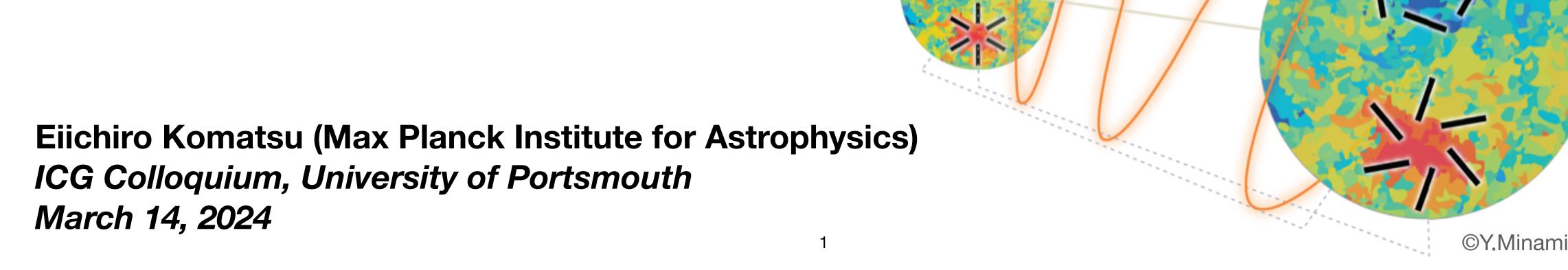
Reference: EK, Nature Rev. Phys. 4, 452 (2022)

$$I_{\text{CS}} = \int d^4x \sqrt{-g} \left(-\frac{\alpha}{4f} \chi F \widetilde{F} \right)$$

$$\frac{1}{\text{MAX-PLANCK-INSTITUT}}$$
FÜR ASTROPHYSIK

Parity Violation in Cosmology

In search of new physics for the Universe



Overarching Theme

Let's find new physics!

- The current cosmological model (*flat \(\Lambda CDM*\)) **requires** new physics beyond the standard model of elementary particles and fields.
 - What is dark matter (CDM)?
 - What is dark energy (/)?
 - Why is the spatial geometry of the Universe Euclidean (flat)?
 - What powered the Big Bang?

Overarching Theme

There are many ideas, but how can we make progress?

- The current cosmological model (*flat \(\Lambda CDM*\)) **requires** new physics beyond the standard model of elementary particles and fields.
 - What is dark matter (CDM)? => CDM, WDM, FDM, ...
 - What is dark energy (/I)? => Dynamical field, modified gravity, quantum gravity, ...
 - Why is the spatial geometry of the Universe Euclidean (flat)? => Inflation, contracting universe, ...
 - What powered the Big Bang? => Scalar field, gauge field, ...

Ove Violation of parity symmetry may hold the answer to these fundamental questions.

- The current cosmological model (*flat \(\Lambda CDM*\)) **requires** new physics beyond the standard model of elementary particles and fields.
 - What is dark matter (CDM)? => CDM, WDM, FDM, ...
 - What is dark energy (/)? => Dynamical field, modified gravity, quantum gravity, ...
 - Why is the spatial geometry of the Universe Euclidean (flat)? => Inflation, contracting universe, ...
 - What powered the Big Bang? => Scalar field, gauge field, ...

Reference: nature reviews physics

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Review Article | Published: 18 May 2022

New physics from the polarized light of the cosmic

microwave background

Eiichiro Komatsu

Key Words:

Cosmic Microwave Background (CMB)

Polarization

Parity Symmetry

Nature Reviews Physics 4, 452-469 (2022) Cite this article

https://wwwmpa.mpa-garching.mpg.de/~komatsu/lectures--reviews.html Lectures & Reviews

2023

- Lecture Slides: "Parity Violation in Cosmology" [7 x 85 min]
 - MC Specialized Course, Department of Physics, Nagoya University (June 6–30)
 - The syllabus is available here.
 - Reference: "New Physics from the Polarized Light of the Cosmic Microwave Background"
 - Nature Reviews Physics, 4, 452-469 (2022 May 18). You can have access to the full text via this link. Supplementary information is available here.
 - Lecture 1: What is parity symmetry? (PDF 3.9 MB; last updated, June 5, 2023)
 - ▶ 1.1 Parity
 - 1.2 Vector and pseudovector
 - 1.3 Discovery of parity violation in β-decay
 - 1.4 Helicity
 - Lecture 2: Chern-Simons interaction (PDF 1.6 MB; last updated, June 8, 2023)
 - 2.1 Parity symmetry in electromagnetism (EM)

Probing Parity Symmetry

Definition

- Parity transformation = Inversion of all spatial coordinates
 - $(x, y, z) \rightarrow (-x, -y, -z)$
- Parity symmetry in physics states:
 - The laws of physics are invariant under inversion of all spatial coordinates.
- Violation of parity symmetry = The laws of physics are <u>not</u> invariant under...
- Ask "When we observe a certain phenomenon in nature, do we also observe its mirror image(*) with equal probability?"
 - (*) "Mirror image" is an ambiguous word. A parity transformation is (x, y, z) -> (-x, -y, -z), whereas a "mirror image" often refers to, e.g., (x, y, z) -> (-x, y, z), where only one of (x,y,z) is flipped.





Parity and Rotation

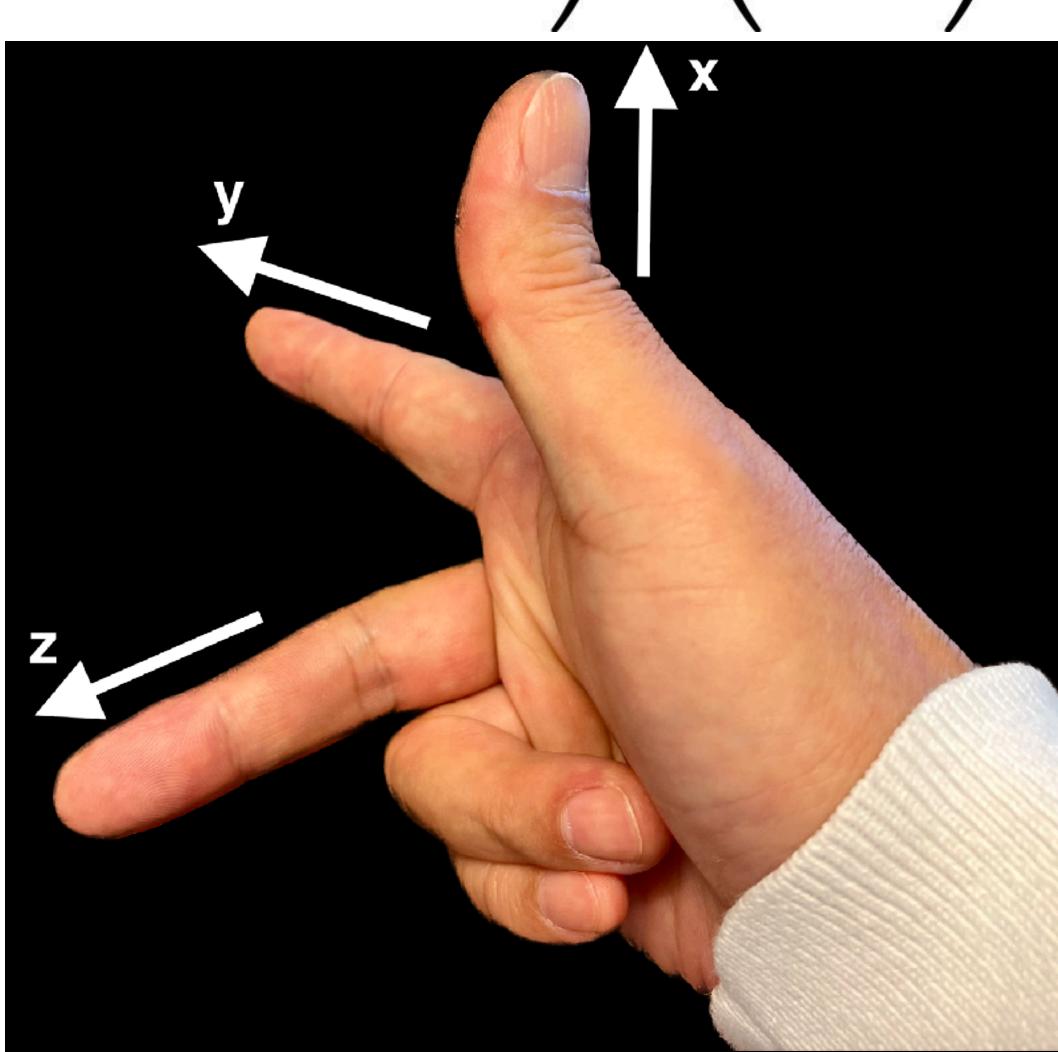
- Parity transformation (x -> -x) and 3d rotation (x -> Rx) are different.
 - R is a continuous transformation and the determinant of R is det(R) = +1.
 - Parity is a discrete transformation and the determinant is -1, as

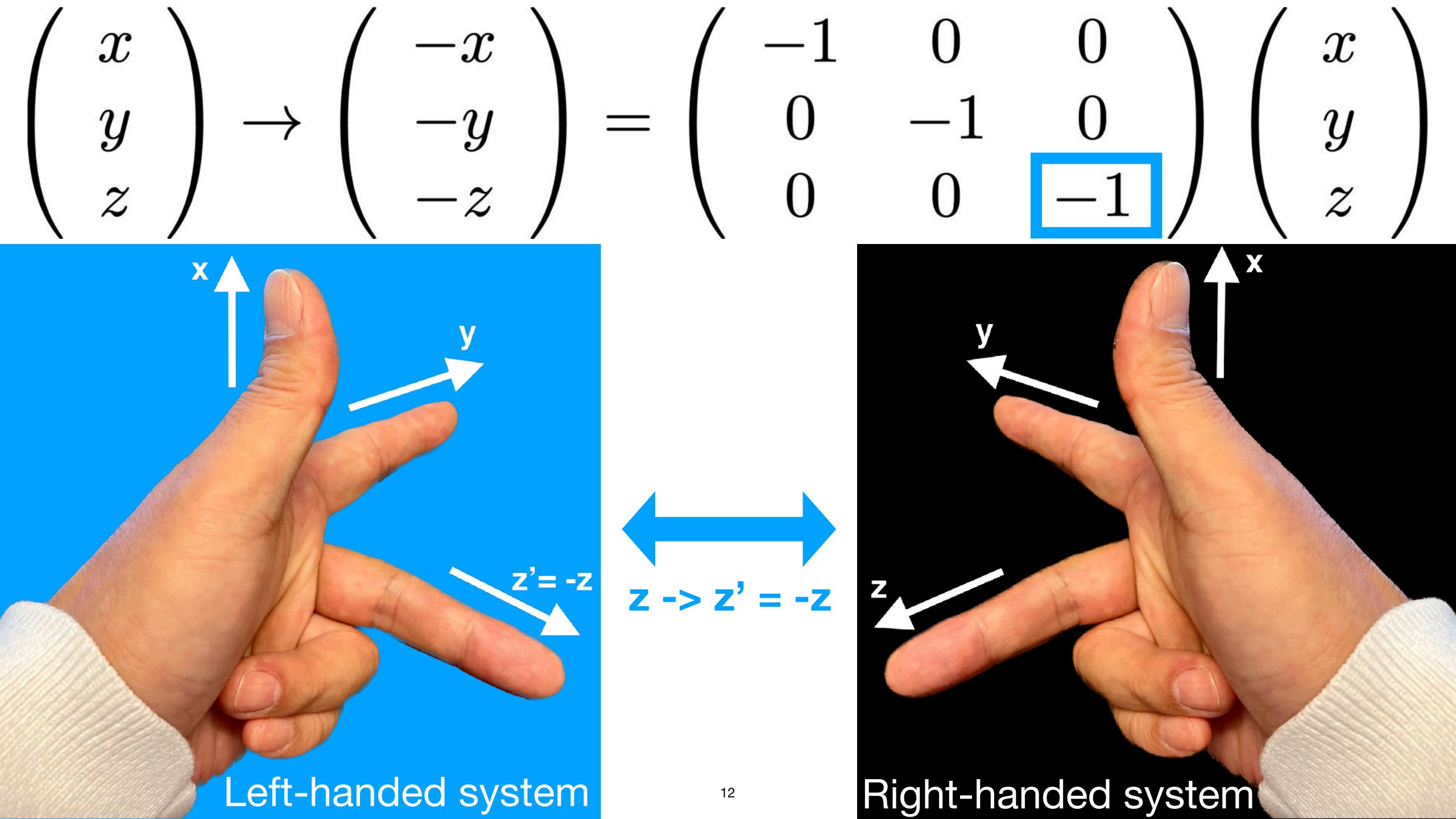
$$\begin{pmatrix} x \\ y \\ z \end{pmatrix} \rightarrow \begin{pmatrix} -x \\ -y \\ -z \end{pmatrix} = \begin{pmatrix} -1 & 0 & 0 \\ 0 & -1 & 0 \\ 0 & 0 & -1 \end{pmatrix} \begin{pmatrix} x \\ y \\ z \end{pmatrix}$$

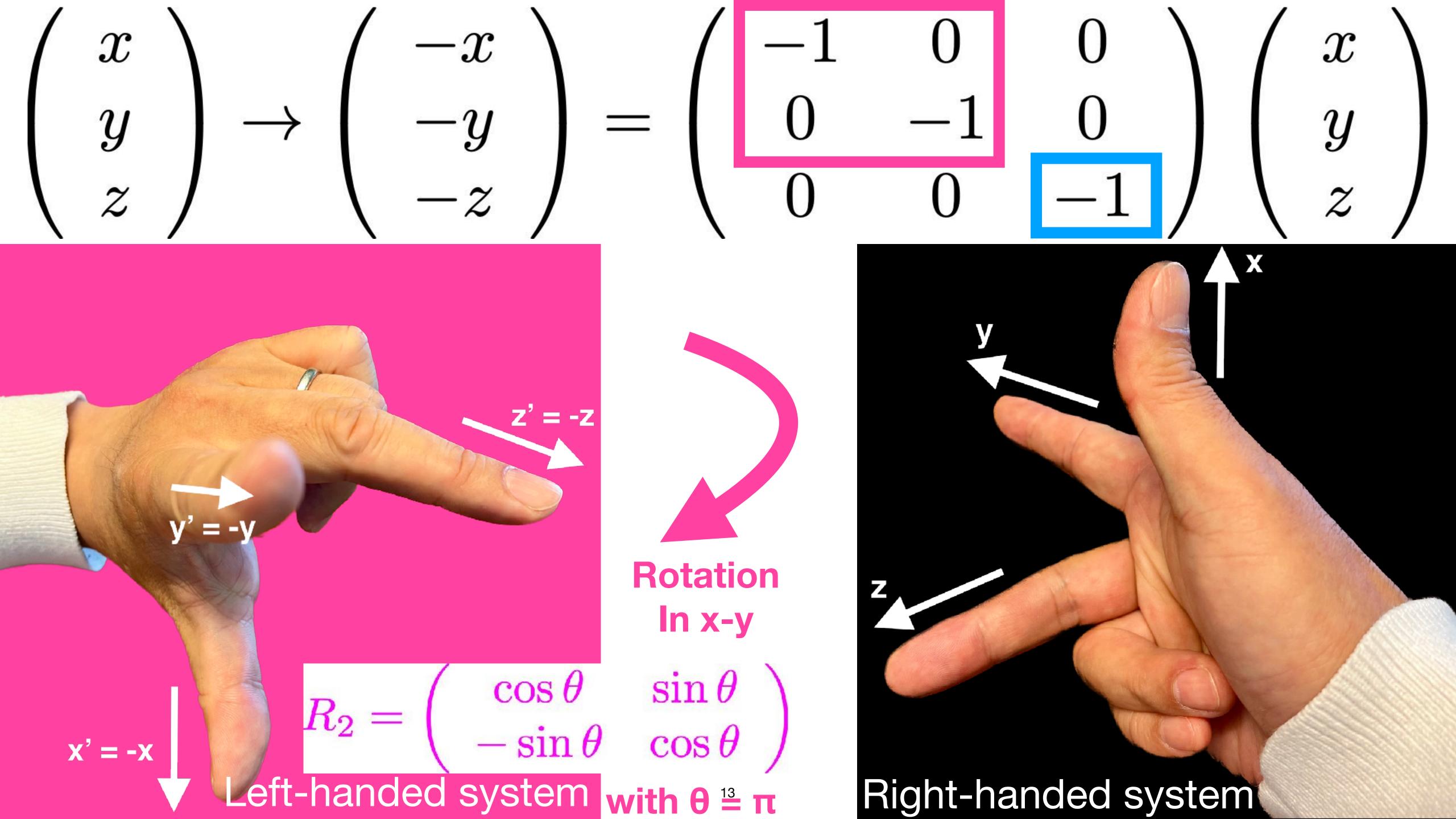
$$\begin{pmatrix} x \\ y \\ z \end{pmatrix} \rightarrow \begin{pmatrix} -x \\ -y \\ -z \end{pmatrix} = \begin{pmatrix} -1 & 0 & 0 \\ 0 & -1 & 0 \\ 0 & 0 & -1 \end{pmatrix} \begin{pmatrix} x \\ y \\ z \end{pmatrix}$$

Parity = Mirror + 2d Rotation

- One may think of parity transformation as a mirror in one of the coordinates (e.g., $z \rightarrow -z$) and 2d rotation by π in the others.
- Let's demonstrate it!

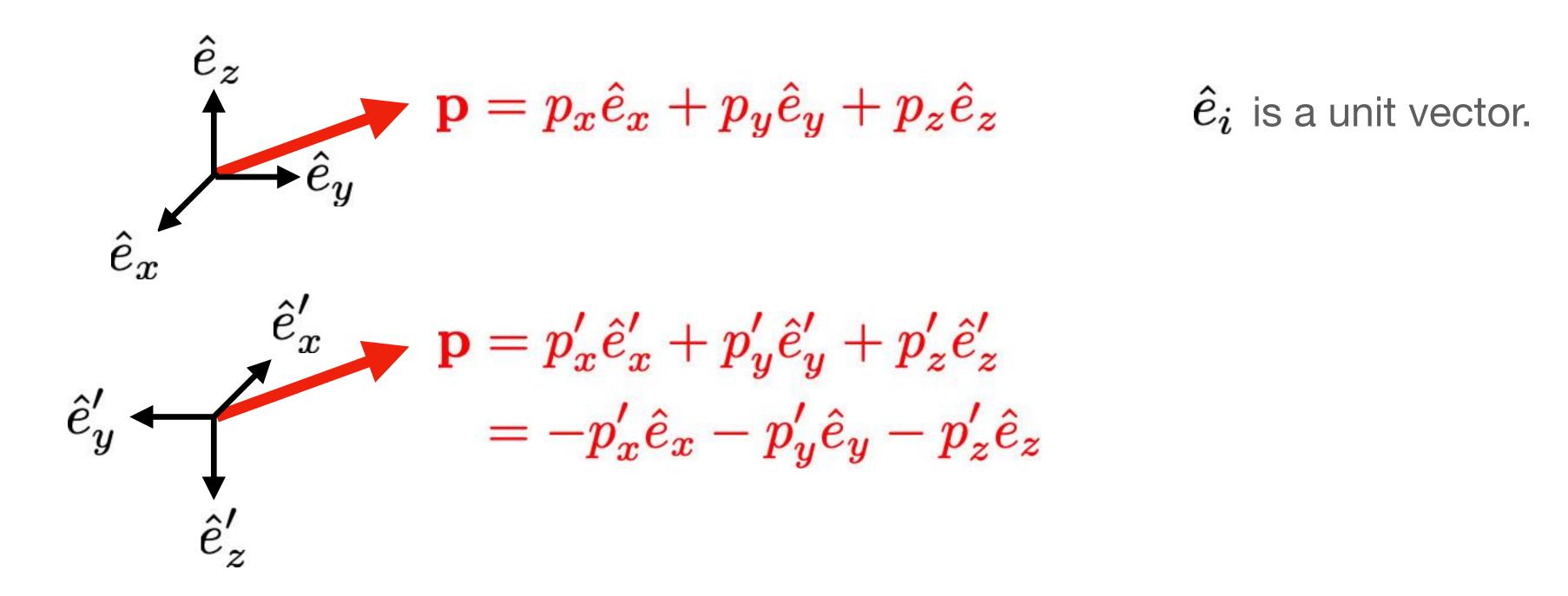






Parity Transformation: Vector

E.g., momentum, electric field

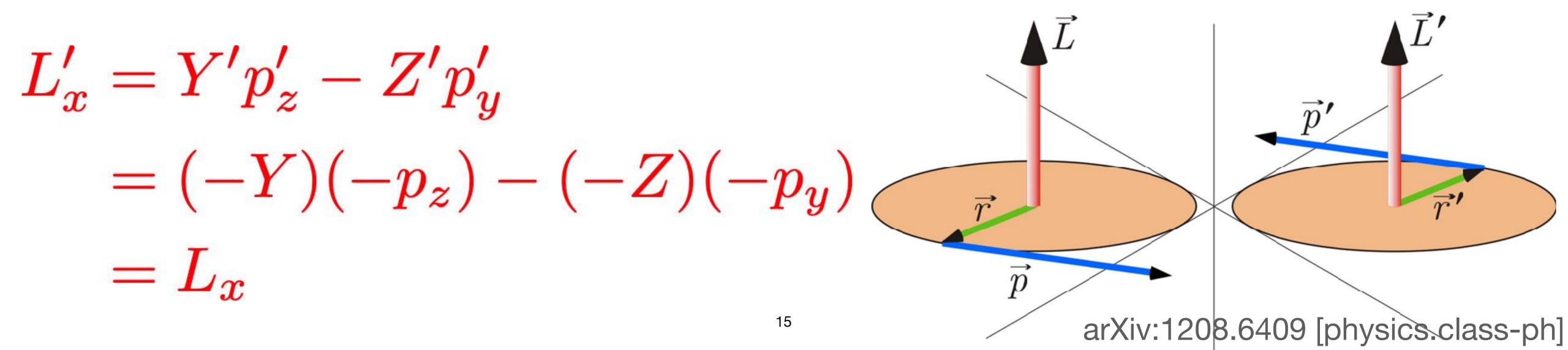


- p is the same vector, written using two different basis vectors.
- Therefore, **p**'s components are transformed as $(p'_x, p'_y, p'_z) = (-p_x, -p_y, -p_z)$

Parity Transformation: Pseudovector

E.g., angular momentum, magnetic field

- Orbital angular momentum, $\mathbf{L} = \mathbf{r} \times \mathbf{p}$, is a pseudovector. Its components do not change under parity transformation: $(L_x', L_y', L_z') = (L_x, L_y, L_z)$
 - Both $\mathbf{r} = (X, Y, Z)$ and $\mathbf{p} = (p_x, p_y, p_z)$ are vectors whose components change sign. Thus, their products do not change, e.g.,



Parity Transformation: Pseudoscalar How to test parity symmetry?

- A dot product of a vector and a pseudovector is a pseudoscalar.
 - Like a scalar, a pseudoscalar is invariant under rotation.
 - But, a pseudoscalar changes sign under parity transformation.
- Experimental test of parity symmetry: Construct a pseudoscalar and see if the average value is zero. If not, the system violates parity symmetry!
 - Example: a dot product of particle A's momentum and particle B's angular momentum: $\mathbf{p}_A \cdot \mathbf{L}_B$. Measure this and average over many trials. Does the average vanish, $\langle \mathbf{p}_A \cdot \mathbf{L}_B \rangle = 0$?

Experimental Test of Parity Conservation in Beta Decay*

C. S. Wu, Columbia University, New York, New York

AND

E. Ambler, R. W. Hayward, D. D. Hoppes, and R. P. Hudson, National Bureau of Standards, Washington, D. C. (Received January 15, 1957)

TN a recent paper on the question of parity in weak interactions, Lee and Yang critically surveyed the experimental information concerning this question and reached the conclusion that there is no existing evidence either to support or to refute parity conservation in weak interactions. They proposed a number of experiments on beta decays and hyperon and meson decays which would provide the necessary evidence for parity conservation or nonconservation. In beta decay, one could measure the angular distribution of the electrons coming from beta decays of polarized nuclei. If an asymmetry in the



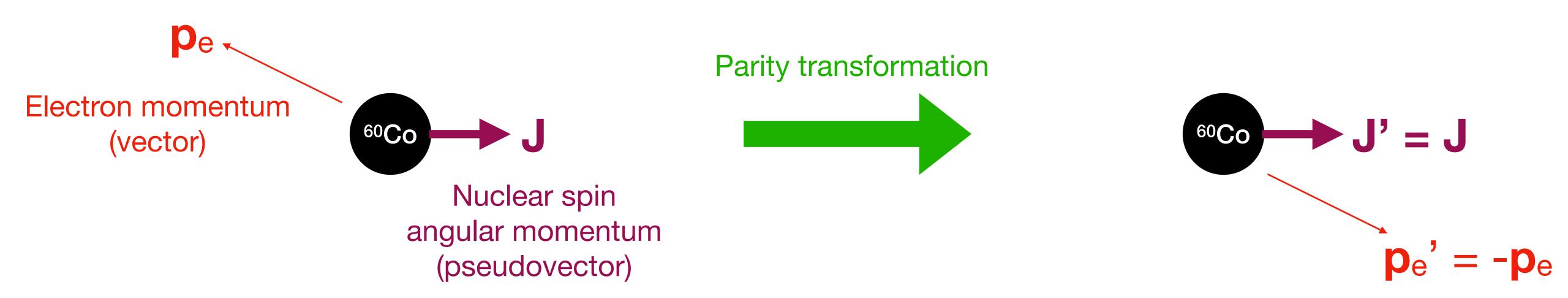
Chien-Shiung Wu



Chen-Ning Yang Tsung-Dao Lee

The Wu Experiment of B-decay

 60 Co -> 60 Ni + e⁻ + $\overline{\nu}_e$ + 2 Y



- Electrons must be emitted with equal probability in all directions relative to J, if parity symmetry is respected in β-decay.
 - This was not observed: $\langle \mathbf{p}_e \cdot \mathbf{J} \rangle \neq 0$. Parity symmetry is violated in β -decay!

Initial reaction

Many physicists did not believe it initially.

- To Lee and Yang's theoretical paper on parity violation in β-decay:
 - Wolfgang Pauli said, "Ich glaube aber nicht, daß der Herrgott ein schwacher Linkshänder ist" (I do not believe that the Lord is a weak left-hander).
- To Wu's discovery paper:
 - Wolfgang Pauli said, "Sehr aufregend. Wie sicher ist die Nachricht?" (Very exciting. How sure is this news?)
- This was shocking news. The weak interaction distinguishes between left and right!
- In this talk we ask, "Does the Universe distinguish between left and right?" Most scientists answer, "No, of course it doesn't". That may well be true, but one must at least have a look to be sure!

ildarchiv der ETH-Bibliothek

Helicity is a pseudoscalar

Party transformation changes "right-handed" to "left-handed" and vice versa

• For massless particles, we define the "helicity", λ , as

$$\mathbf{S} \cdot rac{\mathbf{p}}{|\mathbf{p}|} = \lambda \hbar$$

• For a photon, $\lambda=\pm 1$. S'=S

Parity transformation

Right-handed $\lambda=\pm 1$ Left-handed $\lambda=\pm 1$

- λ is a pseudoscalar because it is a product of a momentum vector (p) and a spin pseudovector (S).
 - On the other hand, "scalar", such as p^2 and S^2 , does not change sign.
- For a graviton, $\lambda = \pm 2$.
- Asymmetry between λ=±1 and ±2 is the sign of parity violation!

Parity Violation in Electromagnetism with

$$I_{\text{CS}} = \int d^4x \sqrt{-g} \left(-\frac{\alpha}{4f} \chi F \widetilde{F} \right)$$

Throughout this talk, I will assume homogeneity and isotropy of space (invariance under 3d translation and rotation).

Maxwell's Equations

In Minkowski space, Heaviside units and c=1

$$abla \cdot \mathbf{E} = \rho, \quad -\dot{\mathbf{E}} + \nabla \times \mathbf{B} = \mathbf{j}$$

$$abla \cdot \mathbf{B} = 0, \quad \dot{\mathbf{B}} + \nabla \times \mathbf{E} = 0$$

 These equations are invariant under Poincaré transformation (spatial translation and rotation and Lorentz boost).

Parity-flipping Maxwell's Equations

In Minkowski space, Heaviside units and c=1

$$(-\nabla) \cdot (-\mathbf{E}) = \rho, \quad -(-\dot{\mathbf{E}}) + (-\nabla) \times \mathbf{B} = (-\mathbf{j})$$

 $(-\nabla) \cdot \mathbf{B} = 0, \quad \dot{\mathbf{B}} + (-\nabla) \times (-\mathbf{E}) = 0$

- These equations are invariant under Poincaré transformation (spatial translation and rotation and Lorentz boost).
- They are also invariant under parity transformation, if E and j are vectors, ρ is a scalar, and B is a pseudovector.

Maxwell's Equations in a covariant form

$$\nabla \cdot \mathbf{E} = \rho$$
, $-\dot{\mathbf{E}} + \nabla \times \mathbf{B} = \mathbf{j}$

$$\nabla \cdot \mathbf{B} = 0, \quad \dot{\mathbf{B}} + \nabla \times \mathbf{E} = 0$$

• These equations can be written in a covariant form as

$$\partial_{\nu}F^{\mu\nu}=j^{\mu}$$

$$\partial_{\nu} \tilde{F}^{\mu\nu} = 0$$

Dual tensor

$$\mu=0,1,2,3\,,\quad j^\mu=(\rho,\mathbf{j})\,,\quad \partial_\mu=\partial/\partial x^\mu\,,\quad x^\mu=(t,\mathbf{x})$$

Antisymmetric Field Strength Tensor, $F_{\mu\nu}$

$$F_{\mu\nu} = -F_{\nu\mu}$$

$$F_{\mu\nu}=\eta_{\mulpha}\eta_{
ueta}F^{lphaeta}$$
 where $\eta_{\mulpha}=\mathrm{diag}(-1,1,1,1)$

$$F_{\mu\nu} = \begin{pmatrix} 0 & -E_x & -E_y & -E_z \\ E_x & 0 & B_z & -B_y \\ E_y & -B_z & 0 & B_x \\ E_z & B_y & -B_x & 0 \end{pmatrix} \qquad \begin{array}{c} \bullet \text{ Equivalently,} \\ F^{0i} = E_i \\ F^{ij} = \epsilon^{ijk} B_k \\ \end{array}$$

Therefore,

$$F^2 \equiv F_{\mu\nu}F^{\mu\nu} = 2(\mathbf{B} \cdot \mathbf{B} - \mathbf{E} \cdot \mathbf{E})$$

This is a *scalar* and is invariant under parity transformation.

Dual Field Strength Tensor, F^µ

$$\widetilde{F}^{\mu\nu} = -\widetilde{F}^{\nu\mu}$$

$$ilde{F}^{\mu
u} = -F^{\nu \mu}$$
 of (0,1,2,3) $ilde{F}^{\mu
u} = rac{1}{2} \epsilon^{\mu
u lpha eta} F_{lpha eta} \quad ext{where} \quad \epsilon^{\mu
u lpha eta} = \left\{ egin{array}{ll} +1 & ext{of (0,1,2,3)} \\ -1 & ext{if (μ, ν, α, β) is odd perm.} \\ & ext{of (0,1,2,3)} \\ 0 & ext{otherwise} \end{array}
ight.$

$$\begin{array}{c} +1 & \text{of } (0,1,2,3) \\ -1 & \text{if } (\mu,\nu,\alpha,\beta) \text{ is odd perm.} \\ 0 & \text{of } (0,1,2,3) \\ \end{array}$$

$$\tilde{F}^{\mu\nu} = \begin{pmatrix} 0 & B_x & B_y & B_z \\ -B_x & 0 & -E_z & E_y \\ -B_y & E_z & 0 & -E_x \\ -B_z & -E_y & E_x & 0 \end{pmatrix}$$

Equivalently,

$$ilde{F}^{0i} = B_i$$

$$ilde{F}^{ij} = -\epsilon^{ijk} E_k$$

Therefore,

$$F\tilde{F} \equiv F_{\mu\nu}\tilde{F}^{\mu\nu} = -4\mathbf{B} \cdot \mathbf{E}$$

This is a pseudoscalar and changes sign under parity transformation!

FF in the action?
$$F^2 \equiv F_{\mu\nu}F^{\mu\nu} = 2(\mathbf{B}\cdot\mathbf{B} - \mathbf{E}\cdot\mathbf{E}) \\ F\tilde{F} \equiv F_{\mu\nu}\tilde{F}^{\mu\nu} = -4\mathbf{B}\cdot\mathbf{E}$$

$$I = -\frac{1}{4} \int d^4x \ F^2 + \int d^4x \ A_{\mu} j^{\mu}$$

 $d^4x = dtd^3\mathbf{x}$

- This action is sufficient to produce all of Maxwell's equations.
- Can we add $\int d^4x \ F ilde{F}$ to the action?
 - The answer is yes. However, this is only a surface term, since FF is a total

derivative:
$$F_{\mu\nu}\tilde F^{\mu\nu}=2\partial_\mu(A_
u\tilde F^{\mu
u})$$
 where $F_{\mu\nu}=\partial_\mu A_
u-\partial_
u A_\mu$

Ni (1977); Turner, Widrow (1987); Carroll, Field, Jackiw (1990)

FF in the action

Chern-Simons term

• Consider
$$I_{\mathrm{CS}}=-rac{1}{4}lpha\int d^4x\; heta F ilde F$$
 with $F ilde F=2\partial_\mu(A_
u ilde F^{\mu
u})$

- α: a dimensionless constant
- θ : a dimensionless pseudoscalar field
- This is not a surface term! Integration by parts gives

$$I_{\rm CS} = \frac{1}{2} \alpha \int d^4 x \; (\partial_{\mu} \theta) A_{\nu} \tilde{F}^{\mu\nu}$$



https://einstein-chair.github.io/simons2023/

- This is a special case of the so-called *Chern-Simons term*, $p_{\mu}A_{\nu}\tilde{F}^{\mu\nu}$

with
$$p_{\mu}=\partial_{\mu} heta$$

Adler (1969); Bell, Jackiw (1969); Fujikawa (1979)

Is there a known example of this term in particle physics?

Yes, a pion. The ABJ anomaly!

Credit: HiggsTar

- A pion is a composite meson composed of a quark and an antiquark.
 - A neutral pion, π^0 , is composed of either $u\bar{u}$ or $d\bar{d}$, and is a pseudoscalar.

(Chinowsky & Steinberger, 1954)

- π⁰ is coupled to photons via l_{CS} where
 - $\theta = \pi^0 / f_{\pi}$ with $f_{\pi} \sim 184$ MeV (pion decay constant)
 - $\alpha = 2\alpha_{EM}N_c/(3\pi)$ with $N_c = 3$ (the number of quark colors) and $\alpha_{EM} \sim 1/137$ (EM fine structure constant)
- π⁰ decays into 2 photons via this term, which has been observed. So, this
 possibility is not completely crazy!

Consistency with gauge invariance

p_μ cannot be arbitrary

$$I_{\rm CS} = \frac{1}{2} \alpha \int d^4 x \ p_{\mu} A_{\nu} \tilde{F}^{\mu\nu}$$

- This action is invariant under the gauge transformation, $A_
 u o A_
 u + \partial_
 u f$
 - if $\partial_{\nu}p_{\mu}-\partial_{\mu}p_{\nu}=0$ Hint: Use integration by parts and the identity
- For example: This implies the presence of a preferred direction in spacetime and violation of Lorentz invariance! $\partial_{\nu} F^{\mu\nu} = 0$
 - p_{μ} is a constant vector and not dynamical, or
 - p_{μ} is a gradient of a dynamical (pseudo)scalar field, such as $p_{\mu} = \partial_{\mu}\theta$.

But see Zhou, Huang, Geng (2023) for a possible way around this in new physics.

The main goal of this talk

Let's find new physics!

We study the cosmological consequence of

$$I_{\rm CS} = -\frac{1}{4}\alpha \int d^4x \; \theta F \tilde{F}$$

- Specifically, we ask if θ is
 - responsible for dark matter and dark energy, or
 - active during cosmic inflation.

The main goal of this talk Let's find new physics!

We study the cosmological consequence of

$$I_{\rm CS} = -\frac{1}{4}\alpha \int d^4x \; \theta F \tilde{F}$$

- Specifically, we ask if θ is
 - · responsible for dark matter and dark energy, or
 - active during cosmic inflation.

More examples:

 Non-Abelian gauge fields [Maleknejad, Sheikh-Jabbari, Soda, Phys. Rept. 528, 161 (2013)]

$$F ilde{F} = F^a_{\mu
u} ilde{F}^{\mu
u a}$$
 $F^a_{\mu
u} = \partial_\mu A^a_
u - \partial_
u A^a_
u + g_A \epsilon^{abc} A^b_
u A^c_
u$

Gravitational CS
 [Alexander, Yunes, Phys. Rept. 480, 1 (2009)]

$$R\tilde{R} = R^{\beta}{}_{\alpha}{}^{\mu\nu}\tilde{R}^{\alpha}{}_{\beta\mu\nu}$$

You can have both!

Mirzagholi, EK, Lozanov, Watanabe (2020)

Correction to Maxwell's equations

In Minkowski space, Heaviside units and c=1

We now derive the correction to Maxwell's equations from

$$d^4x = dtd^3\mathbf{x}$$

• We now derive the correction to Maxwell's equations from
$$I=-\frac{1}{4}\int d^4x \ \left(F^2+\alpha\theta F\tilde{F}\right)+\int d^4x \ A_\mu j^\mu$$

Finding the path that gives a stationary point,

$$\partial_{\nu}F^{\mu\nu} + \alpha(\partial_{\nu}\theta)\tilde{F}^{\mu\nu} = j^{\mu}$$

As expected, only the space-time dependence of the θ field affects Maxwell's equation.

Correction to the EM wave equation in vacuum

With the Chern-Simons term

$$\partial_{\nu}F^{\mu\nu} + \alpha(\partial_{\nu}\theta)\tilde{F}^{\mu\nu} = 0$$
 where $F_{\mu\nu} = \partial_{\mu}A_{\nu} - \partial_{\nu}A_{\mu}$

• With $A^0 = \phi = 0$ in the Lorenz gauge, we find

$$-\Box A^{i} + \alpha(\partial_{\nu}\theta)\tilde{F}^{i\nu} = 0$$

$$egin{align} \Box &= \eta^{lphaeta}\partial_{lpha}\partial_{lpha}\partial_{eta} = -rac{\partial^2}{\partial t^2} +
abla^2 \ A^{\mu} &= \eta^{\mulpha}A_{lpha} = (\phi, \mathbf{A}) \ \end{pmatrix}$$

$$\ddot{\mathbf{A}} - \nabla^2 \mathbf{A} + \alpha \left[-\dot{\theta} (\nabla \times \mathbf{A}) + (\nabla \theta) \times \dot{\mathbf{A}} \right] = 0$$

Correction to the EM wave equation!

Note: A is a vector and θ is a pseudoscalar.

Helicity basis to probe parity symmetry

Going to Fourier space

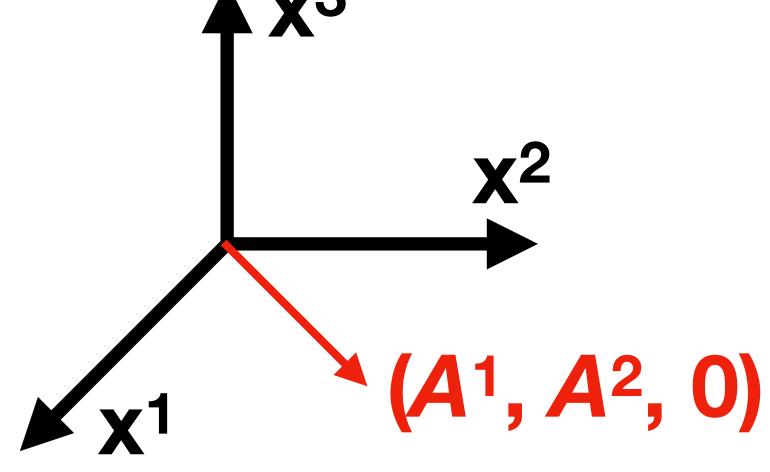
- Fourier transform of $\mathbf{A}(t,\mathbf{x})$ is $\mathbf{A}(t,\mathbf{x})=(2\pi)^{-3/2}\int d^3\mathbf{k}~\mathbf{A_k}(t)e^{i\mathbf{k}\cdot\mathbf{x}}$
 - The EM wave propagates in the direction of \mathbf{k} . The change in \mathbf{A}_k is perpendicular to \mathbf{k} .

"Coulomb gauge"
$$abla \cdot \mathbf{A}(t,\mathbf{x}) = 0 o \mathbf{k} \cdot \mathbf{A}_{\mathbf{k}}(t) = 0$$

• Choose **k** to be on the $z(=x^3)$ axis. The helicity states, $\lambda = \pm 1$, are given

for each Fourier mode by

$$A_{\pm} = \frac{A_{\mathbf{k}}^1 \mp iA_{\mathbf{k}}^2}{\sqrt{2}}$$



Correction to the EM wave equation

In the helicity basis

$$\ddot{\mathbf{A}} - \nabla^2 \mathbf{A} + \alpha \left[-\dot{\theta} (\nabla \times \mathbf{A}) + (\nabla \theta) \times \dot{\mathbf{A}} \right] = 0$$

Correction to the EM wave equation!

• If θ has a time-dependent vacuum expectation value, $\theta(t, \mathbf{x}) \to \theta(t)$, we find in Fourier space

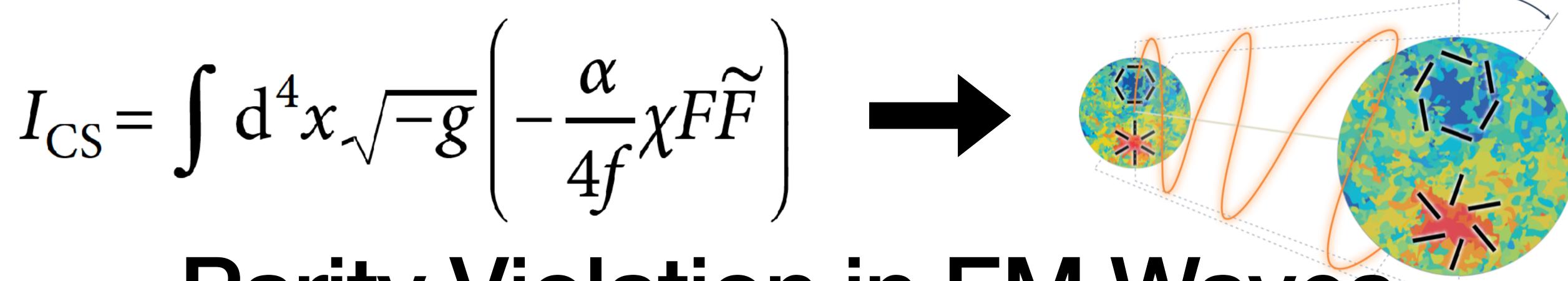
$$\ddot{\mathbf{A}}_{\mathbf{k}} + k^2 \mathbf{A}_{\mathbf{k}} - i\alpha \dot{\bar{\theta}}(\mathbf{k} \times \mathbf{A}) = 0$$

$$\ddot{A}_{\pm} + \left(k^2 \mp k\alpha \dot{\bar{\theta}}\right) A_{\pm} = 0$$

Parity violation

The equation of motion depends on handedness!

Imagine that space is filled with a pseudoscalar field coupled to photons via the CS term.



Parity Violation in EM Waves due to Dark Matter and Dark Energy

Imagine that space is filled with a pseudoscalar field coupled to photons via the CS term.

Scalar field DM/DE coupled to the CS term

DM = Dark Matter; DE = Dark Energy

$$I = \int d^4x \sqrt{-g} \left[-\frac{1}{2} (\partial \chi)^2 - V(\chi) - \frac{1}{4} F^2 - \frac{\alpha}{4f} \chi F \tilde{F} \right]$$

- x is a neutral pseudoscalar field (spin 0).
- Why consider χ as a good DM/DE candidate?
 - Why not? We have an example in the Standard Model: a neutral pion.
 - We expect $\alpha \simeq \alpha_{\rm EM} \simeq 10^{-2}$ and $f < M_{\rm Pl} \simeq 2.4 \times 10^{18}$ GeV.
- χ can be composed of fermions like a pion, or a fundamental pseudoscalar like an "axion" field.

We wrote $rac{\chi}{ heta}=rac{\chi}{f}$

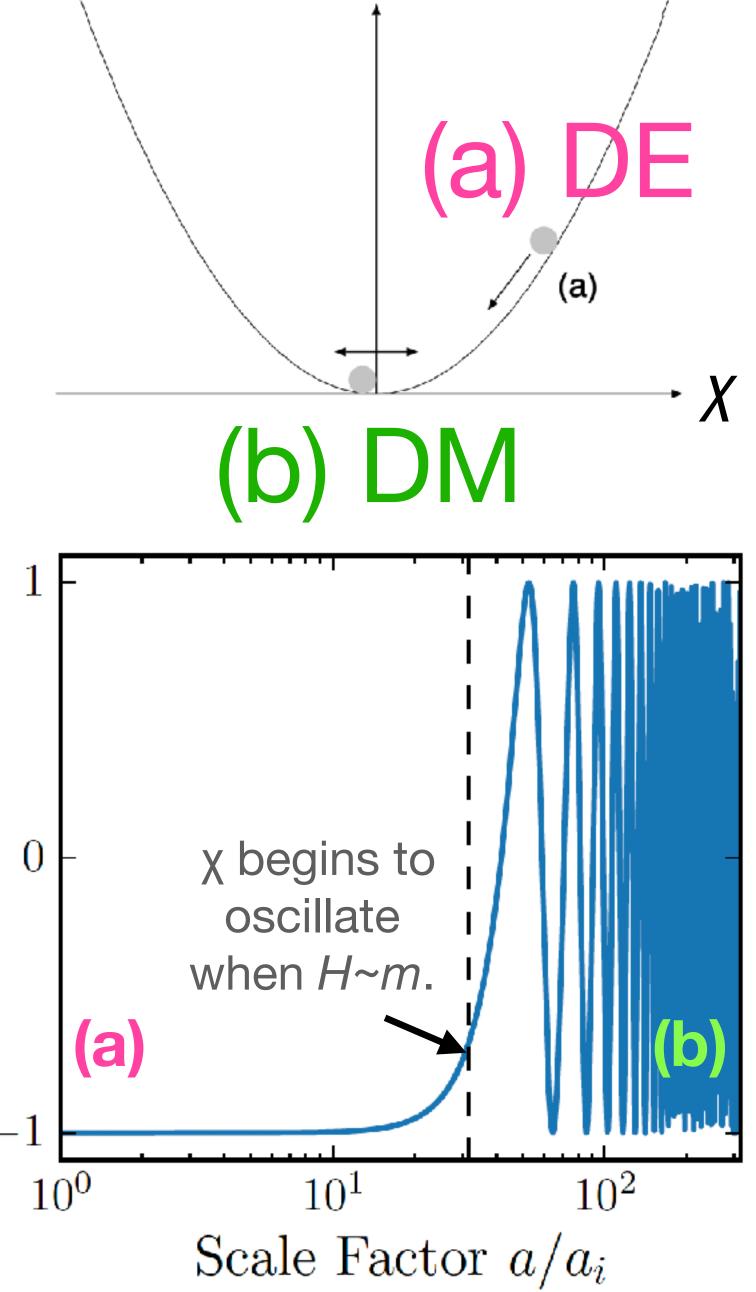
Distinction between DE and DM

How small is its mass? Example of $V(\chi) = m^2 \chi^2/2$

• The useful criterion is the equation of state parameter, w.

$$w = \frac{P}{\rho} = \frac{\langle \dot{\chi}^2 \rangle - m^2 \langle \chi^2 \rangle}{\langle \dot{\chi}^2 \rangle + m^2 \langle \chi^2 \rangle}$$

- $w \simeq -1$: Dark Energy (DE)
 - $m \lesssim H_0 \simeq 10^{-33} \text{ eV}$
- $w \simeq 0$: Dark Matter (DM)
 - $m \gtrsim H_0$



 $i^2\chi^2)/(\dot{\chi}^2$

 $V(\chi)$

Phase velocity of circular polarization states

Expanding space, c=1

We write

$$A''_{\pm} + \omega_{\pm}^2 A_{\pm} = 0, \quad \omega_{\pm}^2 = k^2 \mp \frac{k\alpha\chi'}{f}$$

au: conformal time

- We work in the limit of $k^2\gg k\alpha\chi'/f$. This approximation is accurate for the photons we observe today. (However, ω_\pm^2 can become negative during inflation!)
- The phase velocity of circular polarization states, ω_{\pm}/k , is

$$\frac{\omega_{\pm}}{k} \simeq 1 \mp \frac{\alpha \chi'}{2kf}$$

+: Right-handed state

-: Left-handed state





40

Carroll, Field, Jackiw (1990); Carroll, Field (1991); Harari, Sikivie (1992)

Plane-wave (WKB) Solution

Expanding space, c=1

$$A''_{\pm} + \omega_{\pm}^2 A_{\pm} = 0, \quad \omega_{\pm} \simeq k \mp \frac{\alpha \chi'}{2f}$$

• For $|\omega'_{\pm}| \ll \omega_{\pm}^2$, which is satisfied here, an accurate solution is given by

$$A_{\pm} \simeq C_{\pm} \frac{\exp\left(-i\int d\tau \ \omega_{\pm} + i\delta_{\pm}\right)}{\sqrt{2\omega_{\pm}} \simeq \sqrt{2k}} \quad \text{We can replace ω_{\pm} in amplitude (but not in phase) with k.}$$

where C_+ is the initial amplitude and δ_+ is the initial phase.

Carroll, Field, Jackiw (1990); Carroll, Field (1991); Harari, Sikivie (1992)

Cosmic Birefringence

Rotation of the plane of linear polarization

$$A_{\pm} \simeq C_{\pm} \frac{\exp\left(-i\int d au \; \omega_{\pm} + i\delta_{\pm}\right)}{\sqrt{2\omega_{\pm}} \simeq \sqrt{2k}} \quad \frac{\omega_{\pm}}{k} \simeq 1 \mp \frac{\alpha\chi'}{2kf}$$

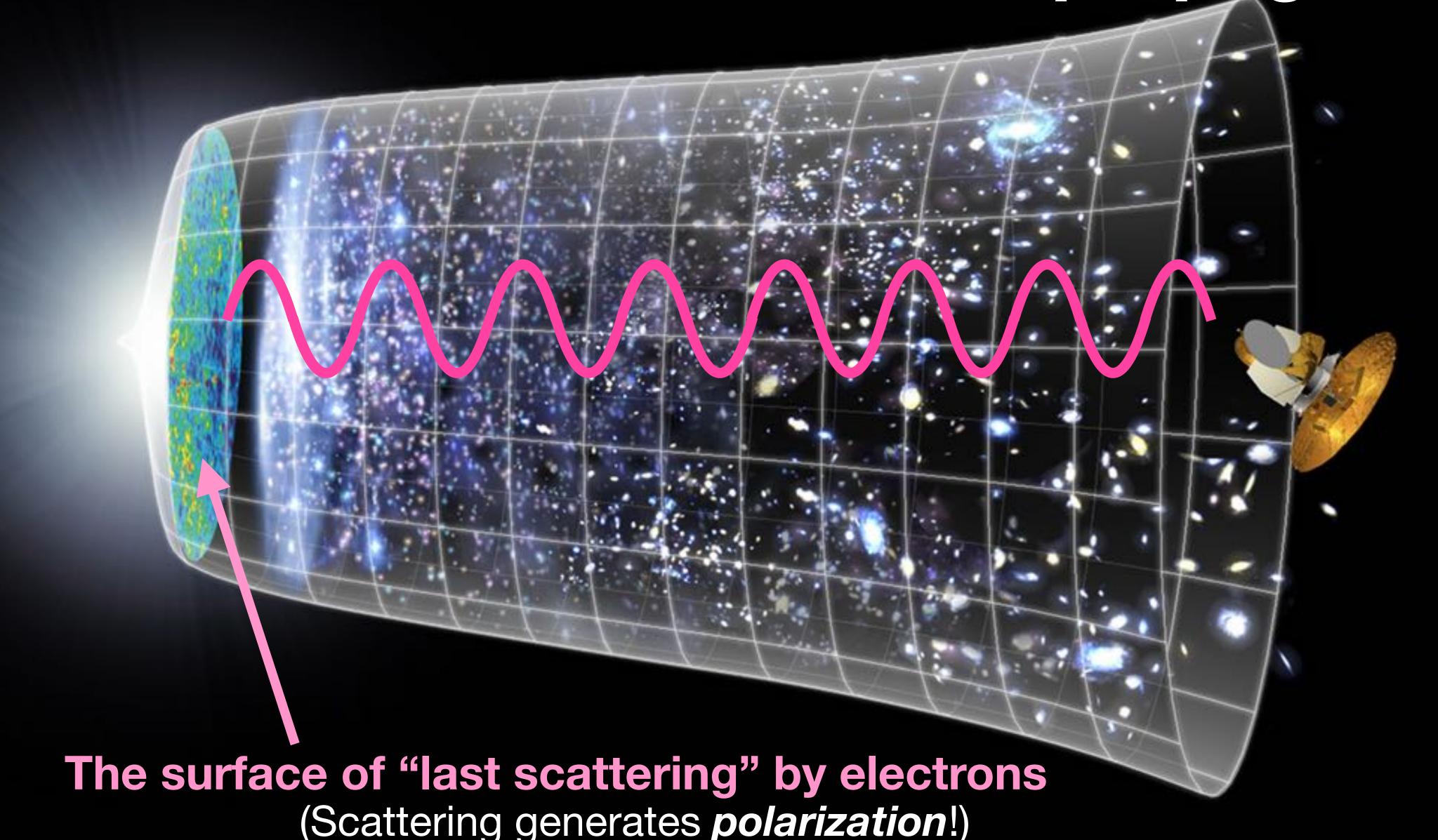
• This rotates the plane of linear polarization of light by

$$\beta = -\int_{\tau_{\rm em}}^{\tau_{\rm obs}} d\tau \left(\omega_{+} - \omega_{-}\right)$$

$$= \frac{\alpha}{2f} \left[\chi(\tau_{\rm obs}) - \chi(\tau_{\rm em})\right] \qquad \tau_{\rm em}$$

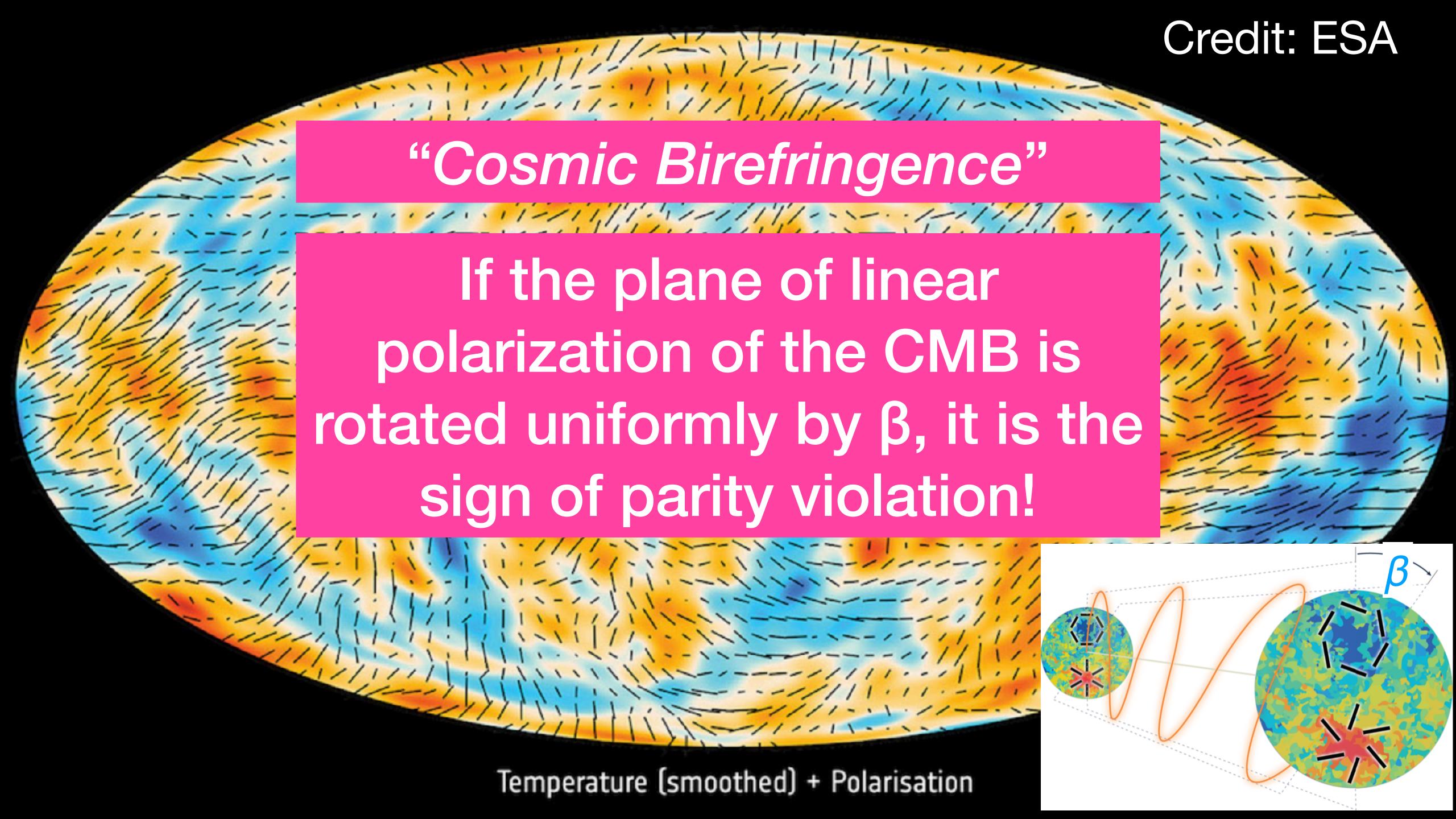
$$\tau_{\rm obs}$$

How does the EM wave of the CMB propagate?



Credit: WMAP Science Team

How does the EM wave of the CMB propagate?



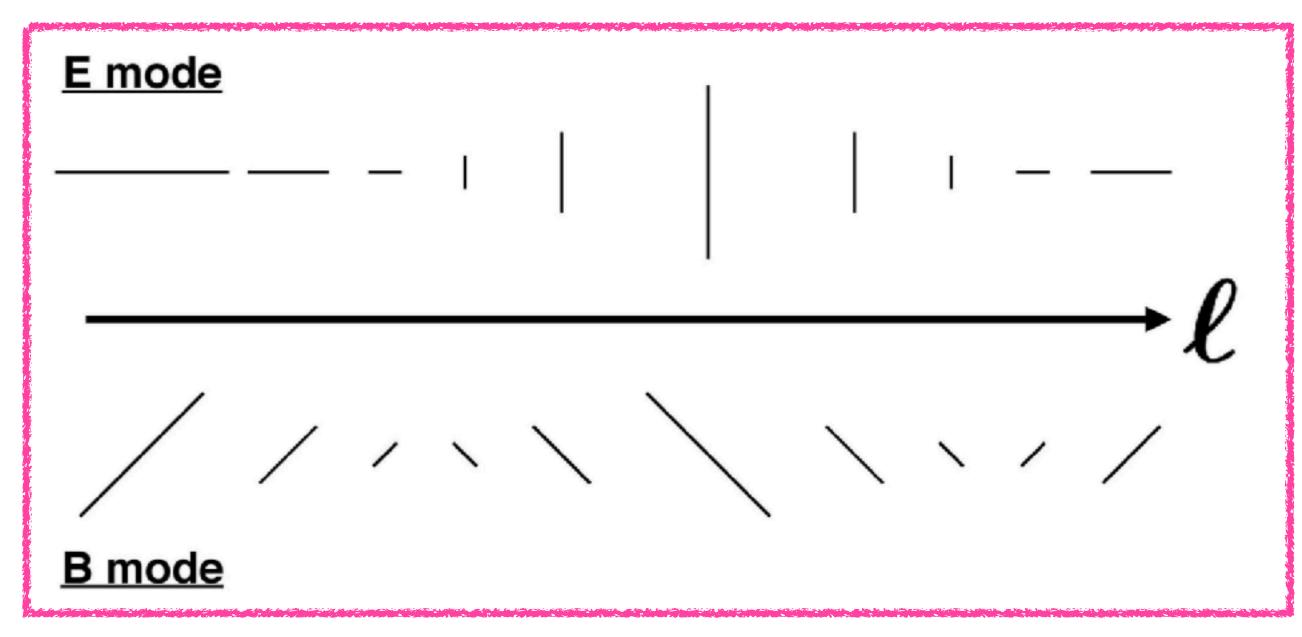
Pseudoscalar: EB correlation

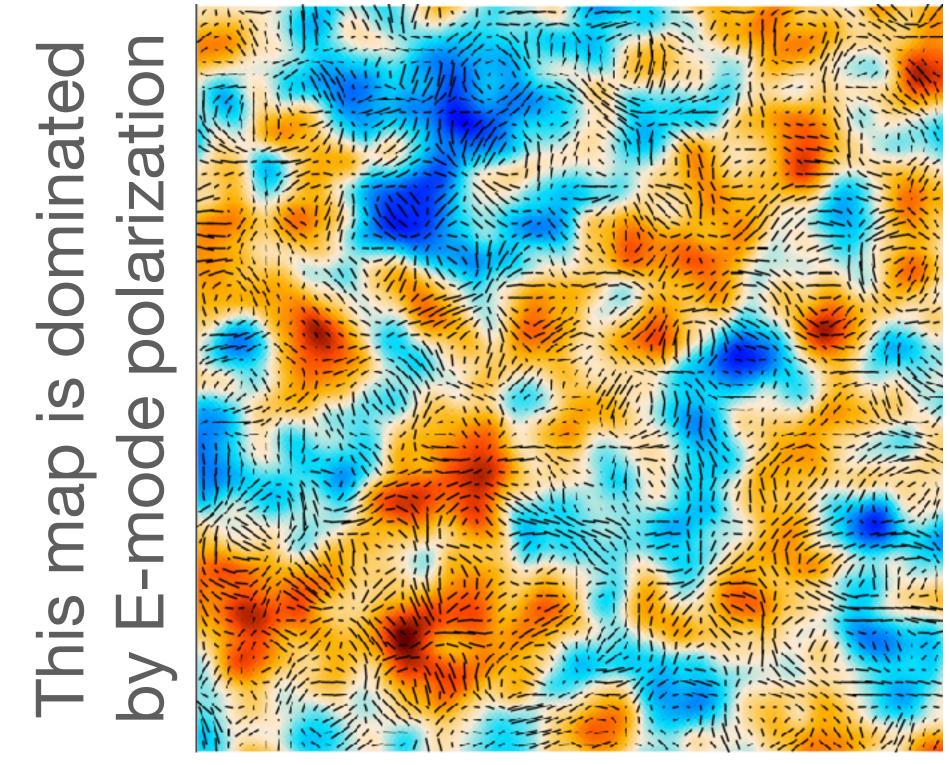
- The observed pattern of the CMB polarization can be decomposed into eigenstates of parity, called "E modes" and "B modes".
- E and B modes are transformed differently under the parity transformation. Therefore, the product of the two, the "EB correlation", is a pseudoscalar.
- The full-sky average of the EB correlation must vanish (to within the measurement uncertainty), if there is no parity violation!

Zaldarriaga, Seljak (1997); Kamionkowski, Kosowsky, Stebbins (1997)

Parity eigenstates: E and B modes

Concept defined in Fourier space

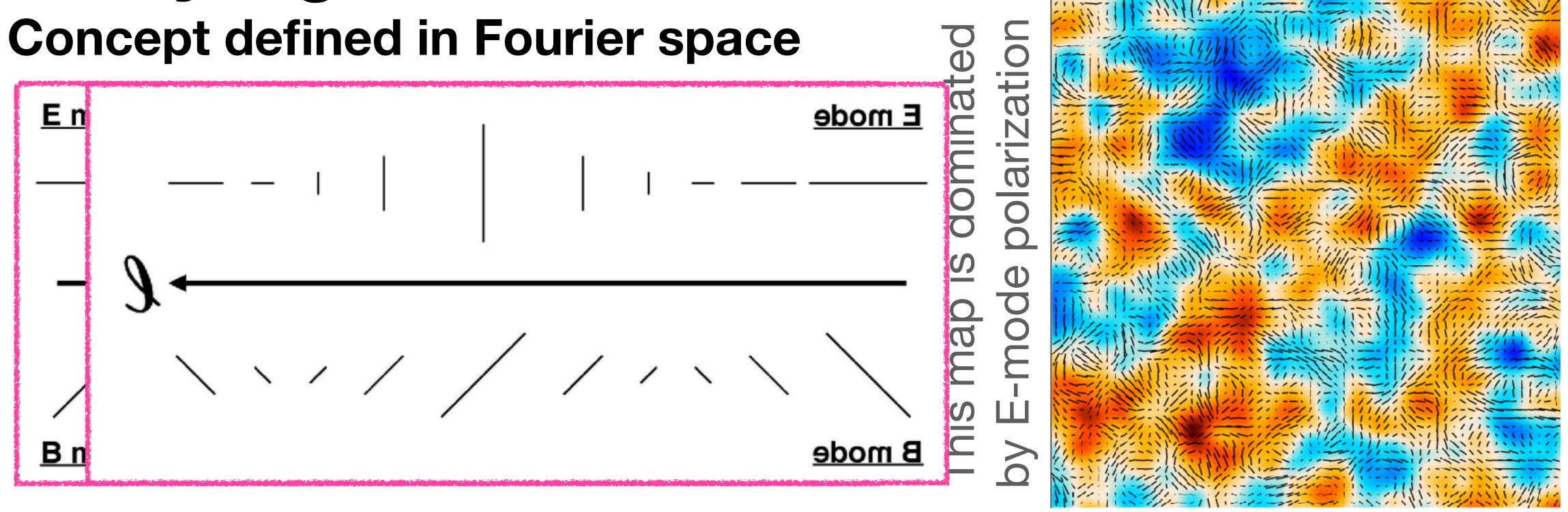




- E-mode: Polarization directions are parallel or perpendicular to the wavenumber direction
- B-mode: Polarization directions are 45 degrees tilted w.r.t the wavenumber direction

Zaldarriaga, Seljak (1997); Kamionkowski, Kosowsky, Stebbins (1997)

Parity eigenstates: E and B modes

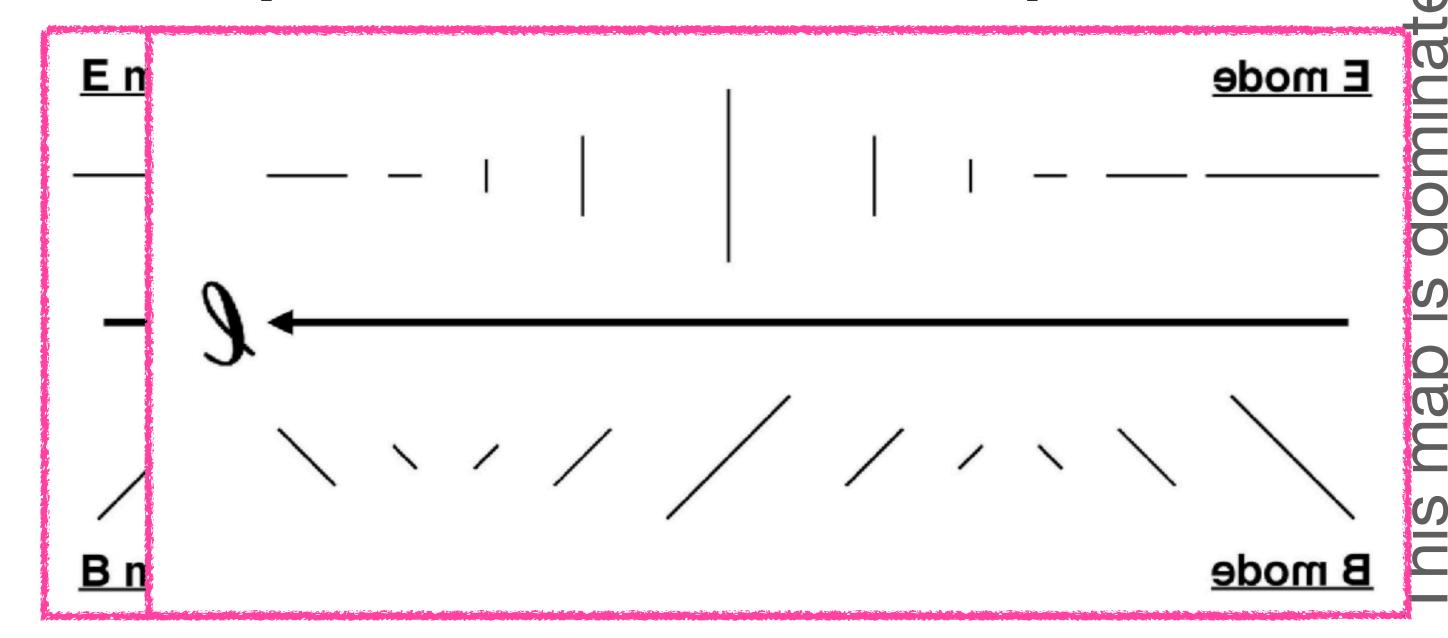


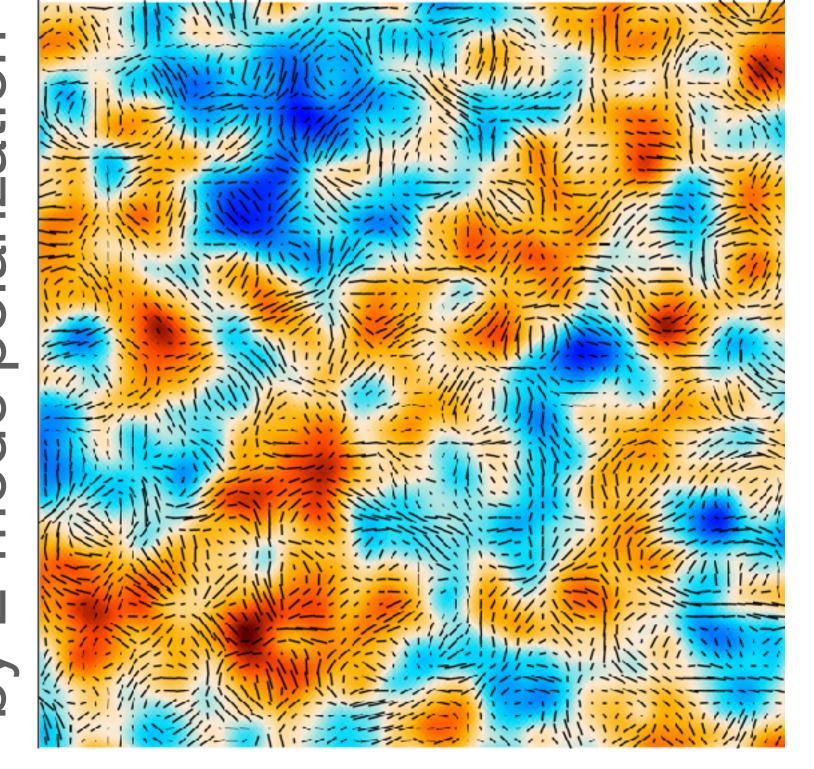
- E-mode: Polarization directions are parallel or perpendicular to the wavenumber direction
- **B-mode**: Polarization directions are **45 degrees tilted** w.r.t the wavenumber direction

Zaldarriaga, Seljak (1997); Kamionkowski, Kosowsky, Stebbins (1997)

Parity eigenstates: E and B modes

Concept defined in Fourier space





$$\langle E_{\ell} E_{\ell'}^* \rangle = (2\pi)^2 \delta_D^{(2)} (\ell - \ell') C_{\ell}^{EE}$$

$$\langle B_{\ell} B_{\ell'}^* \rangle = (2\pi)^2 \delta_D^{(2)} (\ell - \ell') C_{\ell}^{BB}$$

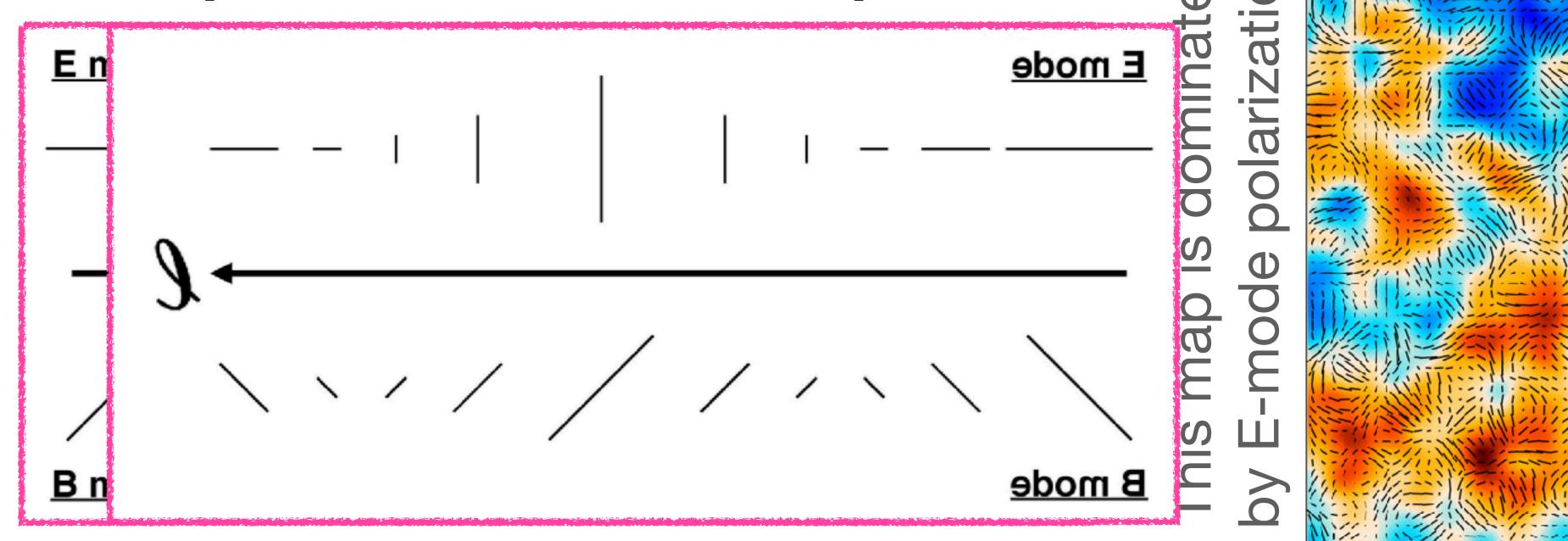
$$\langle T_{\ell} E_{\ell'}^* \rangle = \langle T_{\ell}^* E_{\ell'} \rangle = (2\pi)^2 \delta_D^{(2)} (\ell - \ell') C_{\ell}^{TE}$$

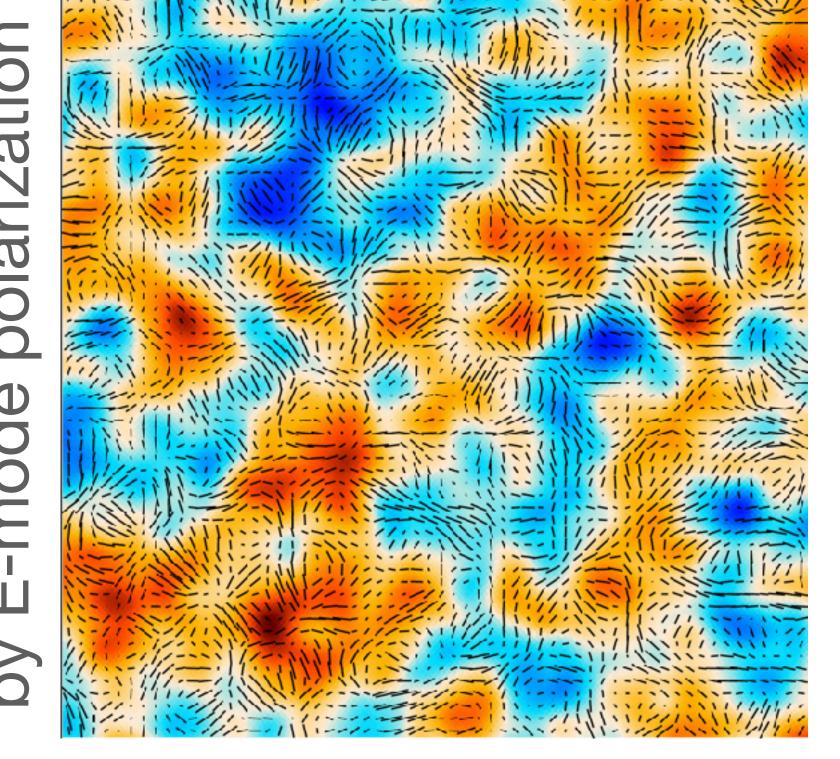
These are scalars and insensitive to parity violation.

Lue, Wang, Kamionkowski (1999); Feng et al. (2005, 2006)

Parity eigenstates: E and B modes

Concept defined in Fourier space





$$\langle E_{\pmb{\ell}} E_{\pmb{\ell}'}^* \rangle = (2\pi)^2 \delta_D^{(2)} (\pmb{\ell} - \pmb{\ell}') C_{\pmb{\ell}}^{EE}$$
 The other combinations, and ,

$$\langle B_{\ell} B_{\ell'}^* \rangle = (2\pi)^2 \delta_D^{(2)} (\ell - 1)^2 \delta_D^{(2)} (\ell - 1$$

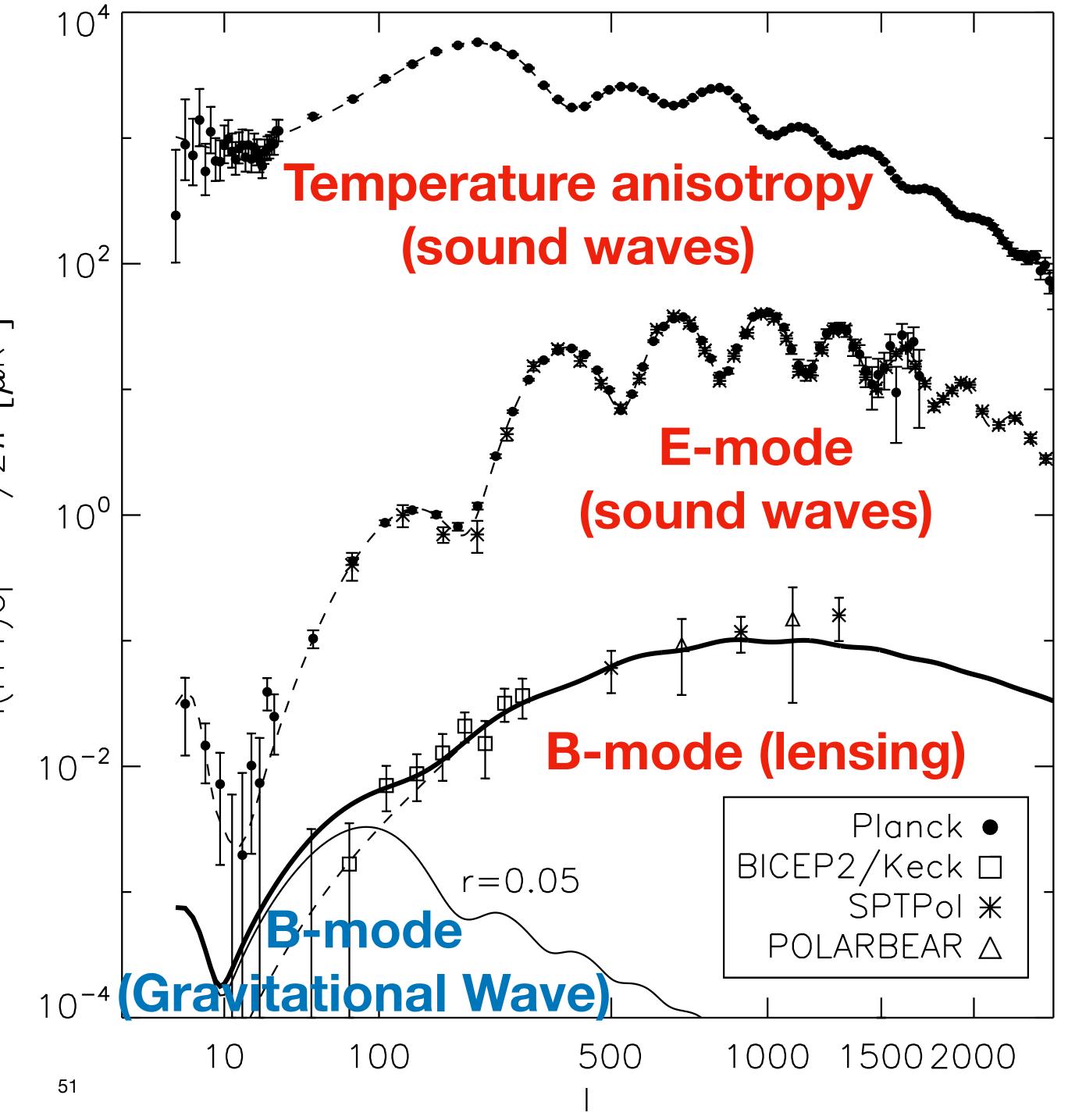
$$\langle T_{\ell} E_{\ell'}^* \rangle = \langle T_{\ell}^* E_{\ell'} \rangle = (2\pi)^2 \delta_D^{(2)} (\ell - \ell') C_{\ell}^{TL}$$

other combinations, <TB> and <EB>, are pseudoscalars and sensitive to parity violation!

CMB Power Spectra

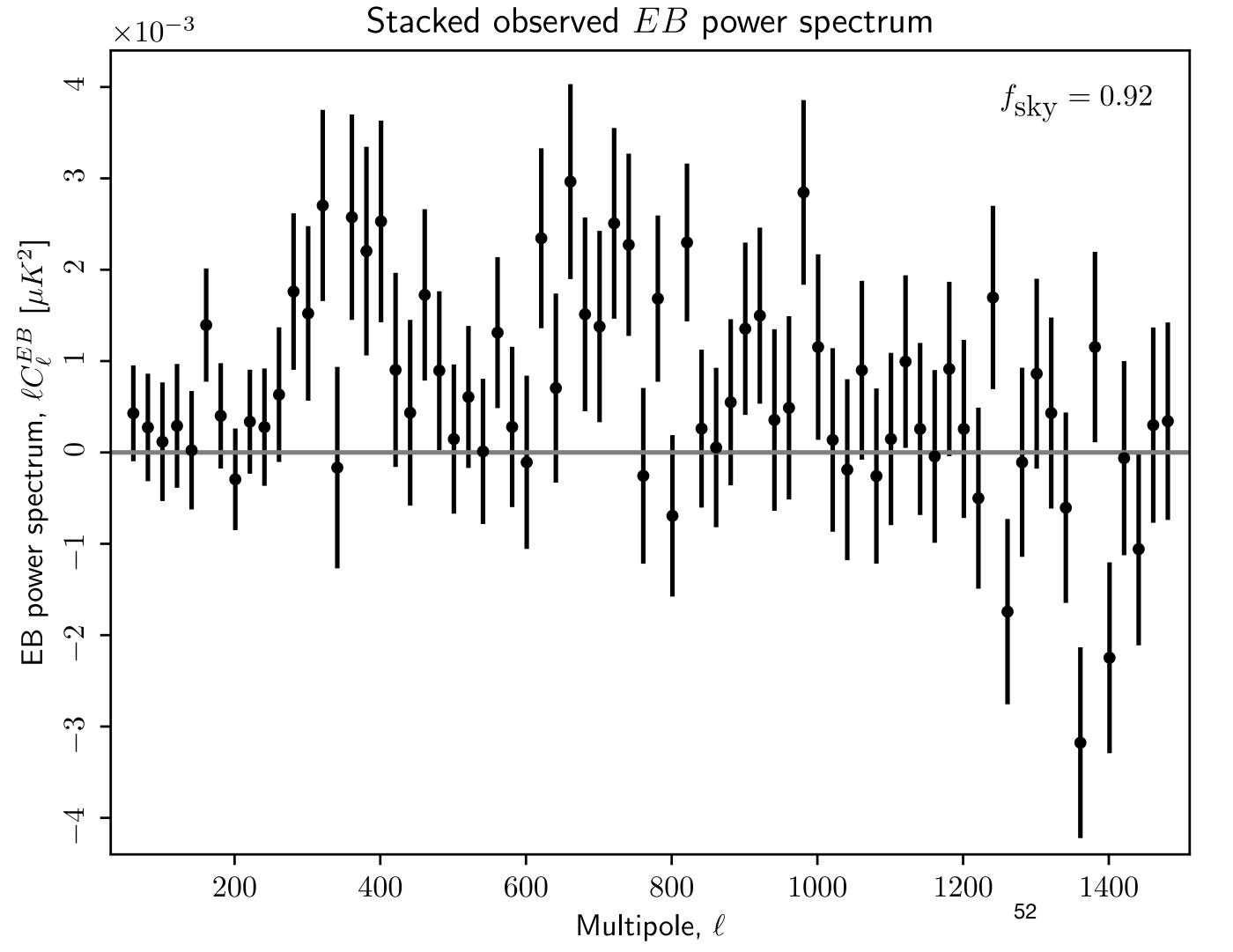
Progress over 30 years

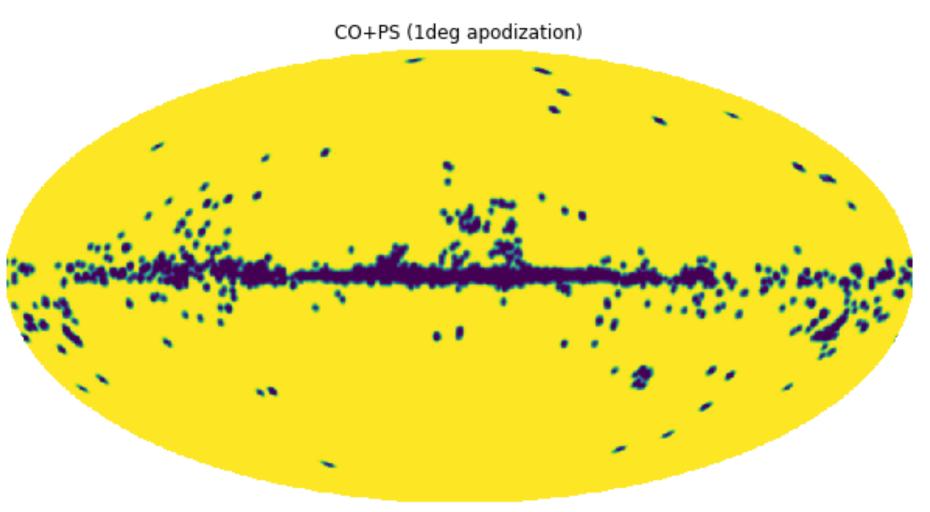
- This is the typical figure seen in talks and lectures on the CMB.
 - The temperature and the E- and B-mode polarization power spectra are well measured.
- Parity violation appears in the TB and EB power spectra, not shown here.



This is the EB power spectrum (WMAP+Planck)

Nearly full-sky data (92% of the sky)

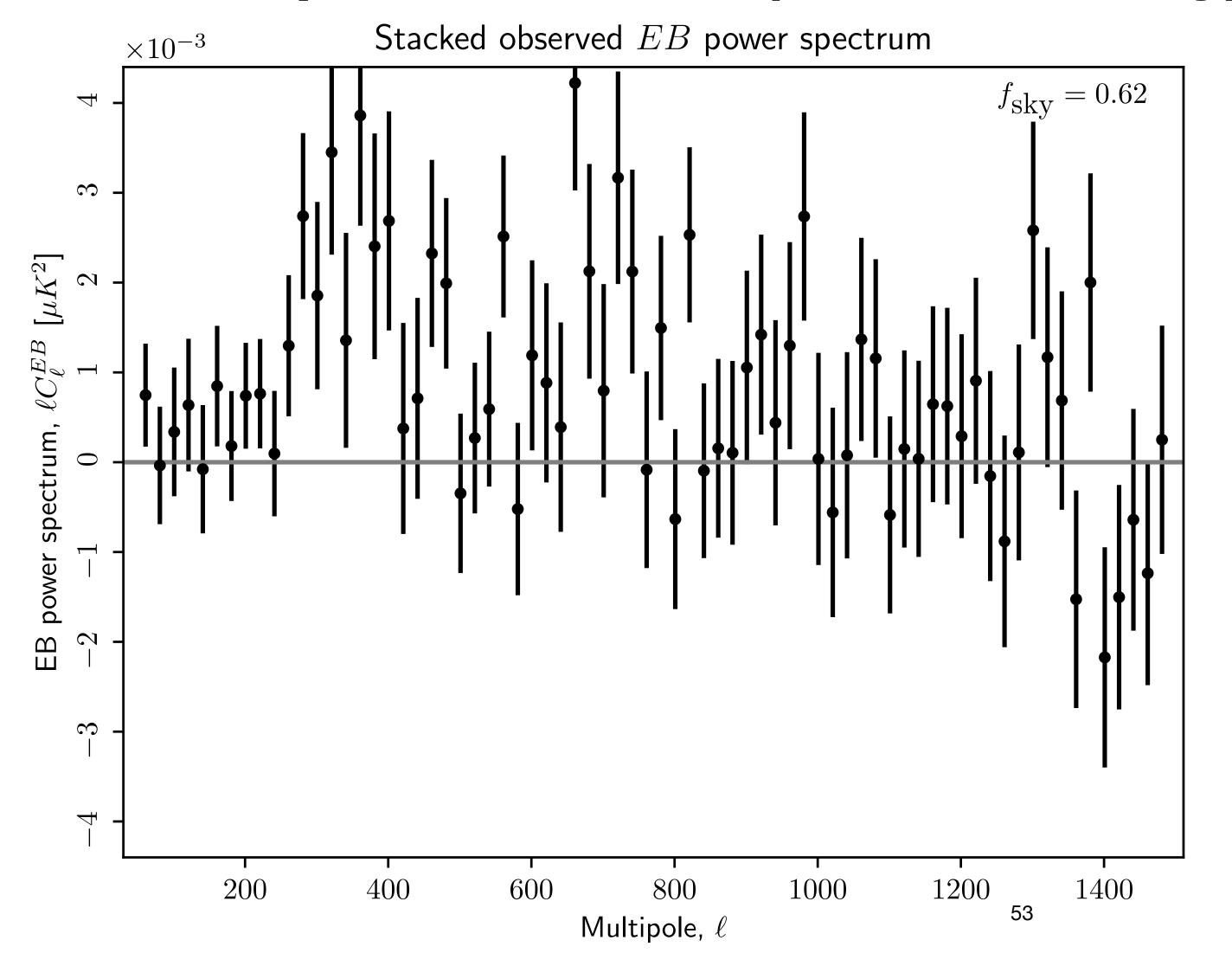


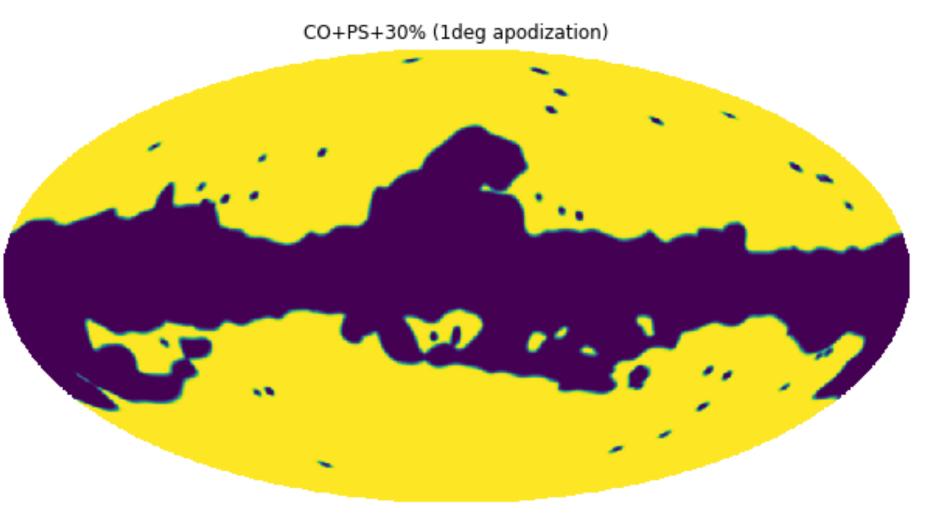


- $\chi^2 = 125.5$ for DOF=72
 - Unambiguous signal of something!

This is the EB power spectrum (WMAP+Planck)

Galactic plane removed (62% of the sky)





- $\chi^2 = 138.4$
 - The signal exists regardless of the Galactic mask. This rules out the Galactic foreground.

Lue, Wang, Kamionkowski (1999); Feng et al. (2005, 2006)

E-B mixing by rotation of the plane of linear polarization

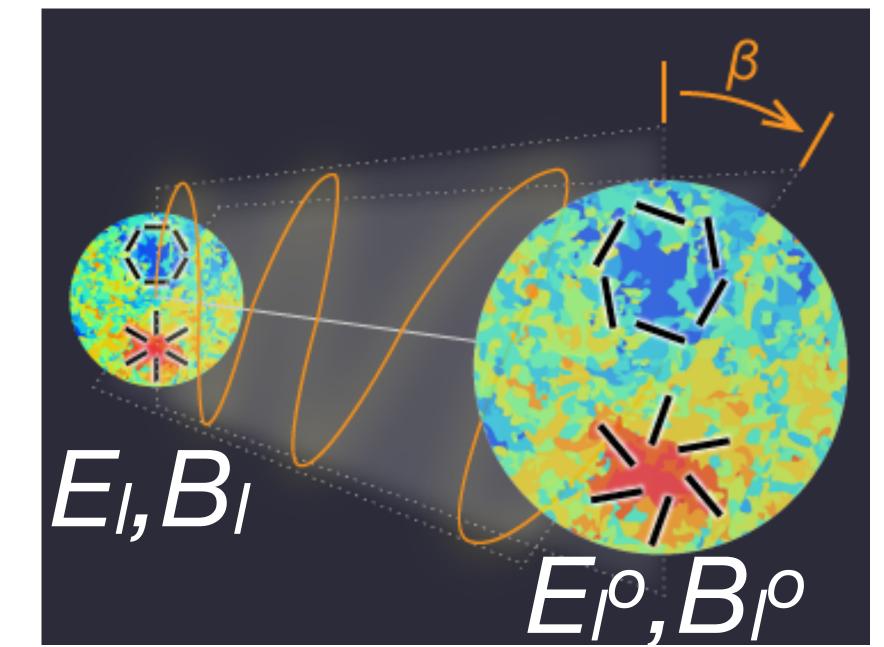
• Observed E- and B-mode polarization, E_I° and B_I°, are related to those before rotation as

$$E_\ell^{\rm o} \pm iB_\ell^{\rm o} = (E_\ell \pm iB_\ell)e^{\pm 2i\beta}$$

which gives

$$E_{\ell}^{o} = E_{\ell} \cos(2\beta) - B_{\ell} \sin(2\beta)$$

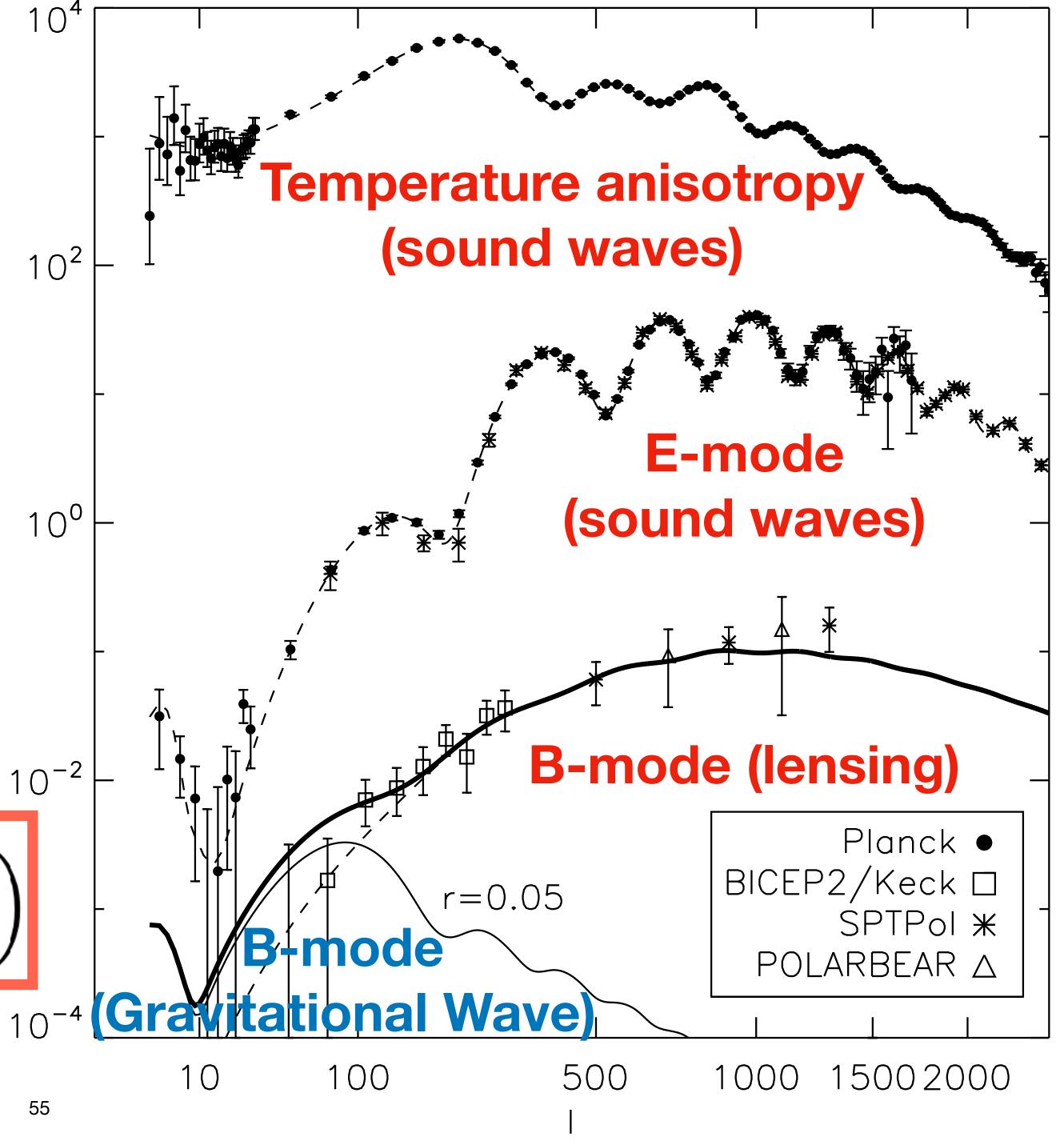
$$B_{\ell}^{o} = E_{\ell} \sin(2\beta) + B_{\ell} \cos(2\beta)$$



CMB Power Spectra

- Rotation of the plane of linear polarization **mixes** E and B modes.
- Therefore, the EB correlation will be given by the difference between the EE and BB correlations.
- Observed EE is much greater than BB. We expect EB to look like EE!

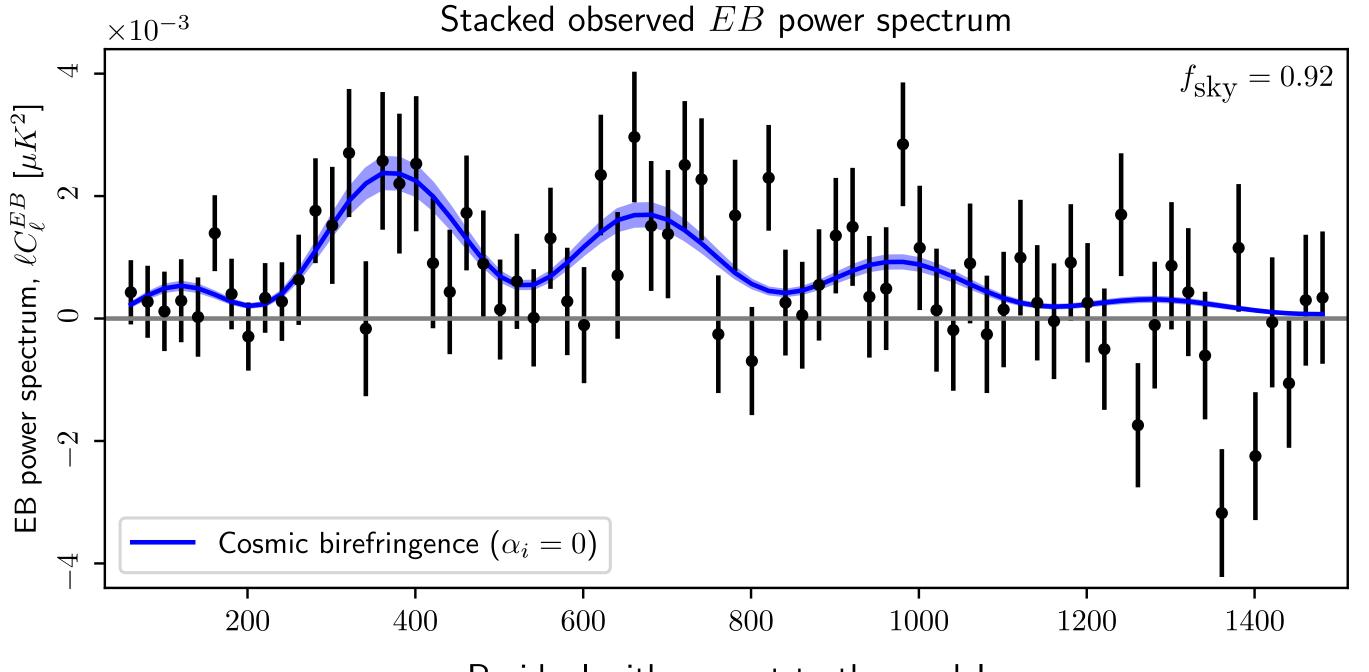
$$C_{\ell}^{EB,o} = \frac{\tan(4\beta)}{2} \left(C_{\ell}^{EE,o} - C_{\ell}^{BB,o} \right)$$

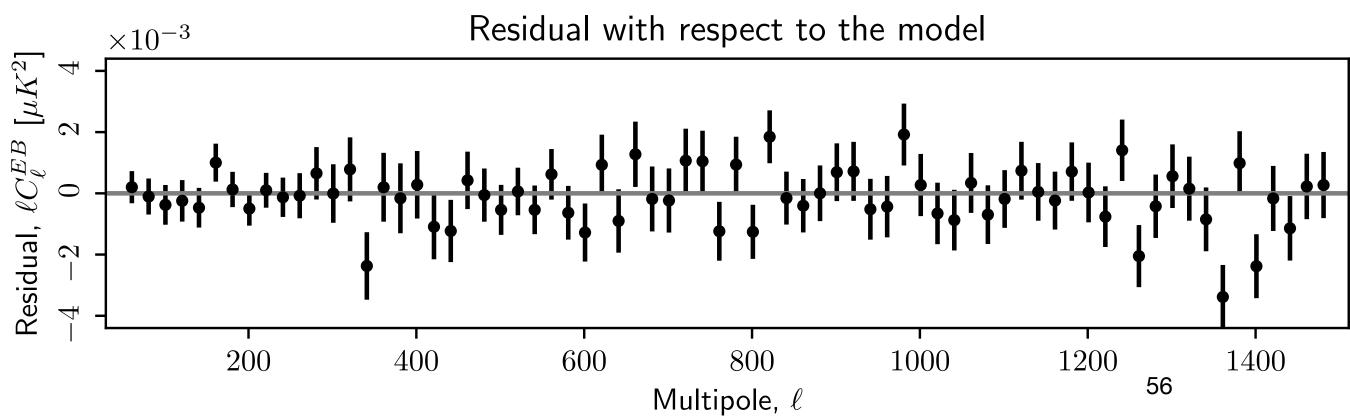


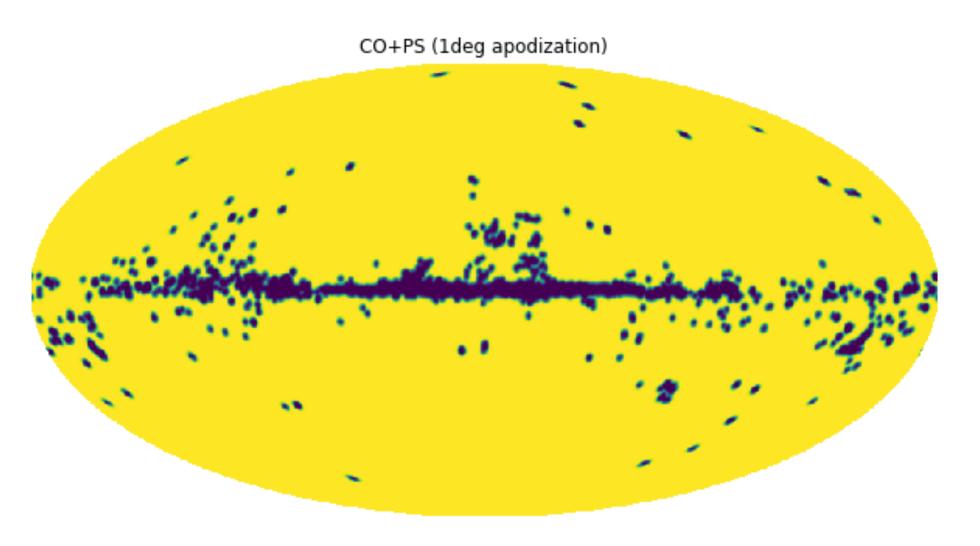
Cosmic Birefringence fits well(?) $C_{\ell}^{EB,o} = \frac{\tan(4\beta)}{2}$

$$C_{\ell}^{EB,o} = \frac{\tan(4\beta)}{2} \left(C_{\ell}^{EE,o} - C_{\ell}^{BB,o} \right)$$

Nearly full-sky data (92% of the sky)





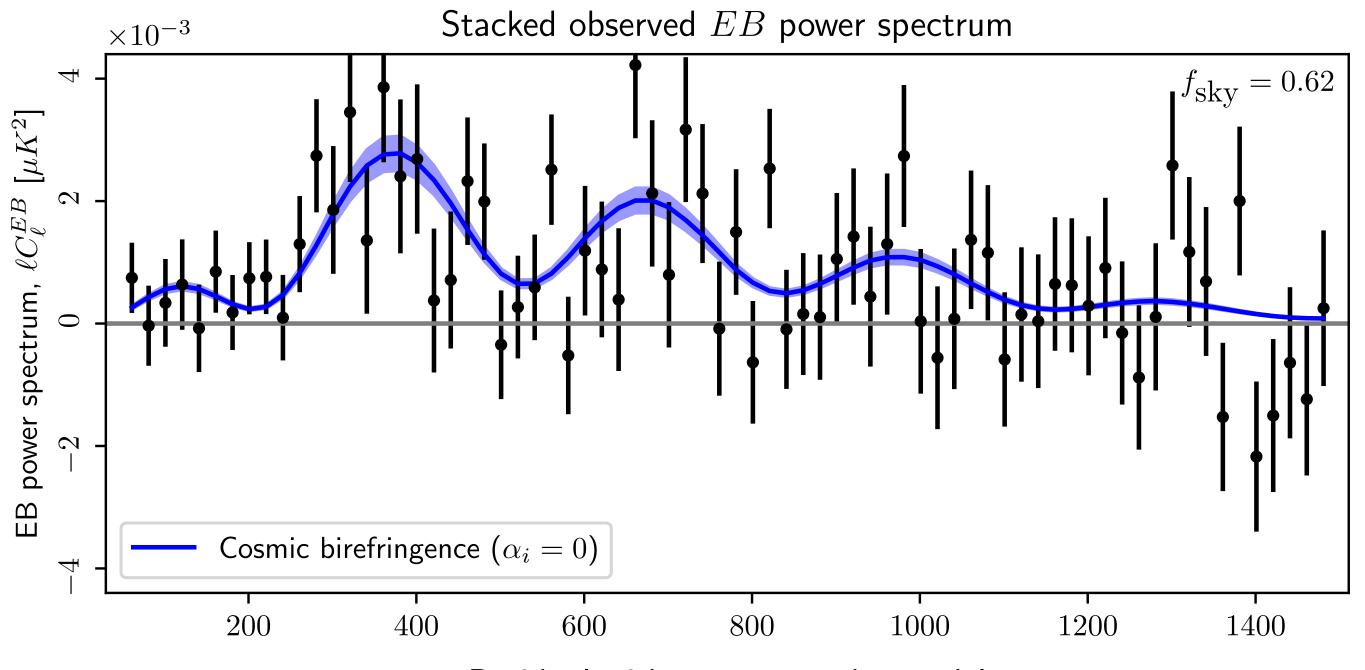


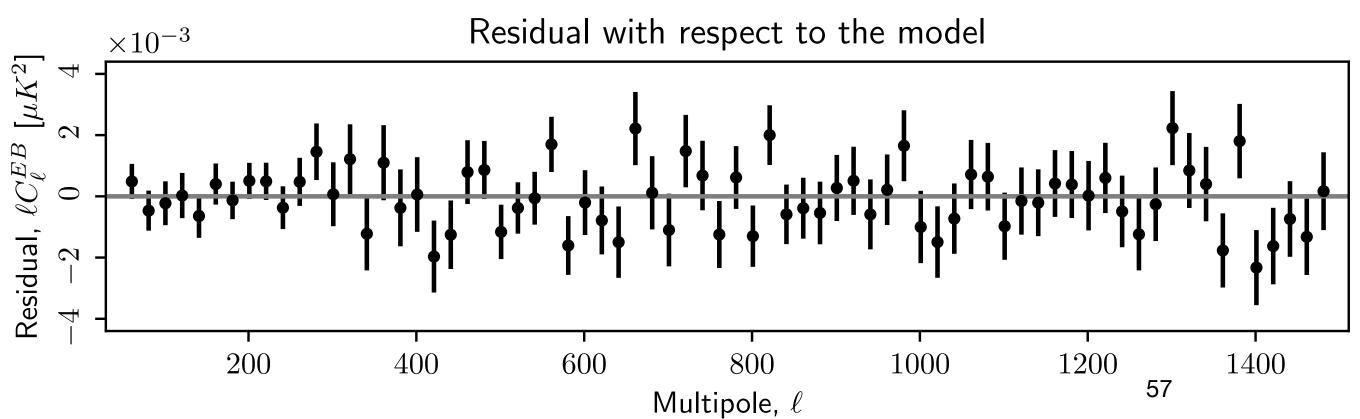
- $\beta = 0.288 \pm 0.032 \text{ deg}$
- $\chi^2 = 66.1$ for DOF=71
 - Good fit! 9σ detection?

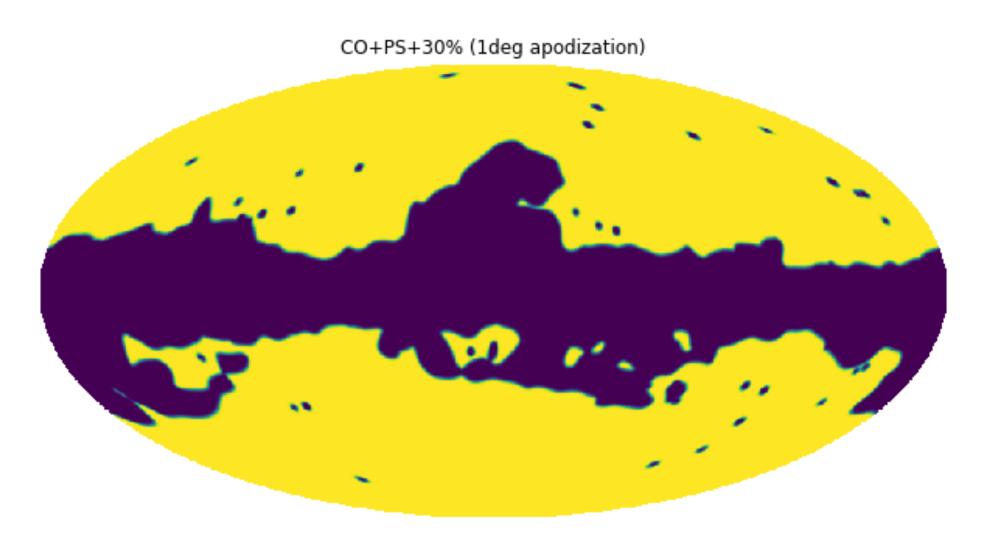
Cosmic Birefringence fits well(?) $C_{\ell}^{EB,o}$ =

$$C_{\ell}^{EB,\mathrm{o}} = rac{ an(4eta)}{2} \left(C_{\ell}^{EE,\mathrm{o}} - C_{\ell}^{BB,\mathrm{o}}
ight)$$

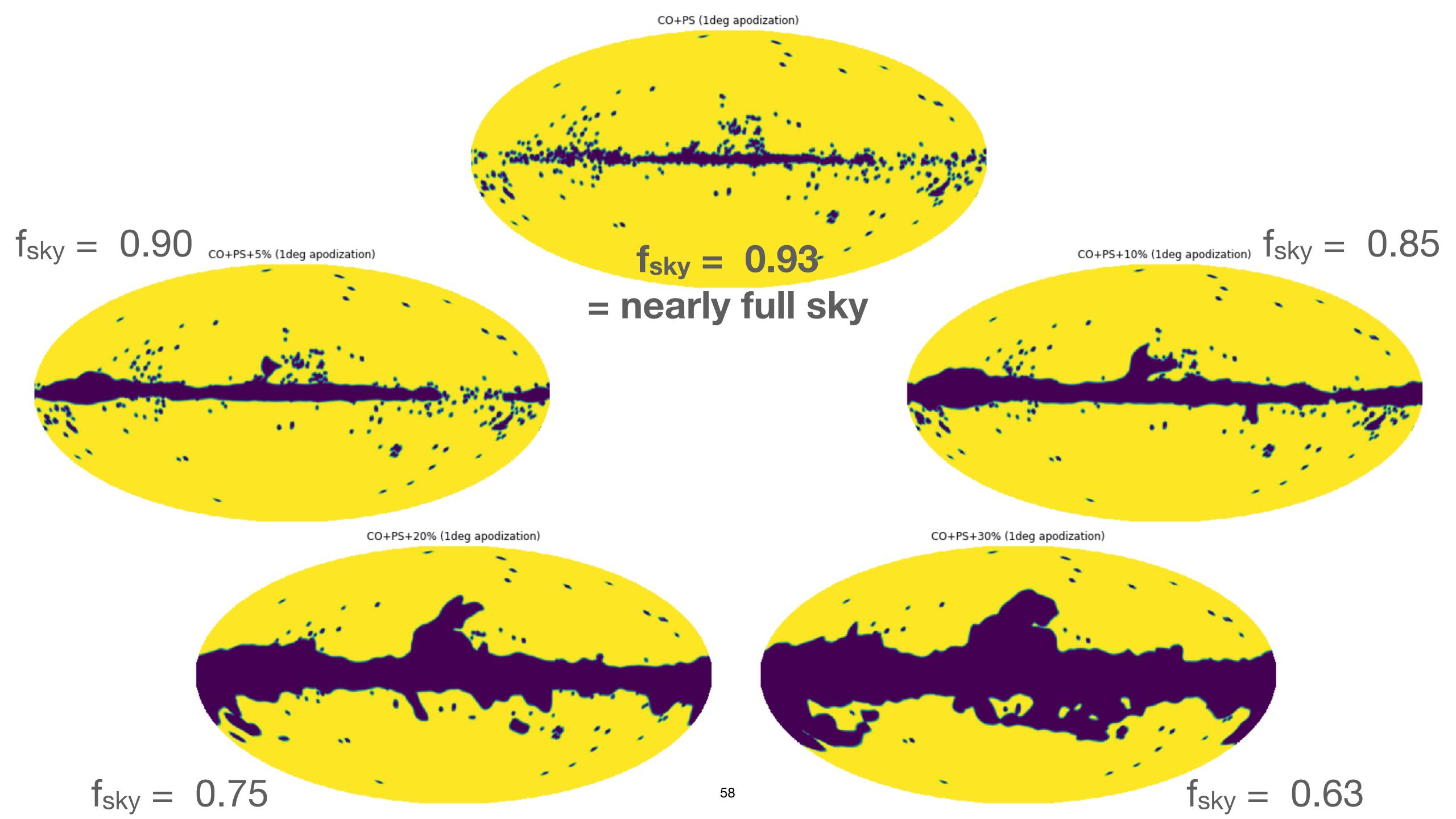
Galactic plane removed (62% of the sky)

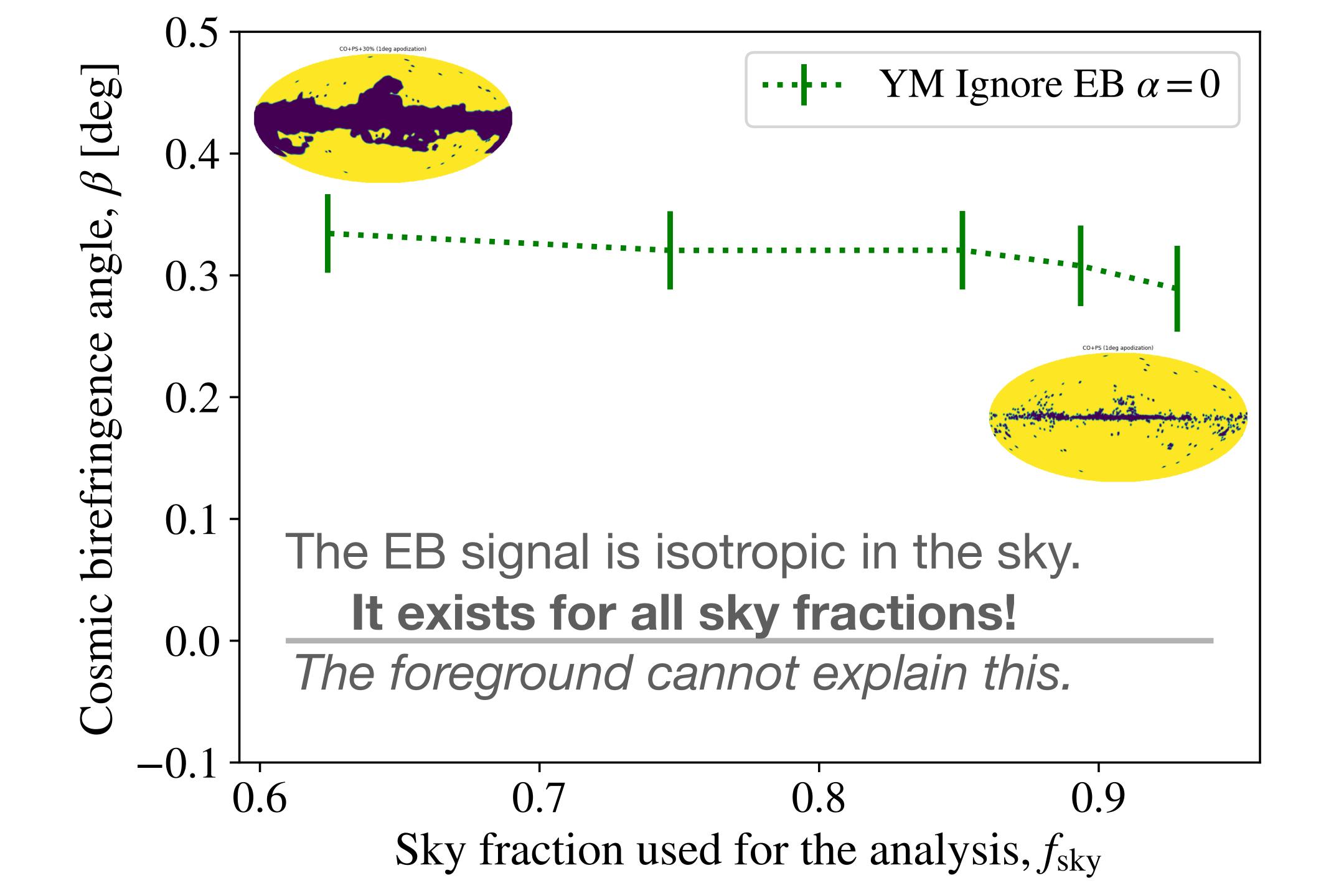






- $\beta = 0.330 \pm 0.035 \text{ deg}$
- $\chi^2 = 64.5$
- Signal is robust with respect to the Galactic mask.





The Biggest Problem: Miscalibration of detectors

Wu et al. (2009); Miller, Shimon, Keating (2009); EK et al. (2011)

Impact of miscalibration of polarization angles

Cosmic or Instrumental?



- Is the plane of linear polarization rotated by the genuine cosmic birefringence effect, or simply because the polarization-sensitive directions of the detectors are rotated with respect to the sky coordinates (and we did not know it)?
- If the detectors are rotated by α , it seems that we can measure only the SUM $\alpha+\beta$.

The past measurements

The quoted uncertainties are all statistical only (68%CL)

- $\alpha+\beta=-6.0\pm4.0$ deg (Feng et al. 2006) first measurement
- $\alpha+\beta=-1.1\pm1.4$ deg (WMAP Collaboration, Komatsu et al. 2009; 2011)
- $\alpha+\beta=0.55\pm0.82$ deg (QUaD Collaboration, Wu et al. 2009)
- •
- $\alpha+\beta=0.31\pm0.05$ deg (Planck Collaboration 2016)
- $\alpha+\beta=-0.61\pm0.22$ deg (POLARBEAR Collaboration 2020)
- $\alpha+\beta=0.63\pm0.04$ deg (SPT Collaboration, Bianchini et al. 2020)
- $\alpha+\beta=0.12\pm0.06$ deg (ACT Collaboration, Namikawa et al. 2020)
- $\alpha+\beta=0.07\pm0.09$ deg (ACT Collaboration, Choi et al. 2020)

Why not yet discovered?

The past measurements

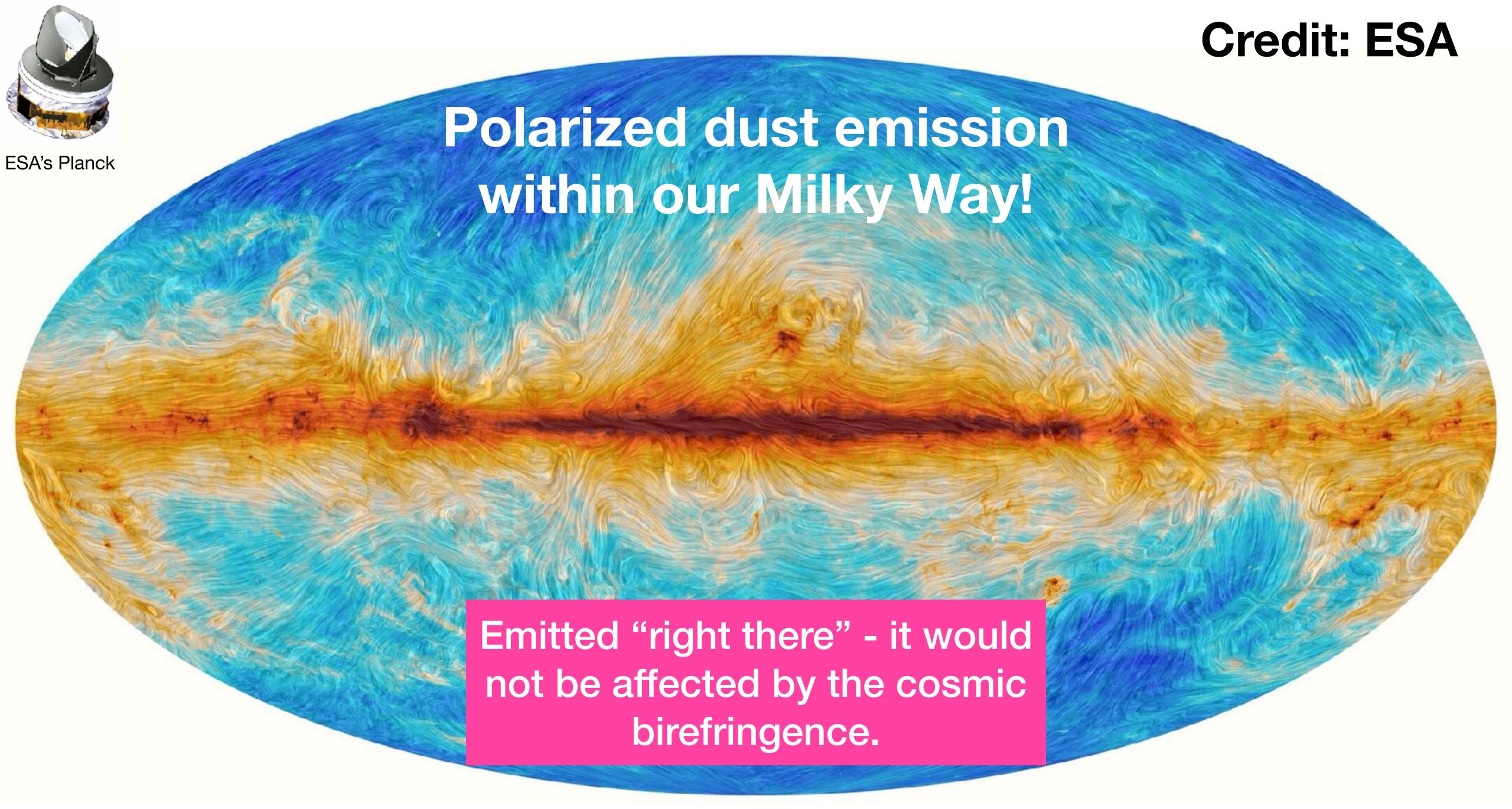
Now including the estimated systematic errors on a

- $\beta = -6.0 \pm 4.0 \pm ??$ deg (Feng et al. 2006)
- $\beta = -1.1 \pm 1.4 \pm 1.5$ deg (WMAP Collaboration, Komatsu et al. 2009; 2011)
- $\beta = 0.55 \pm 0.82 \pm 0.5$ deg (QUaD Collaboration, Wu et al. 2009)
- •
- $\beta = 0.31 \pm 0.05 \pm 0.28$ deg (Planck Collaboration 2016)
- $\beta = -0.61 \pm 0.22 \pm$?? deg (POLARBEAR Collaboration 2020)
- $\beta = 0.63 \pm 0.04 \pm$?? deg (SPT Collaboration, Bianchini et al. 2020)
- $\beta = 0.12 \pm 0.06 \pm$?? deg (ACT Collaboration, Namikawa et al. 2020)
- $\beta = 0.07 \pm 0.09 \pm$?? deg (ACT Collaboration, Choi et al. 2020)

Uncertainty in the calibration of a has been the major limitation

Minami et al. (2019); Minami, EK (2020)

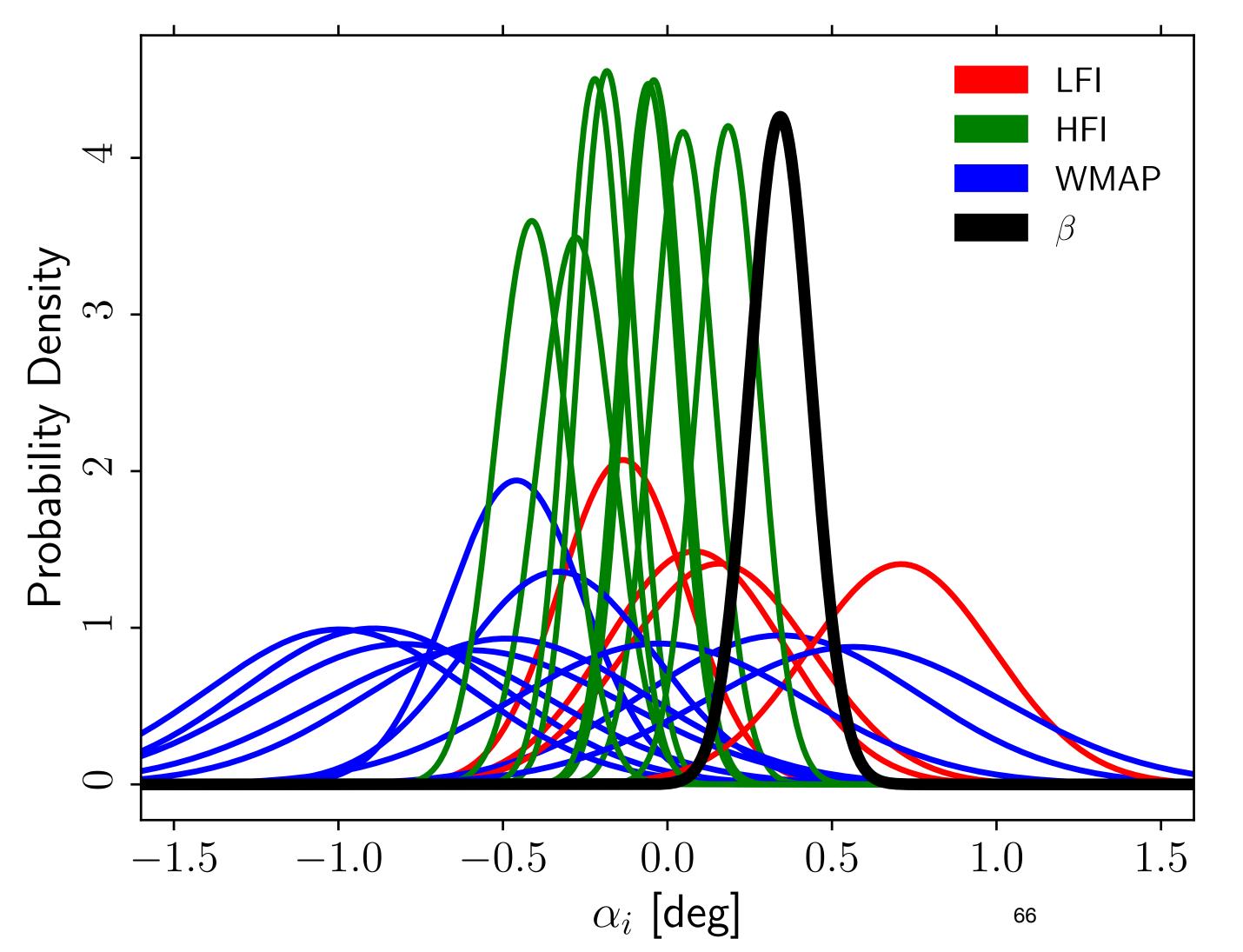
The Key Idea: The polarized Galactic foreground emission as a calibrator



Directions of the magnetic field inferred from polarization of the thermal dust emission in the Milky Way

Miscalibration angles (WMAP and Planck)

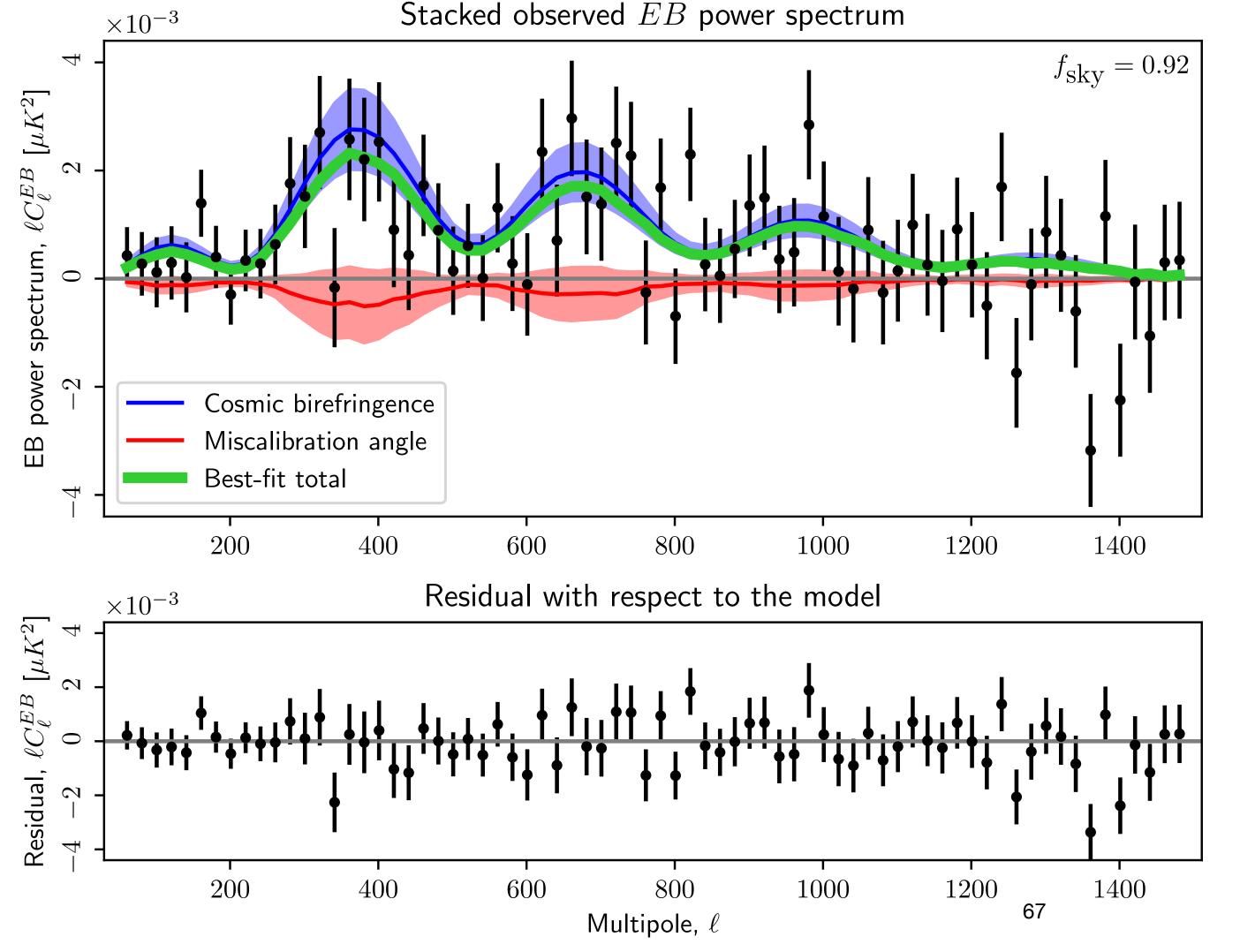
Nearly full-sky data (92% of the sky)

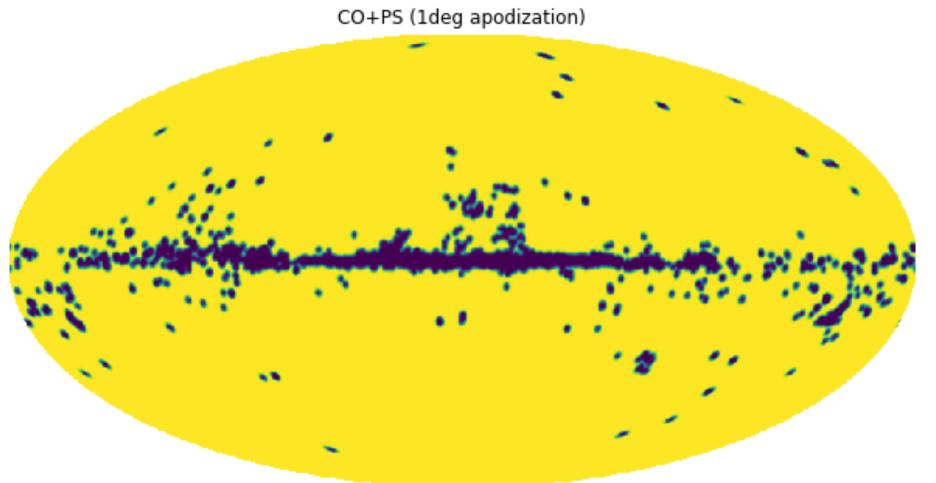


- The angles are all over the place, and are well within the quoted calibration uncertainty of instruments.
 - 1.5 deg for WMAP
 - 1 deg for Planck
- They cancel!
 - The power of adding independent datasets.

Cosmic Birefringence fits well (WMAP+Planck)

Nearly full-sky data (92% of the sky)

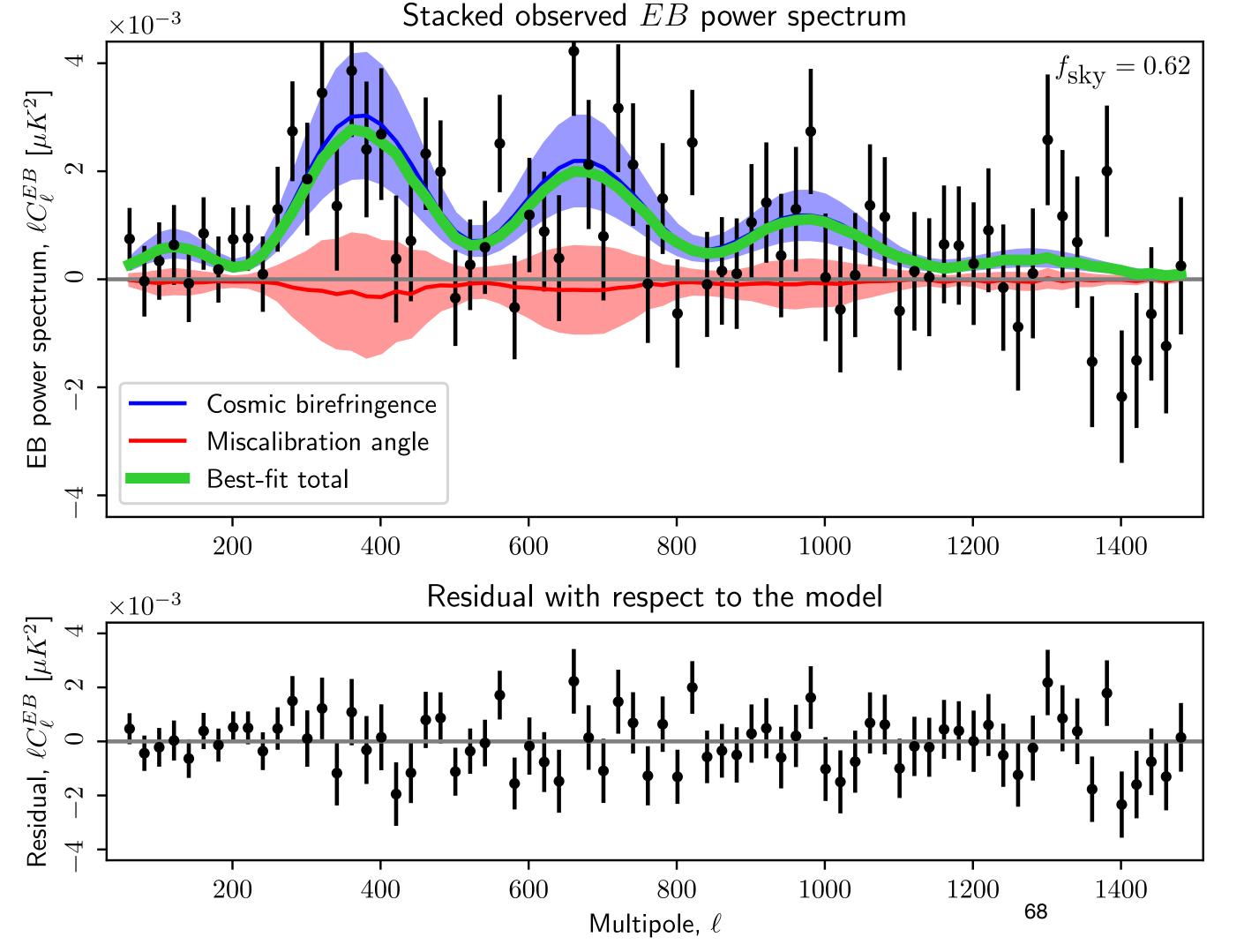


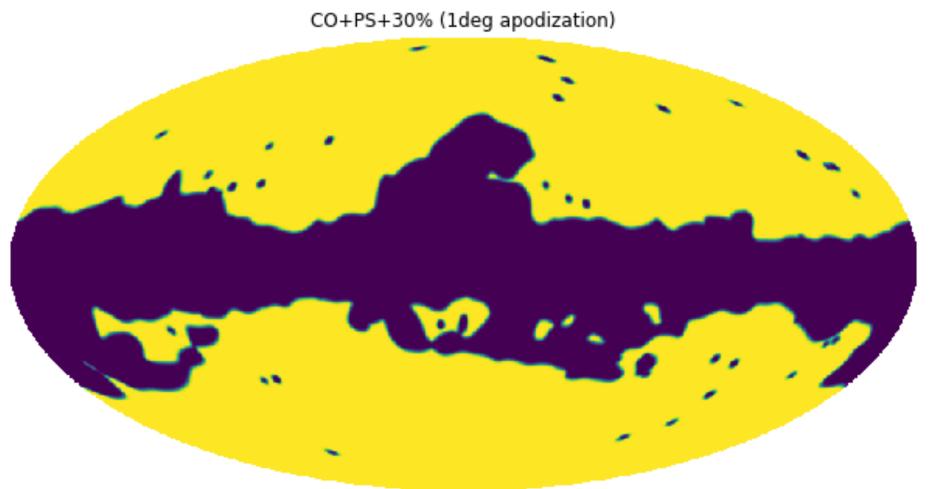


- Miscalibration angles make only small contributions thanks to the cancellation.
- $\beta = 0.34 \pm 0.09 \deg$
- $\chi^2 = 65.3$

Cosmic Birefringence fits well (WMAP+Planck)

Robust against the Galactic mask (62% of the sky)

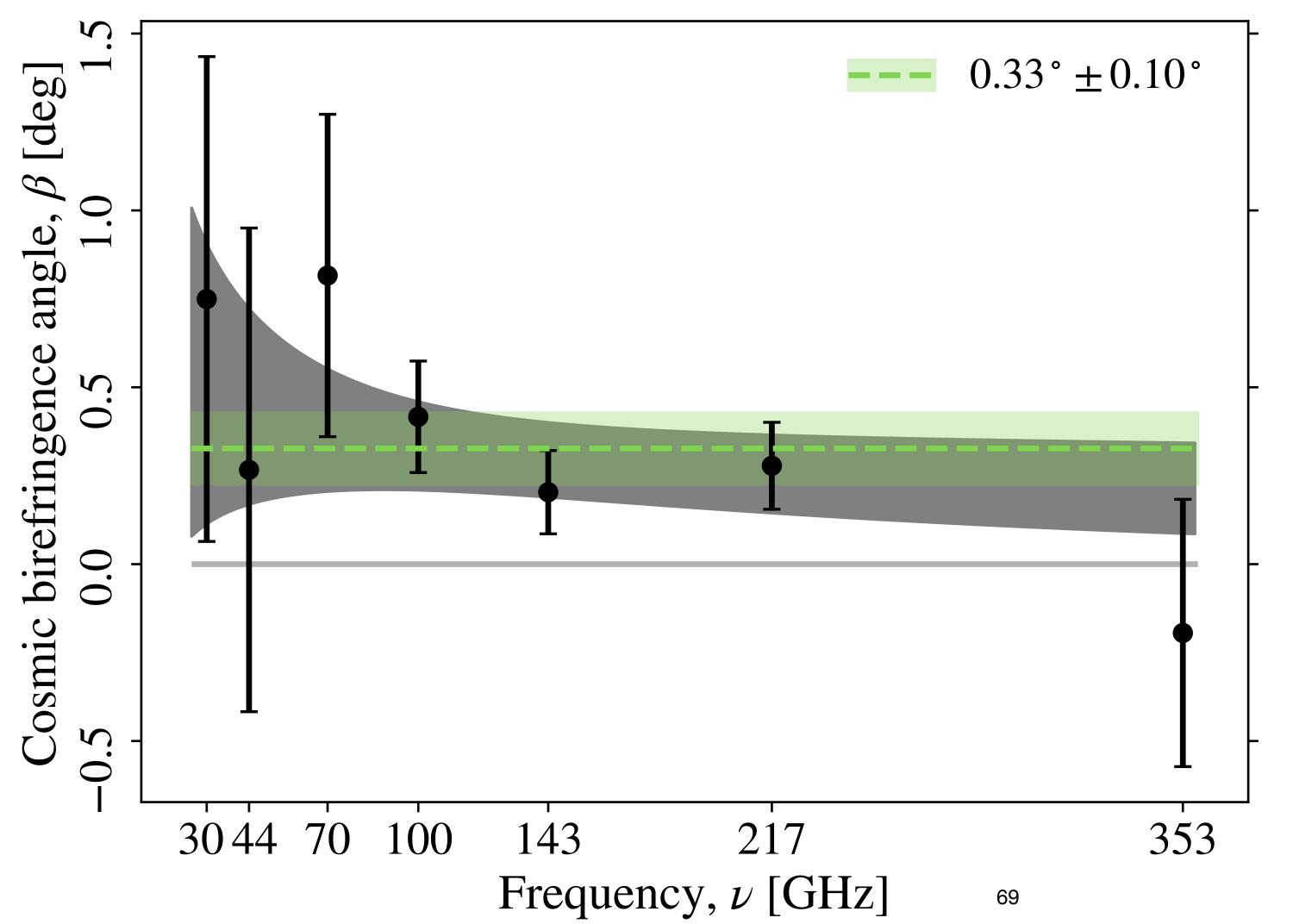




- Miscalibration angles make only small contributions thanks to the cancellation.
- $\beta = 0.37 \pm 0.14 \deg$
- $\chi^2 = 65.8$

No frequency dependence is found

Consistent with the expectation from cosmic birefringence



- Light traveling in a uniform magnetic field also experiences a rotation of the plane of linear polarization, called "Faraday rotation". However, the rotation angle depends on the frequency, as $\beta(\nu) \propto \nu^{-2}$.
- No evidence for frequency dependence is found!
 - For $\beta \propto \nu^n$, $n = -0.20^{+0.41}_{-0.39}$ (68% CL)
 - Faraday rotation (n = -2) is disfavoured.

Is \(\beta \) caused by non-cosmological effects?

We need to measure it in independent experiments.

- The known instrumental effects of the WMAP and Planck missions are shown to have negligible effects on β .
 - However, we can never rule out unknown instrumental effects... We need to measure β in independent experiments.
- The polarized Galactic foreground emission was used to calibrate the instrumental polarization angles, α. The intrinsic EB correlations of the Galactic foreground emission (polarized dust and synchrotron emission) could affect the results.
 - We need to measure β without relying on the foreground by calibrating α well, e.g., Cornelison et al. (BICEP3 Collab.), arXiv:2207.14796; Murphy et al. (ACT Collab.), arXiv:2403.00763.

Implications

DM = Dark Matter; DE = Dark Energy

This term exists for a pion.

What if DM/DE is "pion-like particle"

$$I = \int d^4x \sqrt{-g} \left[-\frac{1}{2} (\partial \chi)^2 - V(\chi) - \frac{1}{4} F^2 - \frac{\alpha}{4f} \chi F \tilde{F} \right]$$

• The measured angle, β, implies that the field has evolved by

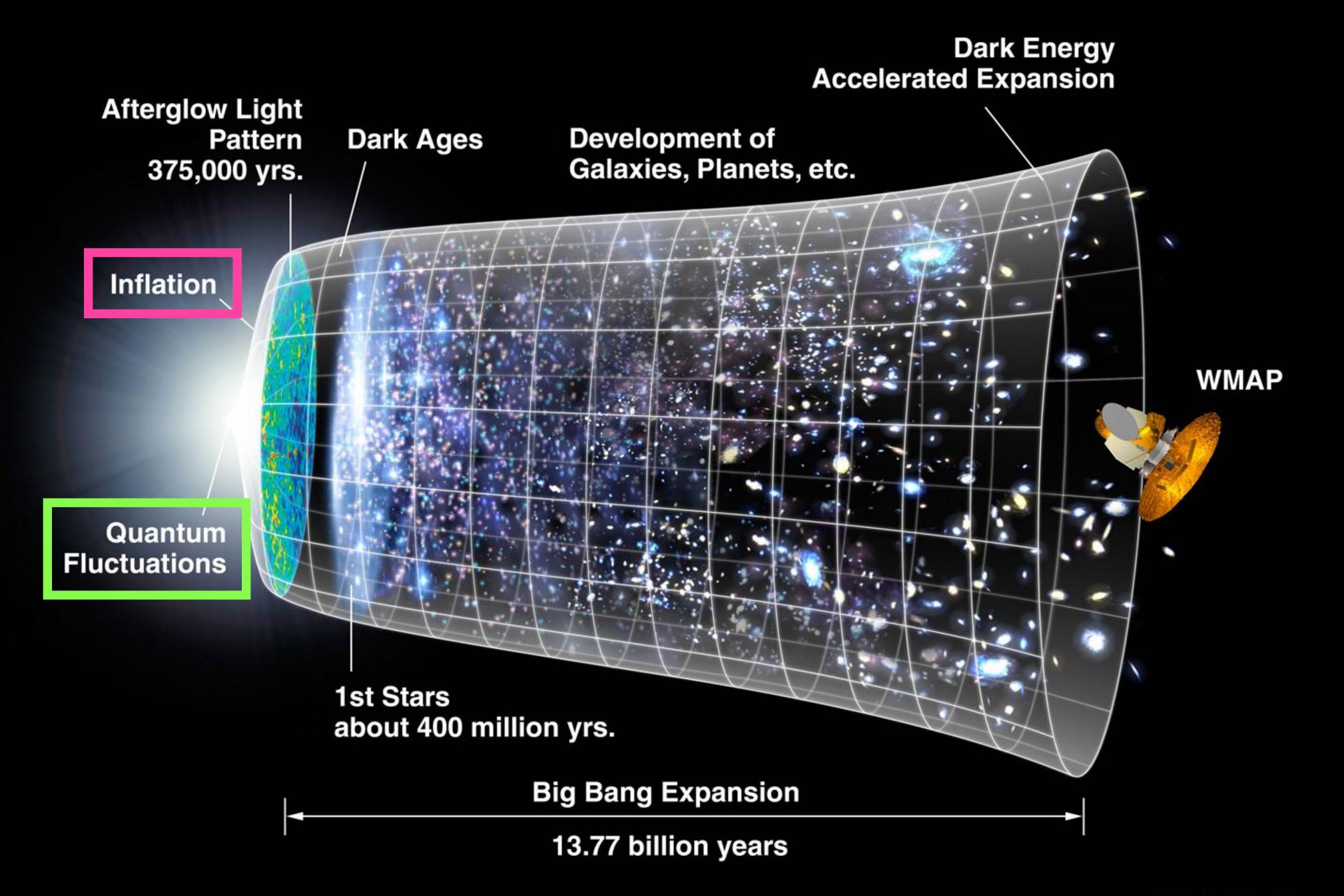
$$\Delta \chi = \chi(\tau_{\rm obs}) - \chi(\tau_{\rm em}) \simeq \frac{10^{-2}}{\alpha} f$$

- If it is due to DE: this measurement rules out DE being a cosmological constant.
- If it is due to DM: at least a fraction of DM violates parity symmetry.

Parity Violation during Cosmic Inflation

72

$$I_{\text{CS}} = \int \mathrm{d}^4 x \sqrt{-g} \left(-\frac{\alpha}{4f} \chi F \widetilde{F} \right) + \begin{cases} \mathbf{Scalar fluctuations} \\ \Box \chi - \frac{\partial V}{\partial \chi} = -\frac{\alpha}{f} \mathbf{E} \cdot \mathbf{B} \\ \mathbf{Gravitational waves} \\ \Box h_{ij} = 16\pi G (E_i E_j + B_i B_j)^{\text{TT}} \end{cases}$$



Cosmic Inflation: Key Features More than 40 years of research in a single slide

- Inflation is the period of accelerated expansion in the very early Universe.
 - If the distance between two points increases as a(t), $d^2a/dt^2 > 0$.

This is the definition of inflation.

- Primordial fluctuations are generated quantum mechanically.
 - Scalar modes: Density fluctuations -> The origin of all cosmic structure.
 - Tensor modes: Gravitational waves -> Yet to be discovered.
 - Vector modes: ?
- A New Paradigm: Sourced contributions (this talk)

Anber, Sorbo (2010); Barnaby, Peloso (2011); Sorbo (2011); Barnaby, Namba, Peloso (2011)

The full action

Observational consequences

$$I = I_{\text{inflation}}$$
 [no one understands this]

Similar phenomenology for non-Abelian gauge fields (Maleknejad et al.)

$$F\tilde{F} = F^a_{\mu\nu}F^{\mu\nu a}$$

$$+ \int d\tau d^3 \mathbf{x} \sqrt{-g} \left[\frac{R}{16\pi G} + \frac{\text{Gravitational waves}}{16\pi G} (E_i E_j + B_i B_j)^{\text{TT}} \right]$$

$$-\frac{1}{2}(\partial\chi)^2 - V(\chi)$$

Scalar fluctuations

$$-rac{1}{4}F^2-rac{lpha}{4f}\chi F ilde{F}$$

Parity violation in A_µ

A note on terminology

"Photons" = Massless spin-1 particles

- Since inflation occurred long before the electroweak symmetry breaking, "photons" as we know them did not exist during inflation.
- We should think of them more generally as "massless spin-1 particles".

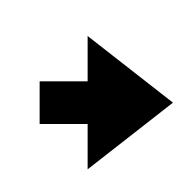
Gravitational waves

$$\Box h_{ij} = 16\pi G (E_i E_j + B_i B_j)^{\mathrm{TT}}$$

Scalar fluctuations

$$\Box \chi - \frac{\partial V}{\partial \chi} = -\frac{\alpha}{f} \mathbf{E} \cdot \mathbf{B}$$

Spin-1 sources, which violate parity symmetry due to the Chern-Simons term.



Non-Gaussian and parityviolating gravitational waves and scalar fluctuations!

Particle production due to xFF during inflation

Kinetic energy of χ is used to produce massless spin-1 particles

$$A''_\pm + \omega_\pm^2 A_\pm = 0$$
 where $egin{cases} \omega_\pm^2 = k^2 \mp rac{2k\xi}{- au} \ \xi = rac{lphaar{\chi}}{2fH} & (-\infty < au < 0) \end{cases}$

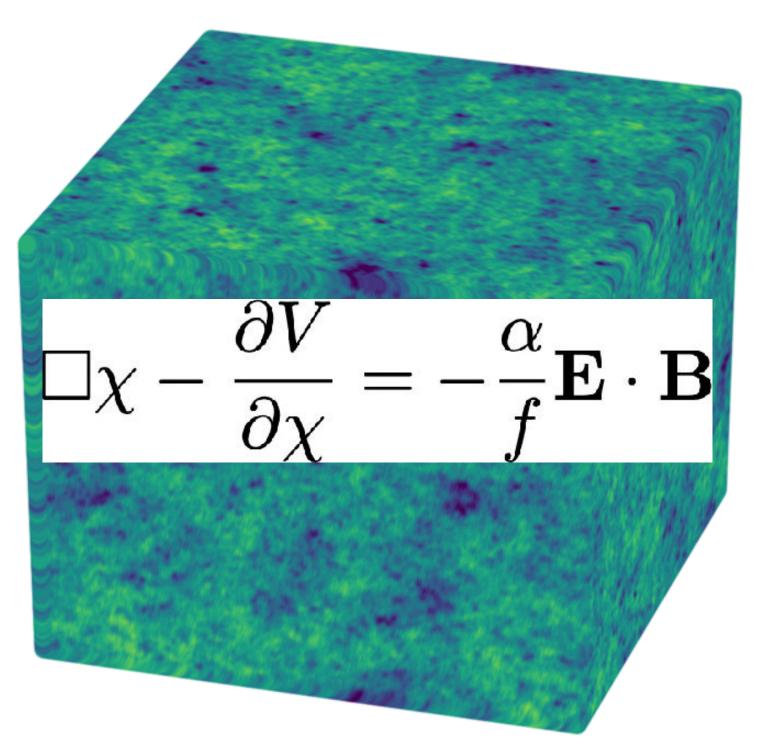
- Instability occurs when $\omega_+^2 < 0$ or $\omega_-^2 < 0$. In other words, $-k\tau < 2 |\xi|$.
 - The mode function for one of the helicity states is amplified on large scales (small - $k\tau$) relative to the vacuum solution, $e^{-ik\tau}/\sqrt{2k}$.
 - The right-handed (+ helicity) state is amplified for ξ >0, whereas the left-handed (- helicity) state remains close to the vacuum solution.
 - Parity violation!

Truly ab initio simulation!

World's first lattice simulation of inflation

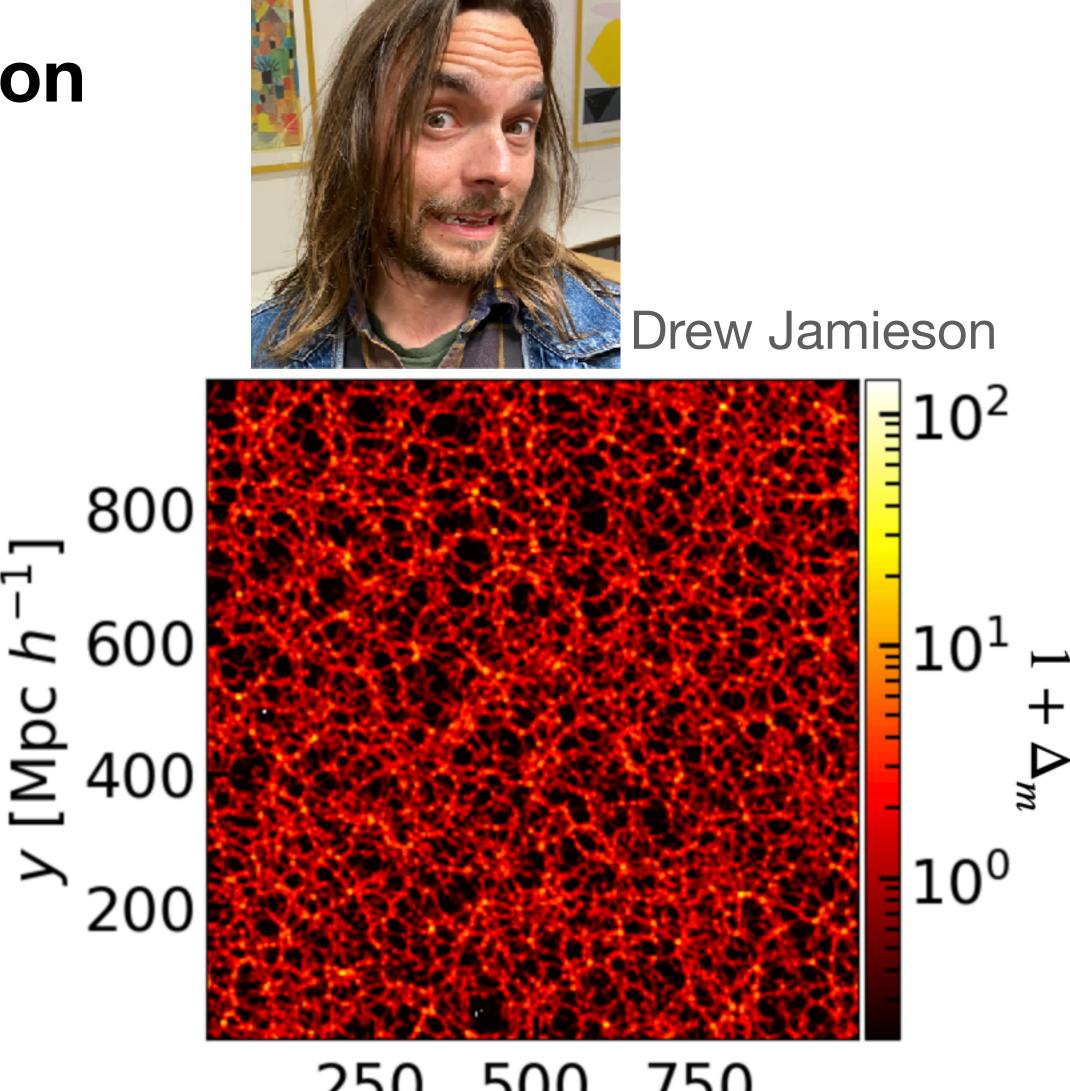


Angelo Caravano





• (Right) Outcome of N-body simulation at z=0, using the left panel as the initial condition.



250 500 750 x [Mpc h^{-1}]

GR + Maxwell (+ Chern-Simons) $\Box = \frac{1}{\sqrt{-g}} \partial_{\mu} (\sqrt{-g} g^{\mu\nu} \partial_{\nu})$ $= \frac{1}{a^2} \left(-\frac{\partial^2}{\partial \tau^2} - 2\frac{a'}{a} \frac{\partial}{\partial \tau} + \nabla^2 \right)$

$$\Box = \frac{1}{\sqrt{-g}} \partial_{\mu} (\sqrt{-g} g^{\mu\nu} \partial_{\nu})$$

$$= \frac{1}{a^2} \left(-\frac{\partial^2}{\partial \tau^2} - 2 \frac{a'}{a} \frac{\partial}{\partial \tau} + \nabla^2 \right)$$

where $g^{\mu\nu}=a^{-2}\mathrm{diag}(-1,\mathbf{1})$

$$I = \int d\tau d^3 \mathbf{x} \sqrt{-g} \left(\frac{R}{16\pi G} - \frac{1}{4}F^2 - \frac{\alpha}{4f} \chi F \tilde{F} \right)^{\sqrt{-g} = a^4}$$

• The F² term contributes to the equation of motion for the GW via the stressenergy tensor (this is the second-order fluctuation).

$$\Box h_{ij} = 16\pi G (E_i E_j + B_i B_j)^{\mathrm{TT}}$$
 "Transverse and Traceless"

- The FF term does **not** contribute directly to the equation of motion for the GW.
 - But, it creates a parity violation in **E** and **B**, which also creates a parity violation in the GW.

Helicity basis to probe parity symmetry

Circular polarization states of GW. GW's helicity is $\lambda = \pm 2$.

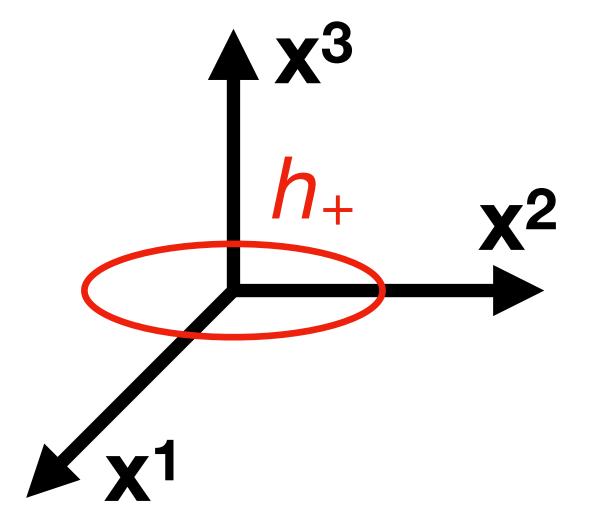
Just like for EM waves,

$$A_{\pm} = \frac{A_{\mathbf{k}}^1 \mp iA_{\mathbf{k}}^2}{\sqrt{2}}$$

$$A_{f k}^1 \mp i A_{f k}^2 \ ar{\lambda}_{-:} ext{Left-handed state} \ A_{-:} ext{Left-handed state}$$

we write the helicity states of GW in Fourier space as

$$h_{\pm 2}=rac{h_{+,\mathbf{k}}\mp ih_{ imes,\mathbf{k}}}{\sqrt{2}}$$
 h_{+2} : Right-handed state h_{-2} : Left-handed state



Parity Violation in GW

For a slowly varying $\xi>0$

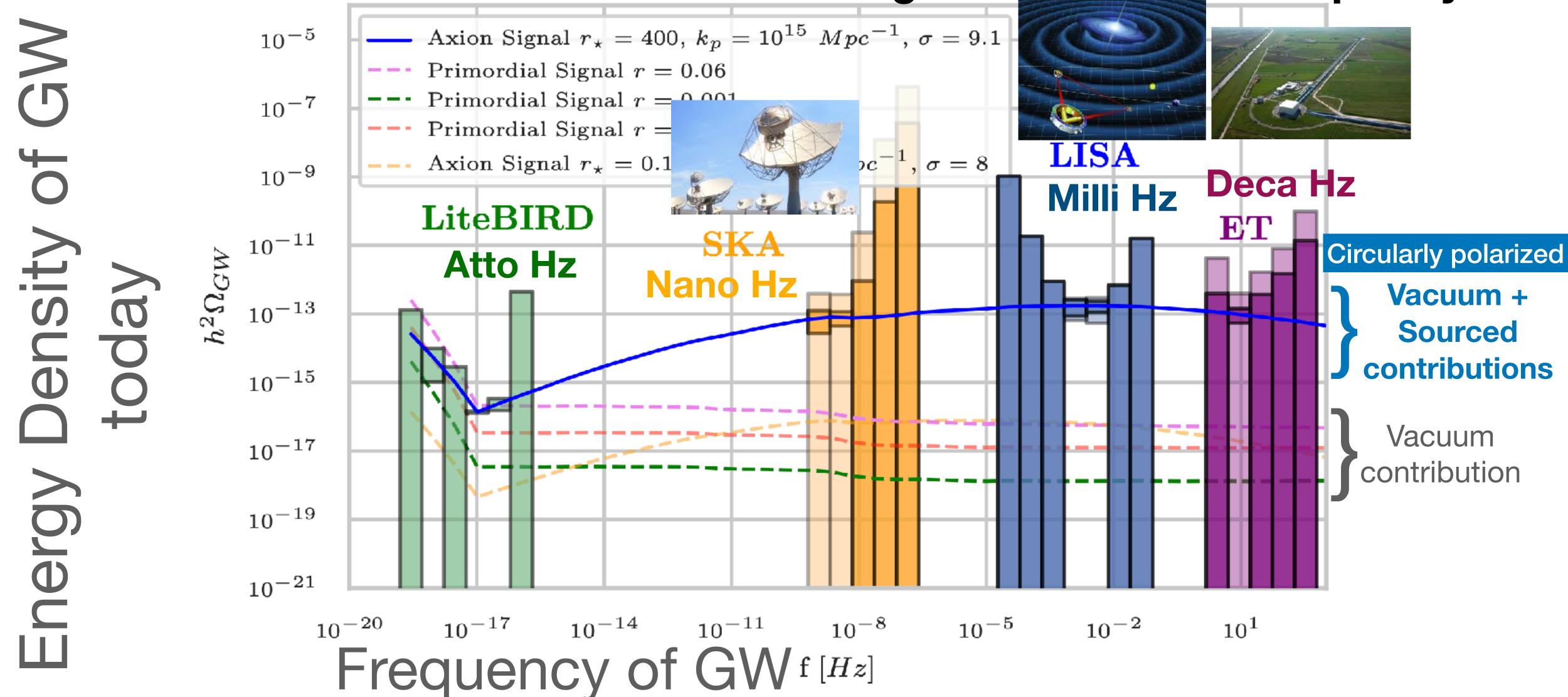
$$\xi = rac{lpha ar{ heta}}{2H} = rac{lpha \dot{ar{\chi}}}{2Hf}$$

$$\begin{split} \frac{k^3 P_{+2}(k)}{2\pi^2} &\simeq \frac{2}{M_{\rm Pl}^2} \left(\frac{H}{2\pi}\right)^2 \begin{bmatrix} 1 + 8.6 \times 10^{-7} \frac{H^2}{M_{\rm Pl}^2} \frac{e^{4\pi\xi}}{\xi^6} \end{bmatrix} \\ \frac{k^3 P_{-2}(k)}{2\pi^2} &\simeq \frac{2}{M_{\rm Pl}^2} \left(\frac{H}{2\pi}\right)^2 \begin{bmatrix} 1 + 8.6 \times 10^{-7} \frac{H^2}{M_{\rm Pl}^2} \frac{e^{4\pi\xi}}{\xi^6} \end{bmatrix} \end{split}$$

- The sourced contributions are almost perfectly circularly polarized.
- The sum of the vacuum and sourced contributions is partially circularly polarized. **This can be observationally tested!** (Seto 2006; Seto, Taruya 2007)

GWs from the early Universe are everywhere!

We can measure it across 21 orders of magnitude in the GW frequency



Experimental Strategy Commonly Assumed So Far

- 1. Detect CMB polarization in multiple frequencies, to make sure that it is from the CMB (i.e., Planck spectrum)
- 2. Check for scale invariance: Consistent with a scale invariant spectrum?
 - Yes => Announce discovery of the vacuum fluctuation in spacetime
 - No => WTF?

New Experimental Strategy: New Standard!

- 1. Detect CMB polarization in multiple frequencies, to make sure that it is from the CMB (i.e., Planck spectrum)
- 2. Check for scale invariance: Consistent with a scale invariant spectrum?
- 3. Parity violating correlations consistent with zero?
- 4. Consistent with Gaussianity?
- If, and ONLY IF Yes to all => Announce discovery of the vacuum fluctuation in spacetime

If not, you may have just discovered new physics during inflation!

- 2. Check for scale invariance: Consistent with a scale invariant spectrum?
- 3. Parity violating correlations consistent with zero?
- 4. Consistent with Gaussianity?

1. D€

• If, and ONLY IF Yes to all => Announce discovery of the vacuum fluctuation in spacetime

Summary

Let's find new physics!

- Violation of parity symmetry is a new topic in cosmology.
- It may hold the answers to fundamental questions, such as
 - What is Dark Matter and Dark Energy?
 - What is the fundamental physics behind cosmic inflation?
- Rich phenomenology of Chern-Simons term: $I_{\rm CS} = \int {\rm d}^4 x \sqrt{-g} \left[-\frac{\alpha}{4f} \chi F \widetilde{F} \right]$
 - Cosmic birefringence 3.6σ hint of the signal

Abelian and non-Abelian gauge fields; Gravitational CS; ...

- Parity-violating and non-Gaussian gravitational waves and scalar fluctuations
- What else should we look at? New and great topics of research.

