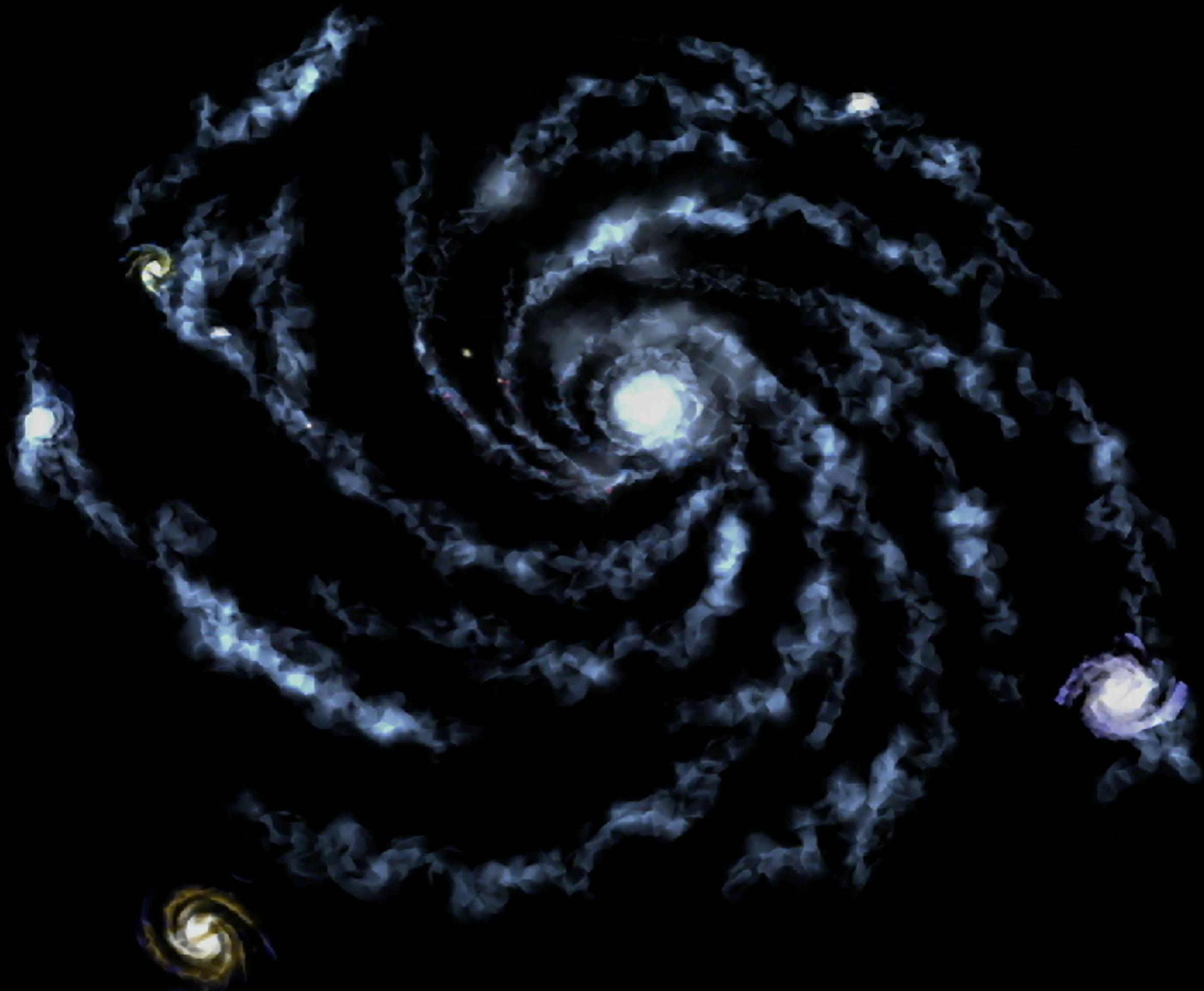
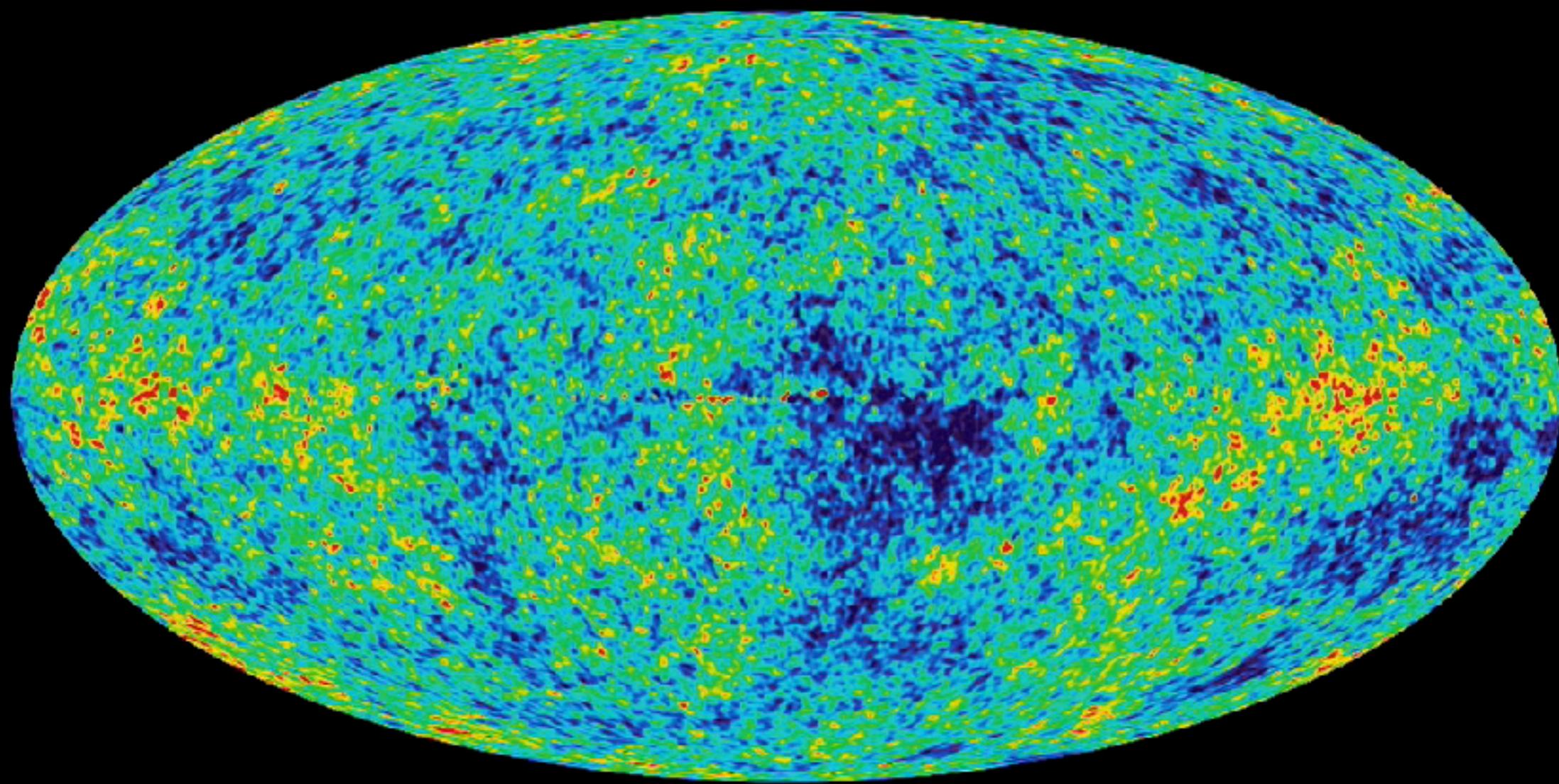


# Finding Cosmic Inflation

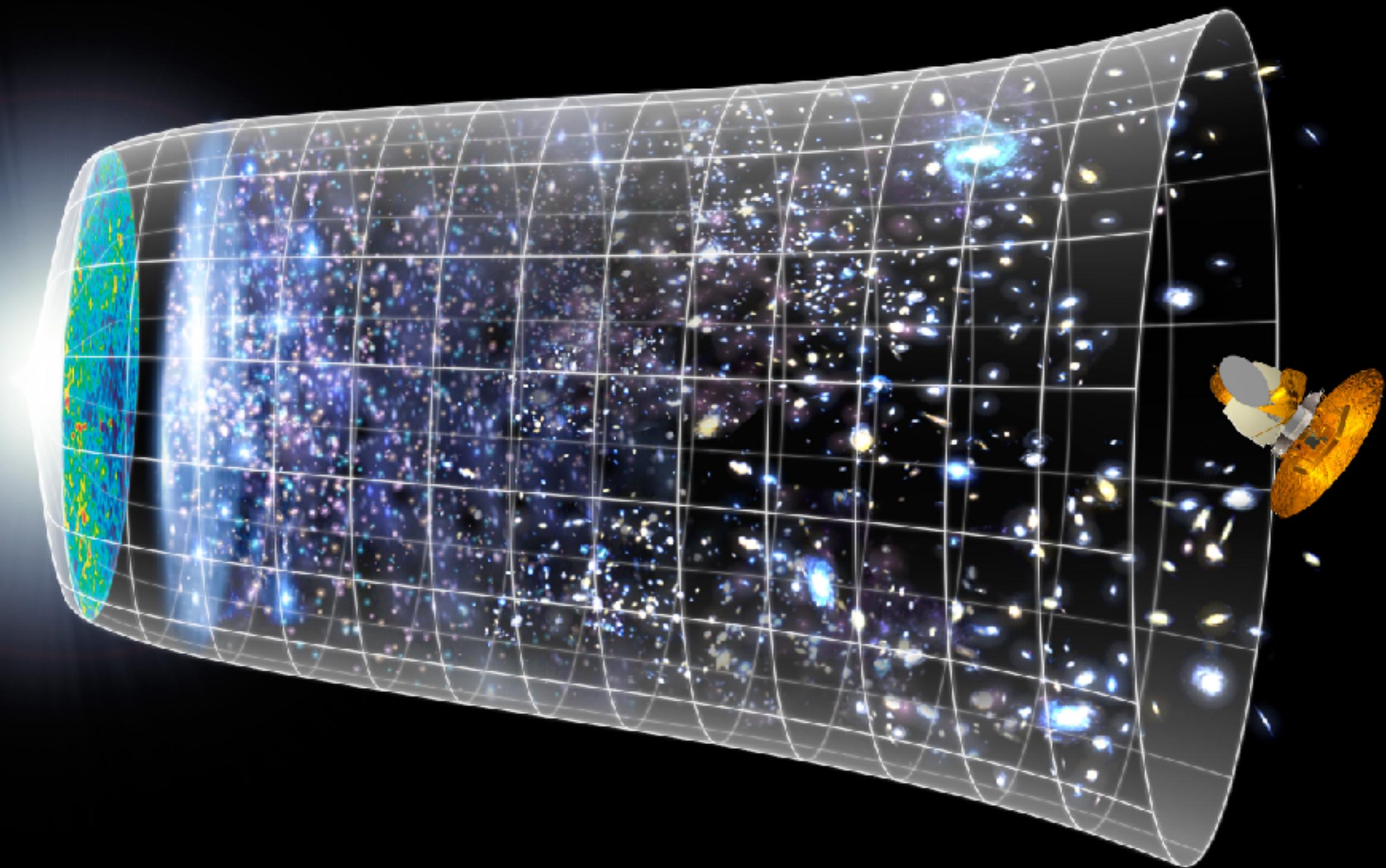
Eiichiro Komatsu  
(MPI für Astrophysik)  
LAM Seminar, April 6, 2018





# A Remarkable Story

- Observations of the cosmic microwave background and their interpretation taught us that **galaxies, stars, planets, and ourselves originated from tiny fluctuations in the early Universe**
- *But, what generated the initial fluctuations?*



Full-dome movie for planetarium  
Director: Hiromitsu Kohsaka

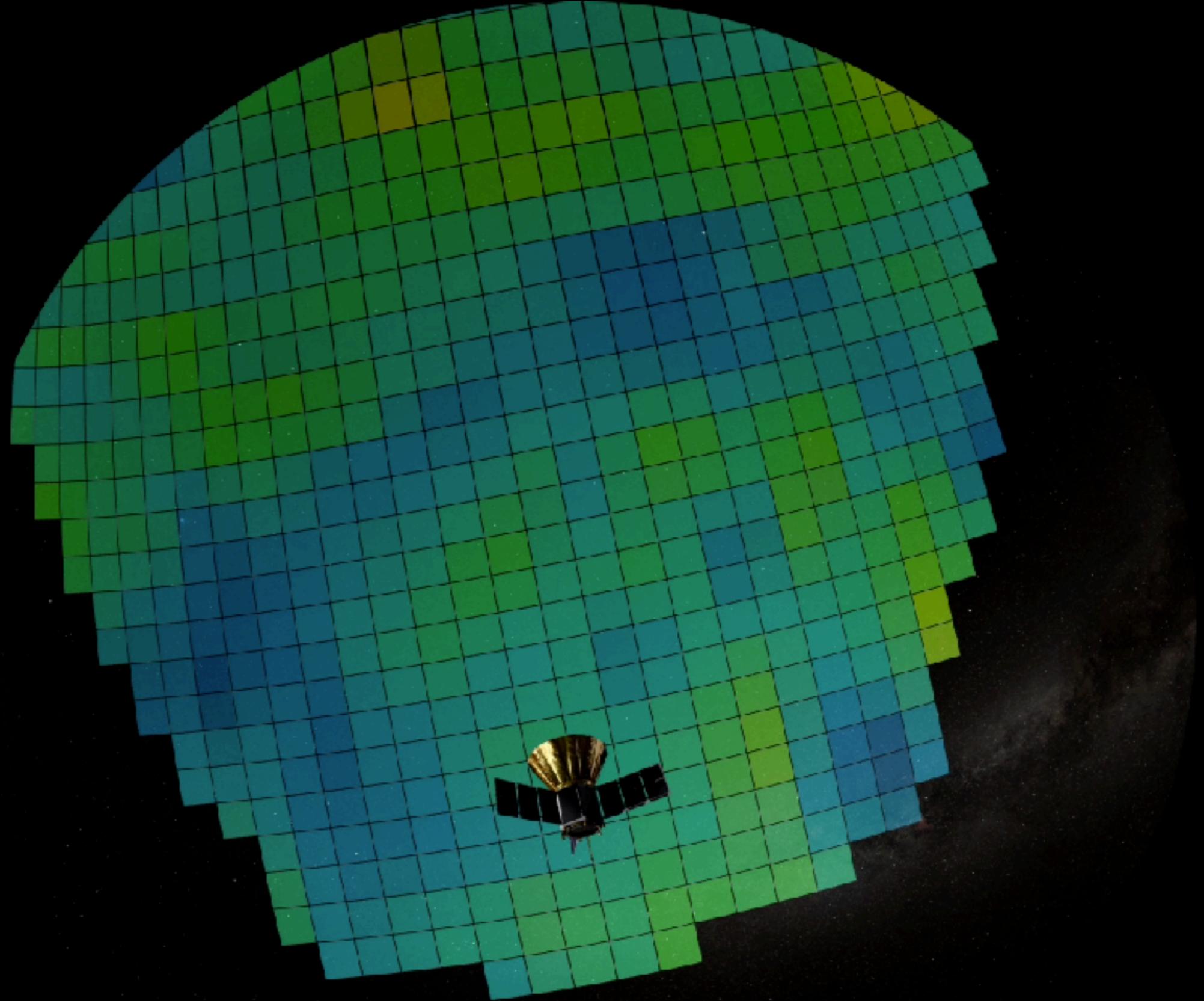
# HORIZON

Beyond the Edge of the Visible Universe

▶ ⏩ 🔊 2:28 / 2:51

⚙️ HD 📺 🗉

HORIZON :Beyond the Edge of the Visible Universe [Trailer]

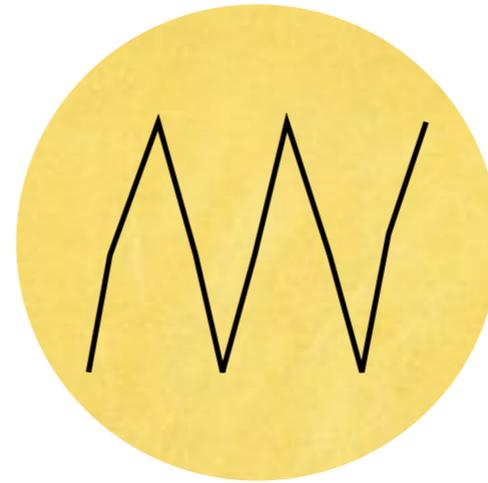


# Leading Idea

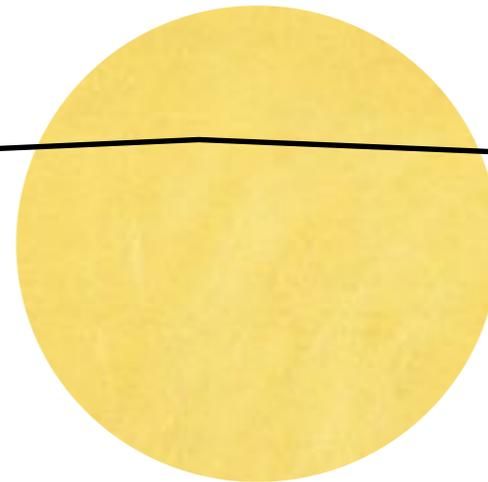
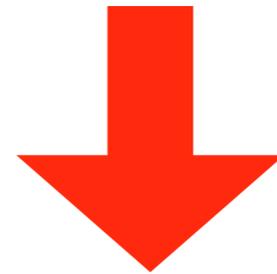
- Quantum mechanics at work in the early Universe
  - “*We all came from quantum fluctuations*”
- But, how did quantum fluctuations on the *microscopic* scales become *macroscopic* fluctuations over large distances?
  - What is the **missing link** between small and large scales?

# Cosmic Inflation

Quantum fluctuations on  
microscopic scales



Inflation!



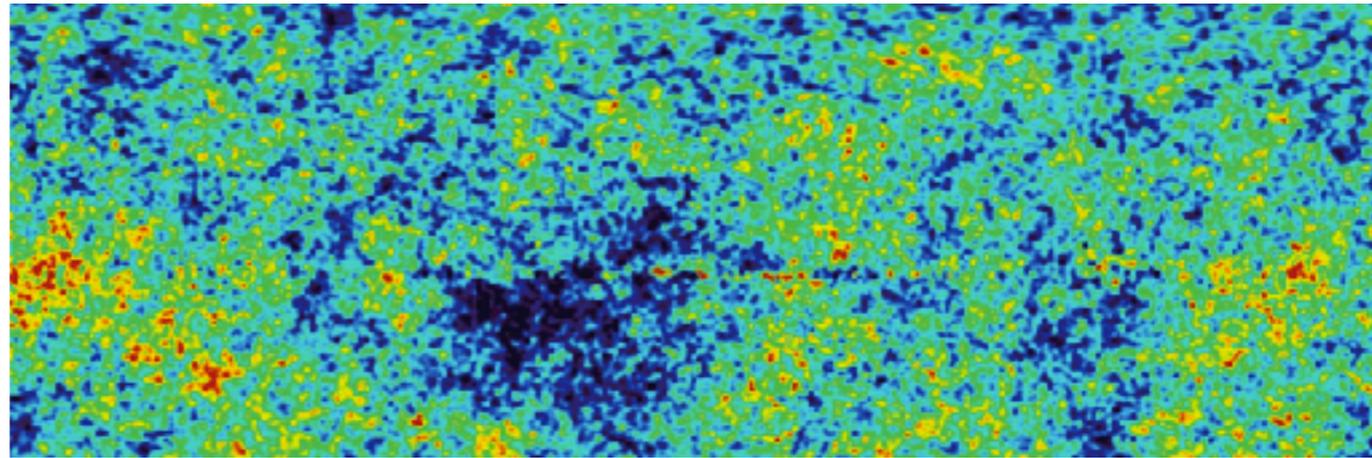
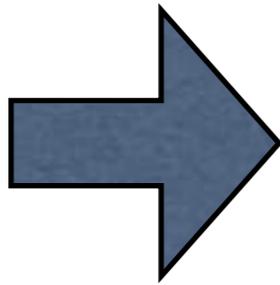
- Exponential expansion (inflation) stretches the wavelength of quantum fluctuations to cosmological scales

# Key Predictions

 $\zeta$ 

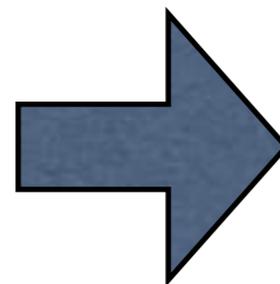
scalar  
mode

- Fluctuations we observe today in CMB and the matter distribution originate from quantum fluctuations during inflation

 $h_{ij}$ 

tensor  
mode

- There should also be *ultra long-wavelength* gravitational waves generated during inflation



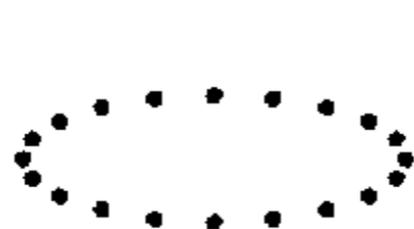
*Starobinsky (1979)*

# We measure distortions in space

- A distance between two points in space

$$d\ell^2 = a^2(t) [1 + 2\zeta(\mathbf{x}, t)] [\delta_{ij} + h_{ij}(\mathbf{x}, t)] dx^i dx^j$$

- $\zeta$ : “curvature perturbation” (scalar mode)
  - Perturbation to the determinant of the spatial metric
- $h_{ij}$ : “gravitational waves” (tensor mode)
  - Perturbation that does not alter the determinant



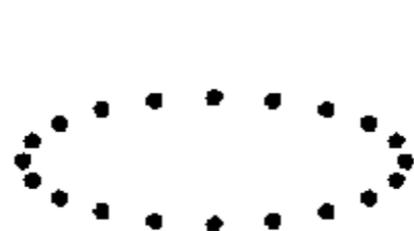
$$\sum_i h_{ii} = 0$$

# We measure distortions in space

- A distance between two points in space

$$d\ell^2 = \underbrace{a^2(t)}_{\text{scale factor}} [1 + 2\zeta(\mathbf{x}, t)] [\delta_{ij} + h_{ij}(\mathbf{x}, t)] dx^i dx^j$$

- $\zeta$ : “curvature perturbation” (scalar mode)
  - Perturbation to the determinant of the spatial metric
- $h_{ij}$ : “gravitational waves” (tensor mode)
  - Perturbation that does not alter the determinant



$$\sum_i h_{ii} = 0$$

# Finding Inflation

- Inflation is the **accelerated**, quasi-exponential expansion. Defining the Hubble expansion rate as  **$H(t)=d\ln(a)/dt$** , we must find

$$\frac{\ddot{a}}{a} = \dot{H} + H^2 > 0 \quad \longrightarrow \quad \epsilon \equiv -\frac{\dot{H}}{H^2} < 1$$

- For inflation to explain flatness of spatial geometry of our observable Universe, we need to have a **sustained** period of inflation. This implies  $\epsilon=O(N^{-1})$  or smaller, where  $N$  is the number of e-folds of expansion counted from the end of inflation:

$$N \equiv \ln \frac{a_{\text{end}}}{a} = \int_t^{t_{\text{end}}} dt' H(t') \approx 50$$

# Have we found inflation?

- *Have we found  $\varepsilon \ll 1$ ?*

$$\varepsilon \equiv -\frac{\dot{H}}{H^2}$$

- To achieve this, we need to map out **H(t)**, and show that it does not change very much with time
  - **We need the “Hubble diagram” during inflation!**

# Fluctuations are proportional to H

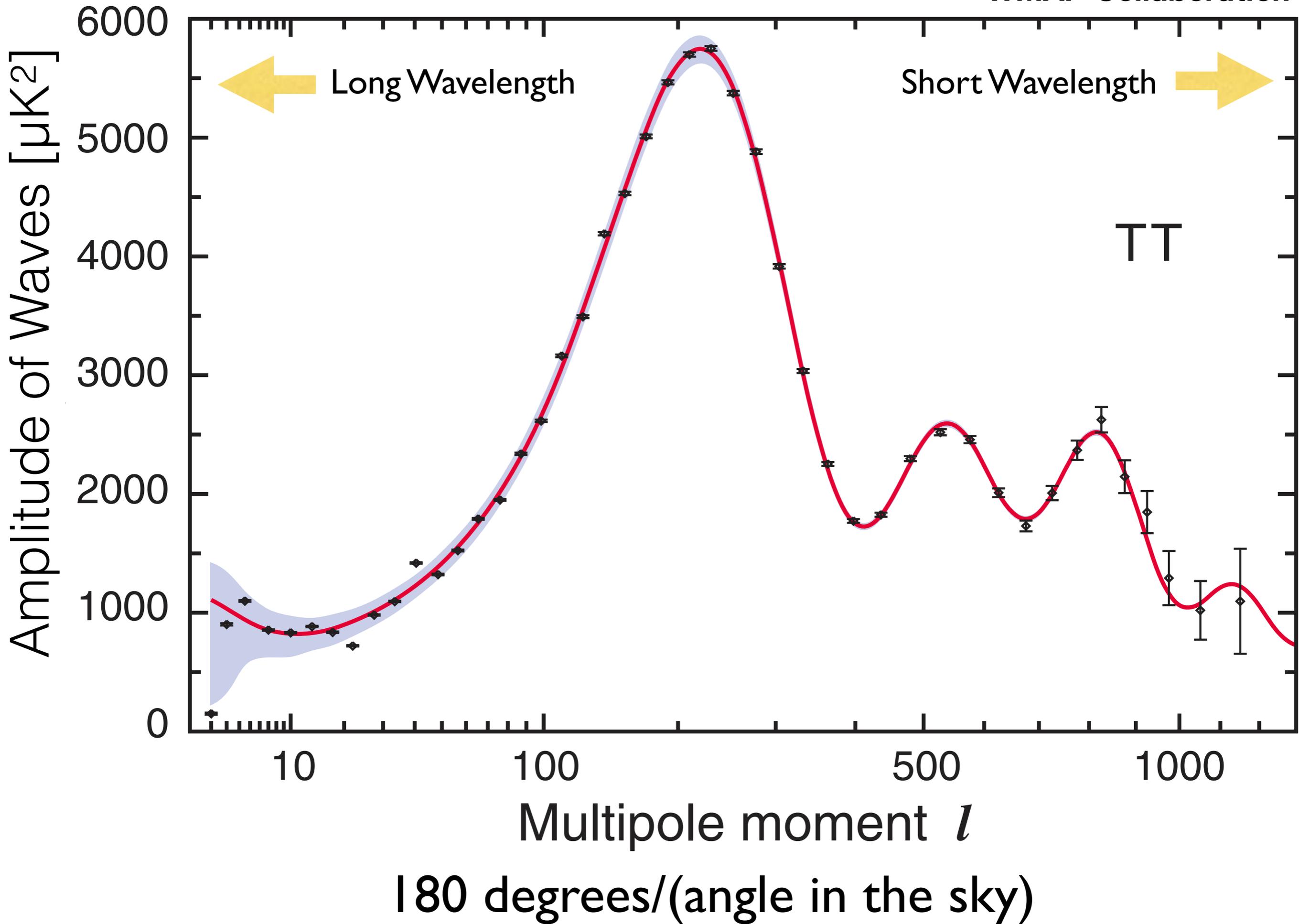
- Both scalar ( $\zeta$ ) and tensor ( $h_{ij}$ ) perturbations are proportional to H
- Consequence of the uncertainty principle
  - [energy you can borrow]  $\sim$  [time you borrow] $^{-1} \sim H$
- **THE KEY:** The earlier the fluctuations are generated, the more its wavelength is stretched, and thus the bigger the angles they subtend in the sky. **We can map H(t) by measuring CMB fluctuations over a wide range of angles**

# Fluctuations are proportional to $H$

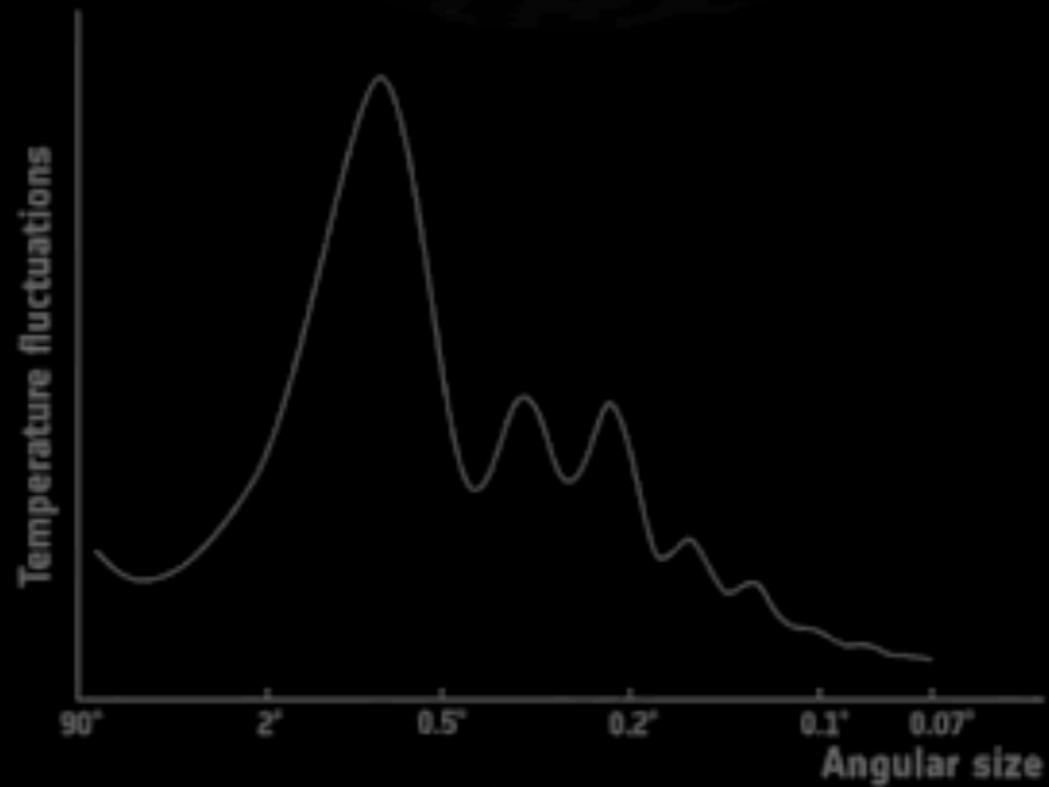
- **We can map  $H(t)$  by measuring CMB fluctuations over a wide range of angles**
  1. We want to show that the amplitude of CMB fluctuations does not depend very much on angles
  2. Moreover, since inflation must end,  $H$  would be a decreasing function of time. It would be fantastic to show that the amplitude of CMB fluctuations actually **DOES** depend on angles such that the small scale has ***slightly*** smaller power

# Data Analysis

- Decompose temperature fluctuations in the sky into a set of waves with various wavelengths
- Make a diagram showing the strength of each wavelength



# Power spectrum, explained

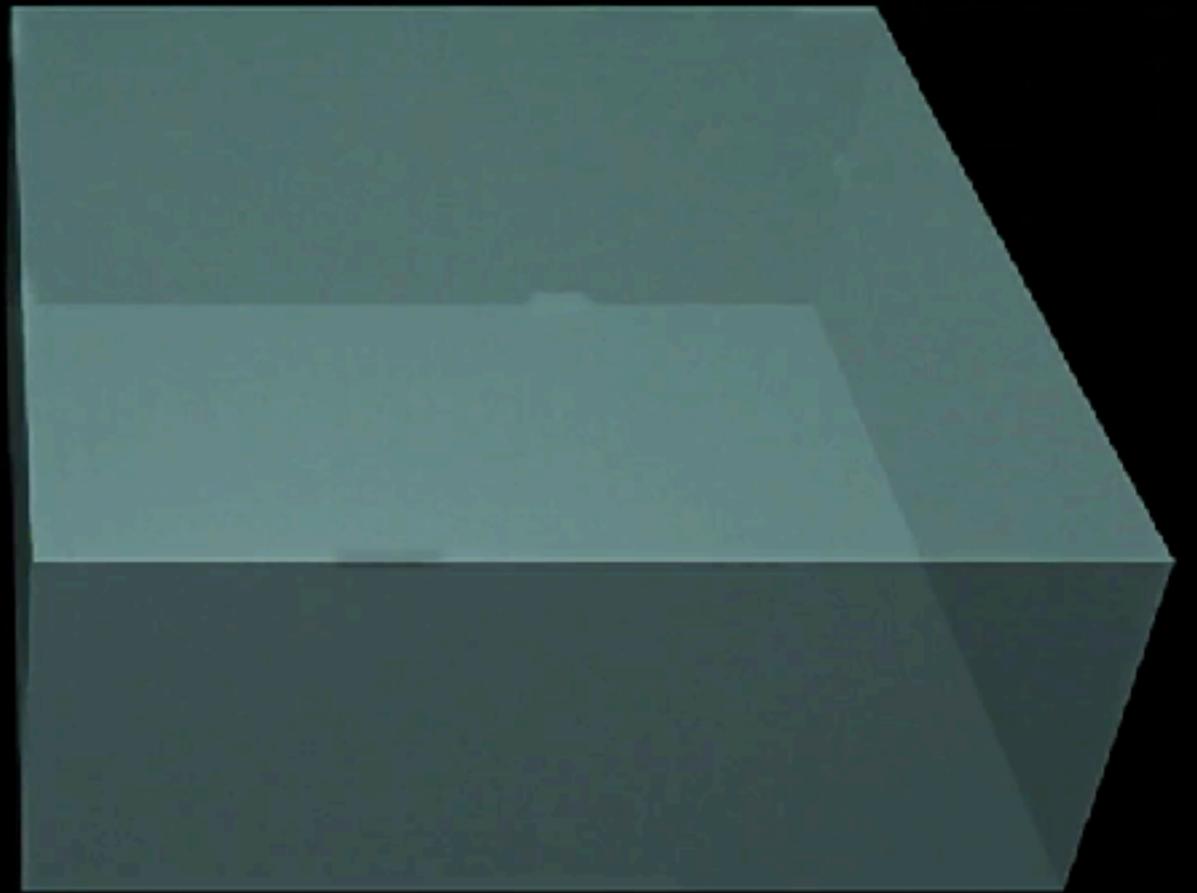
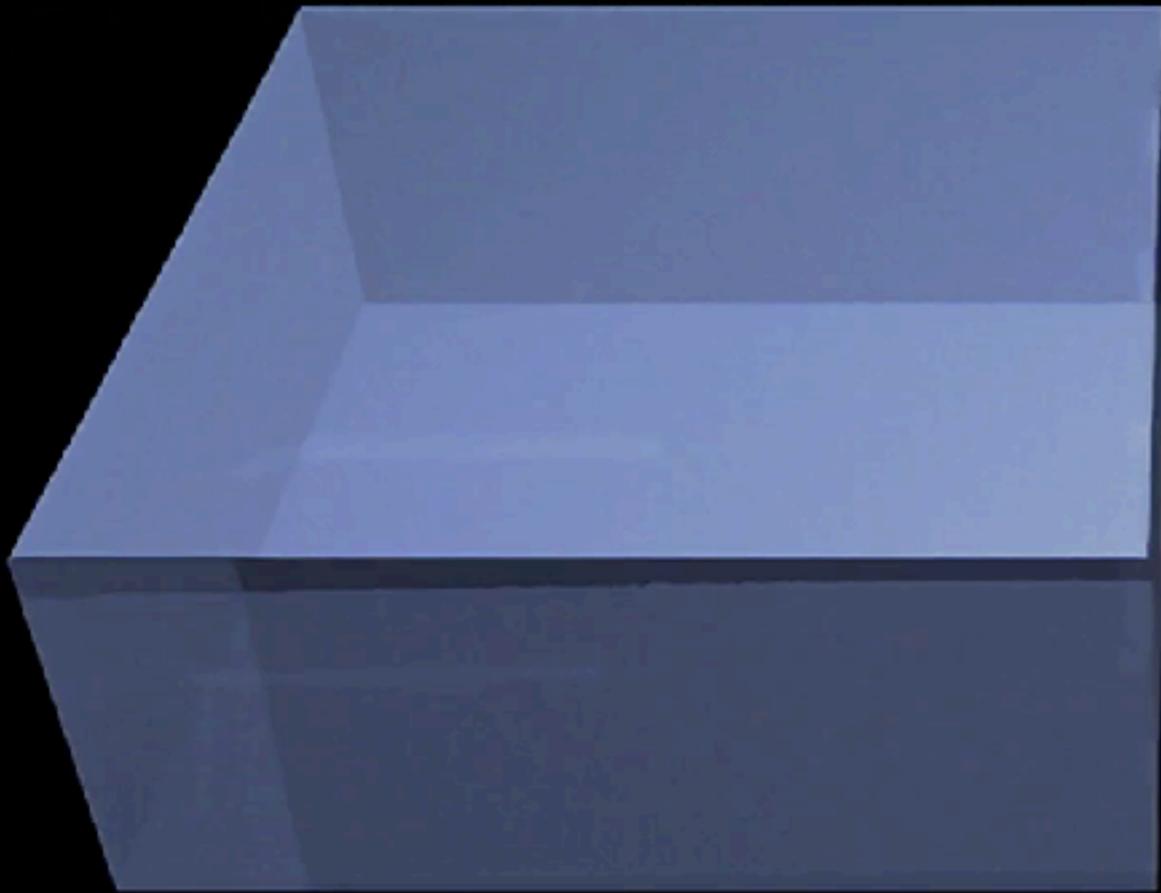




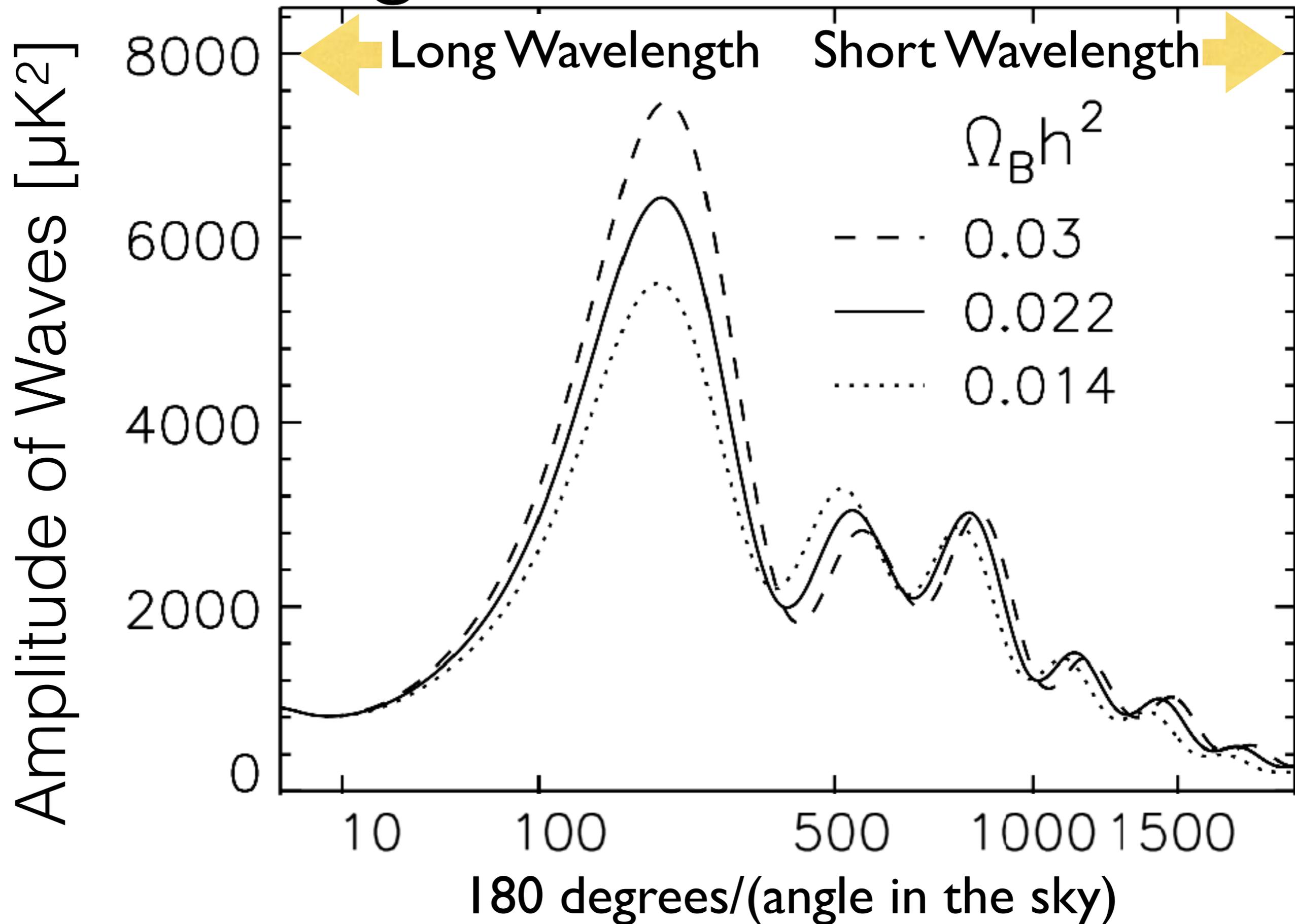


# Soupe Miso Cosmique

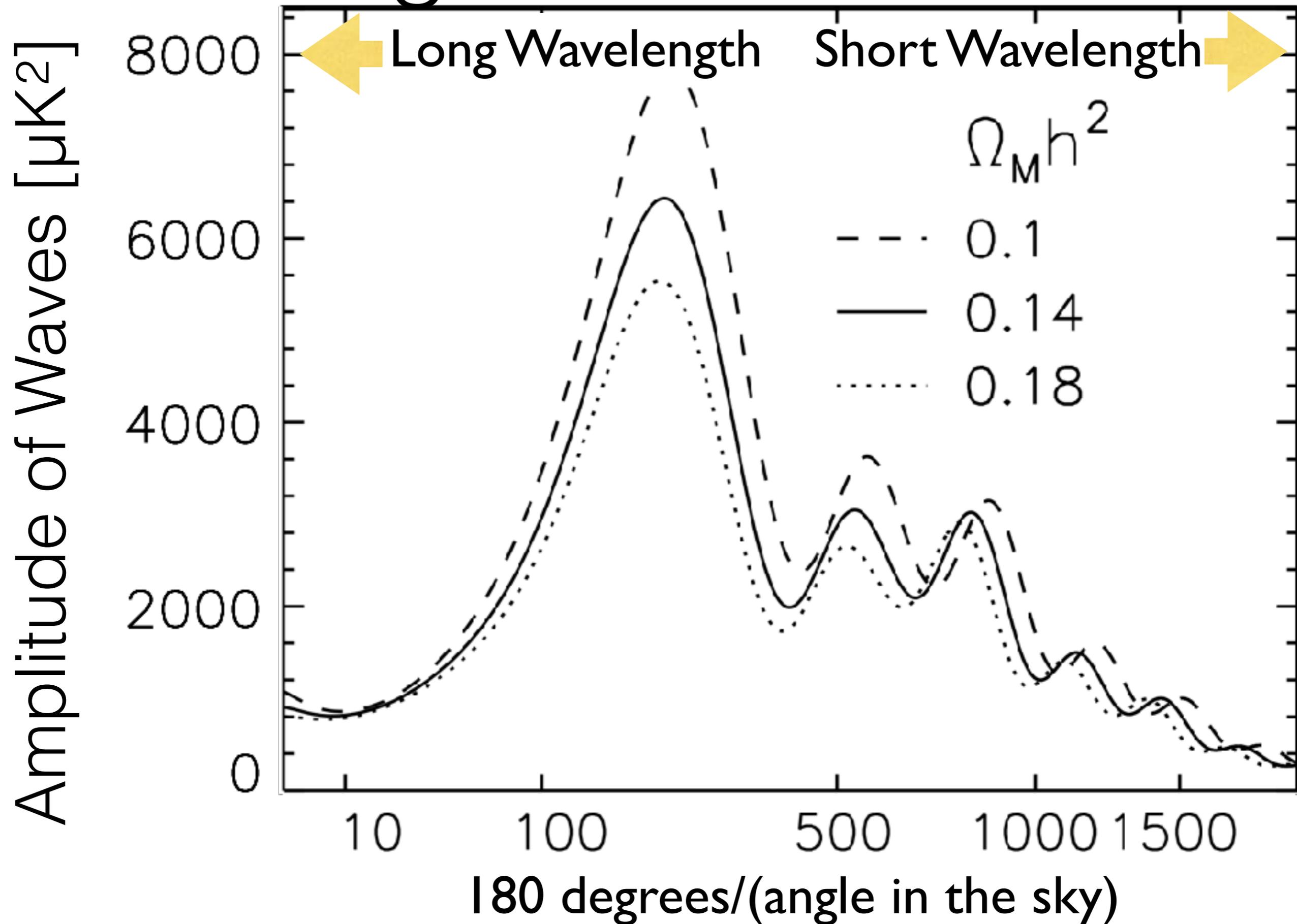
- When matter and radiation were hotter than 3000 K, matter was completely ionised. The Universe was filled with plasma, which behaves just like a soup
- Think about a Miso soup (if you know what it is). Imagine throwing Tofus into a Miso soup, while changing the density of Miso
- And imagine watching how ripples are created and propagate throughout the soup



# Measuring Abundance of H&He

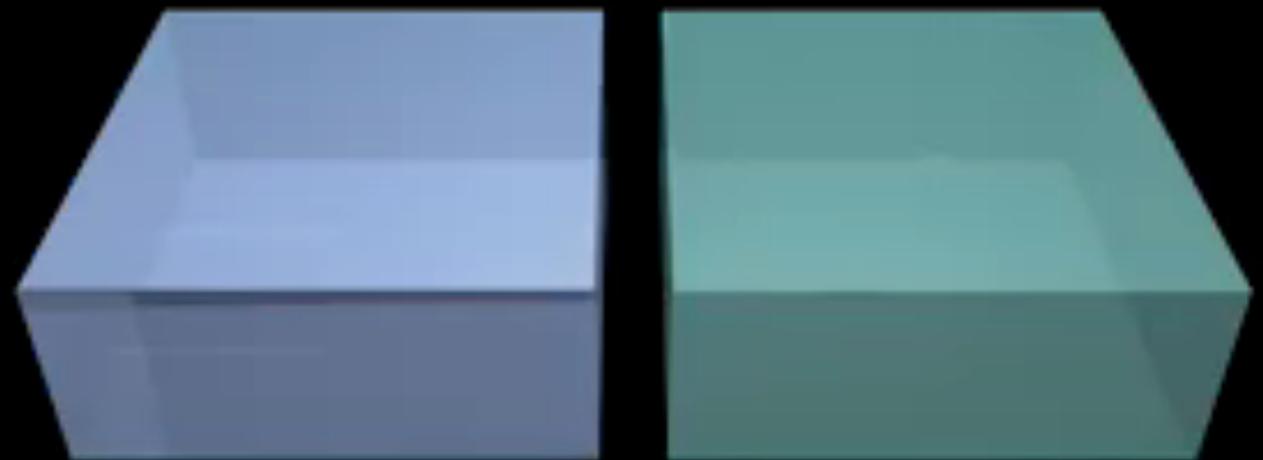


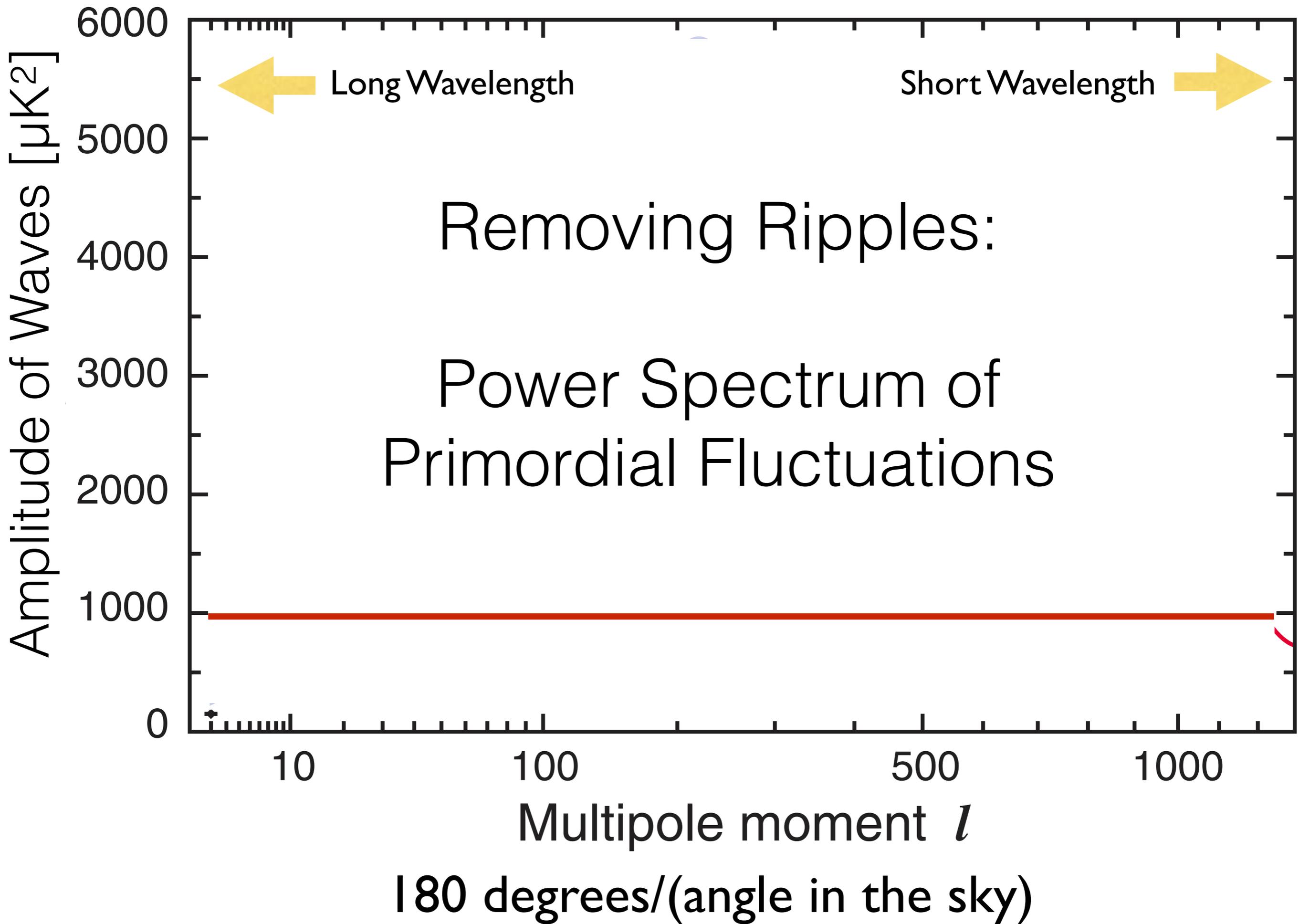
# Measuring Total Matter Density

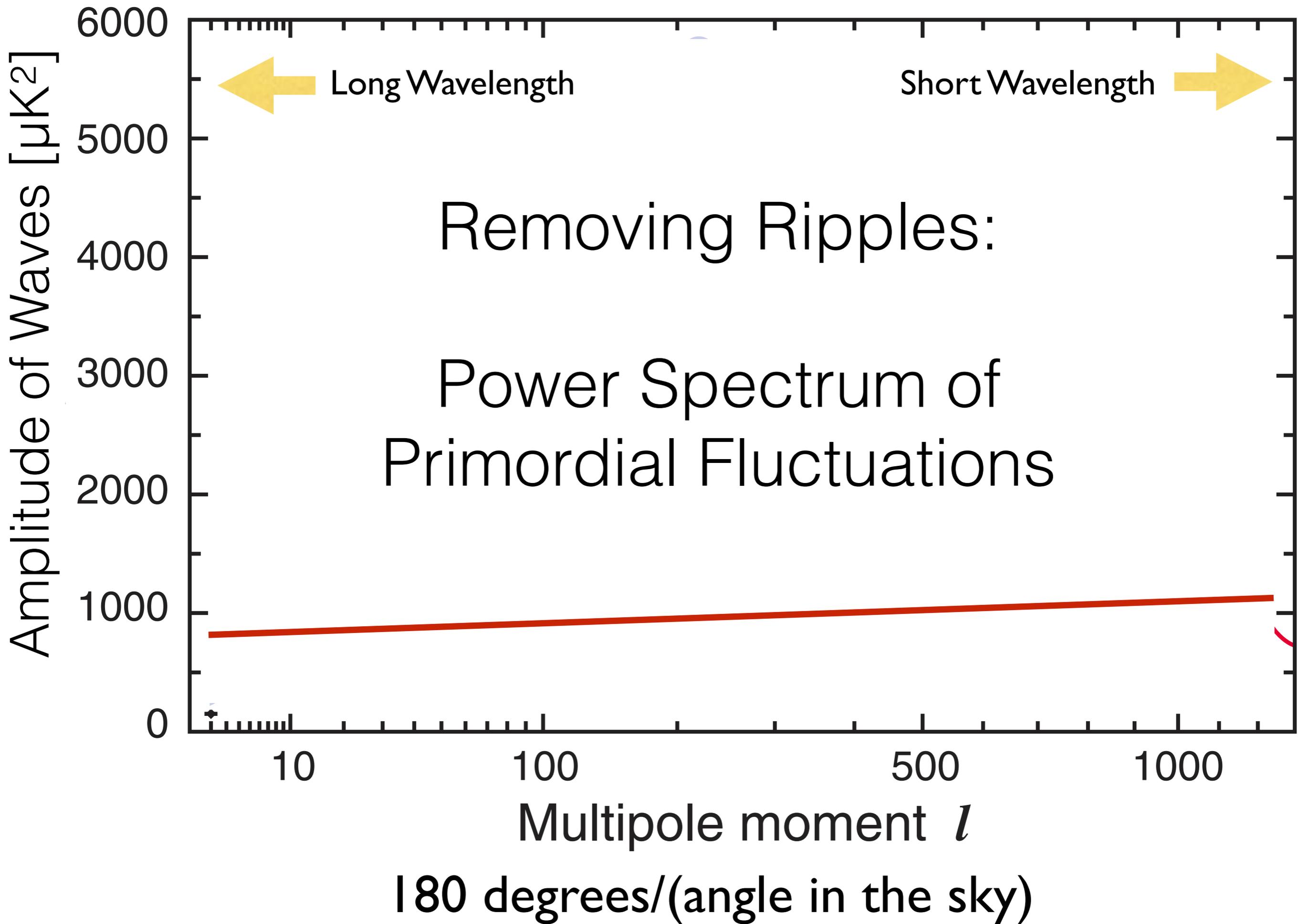


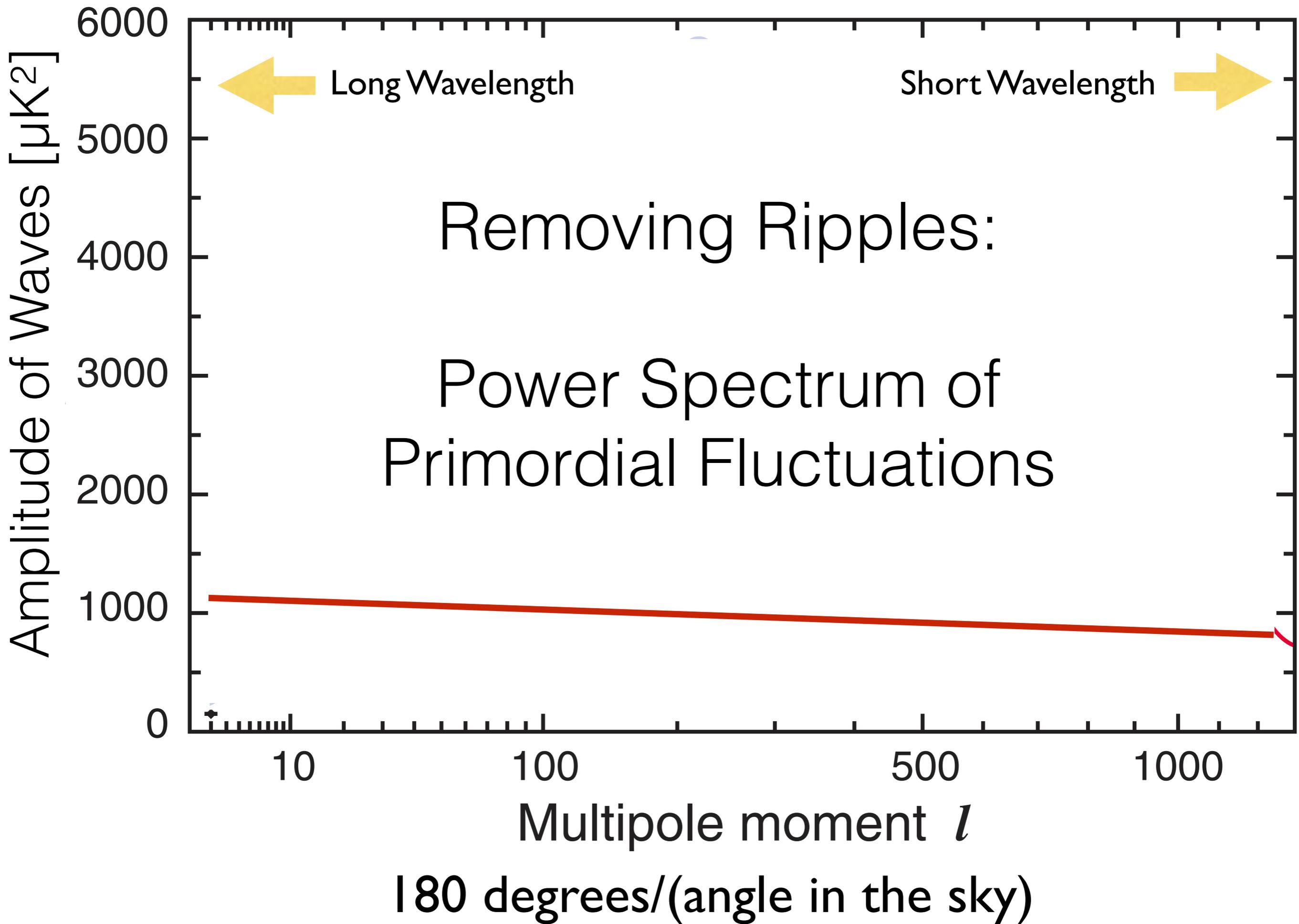
# Origin of Fluctuations

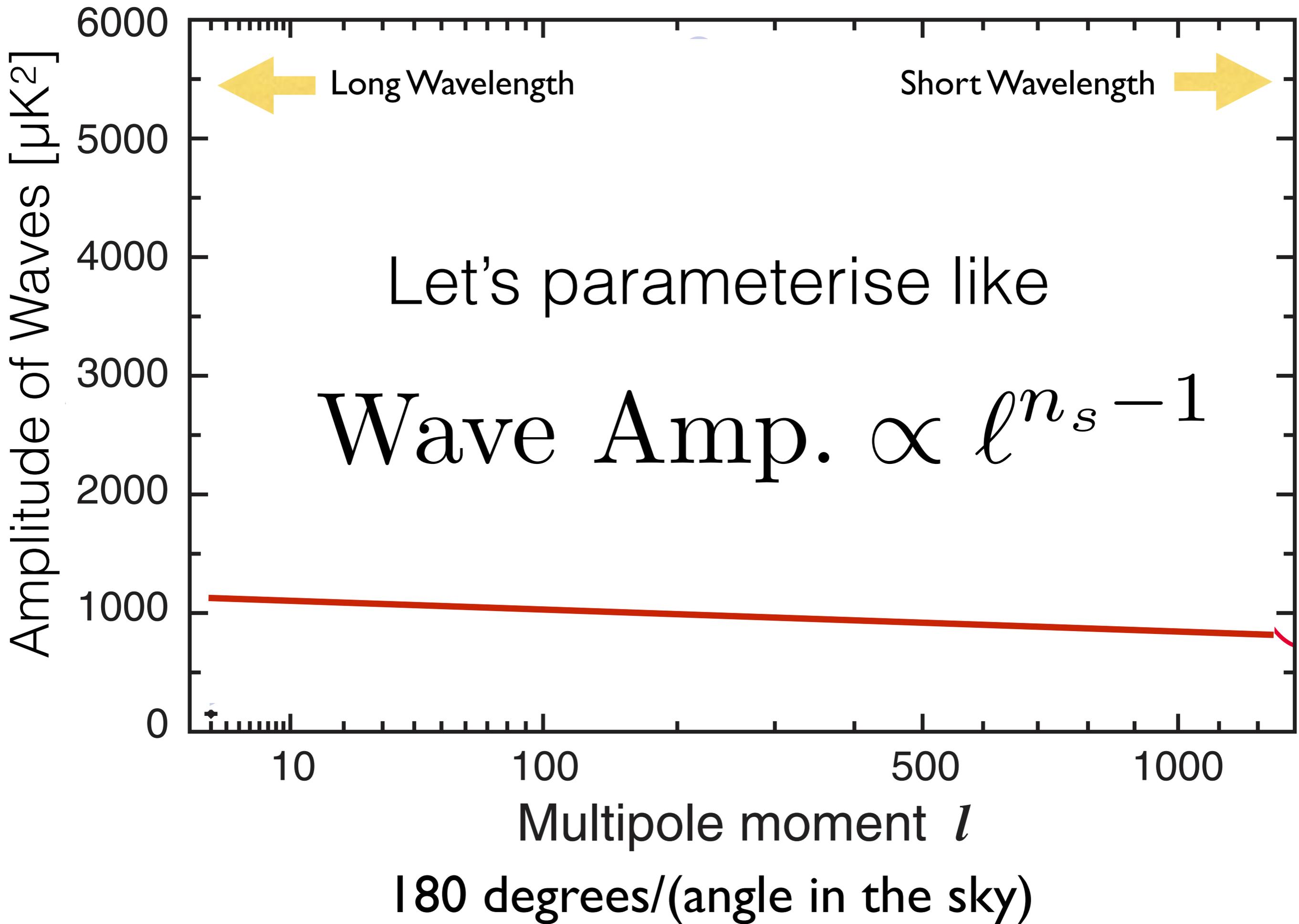
- Who dropped those Tofus into the cosmic Miso soup?

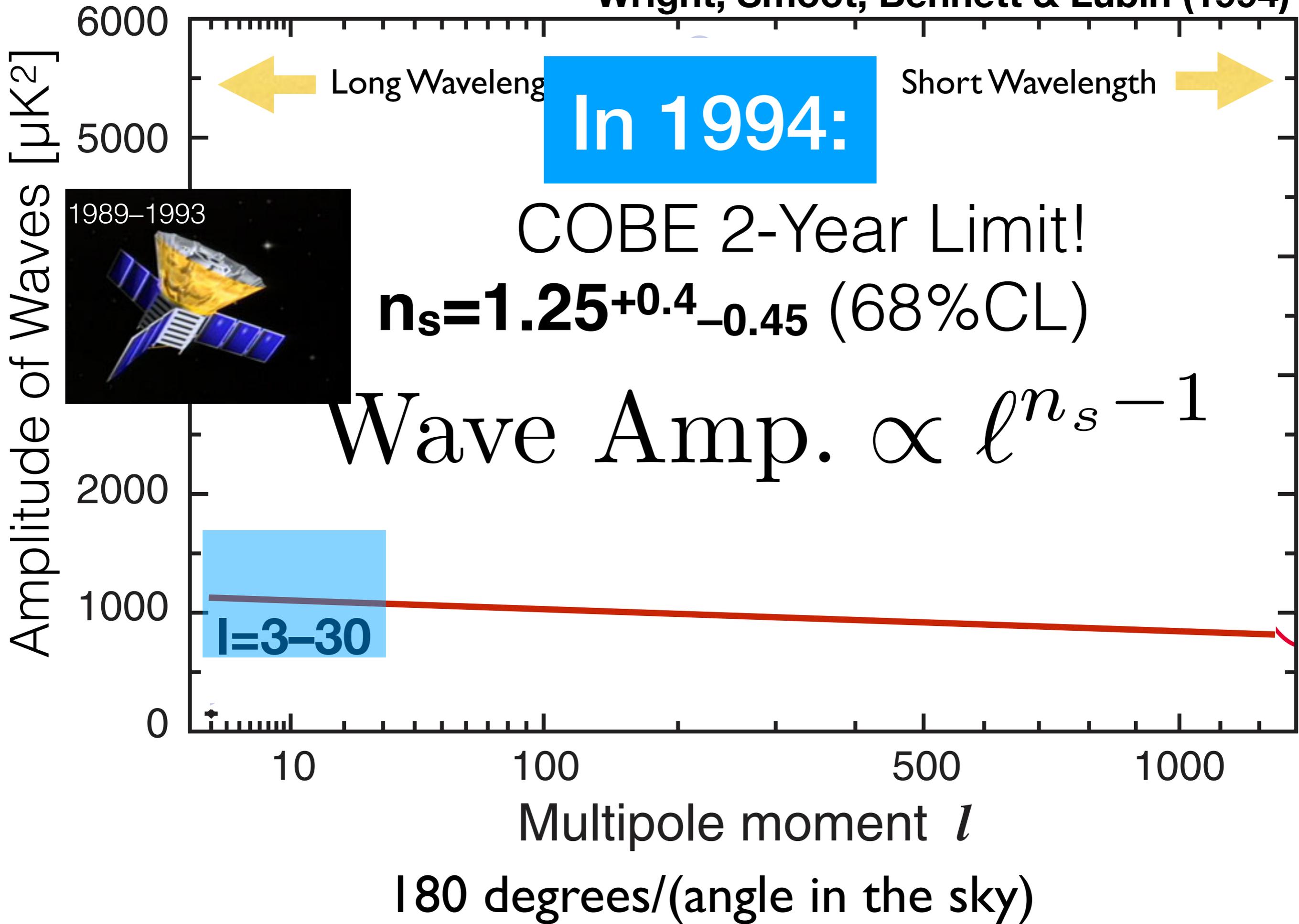


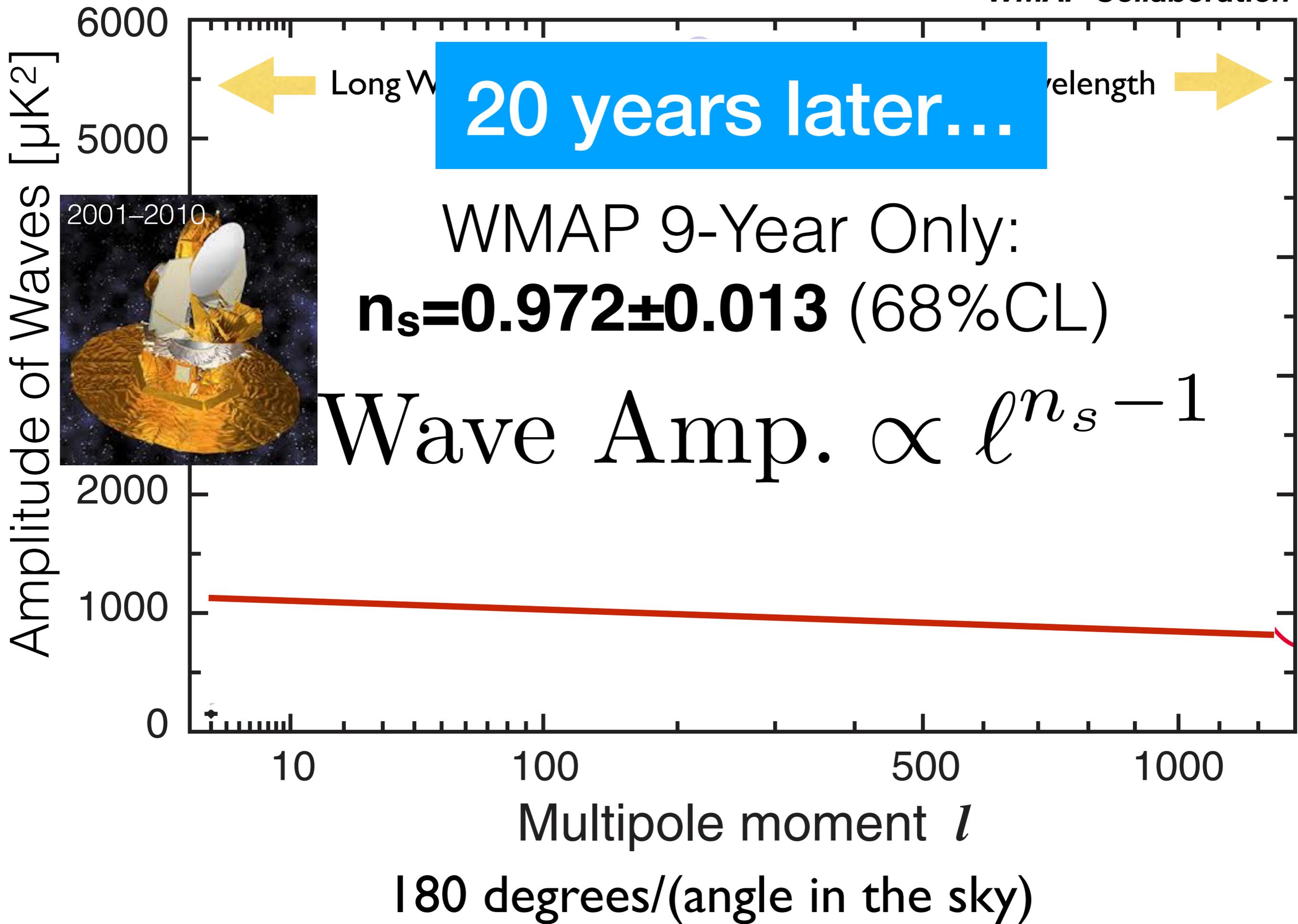












Angular scale

WMAP Collaboration

90° 2° 0.5° 0.2° 0.1°

Amplitude of  $\Delta C_{\ell}^2$

2001–2010

South Pole Telescope  
[10-m in South Pole]

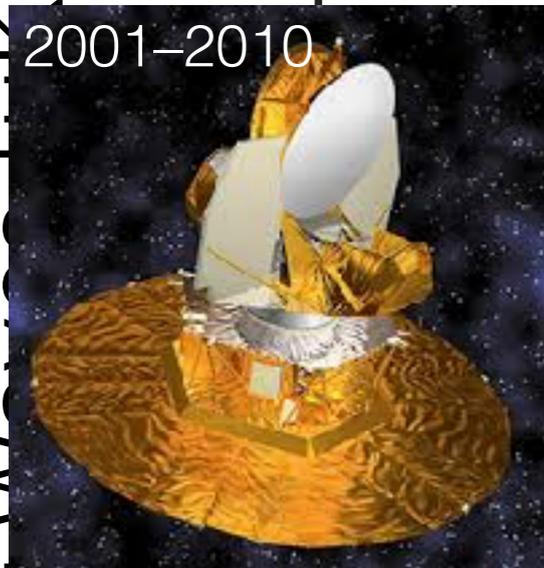
$n_s = 0.965 \pm 0.010$

Atacama Cosmology Telescope  
[6-m in Chile]

100

10 100 500 1000 2000

Multipole moment  $l$



Angular scale

WMAP Collaboration

90°

2°

0.5°

0.2°

0.1°

Amplitude of  $\Delta C_{\ell}^2$

2001–2010

South Pole Telescope  
[10-m in South Pole]

$n_s = 0.961 \pm 0.008$

~5 $\sigma$  discovery of  $n_s < 1$  from the  
CMB data combined with the  
distribution of galaxies

Atacama Cosmology Telescope  
[6-m in Chile]

100

10

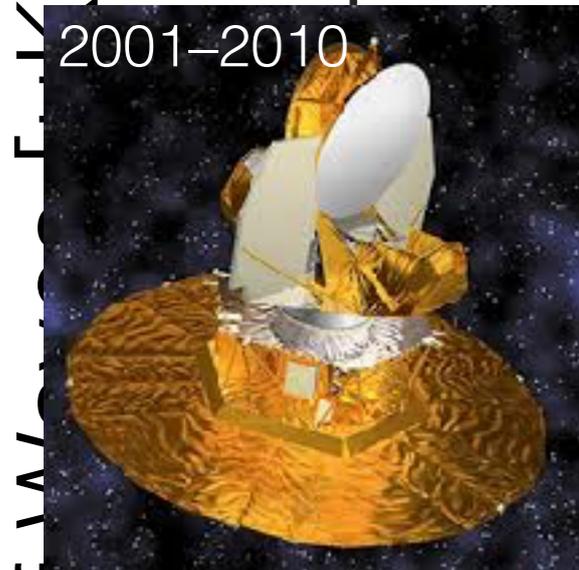
100

500

1000

2000

Multipole moment  $l$



Residual Amplitude of Waves [ $\mu\text{K}^2$ ]

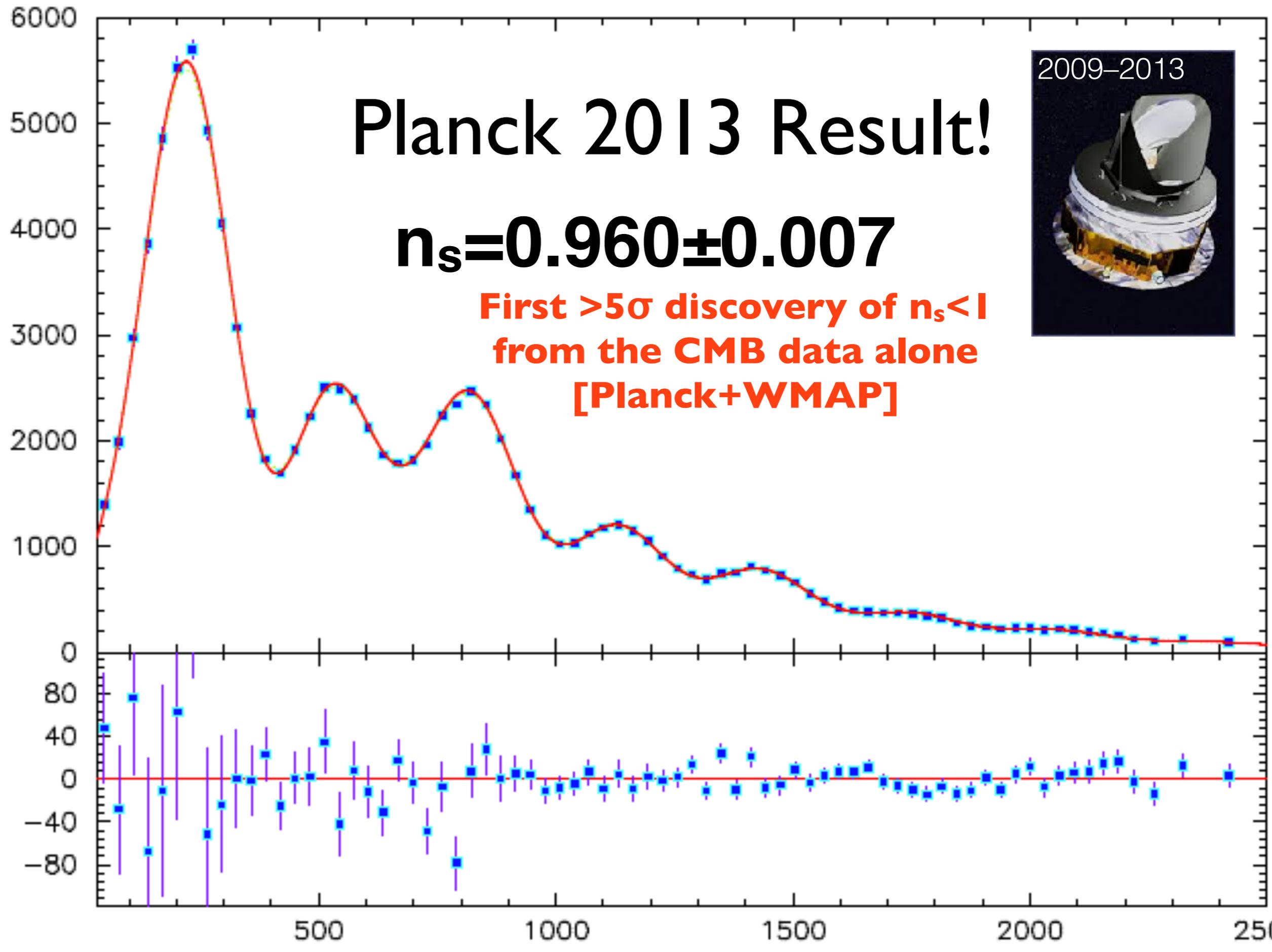
2009–2013



# Planck 2013 Result!

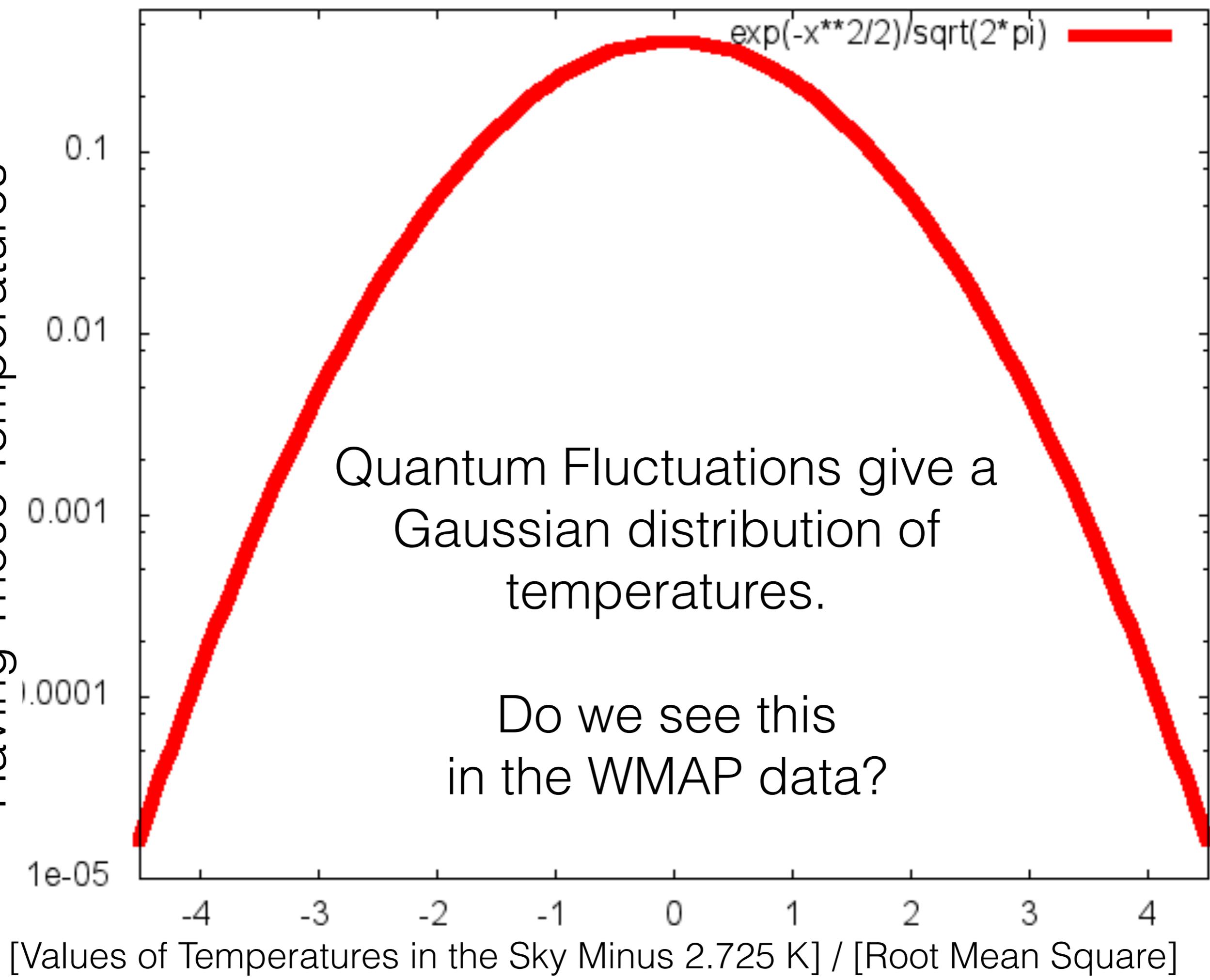
$$n_s = 0.960 \pm 0.007$$

First  $>5\sigma$  discovery of  $n_s < 1$   
from the CMB data alone  
[Planck+WMAP]



$l$  80 degrees/(angle in the sky)

Fraction of the Number of Pixels  
Having Those Temperatures



Fraction of the Number of Pixels  
Having Those Temperatures

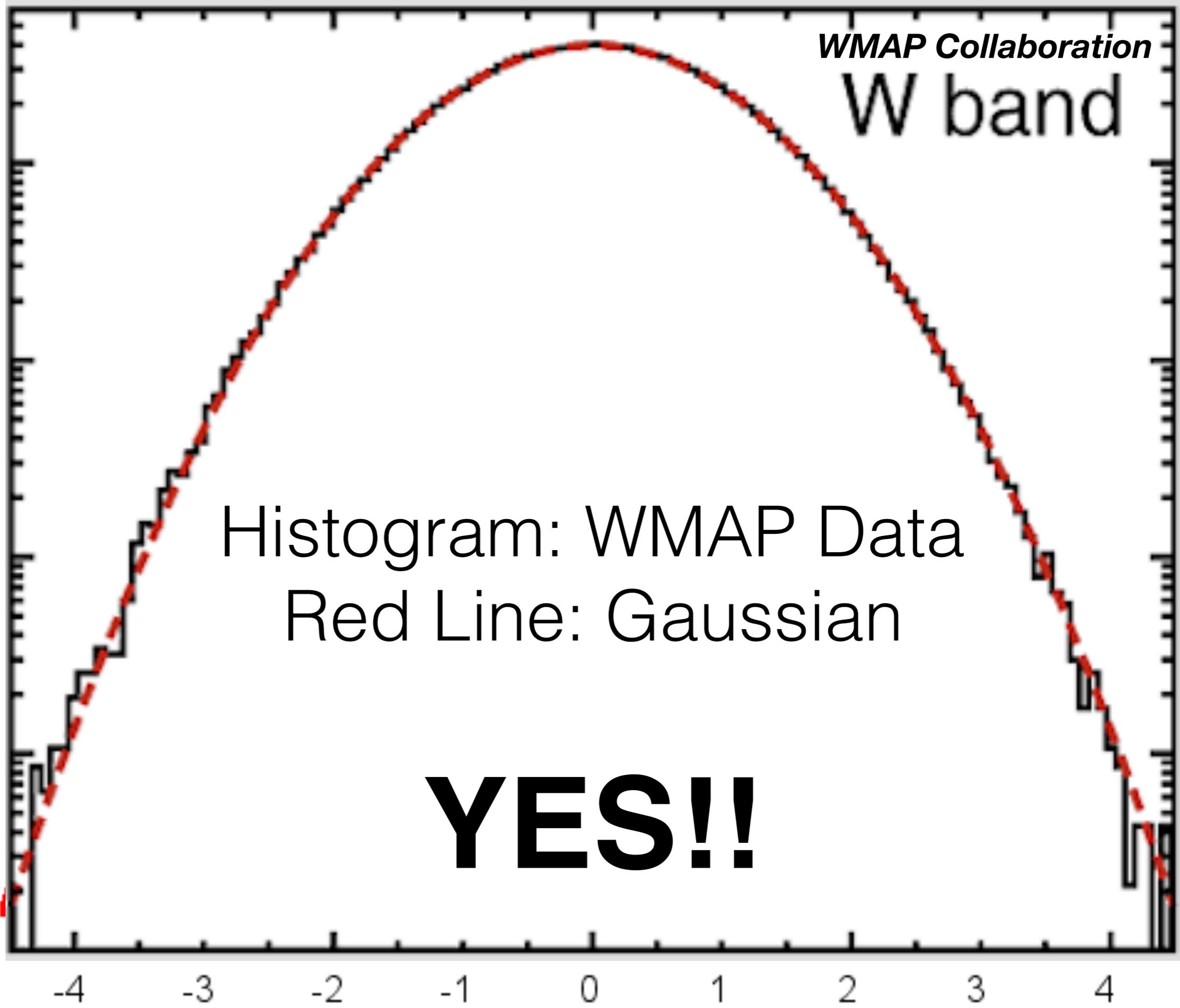
*WMAP Collaboration*  
W band

0.1  
0.01  
0.001  
0.0001  
1e-05

Histogram: WMAP Data  
Red Line: Gaussian

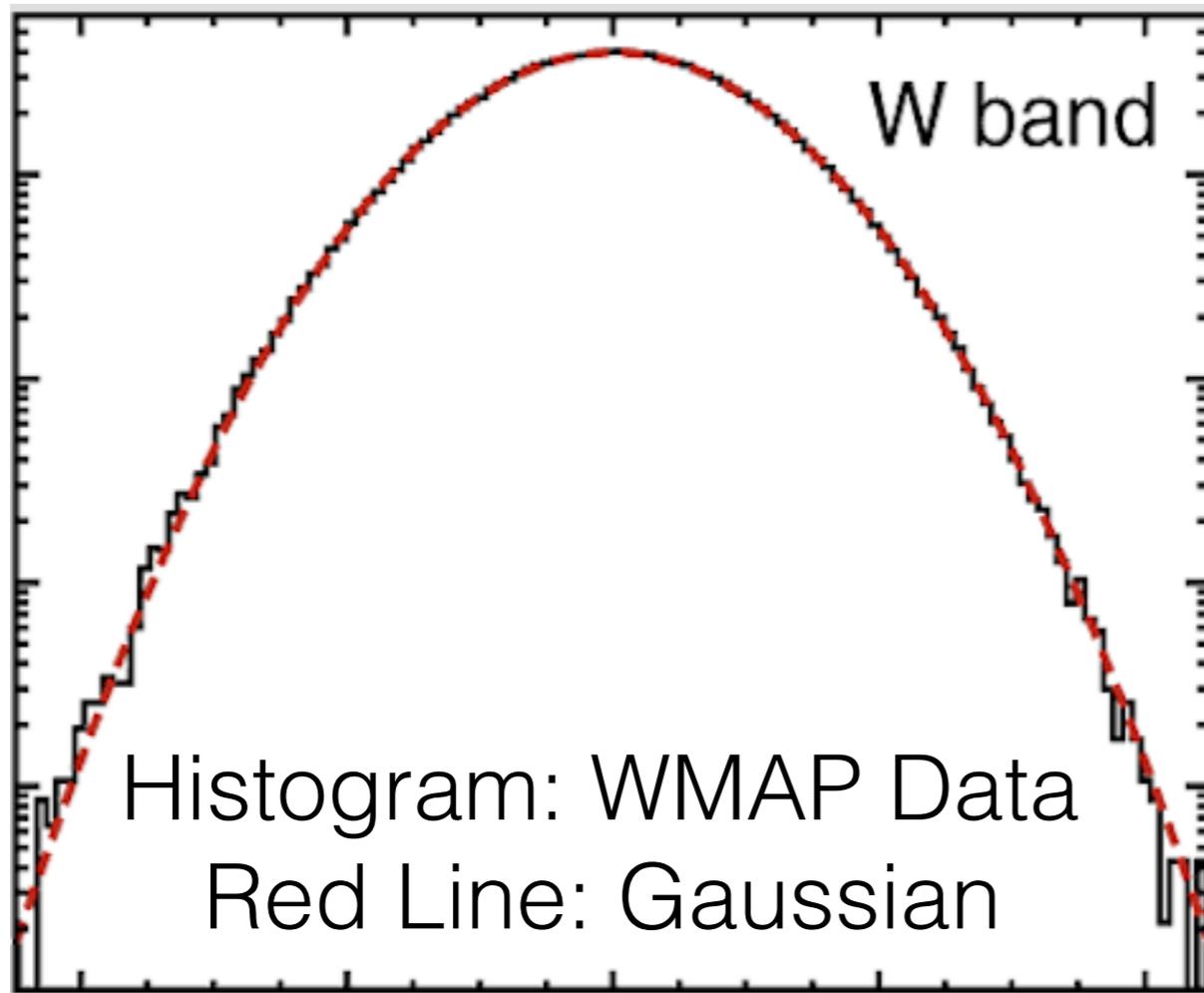
**YES!!**

[Values of Temperatures in the Sky Minus 2.725 K] / [Root Mean Square]



# Testing Gaussianity

Fraction of the Number of Pixels  
Having Those Temperatures



[Values of Temperatures in the Sky Minus  
2.725 K]/ [Root Mean Square]

- Since a Gauss distribution is symmetric, it must yield a vanishing **3-point function**

$$\langle \delta T^3 \rangle \equiv \int_{-\infty}^{\infty} d\delta T P(\delta T) \delta T^3$$

- More specifically, we measure this by averaging the product of temperatures at three different locations in the sky

$$\langle \delta T(\hat{n}_1) \delta T(\hat{n}_2) \delta T(\hat{n}_3) \rangle$$

# Lack of non-Gaussianity

- The WMAP data show that the distribution of temperature fluctuations of CMB is very precisely Gaussian
  - with an upper bound on a deviation of **0.2%** (95%CL)

$$\zeta(\mathbf{x}) = \zeta_{\text{gaus}}(\mathbf{x}) + \frac{3}{5} f_{\text{NL}} \zeta_{\text{gaus}}^2(\mathbf{x}) \text{ with } f_{\text{NL}} = 37 \pm 20 \text{ (68\% CL)}$$

**WMAP 9-year Result**

- The Planck data improved the upper bound by an order of magnitude: deviation is **<0.03%** (95%CL)

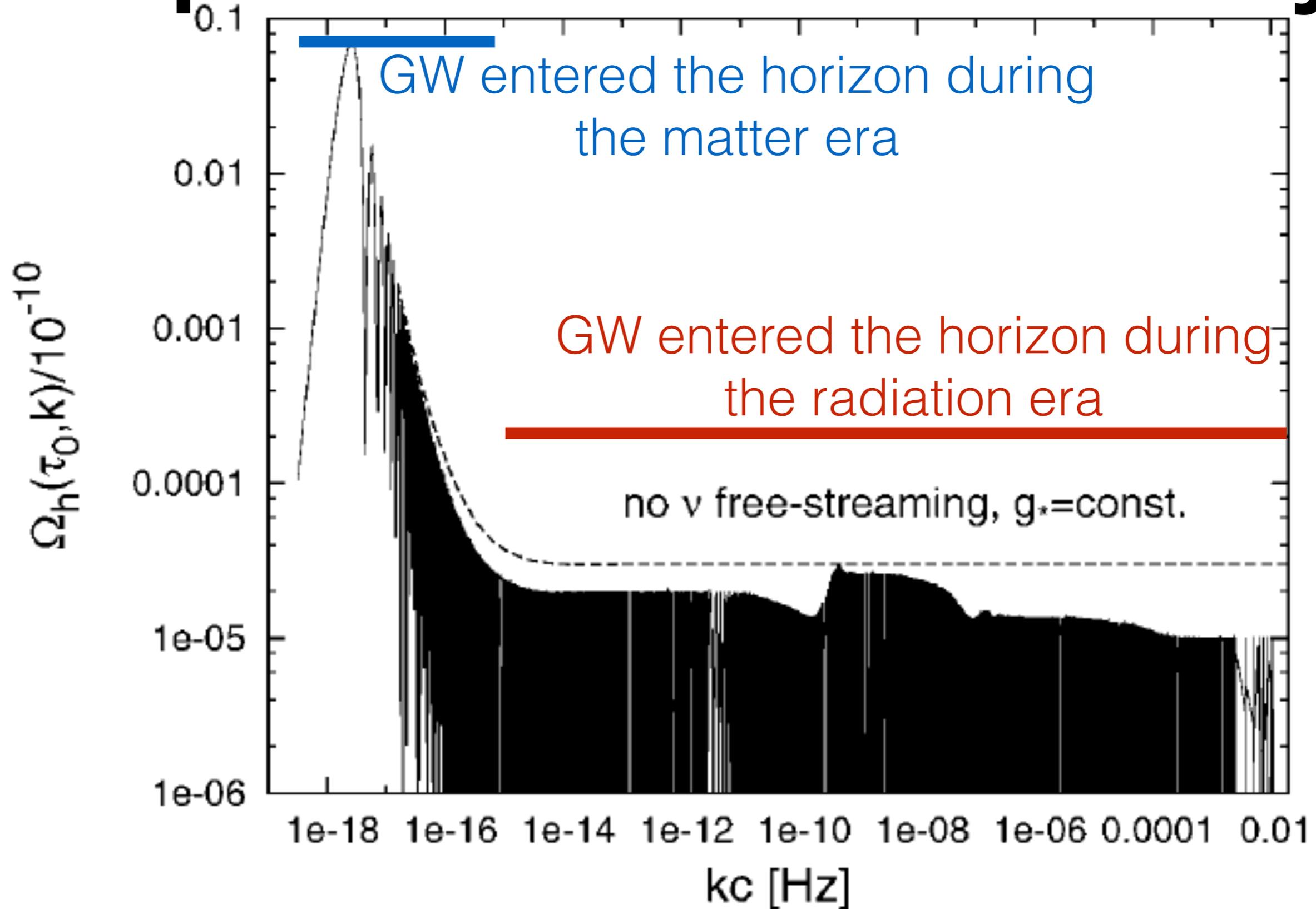
$$f_{\text{NL}} = 0.8 \pm 5.0 \text{ (68\% CL)}$$

**Planck 2015 Result**

# So, have we found inflation?

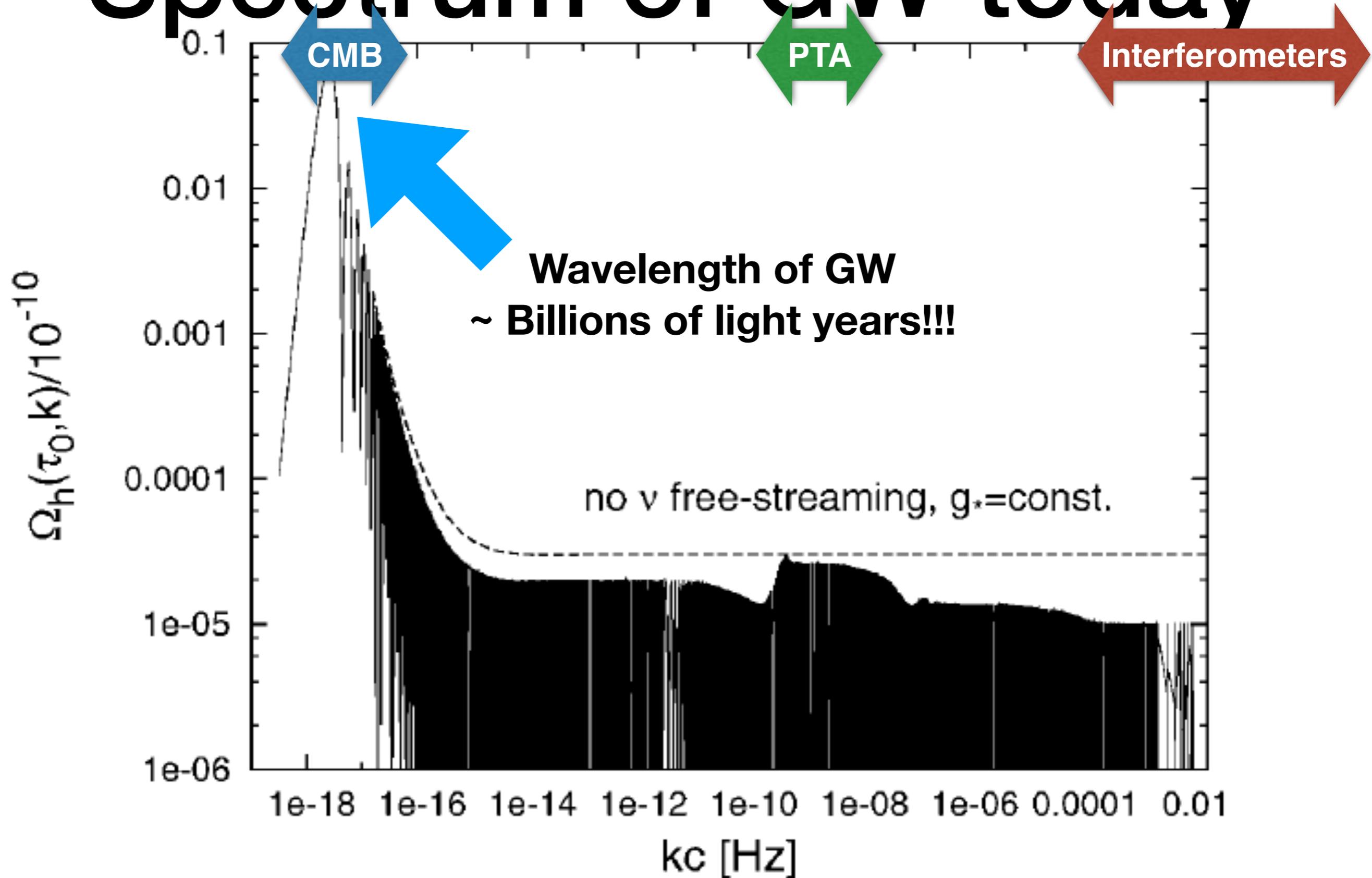
- Single-field slow-roll inflation looks remarkably good:
  - **Super-horizon fluctuation**
  - **Adiabaticity**
  - **Gaussianity**
  - **$n_s < 1$**
- What more do we want? **Gravitational waves**. Why?
  - Because the “*extraordinary claim requires extraordinary evidence*”

# Theoretical energy density Spectrum of GW today



## Theoretical energy density

## Spectrum of GW today



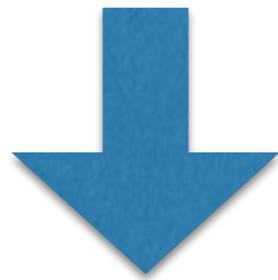
# Finding Signatures of Gravitational Waves in the CMB

- **Next frontier in the CMB research**
  1. Find evidence for nearly scale-invariant gravitational waves
  2. Once found, test Gaussianity to make sure (or not!) that the signal comes from the vacuum fluctuation in spacetime
  3. Constrain inflation models

# Measuring GW

- GW changes distances between two points

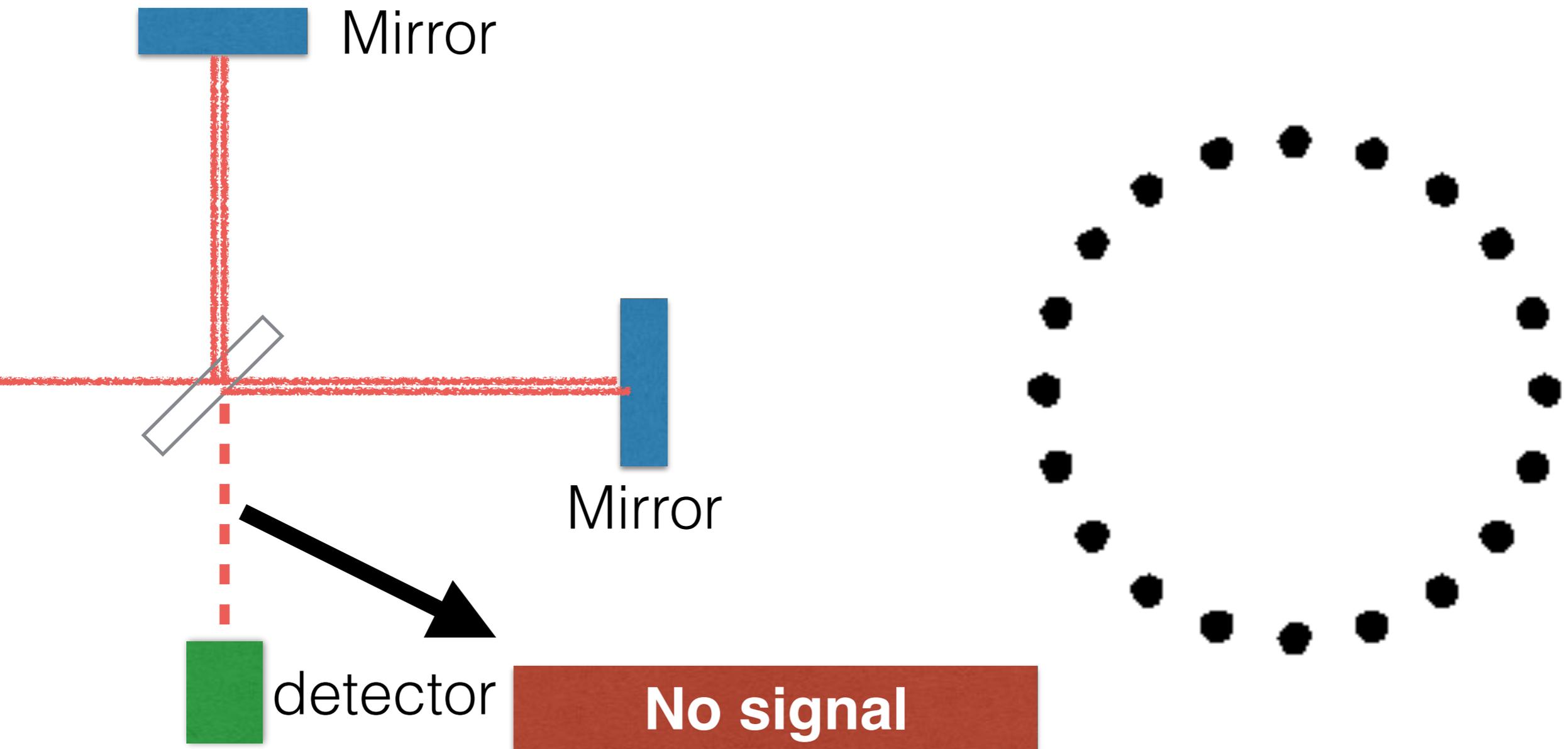
$$d\ell^2 = d\mathbf{x}^2 = \sum_{ij} \delta_{ij} dx^i dx^j$$



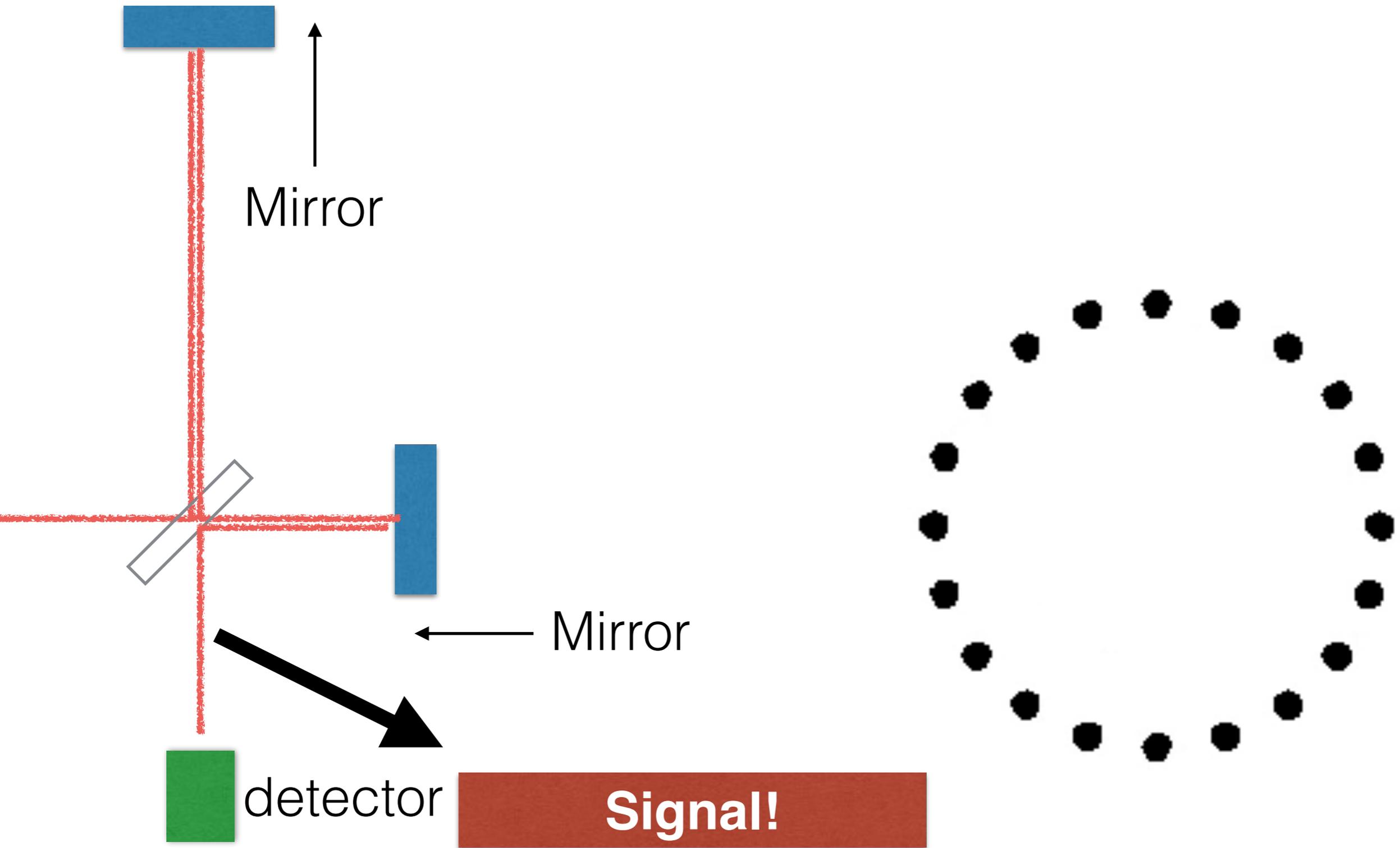
$$d\ell^2 = \sum_{ij} (\delta_{ij} + \underline{h_{ij}}) dx^i dx^j$$



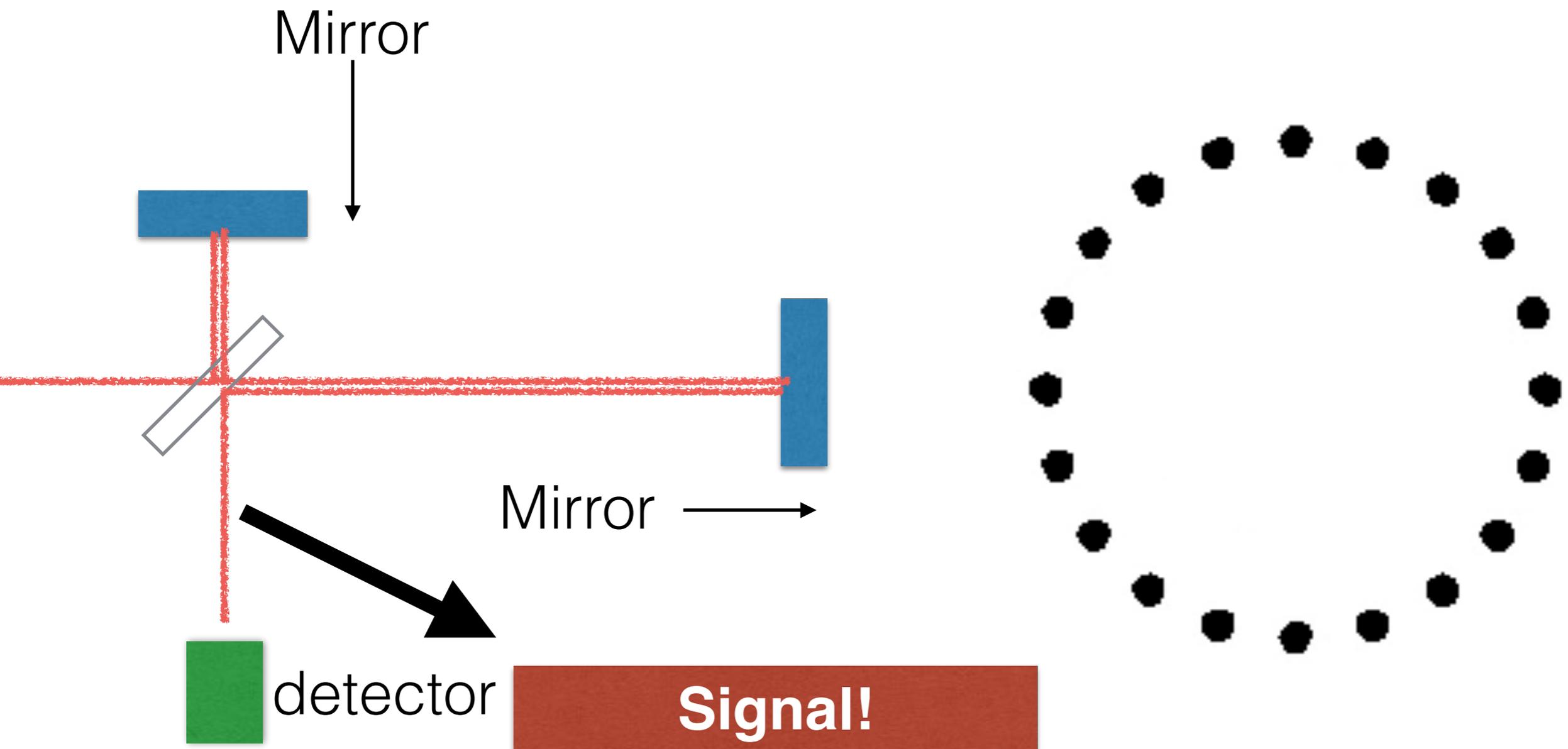
# Laser Interferometer



# Laser Interferometer



# Laser Interferometer



LIGO detected GW from a binary blackholes, with the wavelength of thousands of kilometres

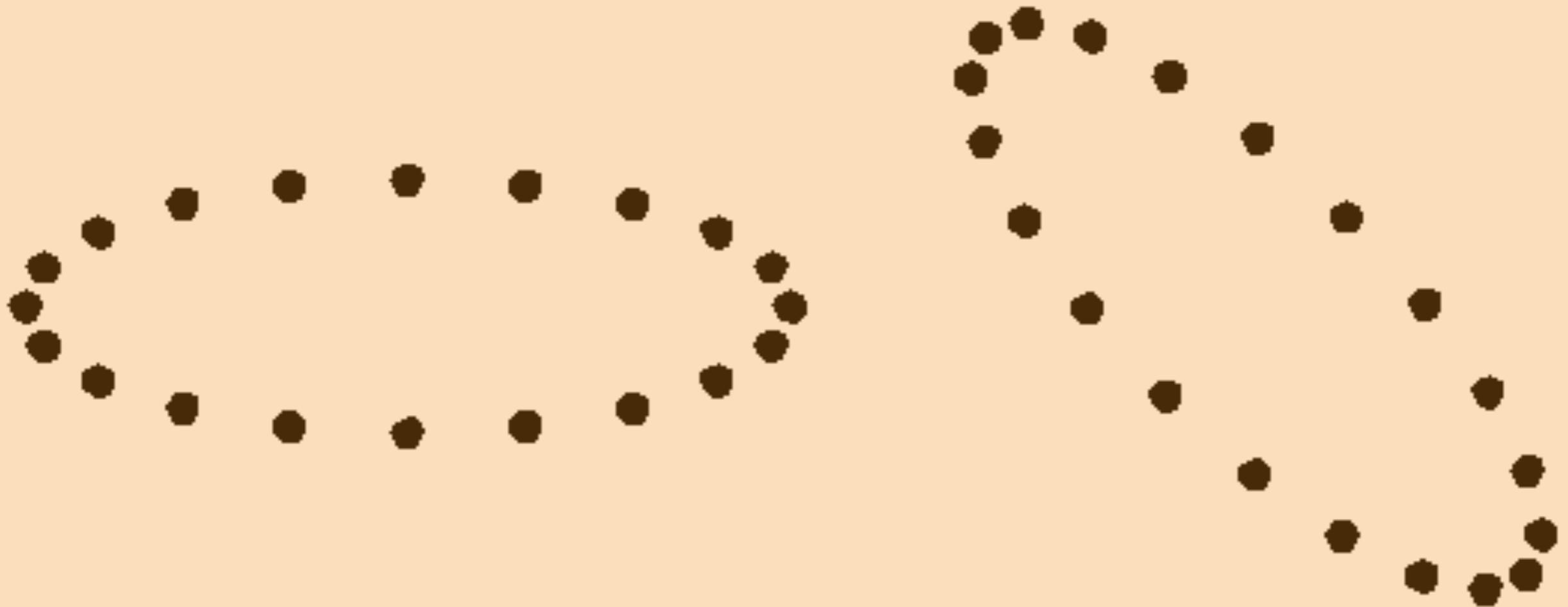
But, the primordial GW affecting the CMB has a wavelength of **billions of light-years!!** How do we find it?

# Detecting GW by CMB

Isotropic electro-magnetic fields

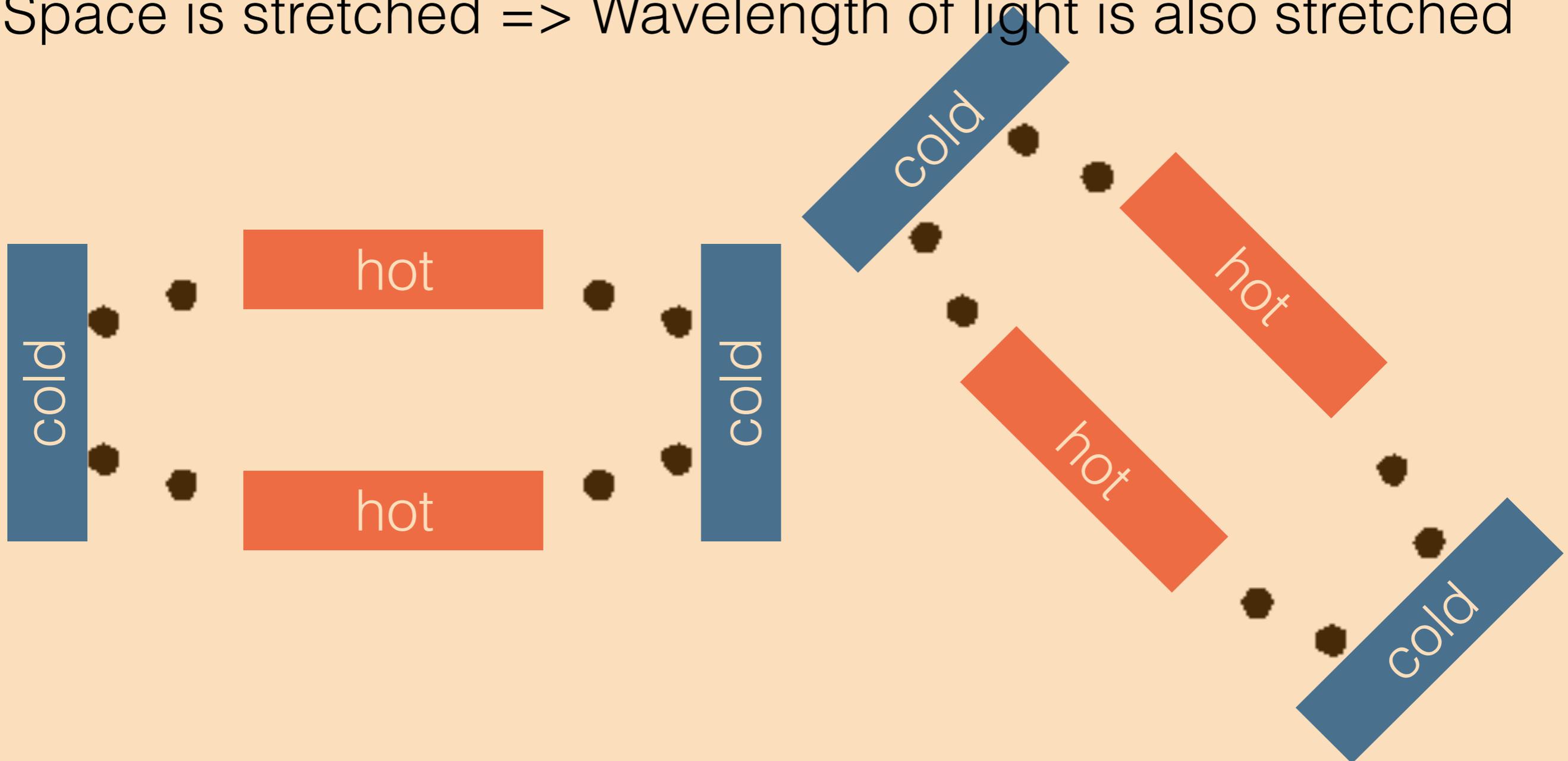
# Detecting GW by CMB

GW propagating in isotropic electro-magnetic fields



# Detecting GW by CMB

Space is stretched => Wavelength of light is also stretched



# Detecting GW by CMB Polarisation

Space is stretched => Wavelength of light is also stretched

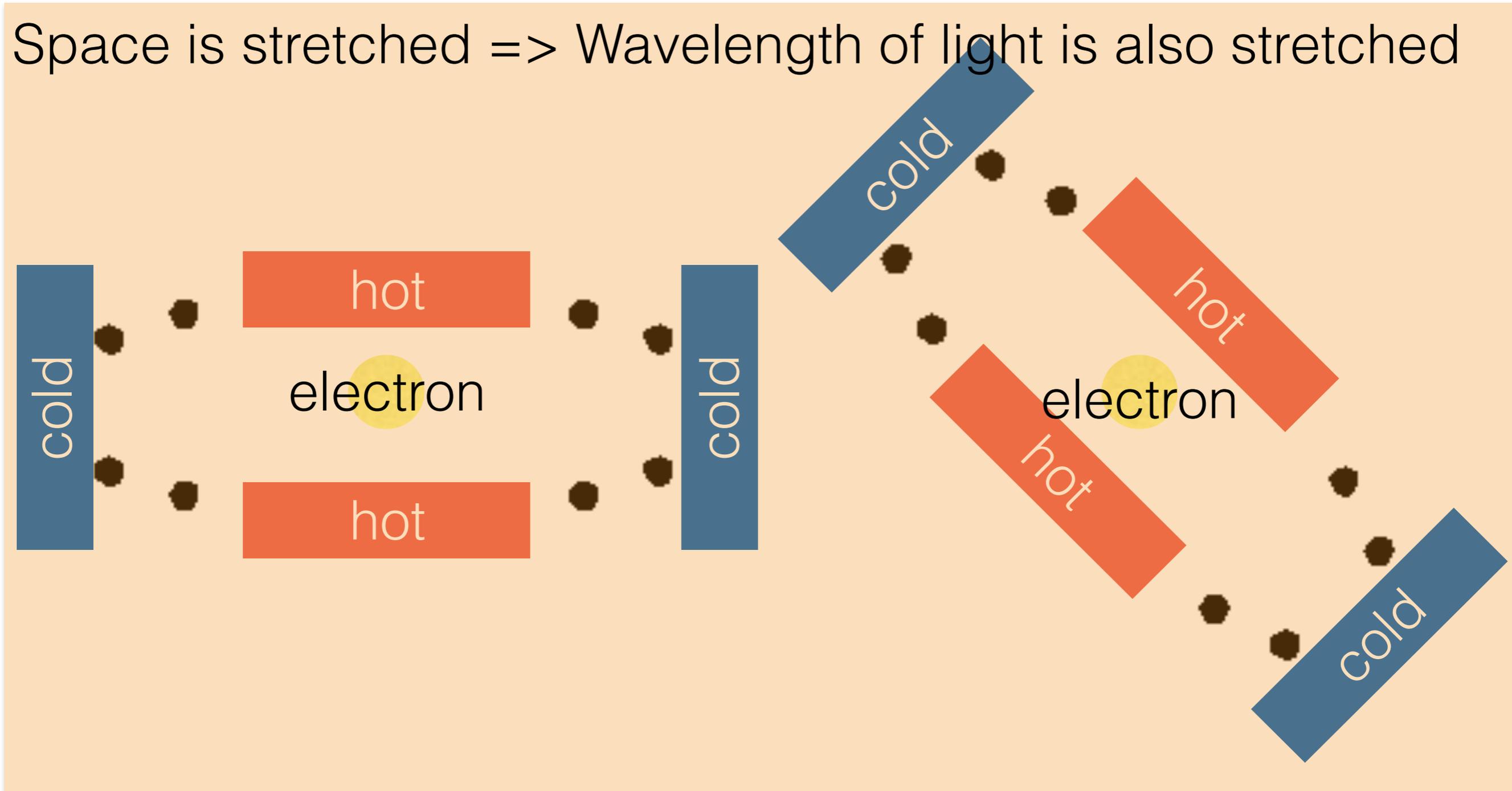


Photo Credit: TALEX



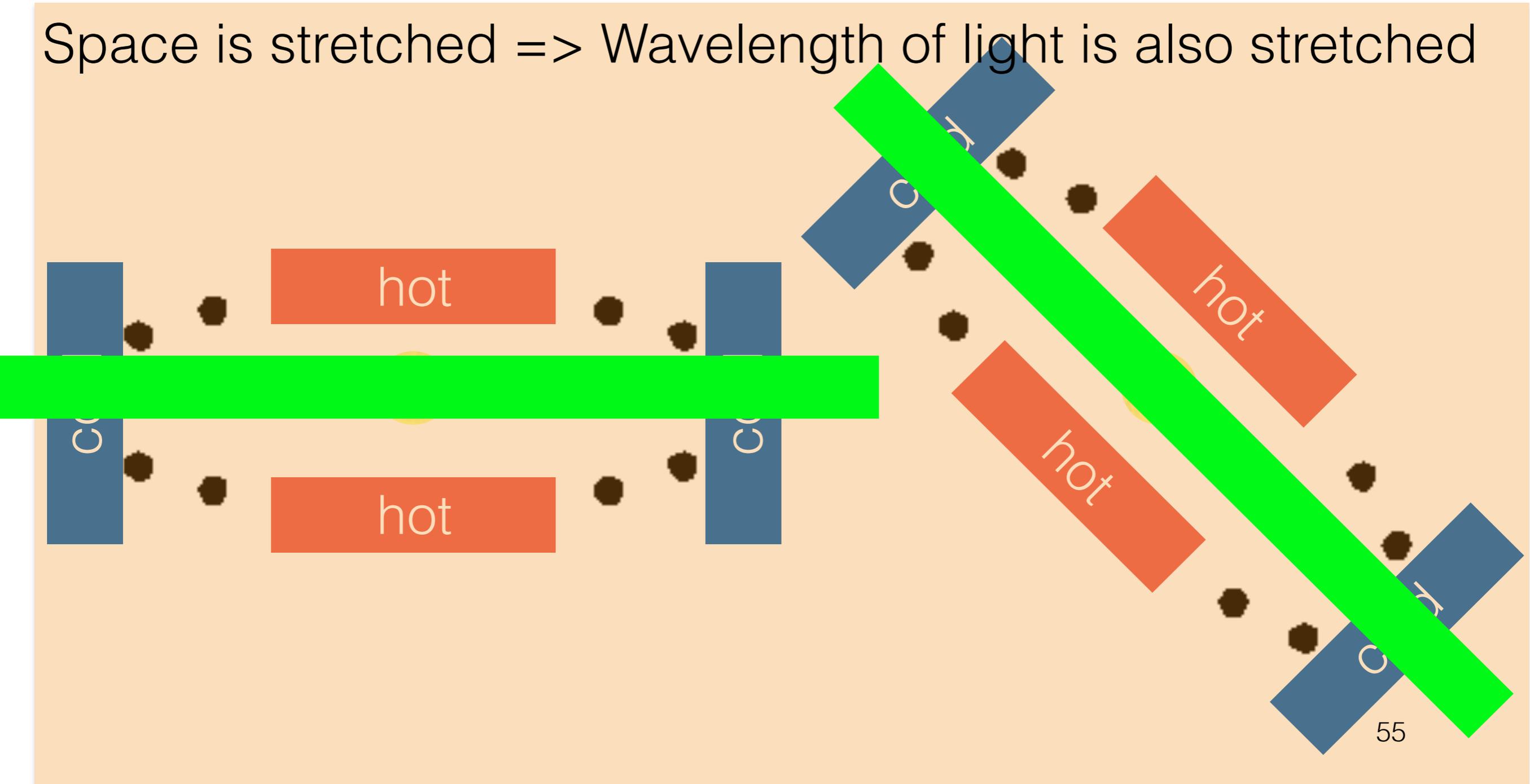
horizontally polarised

Photo Credit: TALEX



# Detecting GW by CMB Polarisation

Space is stretched => Wavelength of light is also stretched

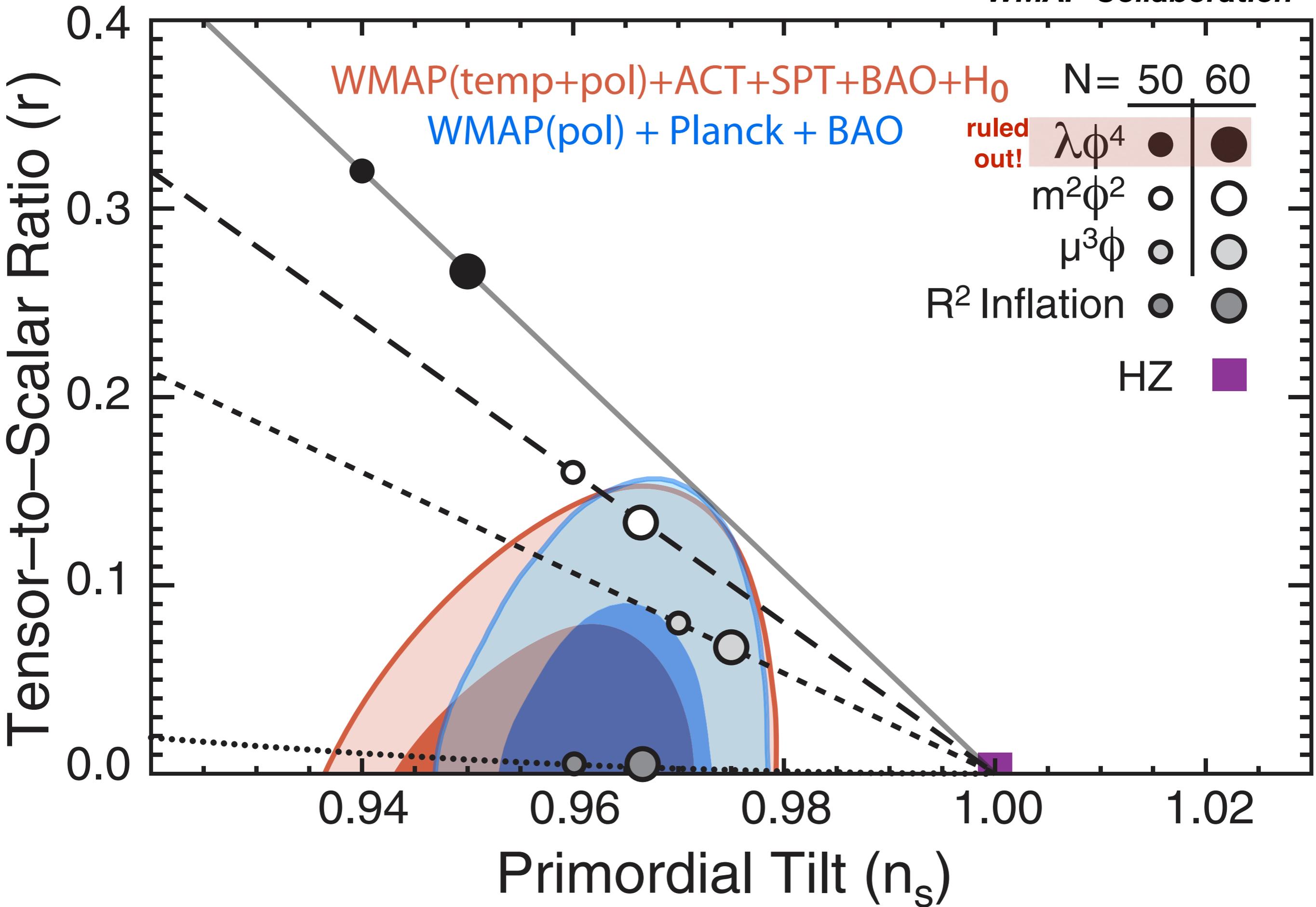


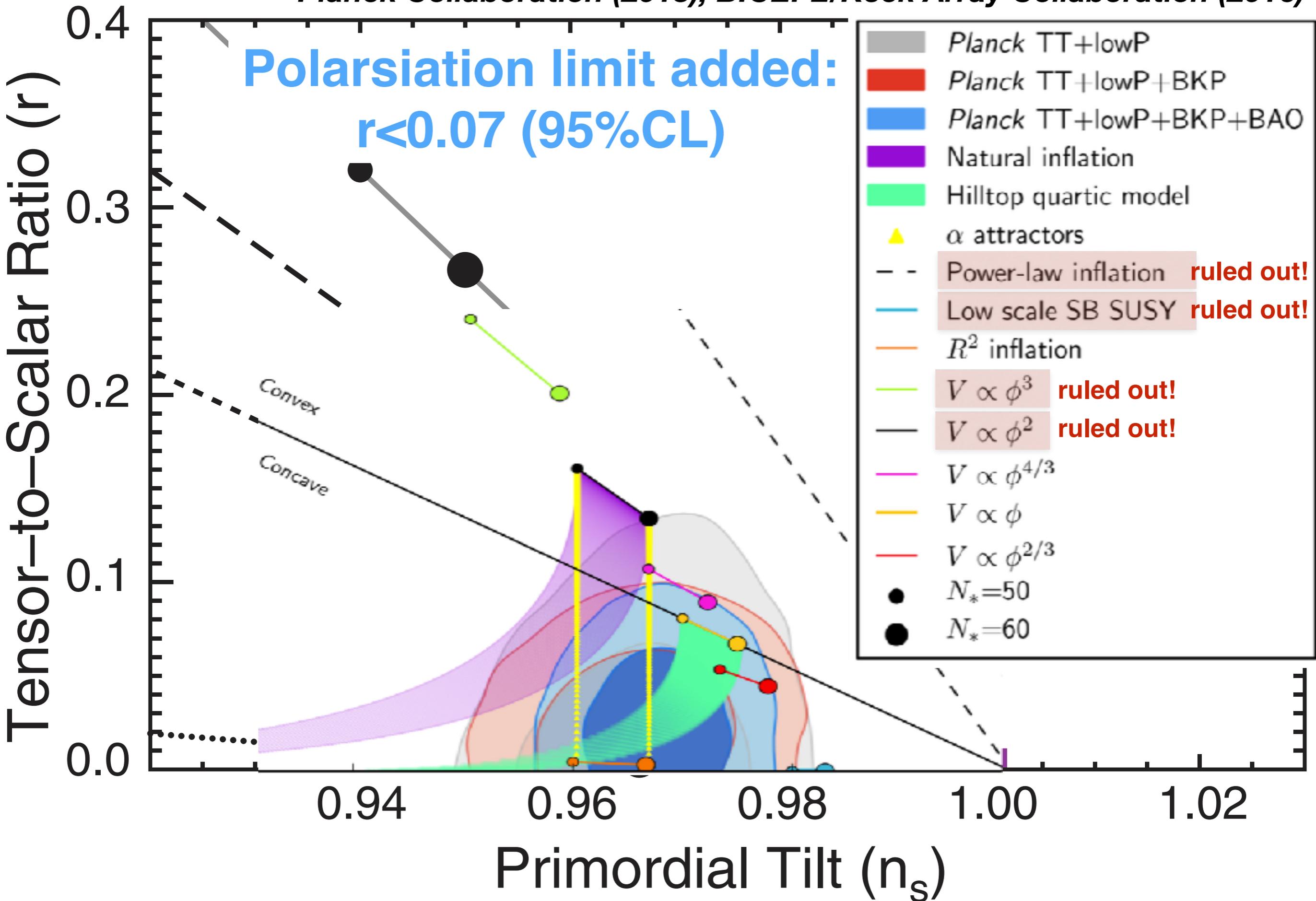
# Tensor-to-scalar Ratio

$$r \equiv \frac{\langle h_{ij} h^{ij} \rangle}{\langle \zeta^2 \rangle}$$

- We really want to find this! The current upper bound is  **$r < 0.07$**  (95%CL)

**BICEP2/Keck Array Collaboration (2016)**





**But, wait a minute...**

# Are GWs from vacuum fluctuation in spacetime, or from sources?

$$\square h_{ij} = -16\pi G \pi_{ij}$$

- **Homogeneous solution:** “GWs from vacuum fluctuation”
- **Inhomogeneous solution:** “GWs from sources”
  - Scalar and vector fields cannot source tensor fluctuations at linear order (possible at non-linear level)
  - SU(2) gauge field can!

Maleknejad & Sheikh-Jabbari (2013); Dimastrogiovanni & Peloso (2013);  
Adshead, Martinec & Wyman (2013); Obata & Soda (2016); ...

# Important Message

$$\square h_{ij} = -16\pi G \pi_{ij}$$

- Do not take it for granted if someone told you that detection of the B-mode polarisation would be a signature of “quantum gravity”!
- Only the homogeneous solution corresponds to the vacuum tensor metric perturbation. **There is no *a priori* reason to neglect an inhomogeneous solution!**
- Contrary, we have several examples in which detectable B-modes are generated by **sources** [U(1) and SU(2)]

# A New Paradigm

- We must **not** assume that detection of gravitational waves (GWs) from inflation immediately implies that GWs are from the vacuum fluctuation in tensor metric perturbation
- The homogeneous solution is related to  $H(t)$  (or the inflaton field excursion; “Lyth bound”) during inflation, but the inhomogeneous solution is **not**.
- **Detection of B-mode polarisation  $\neq$  Vacuum fluctuation in metric**

# Experimental Strategy

## Commonly Assumed So Far

1. Detect B-mode polarisation in multiple frequencies, to make sure that it is the B-mode of the CMB
2. Check for scale invariance: Consistent with a scale invariant spectrum?
  - Yes => Announce discovery of the vacuum fluctuation in spacetime
  - No => WTF?

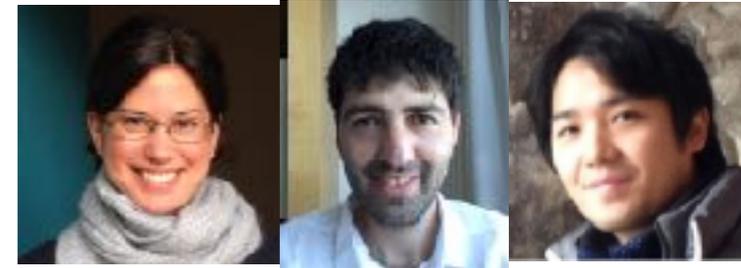
# New Experimental Strategy: New Standard!

1. Detect B-mode polarisation in multiple frequencies, to make sure that it is the B-mode of the CMB
  2. Consistent with a scale invariant spectrum?
  3. Parity violating correlations (TB and EB) consistent with zero?
  4. Consistent with Gaussianity?
- If, and **ONLY IF** Yes to **all** => Announce discovery of the vacuum fluctuation in spacetime

# If not, you may have just discovered new physics during inflation!

2. Consistent with a scale invariant spectrum?
  3. Parity violating correlations (TB and EB) consistent with zero?
  4. Consistent with Gaussianity?
- If, and **ONLY IF** Yes to **all** => Announce discovery of the vacuum fluctuation in spacetime

# GW from Axion-SU(2) Dynamics



$$\mathcal{L} = \mathcal{L}_{GR} + \mathcal{L}_\phi + \mathcal{L}_\chi - \frac{1}{4} F_{\mu\nu}^a F^{a\mu\nu} + \frac{\lambda \chi}{4f} F_{\mu\nu}^a \tilde{F}^{a\mu\nu}$$

- $\phi$ : inflaton field => Just provides quasi-de Sitter background
- $\chi$ : pseudo-scalar “axion” field. Spectator field (i.e., negligible energy density compared to the inflaton)
- Field strength of an SU(2) field  $A_\nu^a$ :

$$F_{\mu\nu}^a \equiv \partial_\mu A_\nu^a - \partial_\nu A_\mu^a - g\epsilon^{abc} A_\mu^b A_\nu^c$$

# Background and Perturbation



- In an inflating background, the SU(2) field has a background solution:

$$A_i^a = [\text{scale factor}] \times Q \times \delta_i^a$$

$$Q \equiv (-f \partial_\chi U / 3g\lambda H)^{1/3}$$

**U: axion potential**

- Perturbations contain a tensor mode (as well as S&V)

$$\delta A_i^a = t_{ai} + \dots$$

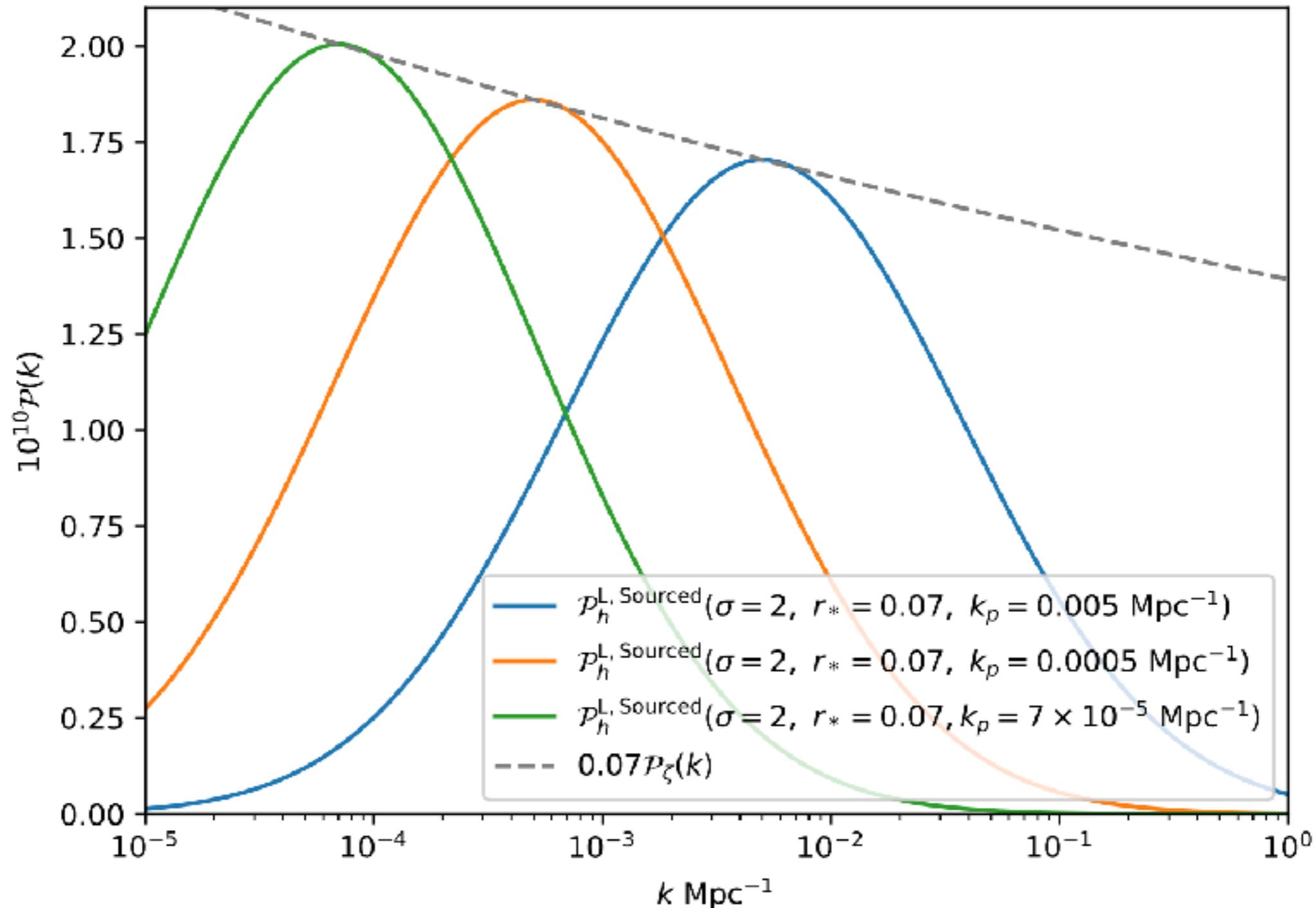
$$t_{ii} = \partial_a t_{ai} = \partial_i t_{ai} = 0$$

# Scenario

- The SU(2) field contains tensor, vector, and scalar components
- The tensor components are amplified strongly by a coupling to the axion field
  - But, only one helicity is amplified  $\Rightarrow$  GW is **chiral**  
(well-known result)
- Brand-new result: **GWs sourced by this mechanism are strongly non-Gaussian!**

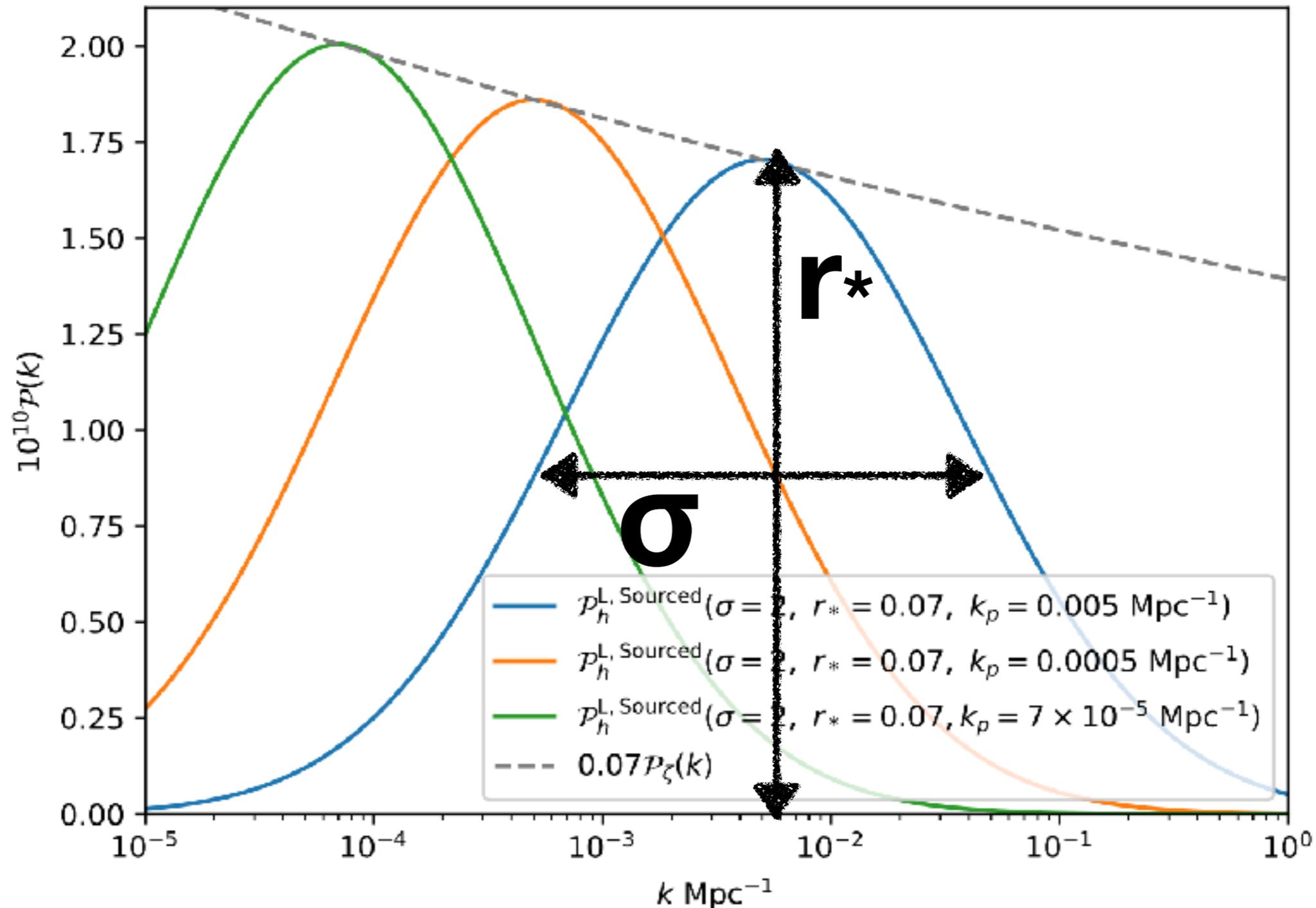
*Agrawal, Fujita & EK (2017)*

# Example Tensor Spectra



- Sourced tensor spectrum can be close to scale invariant, but can also be bumpy

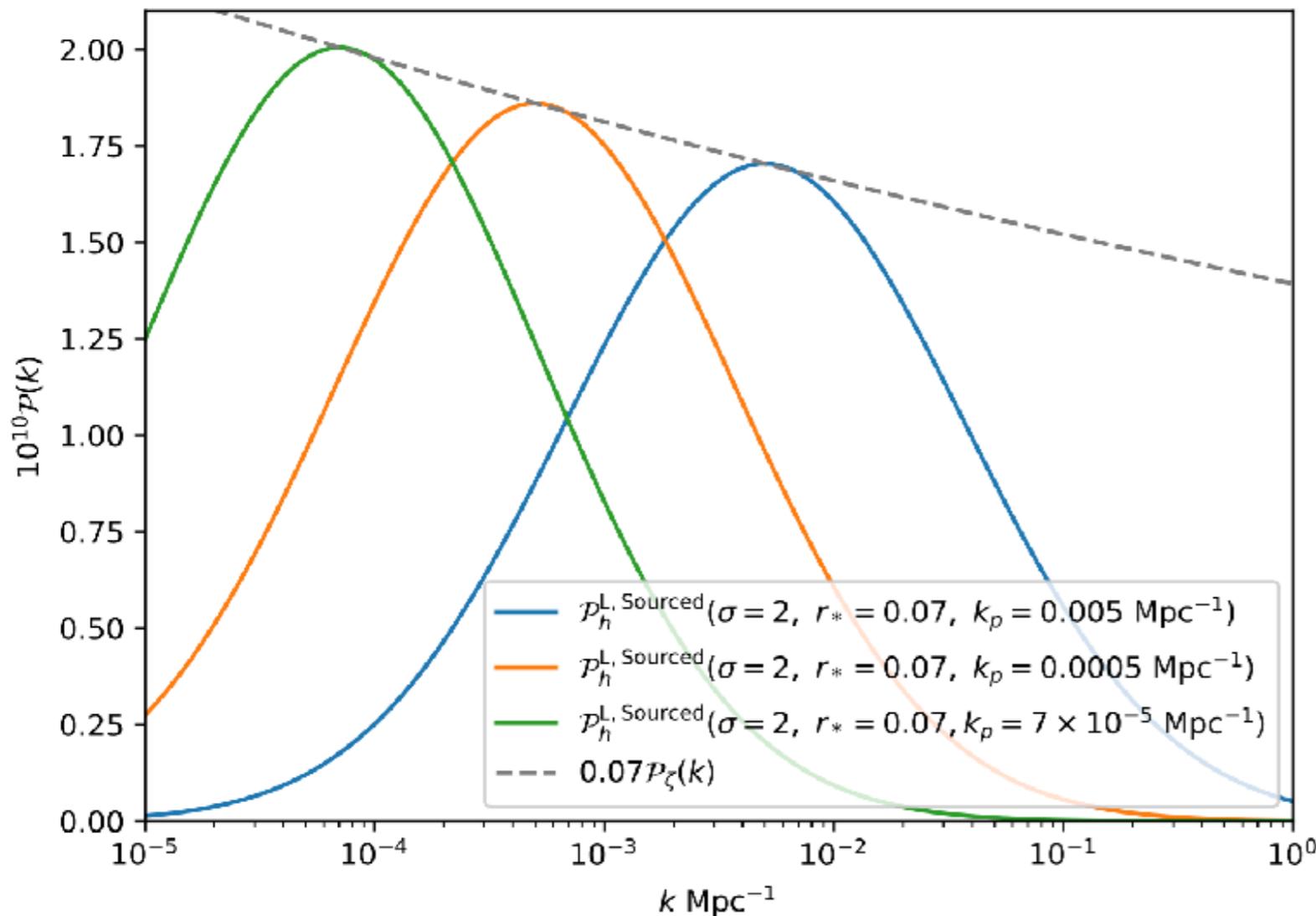
# Example Tensor Spectra



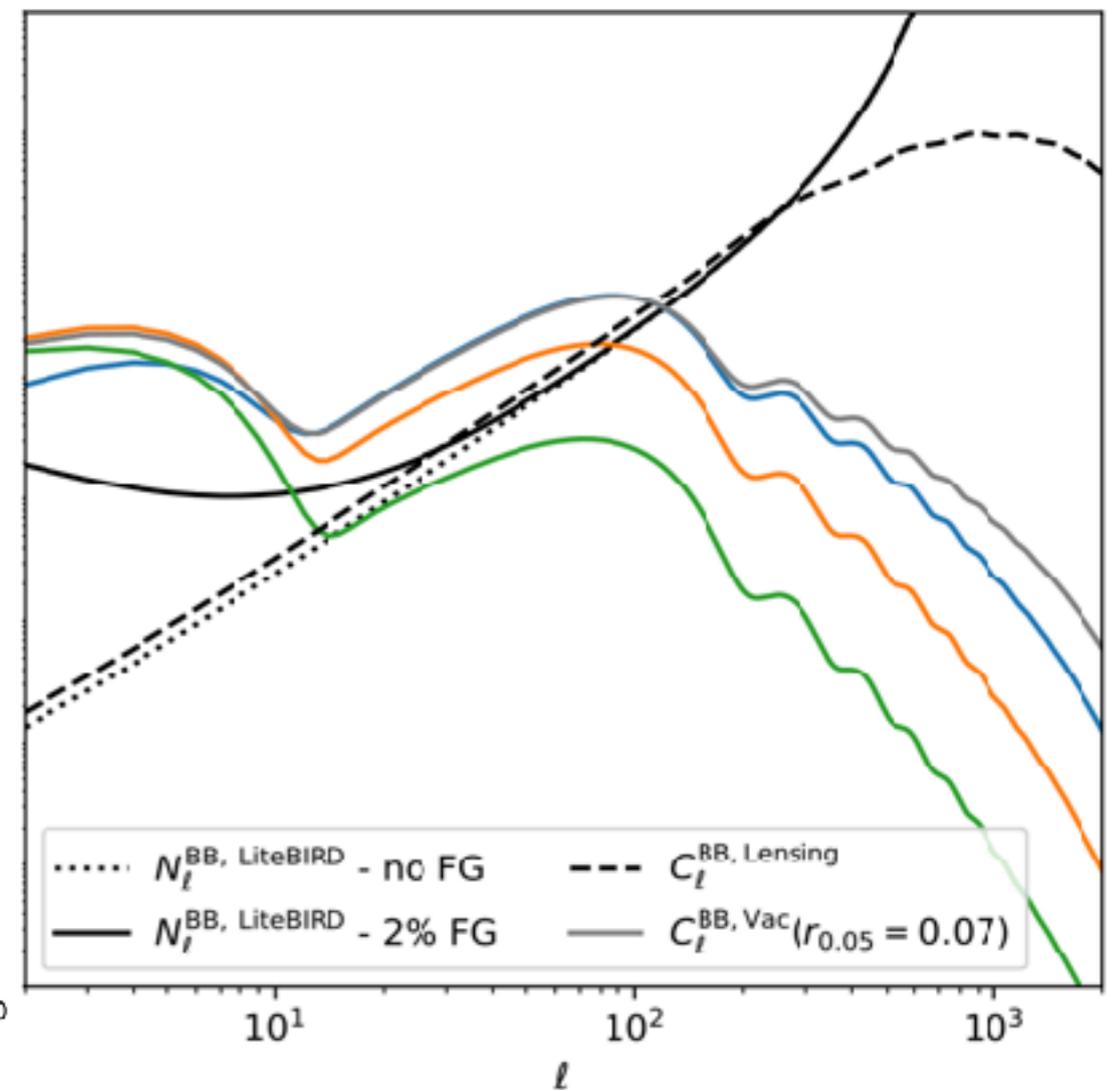
- Sourced tensor spectrum can be close to scale invariant, but can also be bumpy

# Example Tensor Spectra

## Tensor Power Spectrum, $P(k)$

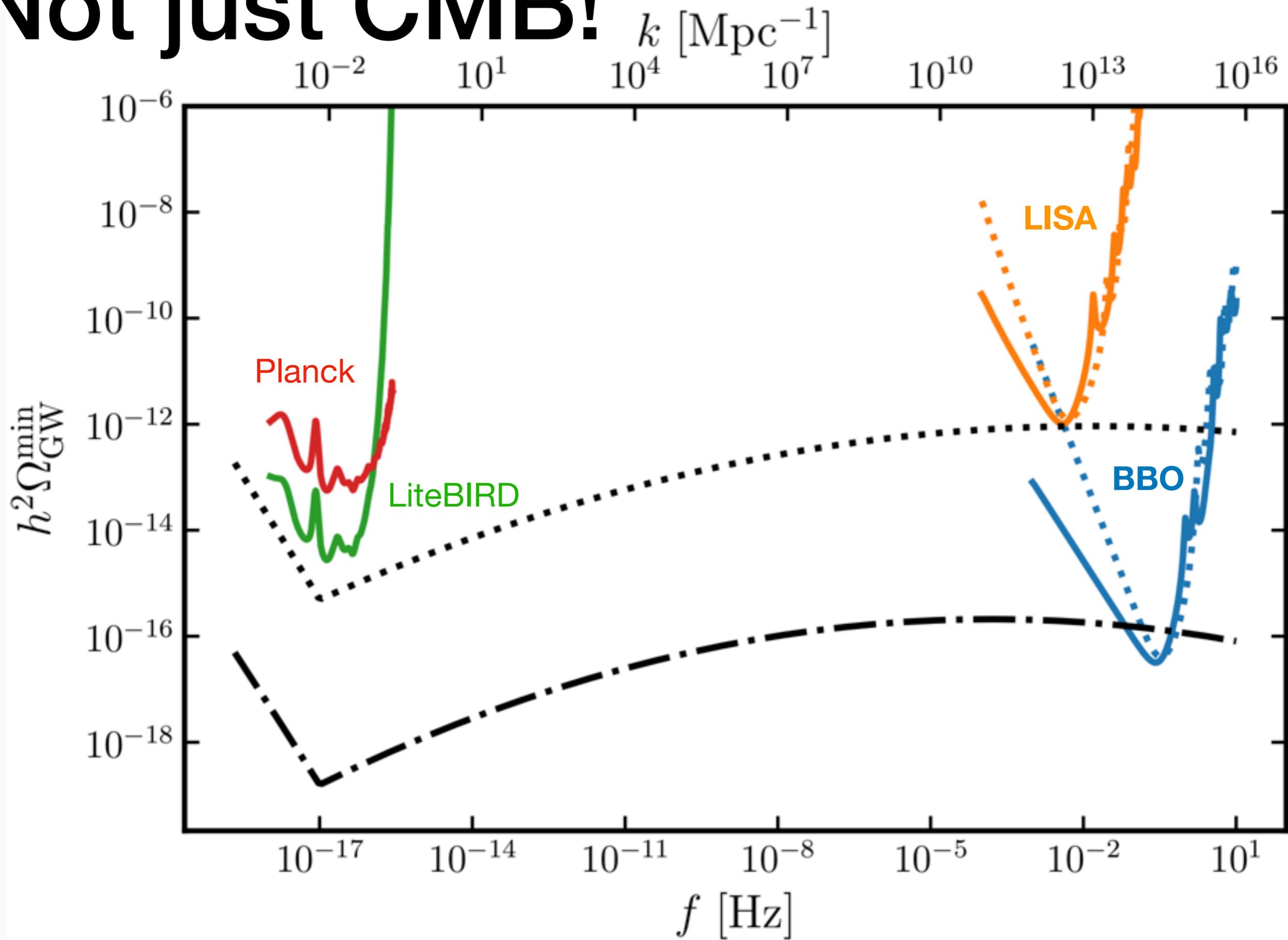


## B-mode CMB spectrum, $C_l^{\text{BB}}$



- Sourced tensor spectrum can be close to scale invariant, but can also be bumpy

# Not just CMB!



# Large bispectrum in GW from SU(2) fields



Aniket Agrawal  
(MPA)

$$\frac{B_h^{RRR}(k, k, k)}{P_h^2(k)} \approx \frac{25}{\Omega_A}$$



Tomo Fujita  
(Kyoto)

$$\langle \hat{h}_R(\mathbf{k}_1) \hat{h}_R(\mathbf{k}_2) \hat{h}_R(\mathbf{k}_3) \rangle = (2\pi)^3 \delta \left( \sum_{i=1}^3 \mathbf{k}_i \right) B_h^{RRR}(k_1, k_2, k_3)$$

- $\Omega_A \ll 1$  is the energy density fraction of the gauge field
- $B_h/P_h^2$  is of order unity for the vacuum contribution  
[Maldacena (2003); Maldacena & Pimentel (2011)]
- *Gaussianity offers a powerful test of whether the detected GW comes from the vacuum or sources*

# NG generated at the tree level

$$L_3^{(i)} = c^{(i)} \left[ \epsilon^{abc} t_{ai} t_{bj} \left( \partial_i t_{cj} - \frac{m_Q^2 + 1}{3m_Q \tau} \epsilon^{ijk} t_{ck} \right) \right.$$

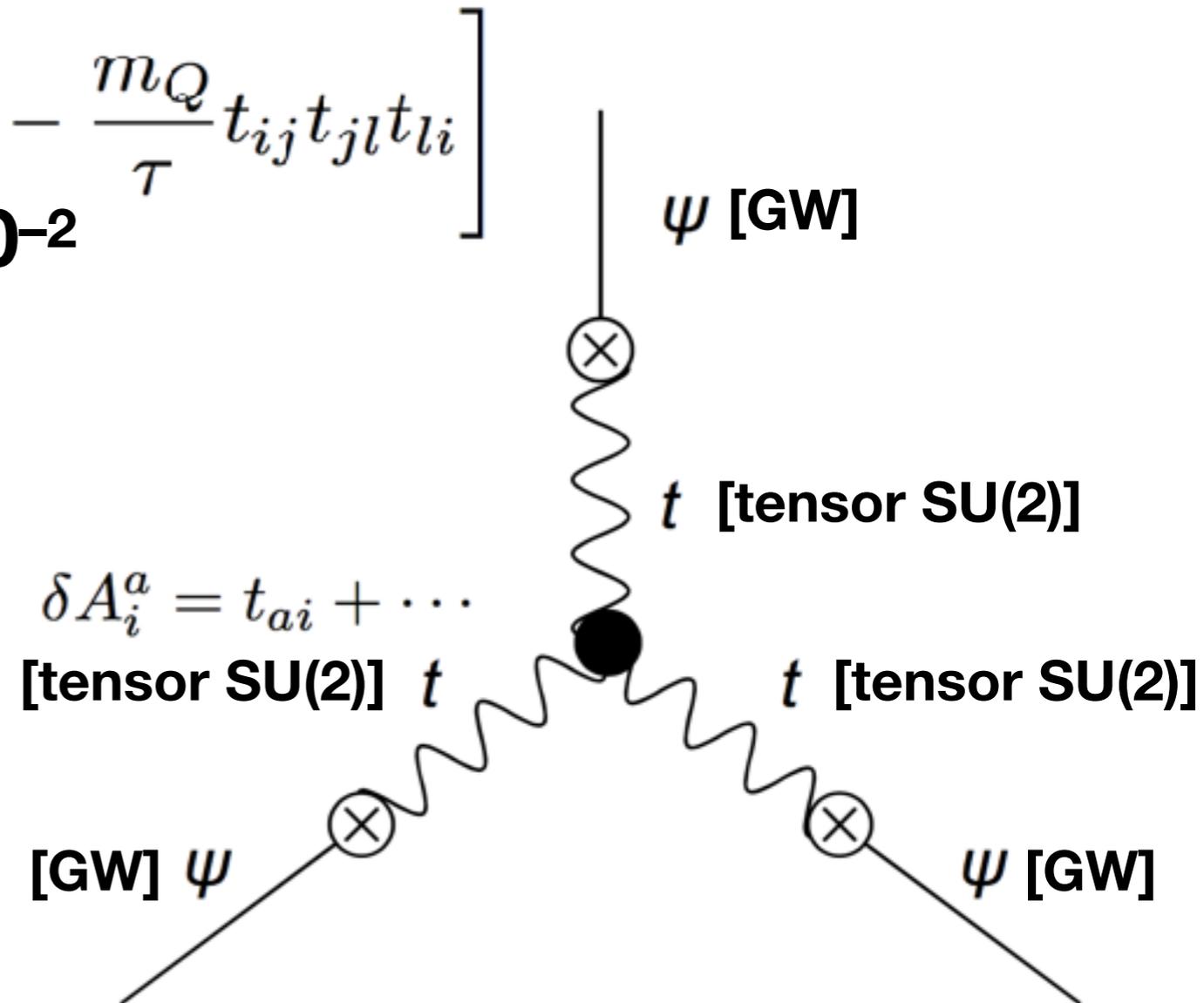
$$\left. - \frac{m_Q}{\tau} t_{ij} t_{jl} t_{li} \right]$$

$$c^{(i)} = g = m_Q^2 H / \sqrt{\epsilon_B} M_{\text{Pl}} \sim 10^{-2}$$

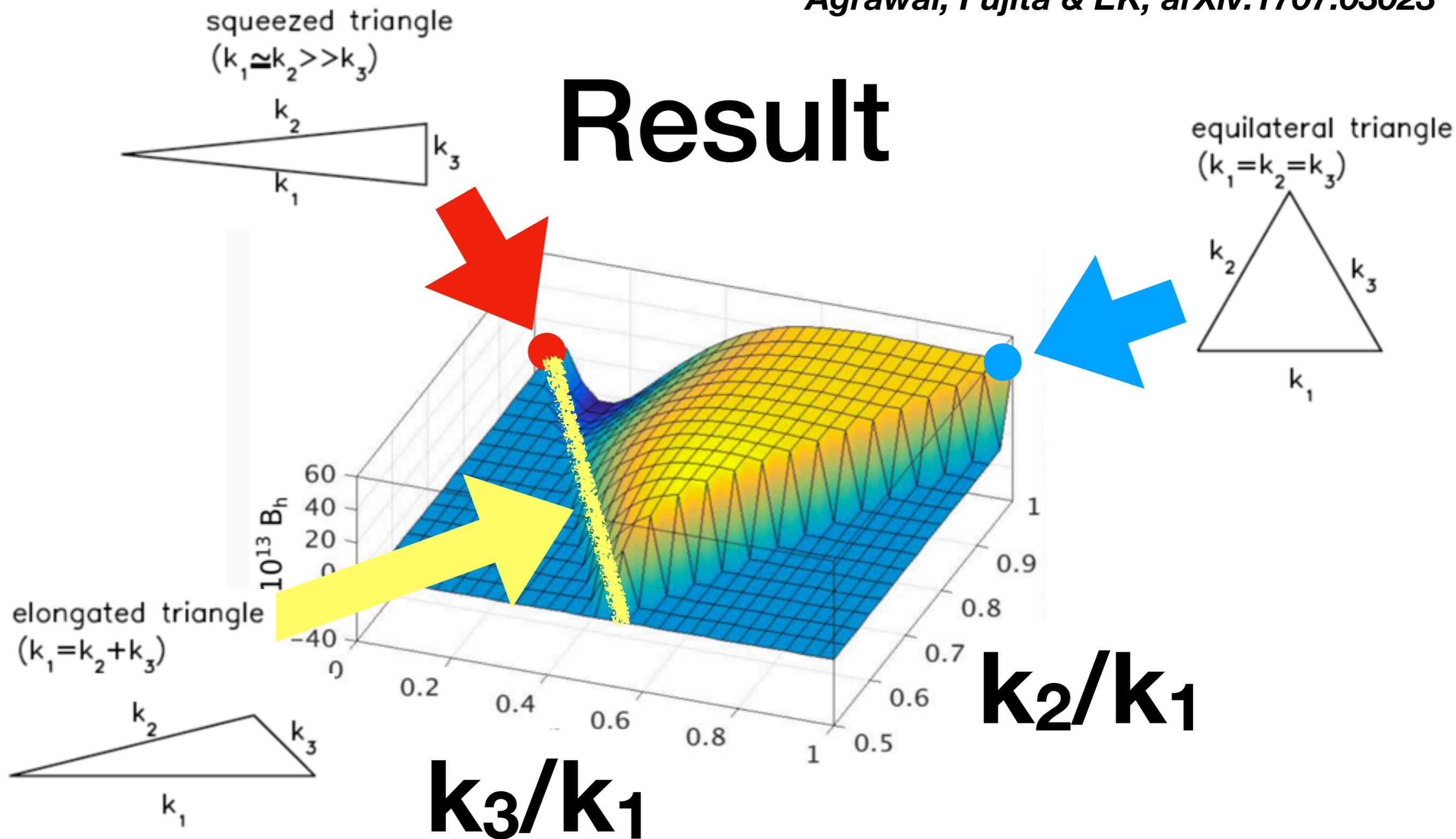
$$\epsilon_B \equiv \frac{g^2 Q^4}{H^2 M_{\text{Pl}}^2} \simeq \frac{2\Omega_A}{1 + m_Q^{-2}} \ll 1$$

$$m_Q \equiv gQ/H \quad [m_Q \sim \text{a few}]$$

- This diagram generates second-order equation of motion for GW



# Result



- This shape is similar to, but not exactly the same as, what was used by the Planck team to look for tensor bispectrum

# Current Limit on Tensor NG

- The Planck team reported a limit on the tensor bispectrum in the following form:

$$f_{\text{NL}}^{\text{tens}} \equiv \frac{B_h^{+++}(k, k, k)}{F_{\text{scalar}}^{\text{equil.}}(k, k, k)}$$

- The denominator is the **scalar** equilateral bispectrum template, giving  $F_{\text{scalar}}^{\text{equil.}}(k, k, k) = (18/5)P_{\text{scalar}}^2(k)$
- The current 68%CL constraint is  $f_{\text{NL}}^{\text{tens}} = 400 \pm 1500$

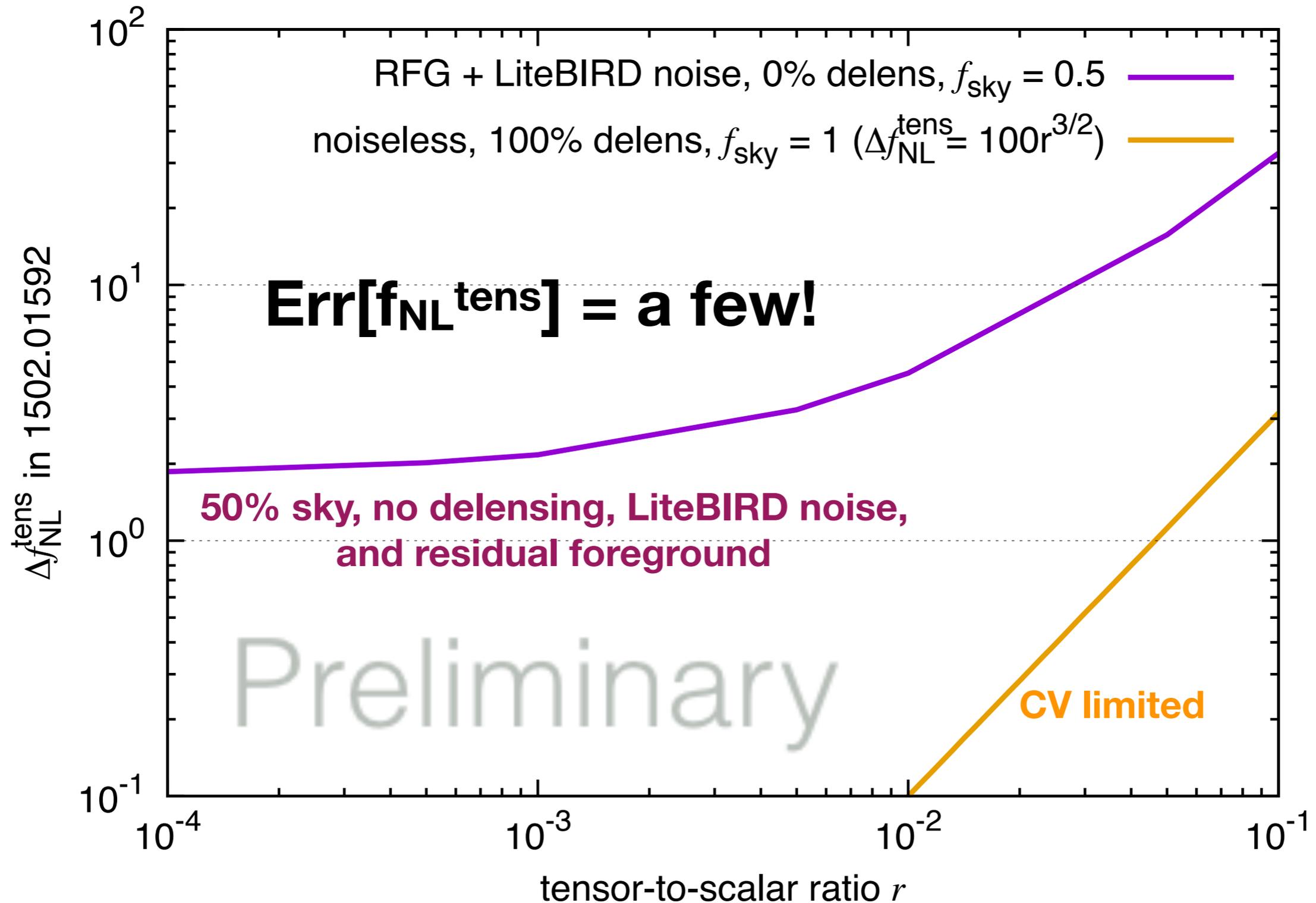
# SU(2), confronted

- The SU(2) model of Dimastrogiovanni et al. predicts:

$$f_{\text{NL}}^{\text{tens}} \approx \frac{125}{18\sqrt{2}} \frac{r^2}{\epsilon_B} \approx 2.5 \frac{r^2}{\Omega_A}$$

- The current 68%CL constraint is  $f_{\text{NL}}^{\text{tens}} = 400 \pm 1500$ 
  - This is already constraining!

# LiteBIRD would nail it!



# JAXA

+ possible participations  
from USA, Canada,  
Europe

## LiteBIRD

2025– [proposed]



Target:  $\delta r < 0.001$

# JAXA

+ possible participations  
from USA, Canada,  
Europe

## LiteBIRD

2025– [proposed]



**Polarisation satellite dedicated to  
measure CMB polarisation from  
primordial GW, with a few thousand  
super-conducting detectors in space**

# JAXA

+ possible participations  
from USA, Canada,  
Europe

## LiteBIRD

2025– [proposed]

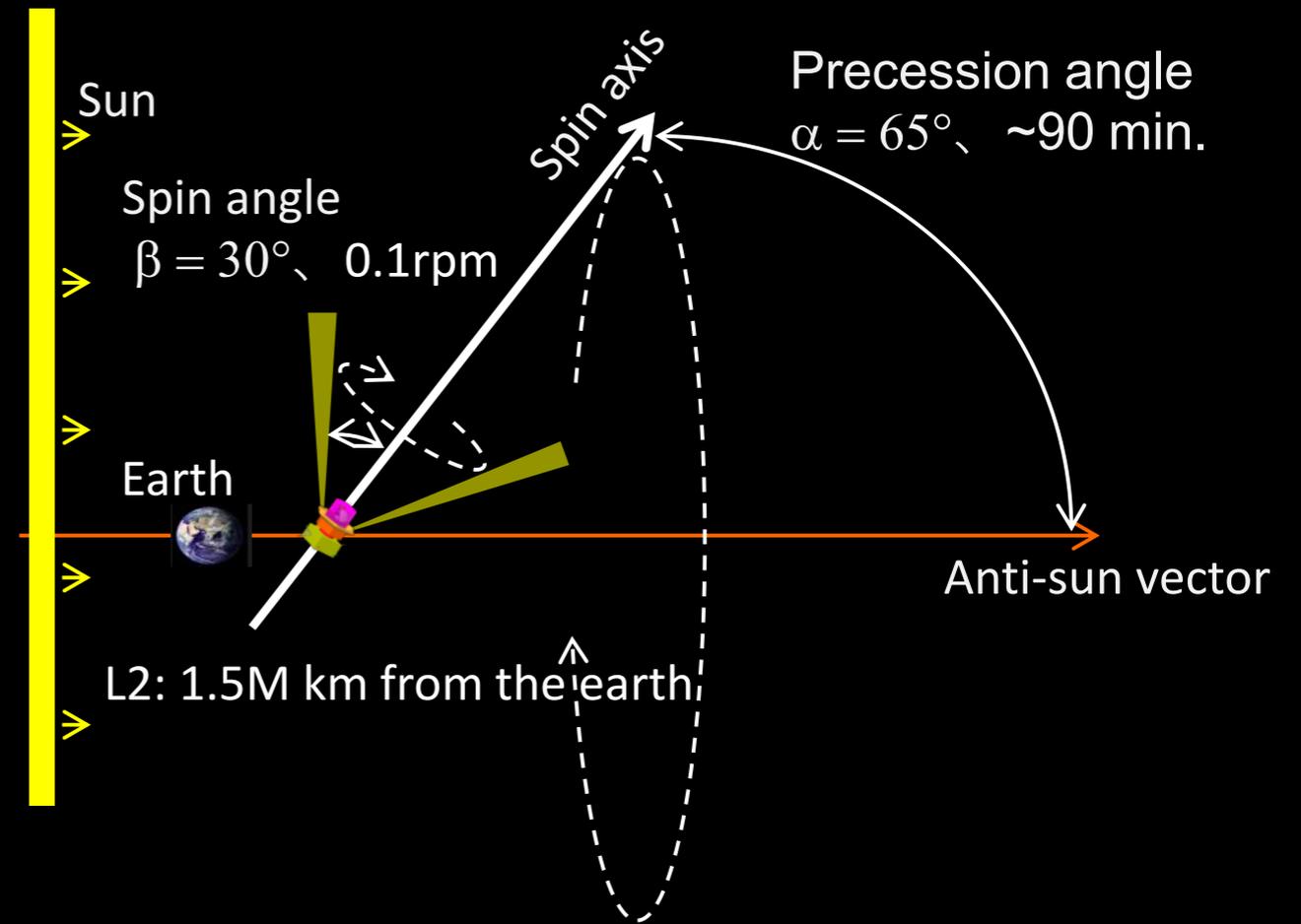


**Down-selected by JAXA as  
one of the two missions  
competing for a launch in mid 2020's**

# Observation Strategy



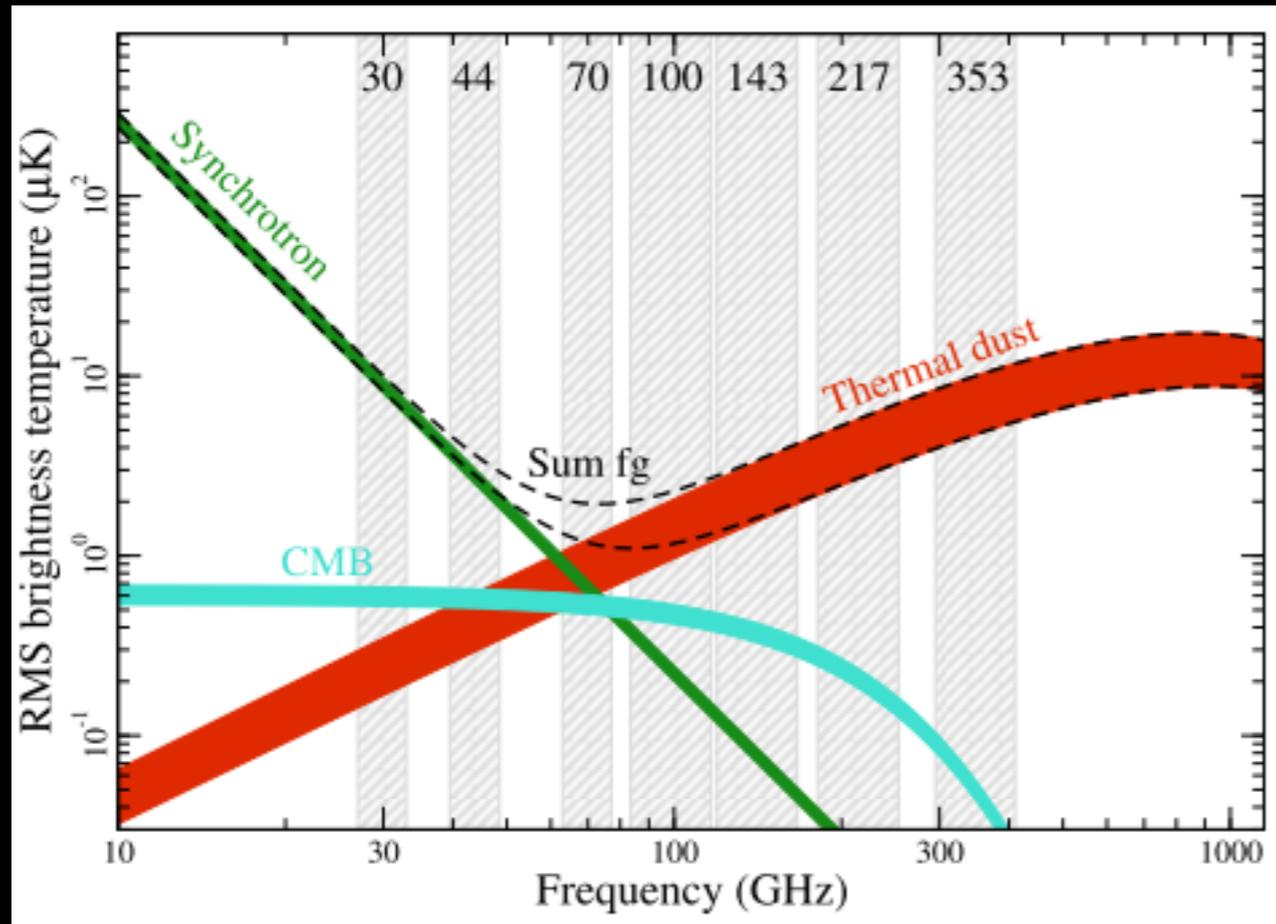
JAXA H3 Launch Vehicle (JAXA)



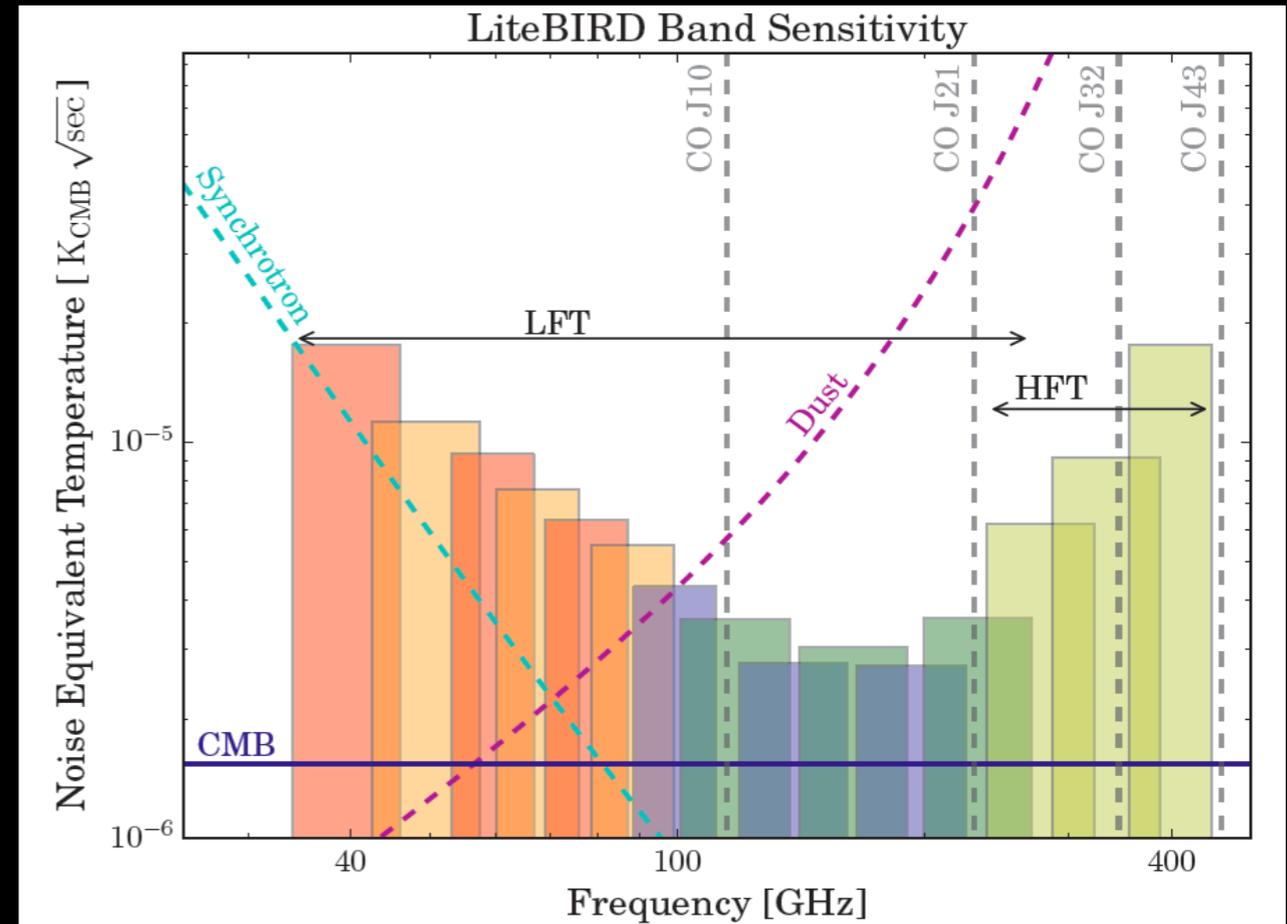
- Launch vehicle: **JAXA H3**
- Observation location: Second Lagrangian point (**L2**)
- Scan strategy: **Spin and precession, full sky**
- Observation duration: **3-years**
- Proposed launch date: **Mid 2020's**

*Slide courtesy Toki Suzuki (Berkeley)*

# Foreground Removal



Polarized galactic emission (Planck X)

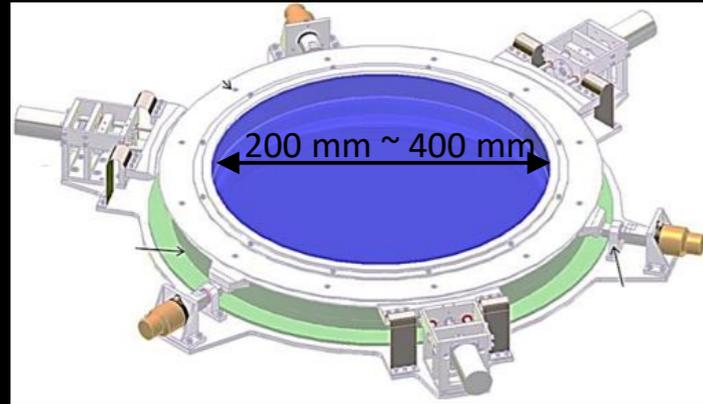


LiteBIRD: 15 frequency bands

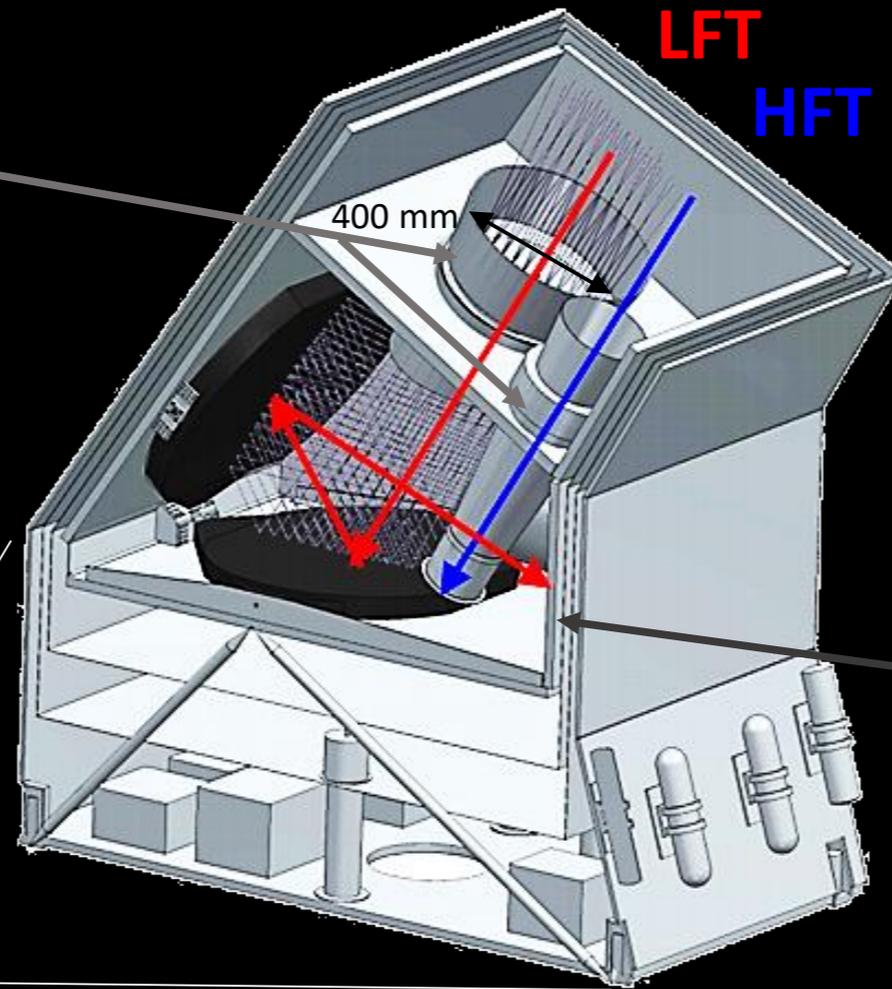
- Polarized foregrounds
  - Synchrotron radiation and thermal emission from inter-galactic dust
  - Characterize and remove foregrounds
- 15 frequency bands between 40 GHz - 400 GHz
  - Split between Low Frequency Telescope (LFT) and High Frequency Telescope (HFT)
  - LFT: 40 GHz – 235 GHz
  - HFT: 280 GHz – 400 GHz

Slide courtesy Toki Suzuki (Berkeley)

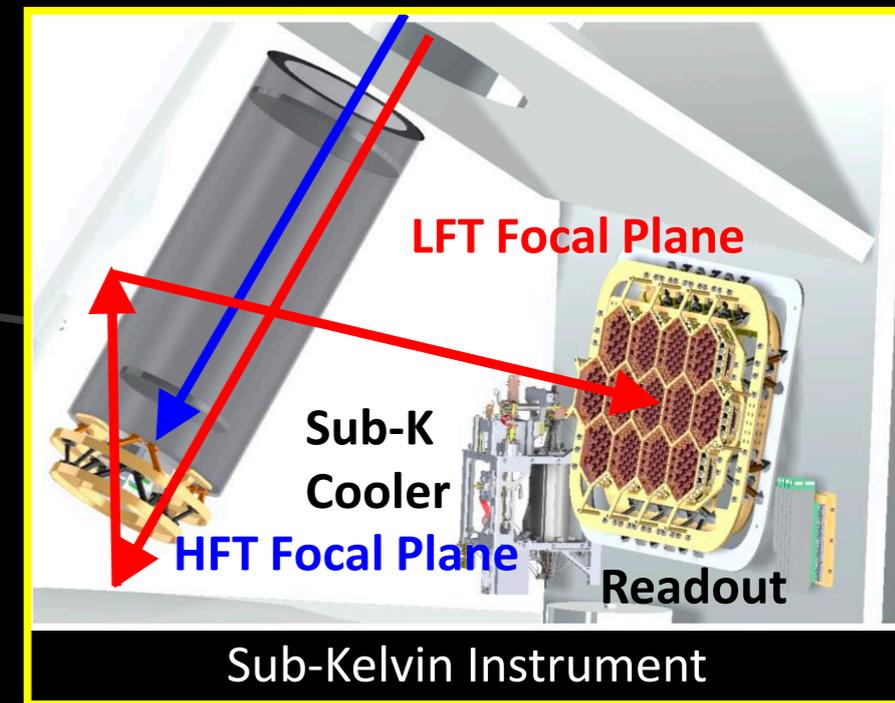
# Instrument Overview



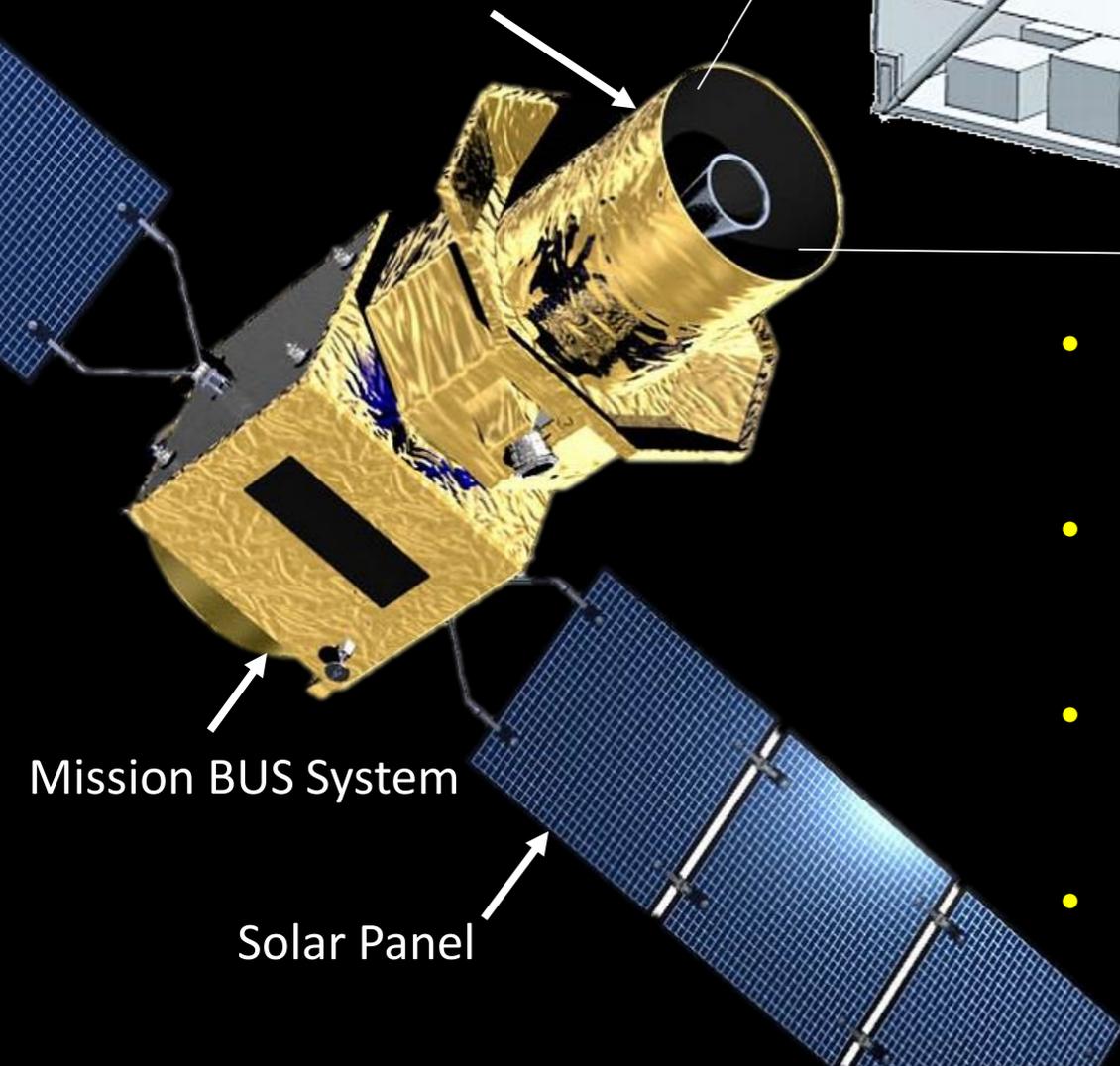
Half-wave plate



Stirling & Joule Thomson Coolers



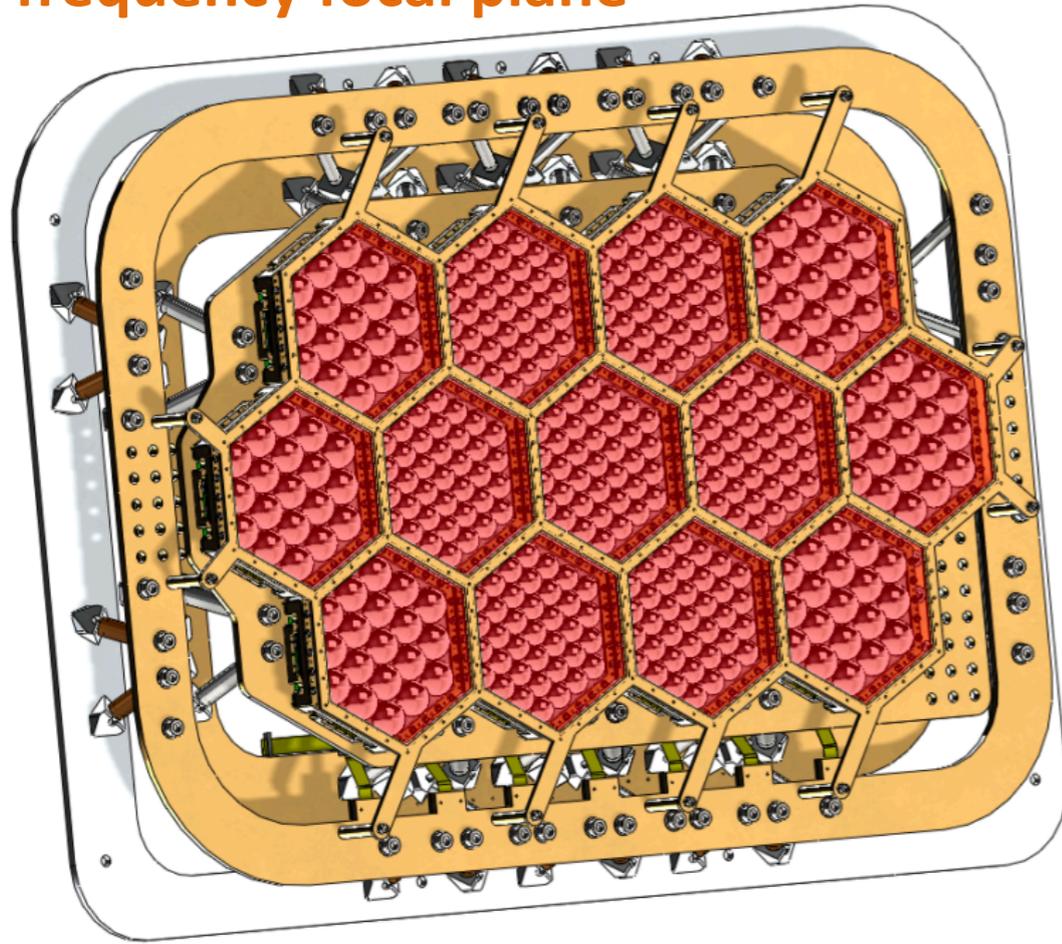
Cold Mission System



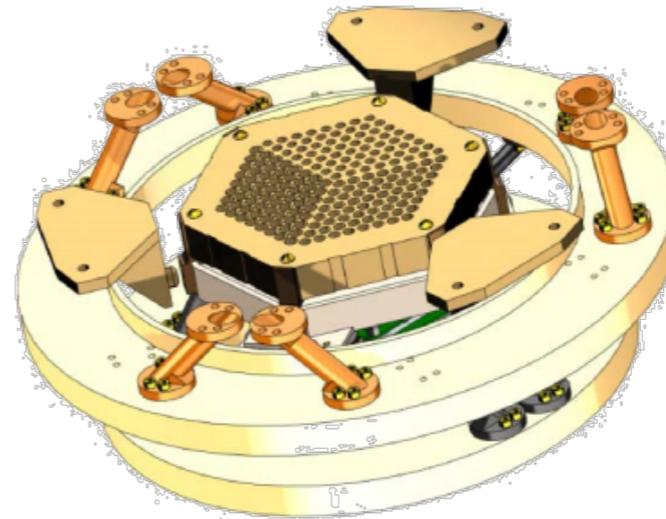
- **Two telescopes**
  - Crossed-Dragone (LFT) & on-axis refractor (HFT)
- **Cryogenic rotating achromatic half-wave plate**
  - Modulates polarization signal
- **Stirling & Joule Thomson coolers**
  - Provide cooling power above 2 Kelvin
- **Sub-Kelvin Instrument**
  - Detectors, readout electronics, and a sub-kelvin cooler

# LFT and HFT focal plane units using TES

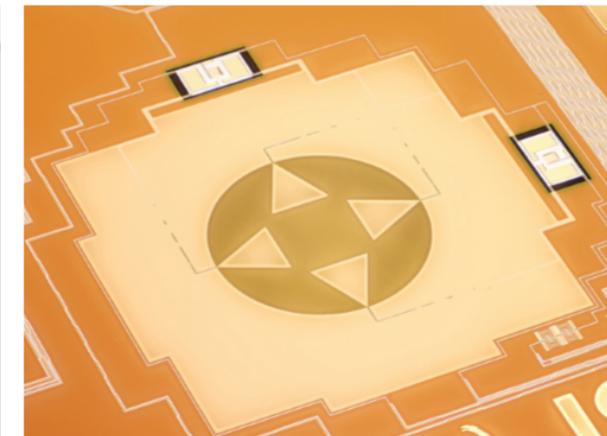
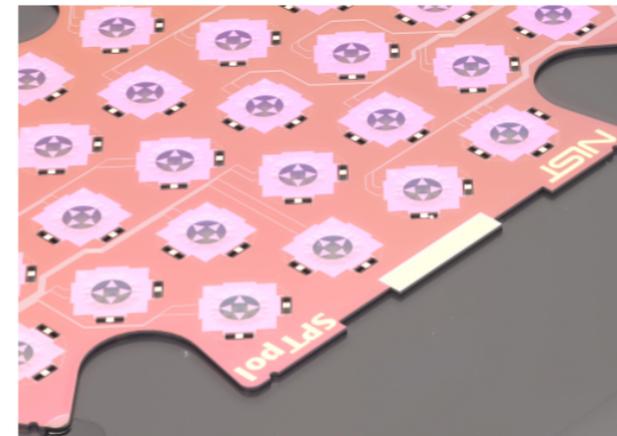
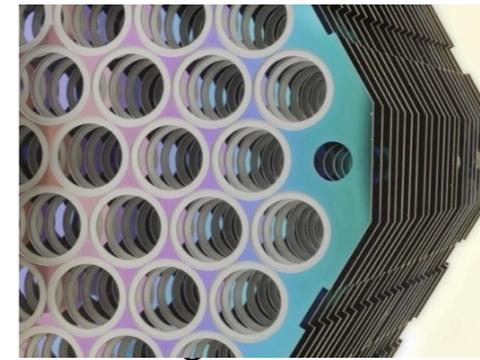
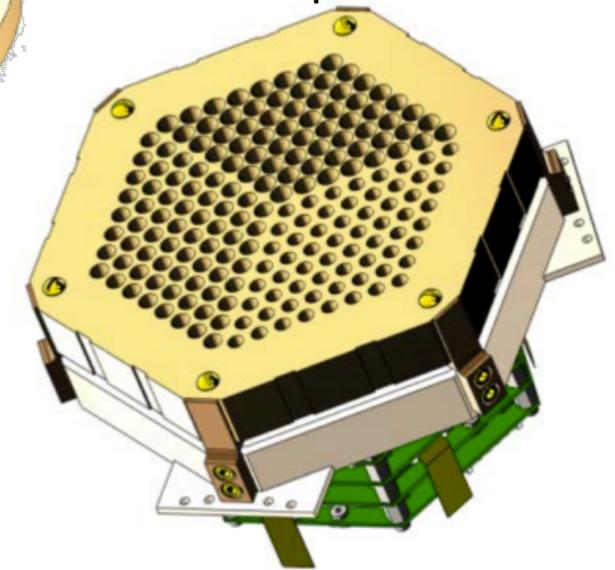
## Low frequency focal plane



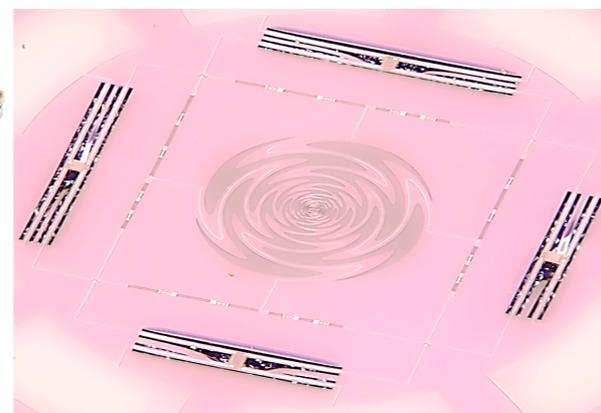
## High frequency focal plane



Each color per feed, and three colors within one focal plane.



Three colors per pixel with a lenslet coupling.



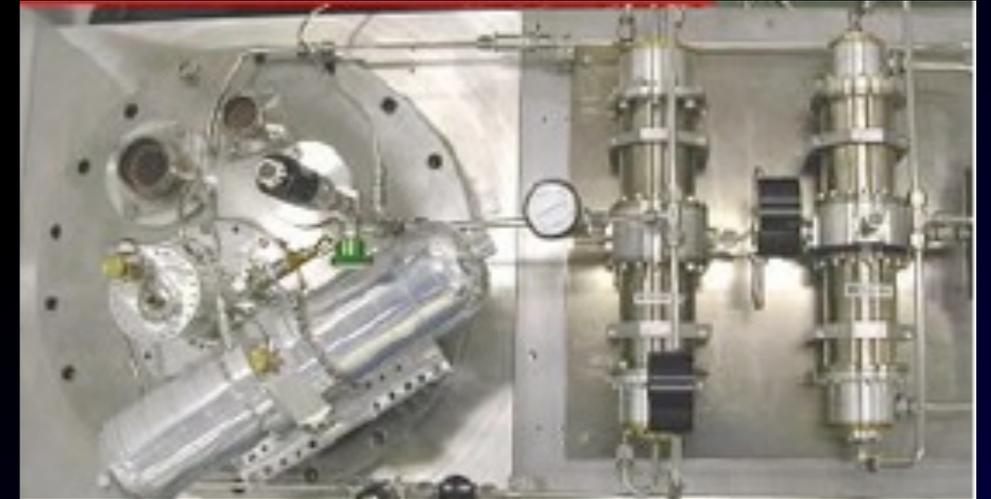
- The current baseline design uses a single ADR to cool the both focal planes.
- The LF focal plane has \*\* TESs and the HF focal plane has \*\* TESs.
- The TES is read by SQUID together with the readout electronics is based on the digital frequency multiplexing system.
- The effect of the cosmic ray is evaluated by building a model. The irradiation test is in plan.

*Slide courtesy Tomo Matsumura (Kavli IPMU)*

# Cooling system

## Cryogenics

- Warm launch
- 3 years of observations
- 4 K for the mission instruments (optical system)
- 100 mK for the focal plane



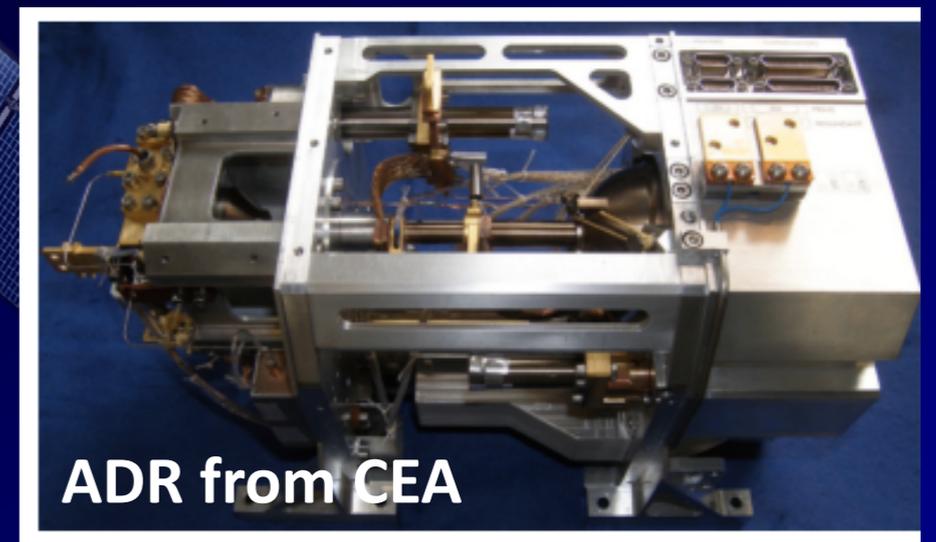
SHI/JAXA

## Mechanical cooler

- The 2-stage Stirling cooler and 4K-JT cooler from the heritage of the JAXA satellites, **Akari** (Astro-F), **JEM-SMILES** and **Astro-H**.
- The 1K-JT provides the 1.7 K interface to the sub-Kelvin stage.

## Sub-Kelvin cooler

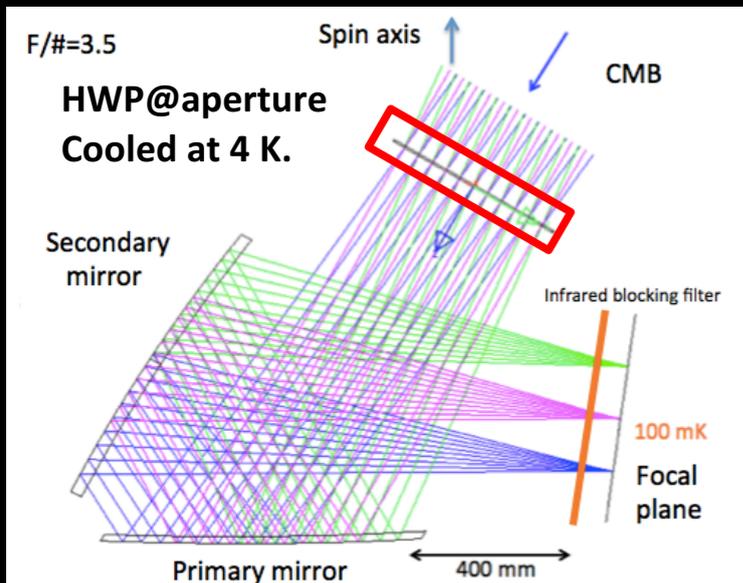
- ADR has a high-TRL and extensive development toward **Astro-H**, **SPICA**, and **Athena**.
- Closed dilution with the Planck heritage is also under development.



ADR from CEA

**Slide courtesy Tomo Matsumura (Kavli IPMU)**

# Polarization modulator



- Due to our focus on the primordial signal at low  $l$ , we employ the continuously rotating achromatic half-wave plate (HWP).
- The HWP modulator suffices mitigating the  $1/f$  noise and the differential systematics.

## Broadband coverage

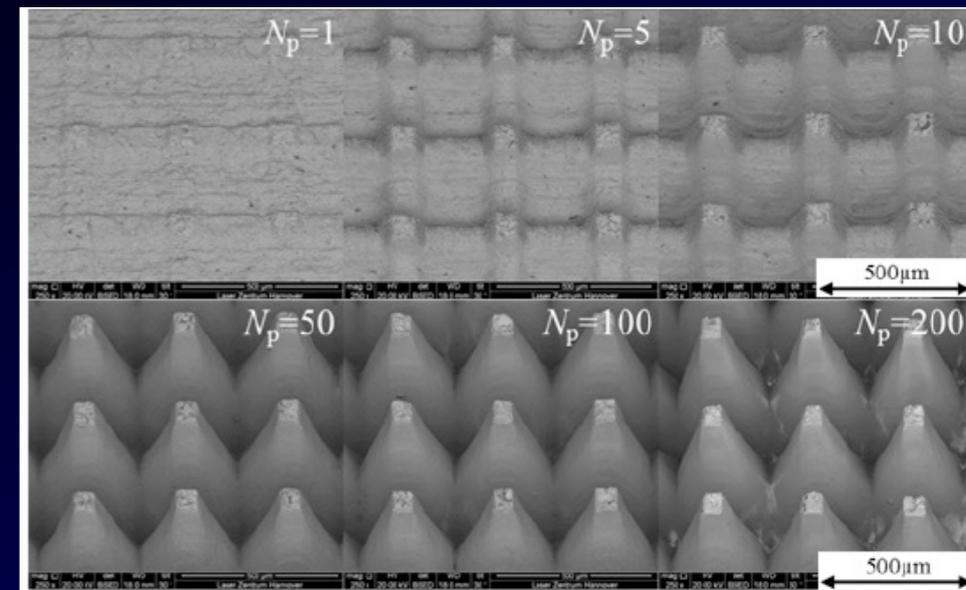
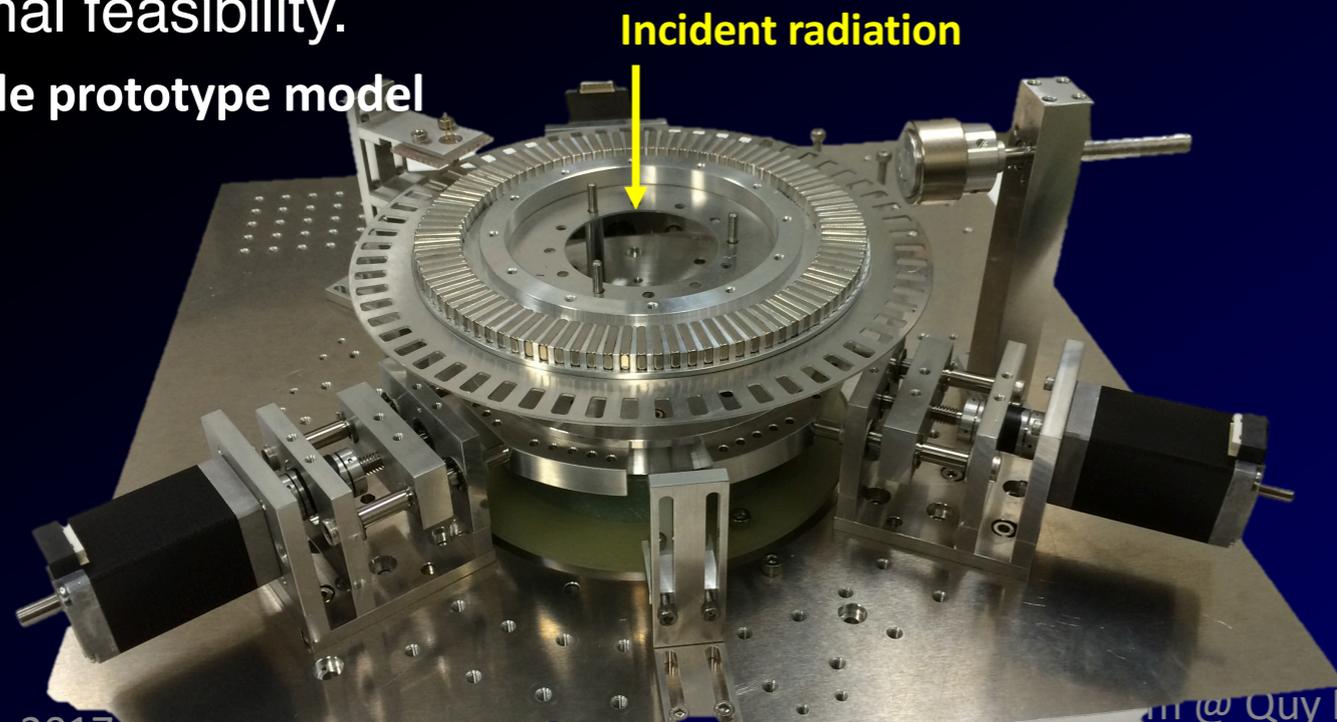
- The broadband coverage is done by the sub-wavelength anti-reflection structure.
- The broadband modulation efficiency is achieved by using 9-layer achromatic HWP.

Note: we also employ the polarization modulator for HFT.

## Rotational mechanism

The continuous rotation is achieved by employing the superconducting magnetic bearing. This system has a heritage from EBEX. The prototype system has built and test the kinetic and thermal feasibility.

The 1/9 scale prototype model



The proton irradiation test is conducted to key components, including sapphire, YBCO, and magnets. We have not found the no-go results. And the further test is in progress.

# Summary

- Inflation looks good: all the CMB data support it
- **Next frontier**: Using CMB polarisation to find GWs from inflation. **Definitive evidence for inflation!**
- With LiteBIRD we plan to reach  $r \sim 10^{-3}$ , i.e., 100 times better than the current bound
- GW from vacuum or sources? An exciting window to new physics