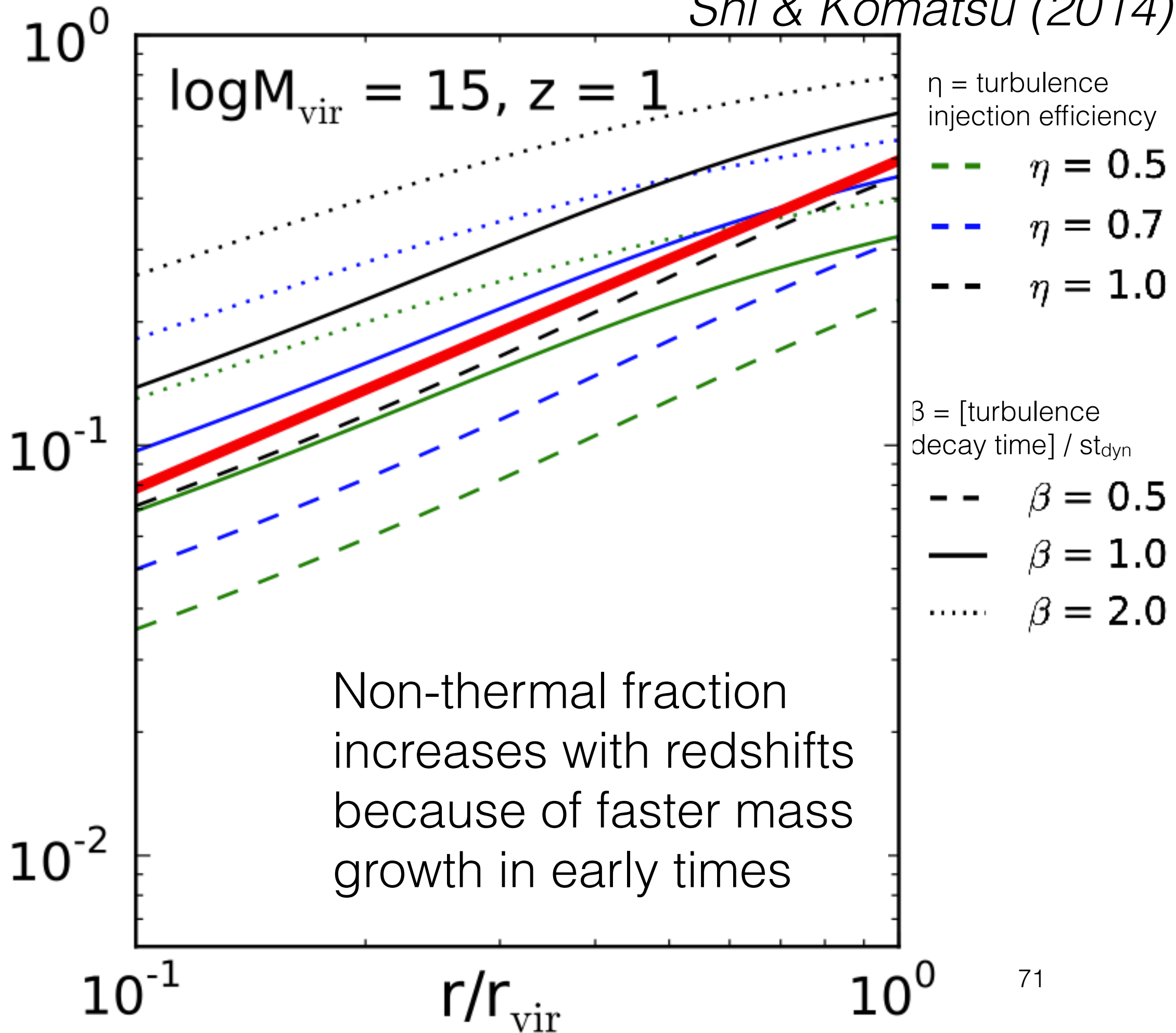
# Non-thermal Fraction, $f_{nth} = P_{nth} / (P_{th} + P_{nth})$

Shi & Komatsu (2014)



# Non-thermal Fraction, $f_{\text{nth}} = P_{\text{nth}} / (P_{\text{th}} + P_{\text{nth}})$

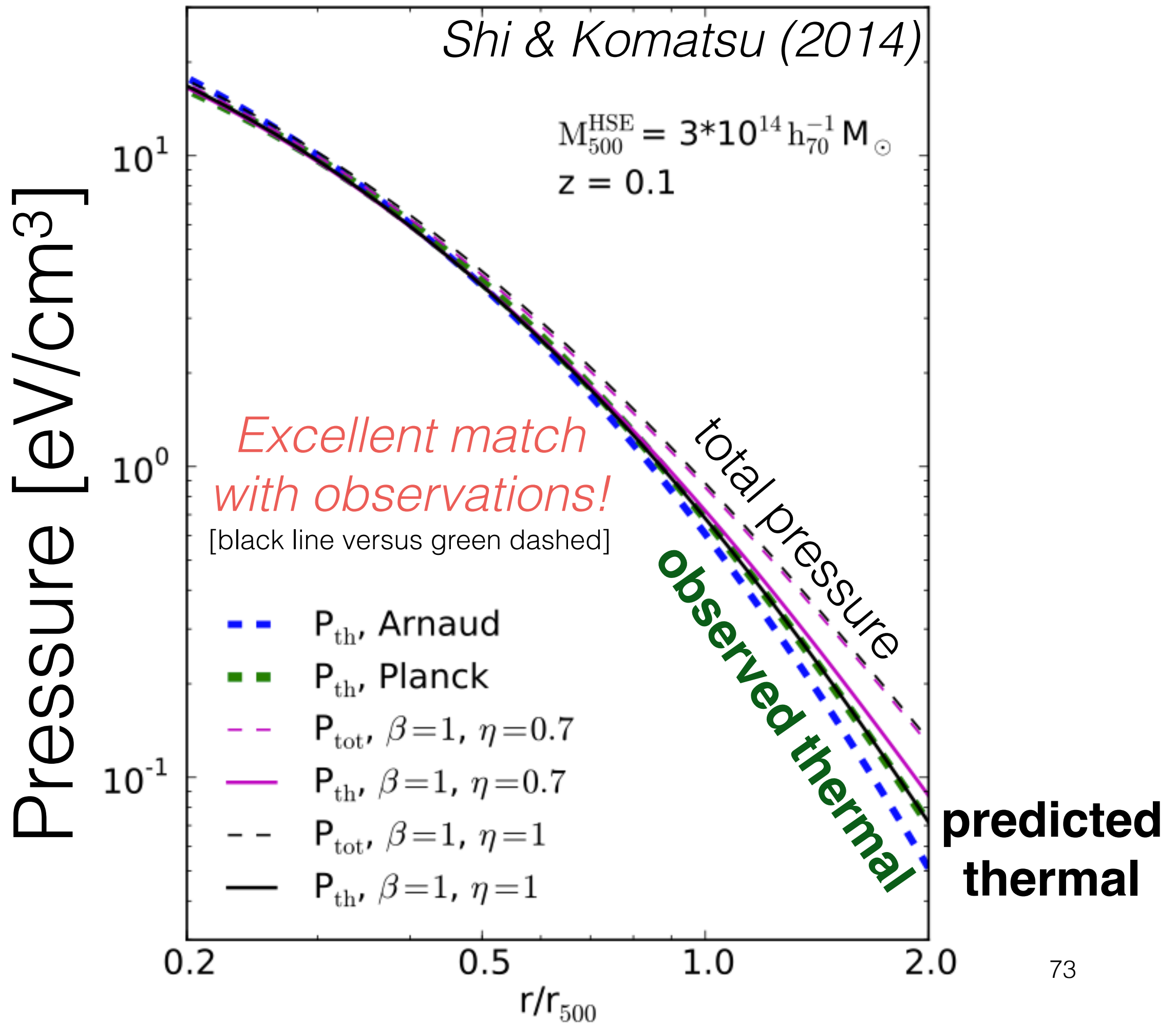
*Shi & Komatsu (2014)*





# With $P_{\text{non-thermal}}$ computed

- We can now predict the X-ray and SZ observables, by subtracting  $P_{\text{non-thermal}}$  from  $P_{\text{total}}$ , which is fixed by the total mass
- We can then predict what the bias in the mass estimation if hydrostatic equilibrium with thermal pressure is used





# Summary

- New results on the SZ effect, *from small to large*:
  1. The first SZ image by ALMA - opening up a new study of cluster astrophysics via pressure fluctuations
  2. The SZ power spectrum at  $l < 1000$  has been determined finally! **Next: to get  $\sigma_8$  out of it**
  3. We now understand, *quantitatively*, the origin and distribution of non-thermal pressure in cluster outskirts



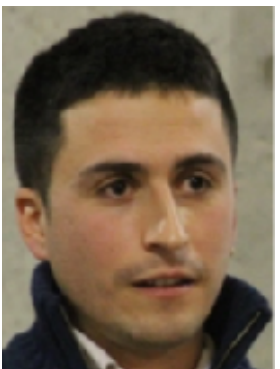
T. Kitayama



K. Dolag



X. Shi



B. Bolliet

# Compton Y Map of RXJ1347–1145

## ALMA



on-source integration times

**5.6 hours** with 7-m array

**2.6 hours** with 12-m array

**Thank you TAC!**

beam



46:00.0

34.0

32.0

13:47:30.0

28.0

100 kpc/h

[ $10^{-4}$ ]



-5

-4

-3

-2

-1

0

1

2

3

4

5

