



WMAP 5-Year Results: Implications for Inflation

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WMAP 5-Year Papers

- **Hinshaw et al.**, “*Data Processing, Sky Maps, and Basic Results*” [0803.0732](#)
- **Hill et al.**, “*Beam Maps and Window Functions*” [0803.0570](#)
- **Gold et al.**, “*Galactic Foreground Emission*” [0803.0715](#)
- **Wright et al.**, “*Source Catalogue*” [0803.0577](#)
- **Nolta et al.**, “*Angular Power Spectra*” [0803.0593](#)
- **Dunkley et al.**, “*Likelihoods and Parameters from the WMAP data*” [0803.0586](#)
- **Komatsu et al.**, “*Cosmological Interpretation*” [0803.0547](#)

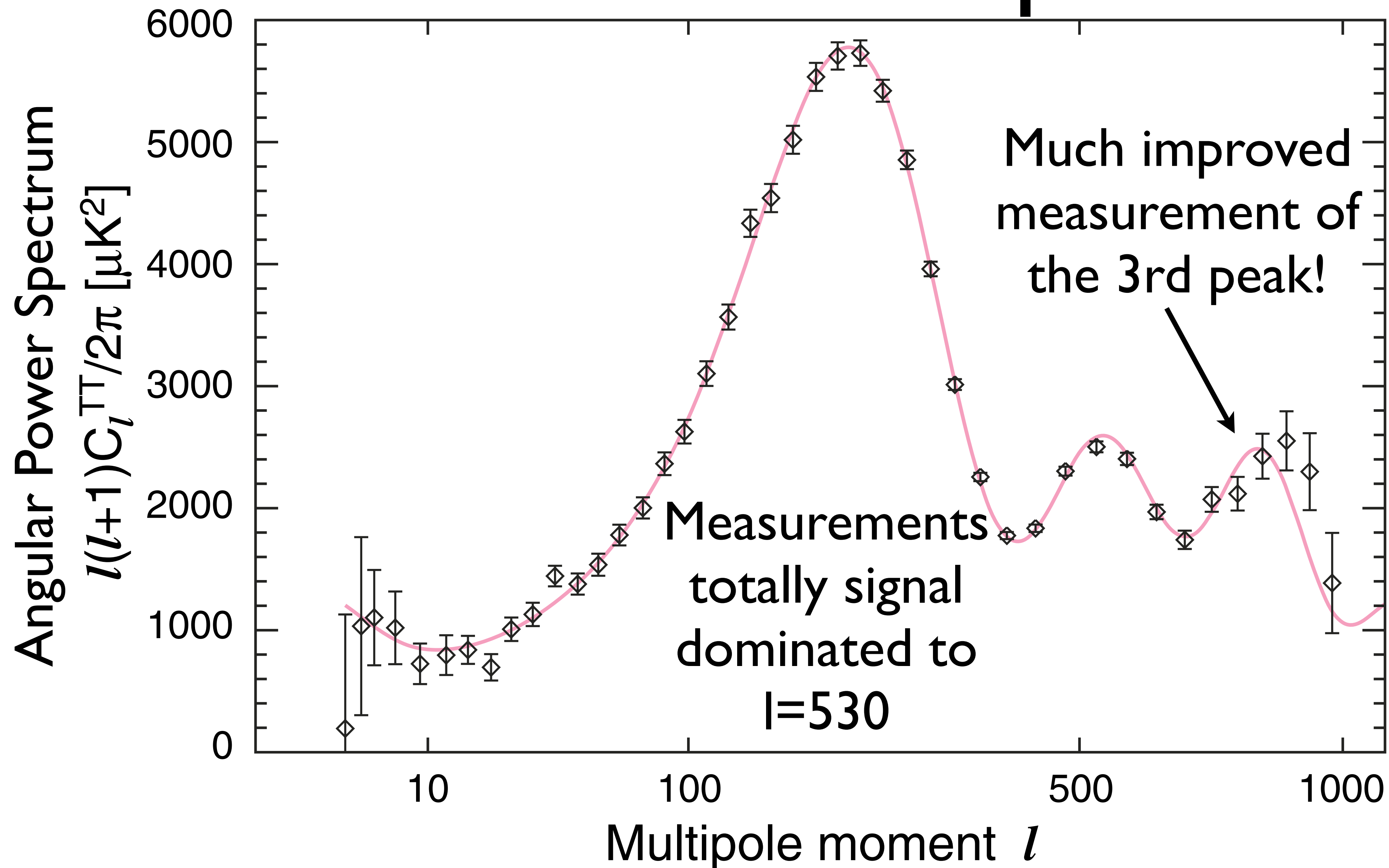
WMAP 5-Year Science Team

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Special
Thanks to
WMAP
Graduates!

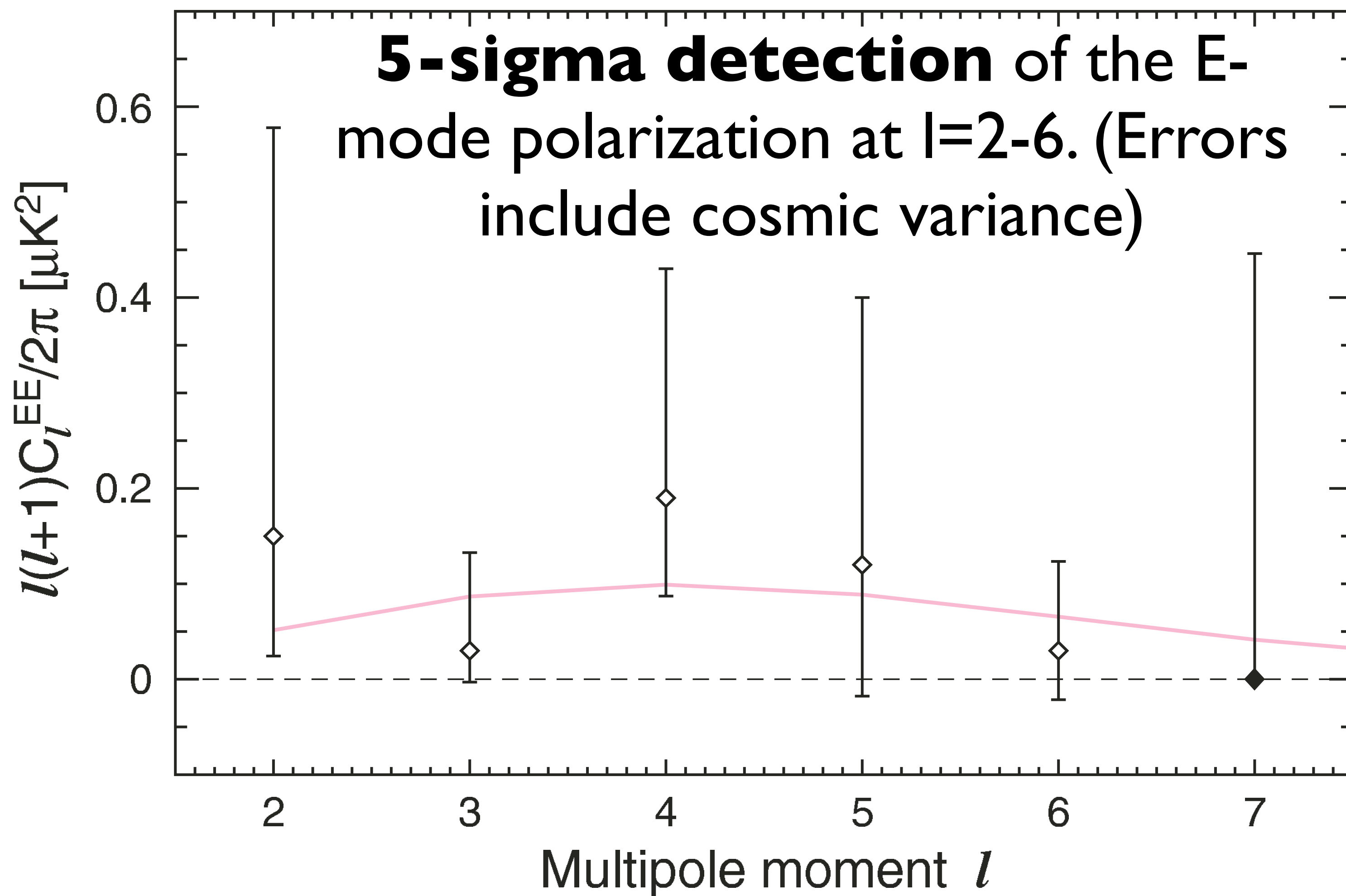
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5-Year TT Power Spectrum



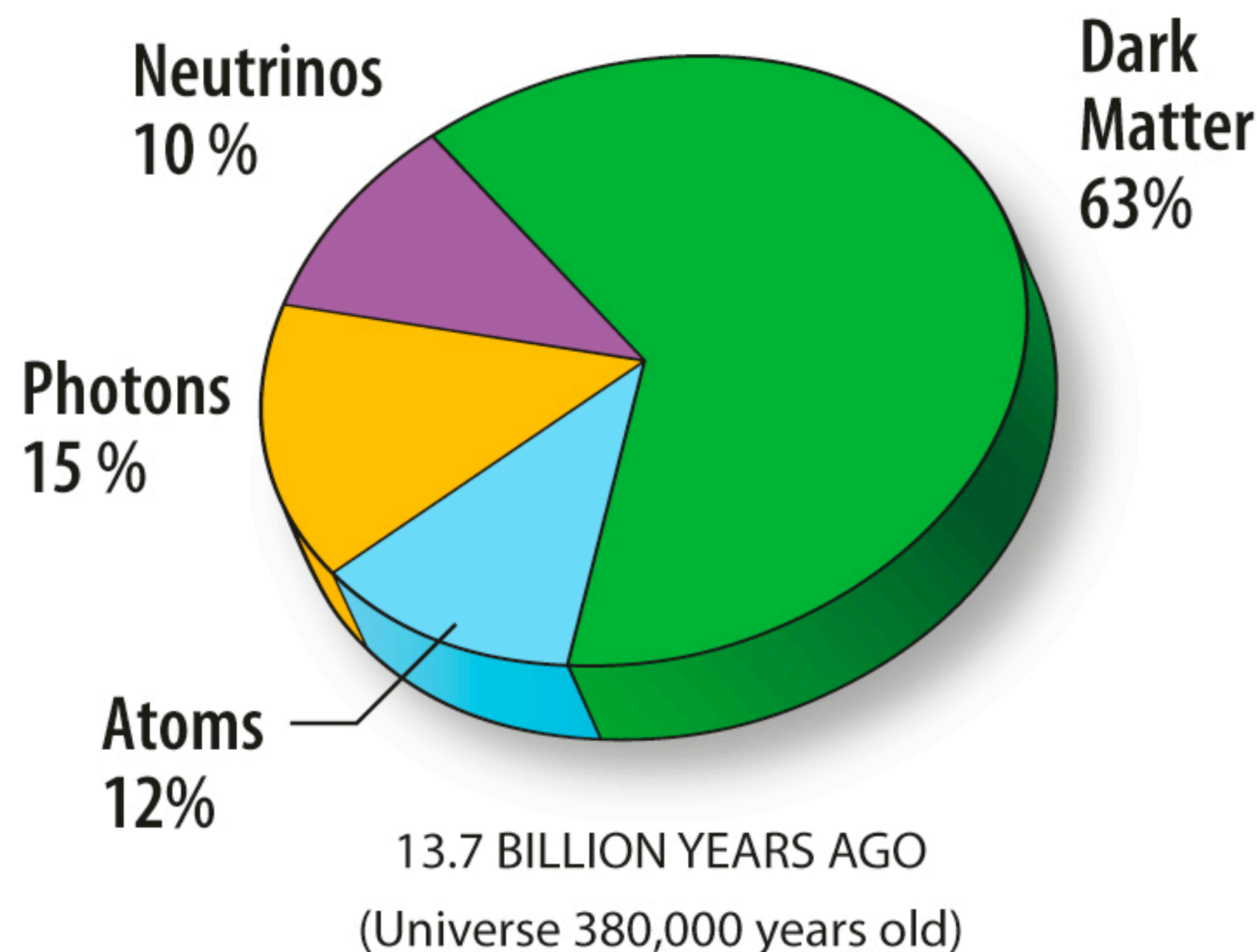
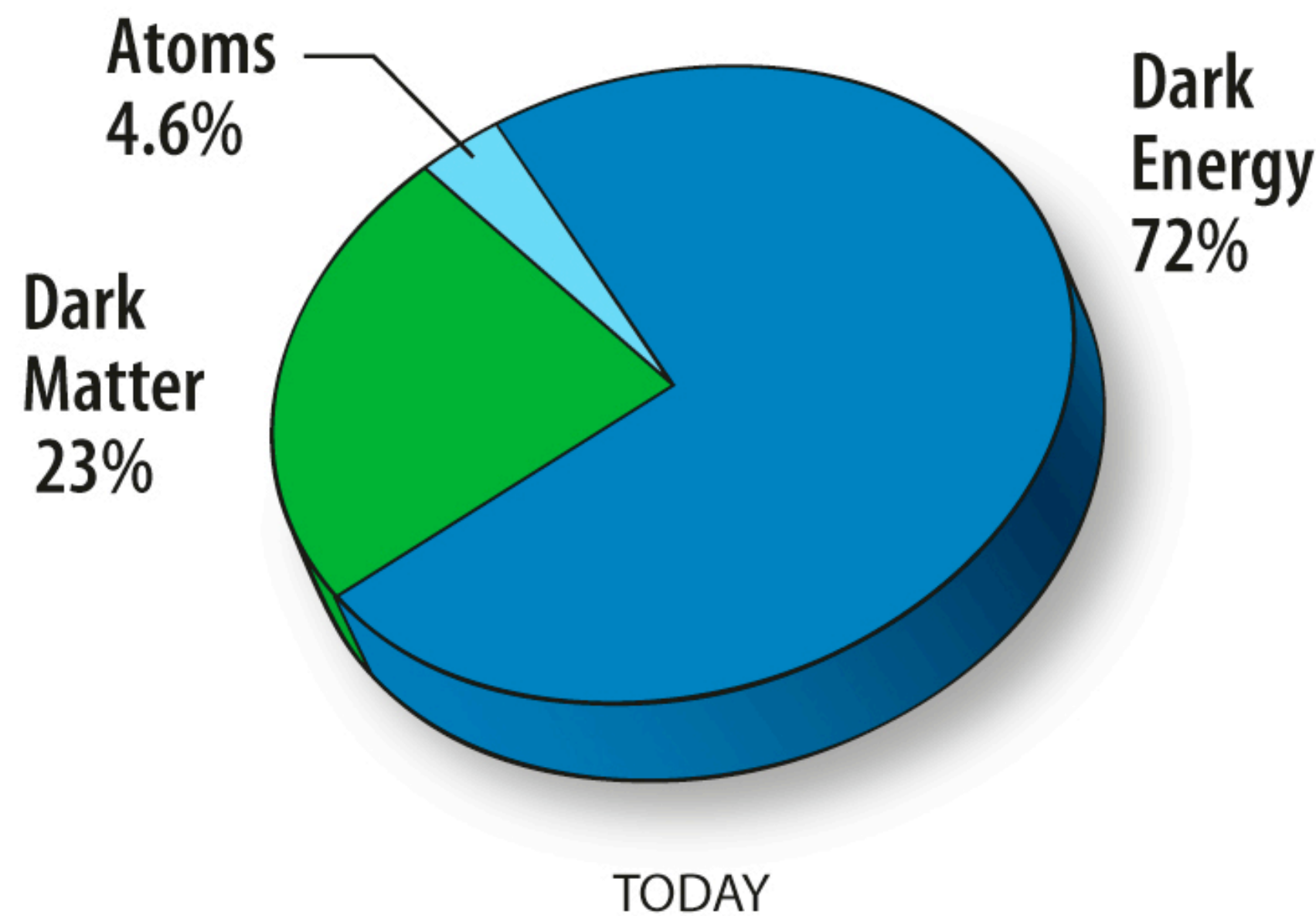
5-Year E-Mode Polarization Power Spectrum at Low l

E-Mode Angular Power Spectrum



Black Symbols are upper limits

~WMAP 5-Year~ Pie Chart Update!



- Universe today
 - Age: **13.73 +/- 0.12 Gyr**
 - Atoms: **4.62 +/- 0.15 %**
 - Dark Matter: **23.3 +/- 1.3%**
 - Vacuum Energy: **72.1 +/- 1.5%**
- When CMB was released 13.7 B yrs ago
 - A significant contribution from the *cosmic neutrino background*

Testing Cosmic Inflation

~5 Tests~

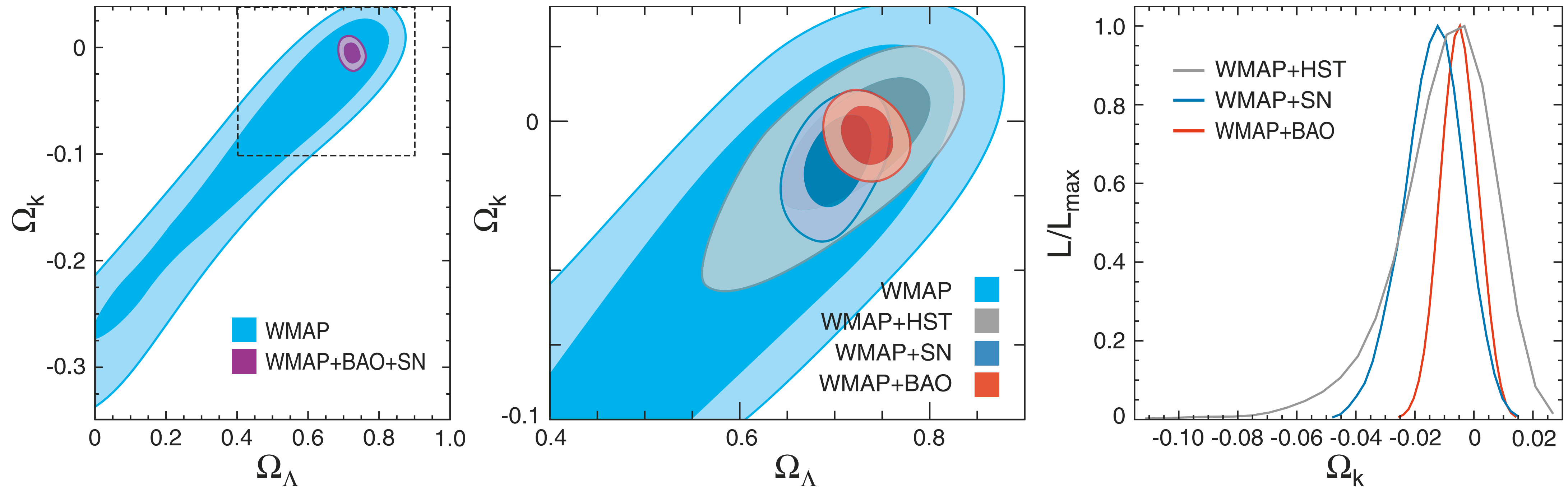
- Is the observable universe flat?
- Are the primordial fluctuations nearly Gaussian?
- Are the primordial fluctuations adiabatic?
- Is the power spectrum nearly scale invariant?
 - I talked about this already.
- Is the amplitude of gravitational waves reasonable?

How Do We Test Inflation?

- The WMAP data alone can put tight limits on most of the items in the check list. (For the WMAP-only limits, see Dunkley et al.)
- However, we can improve the limits on many of these items by adding the extra information from the **cosmological distance measurements**:
 - *Luminosity Distances* from Type Ia Supernovae (SN)
 - *Angular Diameter Distances* from the Baryon Acoustic Oscillations (BAO) in the distribution of galaxies

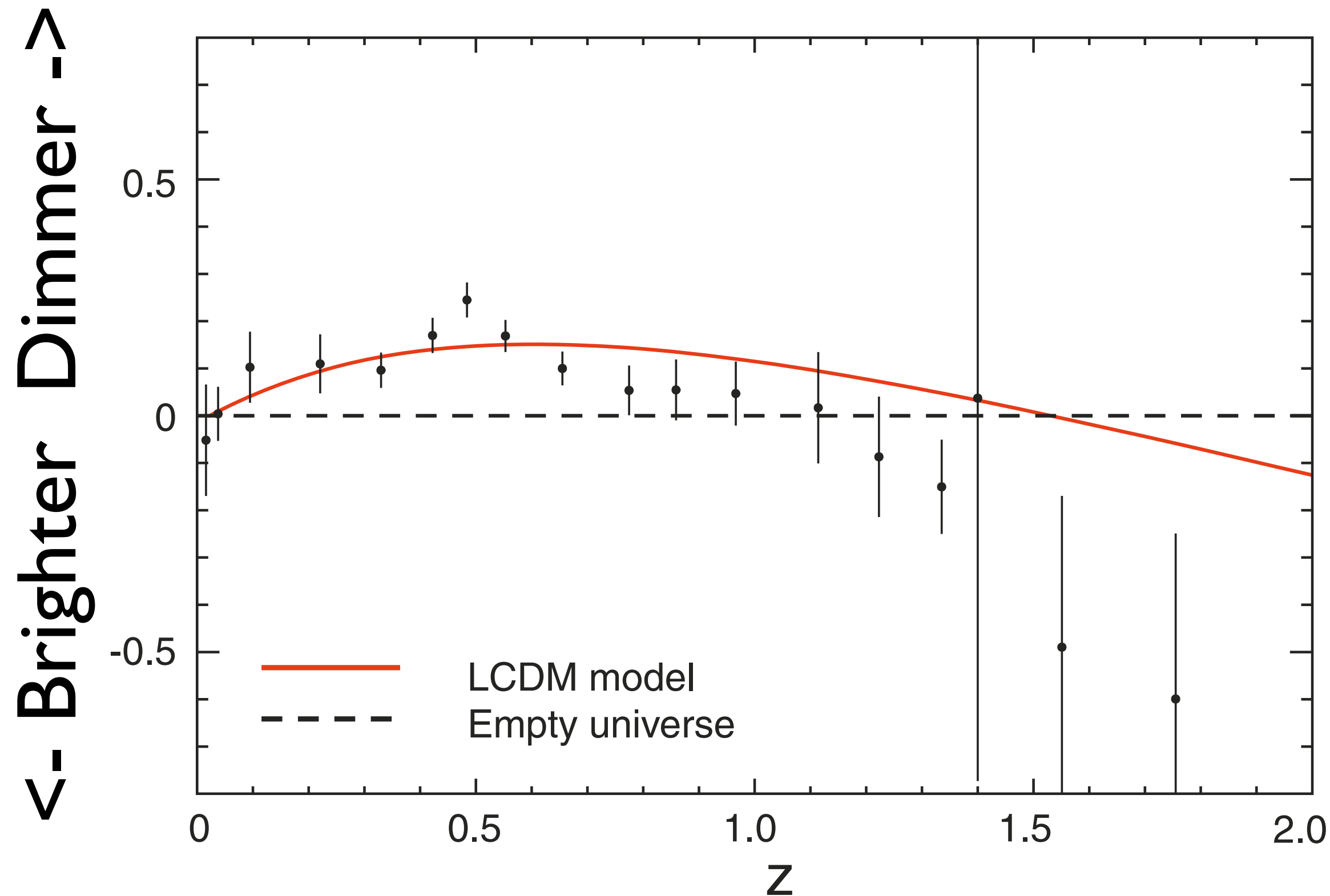
Example: Flatness

Komatsu et al.



- WMAP measures the angular diameter distance to the decoupling epoch at $z=1090$.
- The distance depends on curvature AND other things, like the energy content; thus, we need more than one distance indicators, in order to constrain, e.g., Ω_m and H_0

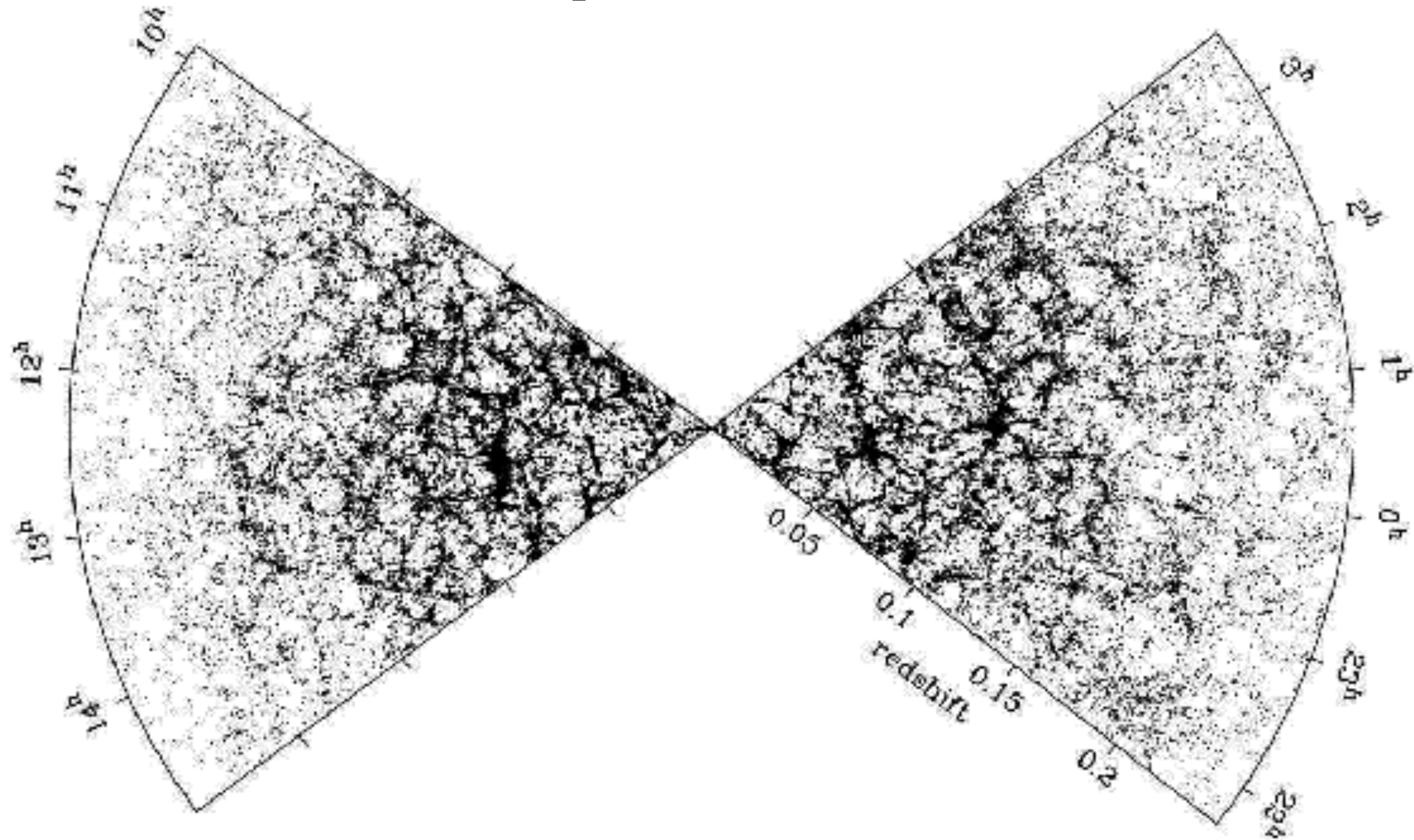
Type Ia Supernova (SN) Data



From these measurements, we get the **relative** luminosity distances between Type Ia SNe. Since we marginalize over the absolute magnitude, the current SN data are **not** sensitive to the absolute distances.

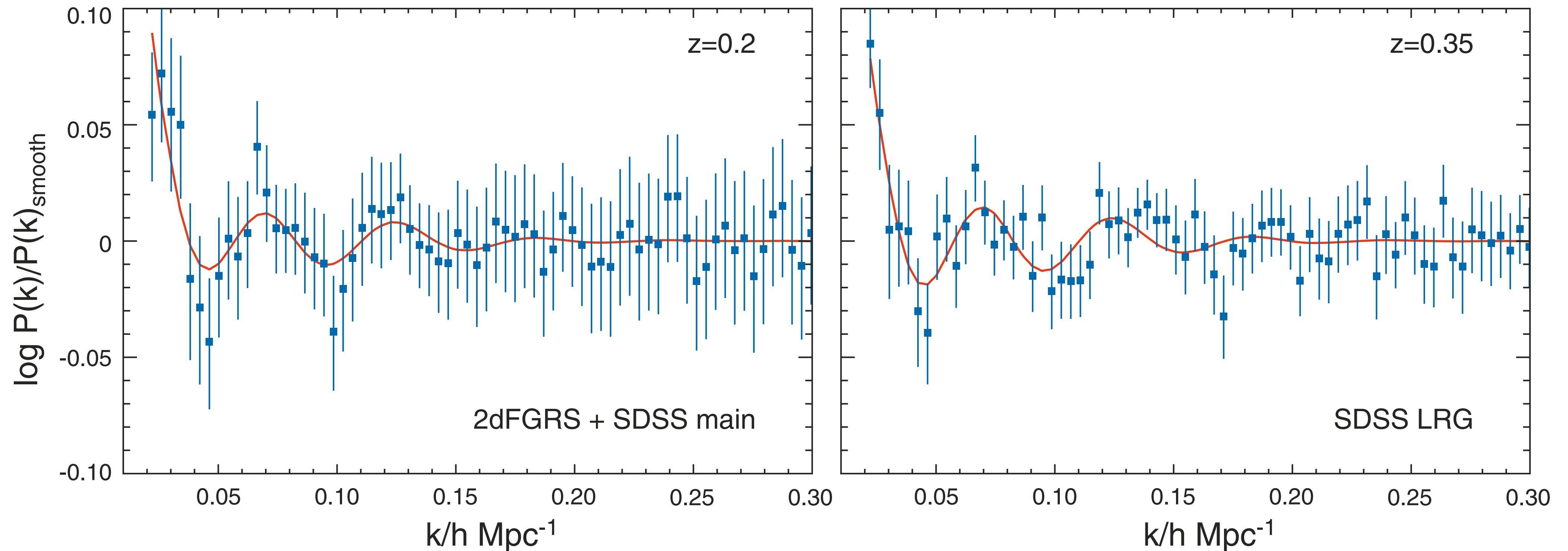
- Riess et al. (2004; 2006) HST data
- Astier et al. (2006) Supernova Legacy Survey (SNLS)
- Wood-Vasey et al. (2007) ESSENCE data

BAO in Galaxy Distribution *Tegmark et al.*



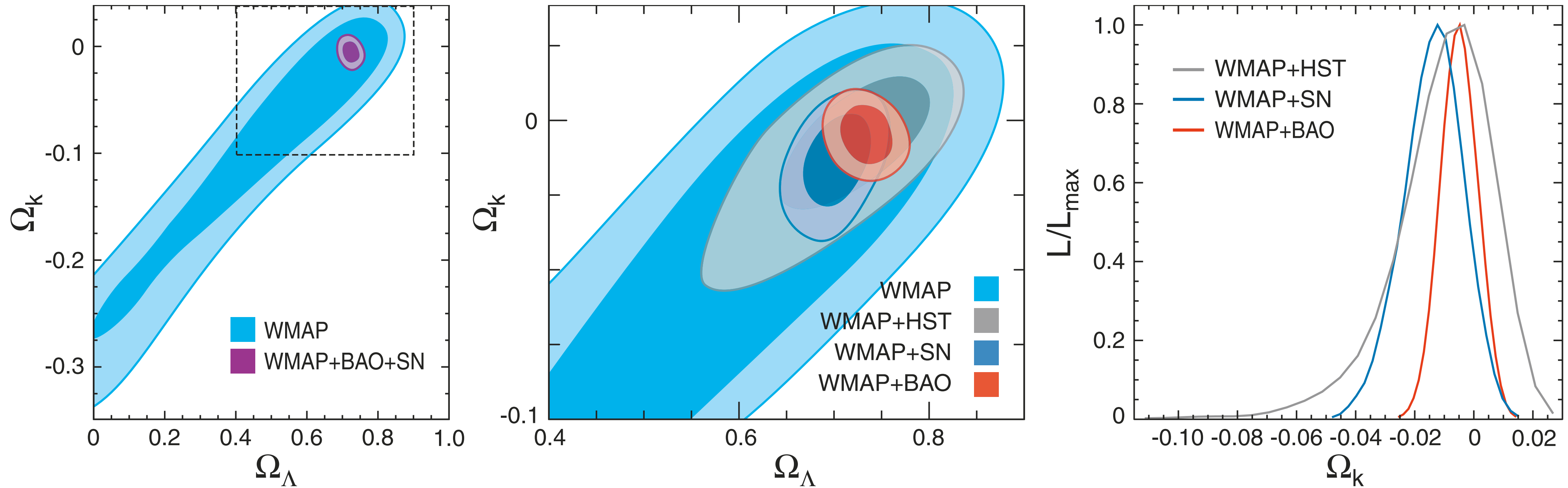
- The same acoustic oscillations should be hidden in this galaxy distribution...

BAO in Galaxy Distribution *Dunkley et al.*



- BAO measured from SDSS (main samples and LRGs) and 2dFGRS (Percival et al. 2007)
- Just like the acoustic oscillations in CMB, the galaxy BAOs can be used to measure the **absolute** distances ¹²

As a result..



- **$-0.0181 < \Omega_k < 0.0071$** (95% CL) for $w = -1$
(i.e., dark energy being a cosmological constant)
- The constraint driven mostly by WMAP+BAO

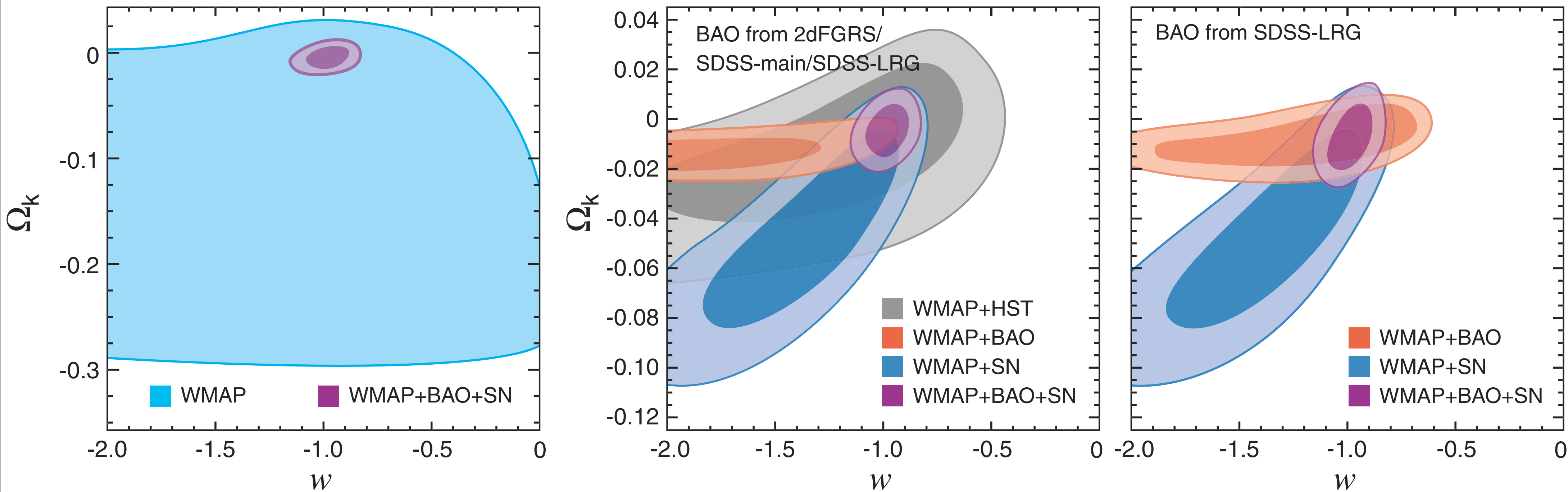
How Big Is Our Universe?

- By definition, the curvature radius of the universe is given by
 - $R_{\text{curv}} = 3h^{-1}\text{Gpc} / \text{sqrt}(\Omega_k)$
 - For negatively curved space ($\Omega_k > 0$): $R > 33h^{-1}\text{Gpc}$
 - For positively curved space ($\Omega_k < 0$): $R > 23h^{-1}\text{Gpc}$
- The particle horizon today is $9.7h^{-1}\text{Gpc}$
 - The curvature radius of the universe is at least 3 times as large as the observable universe.

How Long Did Inflation Last?

- The universe had expanded by $e^{N_{\text{tot}}}$ during inflation.
 - Q. How long should inflation have lasted to explain the observed flatness of the universe?
 - A. $N_{\text{total}} > 36 + \ln(T_{\text{reheating}}/1 \text{ TeV})$
 - A factor of 10 improvement in Ω_k will raise this lower limit by 1.2.
 - Lower if the reheating temperature was $< 1 \text{ TeV}$
- This is the check list #1

What If Dark Energy Was Not Vacuum Energy ($w \neq -1$)...



● WMAP+BAO \rightarrow Curvature; WMAP+SN \rightarrow w

● WMAP+BAO+SN \rightarrow Simultaneous limit

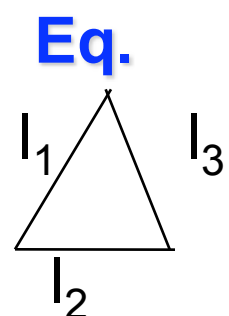
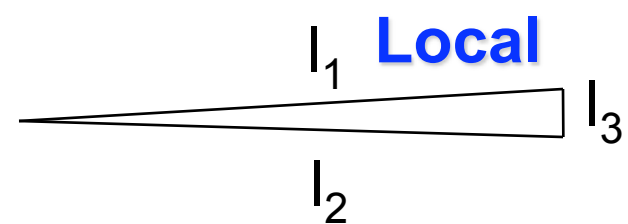
● $-0.0175 < \Omega_k < 0.0085$; $-0.11 < 1+w < 0.14$ (95% CL)

Check list #2: Gaussianity

- In the simplest model of inflation, the distribution of primordial fluctuations is close to a Gaussian with random phases.
- The level of non-Gaussianity predicted by the simplest model is well below the current detection limit.
- A convincing detection of primordial non-Gaussianity will rule out most of inflation models in the literature.
 - **Convincing Detection of non-Gaussianity would be a breakthrough in cosmology**

Triangles on the Sky: Angular Bispectrum

- Non-zero bispectrum means the detection of non-Gaussianity. **It's always easy to look for deviations from zero!**
- There are many triangles to look for, but...
 - Will focus on two classes



- "Squeezed" parameterized by f_{NL}^{local}
- "Equilateral" parameterized by f_{NL}^{equil}

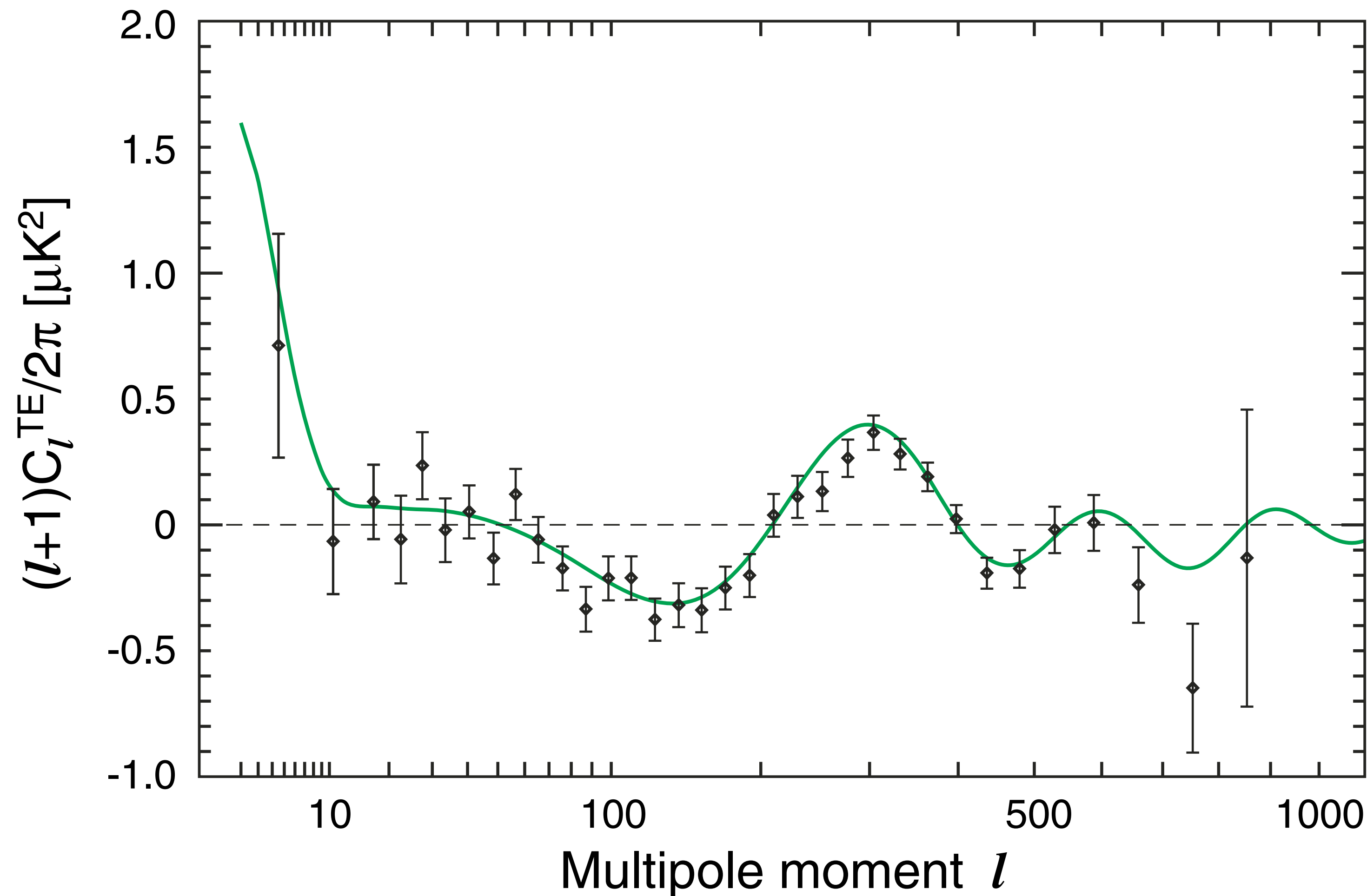
No Detection at $\geq 95\% \text{CL}$

- $-9 < f_{\text{NL}}(\text{local}) < 111$ (95% CL)
- $-151 < f_{\text{NL}}(\text{equilateral}) < 253$ (95% CL)
- These numbers mean that the primordial curvature perturbations are Gaussian to **0.1% level**.
 - This result provides the strongest evidence for quantum origin of primordial fluctuations during inflation.

Check List #3: Adiabaticity

- The **adiabatic relation** between radiation and matter:
 - $3\delta\rho_{\text{radiation}}/(4\rho_{\text{radiation}}) = \delta\rho_{\text{matter}}/\rho_{\text{matter}}$
- *Deviation from adiabaticity*: A simple-minded quantification
 - Fractional deviation of A from B = $(A-B) / [(A+B)/2]$
 - $\delta_{\text{adi}} = [3\delta\rho_{\text{radiation}}/(4\rho_{\text{radiation}}) - \delta\rho_{\text{matter}}/\rho_{\text{matter}}] / \{ [3\delta\rho_{\text{radiation}}/(4\rho_{\text{radiation}}) + \delta\rho_{\text{matter}}/\rho_{\text{matter}}] / 2 \}$
 - Call this the “**adiabaticity deviation parameter**”
 - “Radiation and matter obey the adiabatic relation to $(100\delta_{\text{adi}})\%$ level.”

WMAP 5-Year TE Power Spectrum



- The negative TE at $l \sim 100$ is the distinctive signature of super-horizon adiabatic perturbations (Spergel & Zaldarriaga 1997)
- Non-adiabatic perturbations would fill in the trough, and shift the zeros.

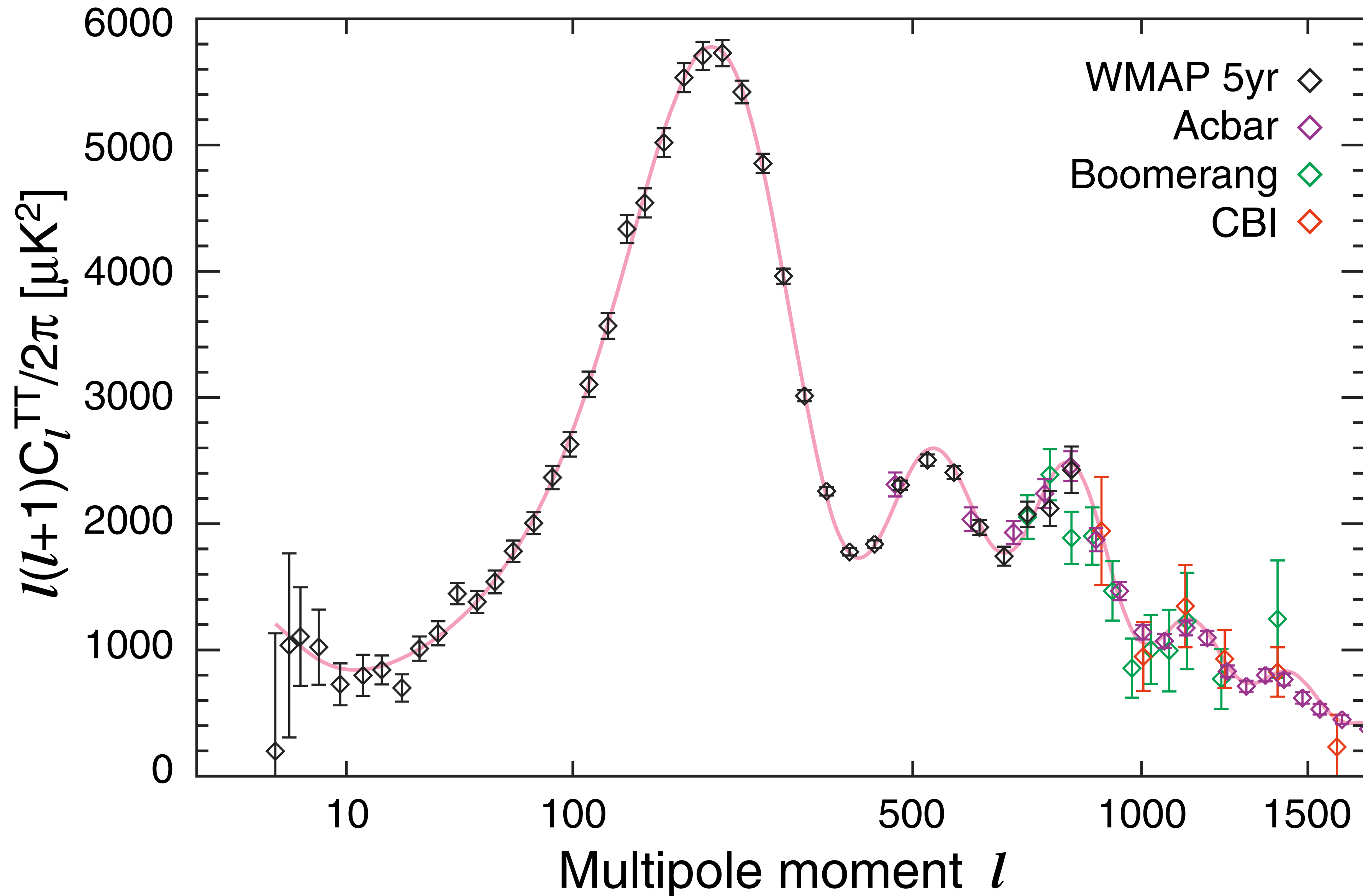
Axion Dark Matter?

- CMB and axion-type dark matter are adiabatic to **8.6%**
- **This puts a severe limit on axions being the dominant dark matter candidate.**

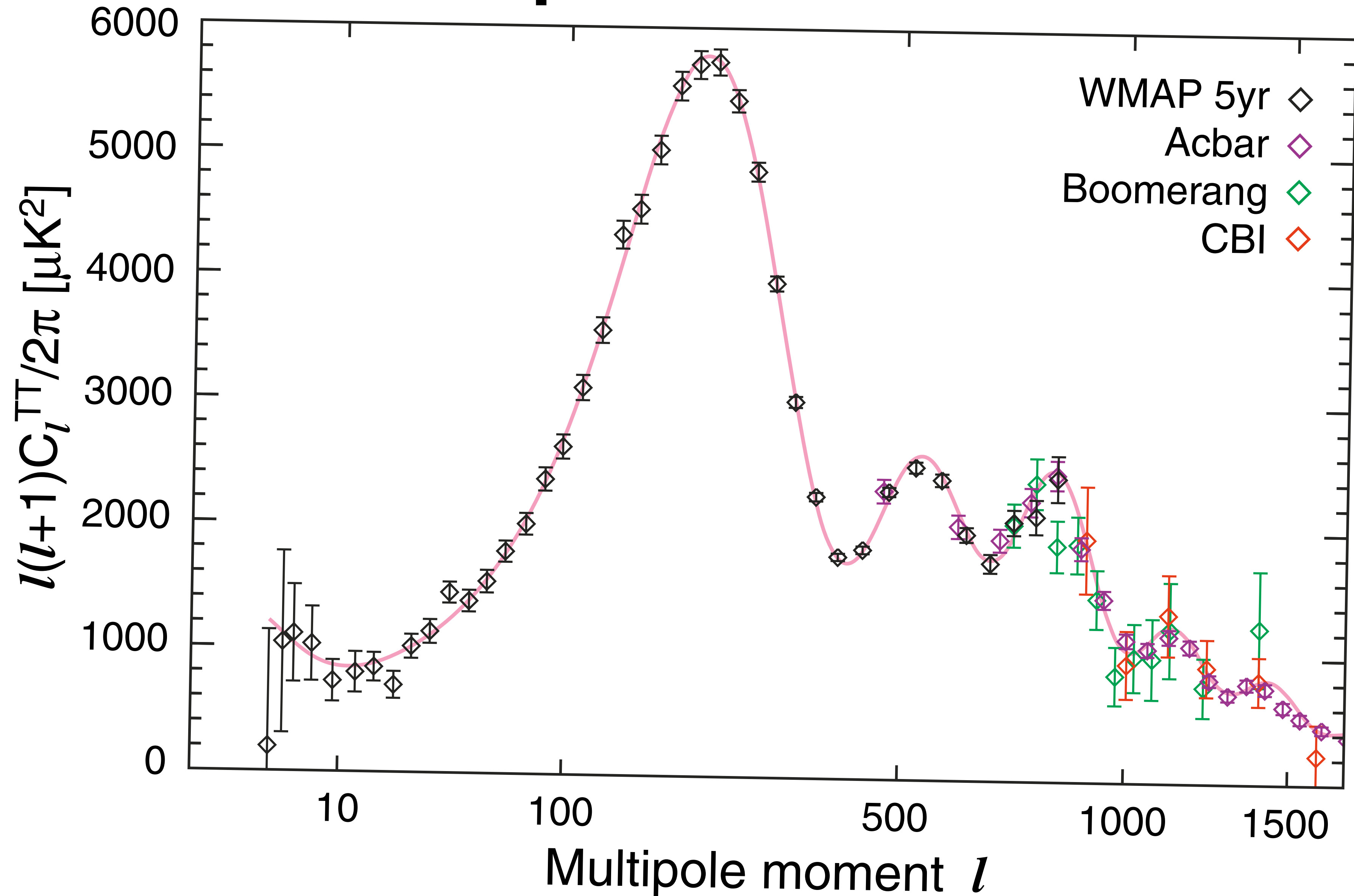
$$\frac{\Omega_a}{\Omega_c} < \frac{3.0 \times 10^{-39}}{\theta_a^5 \gamma^6} \left(\frac{0.01}{r} \right)^{7/2}$$

The non-adiabatic perturbations, combined with the expression for Ω_a , constrain $\Omega_a^{1/7}$.

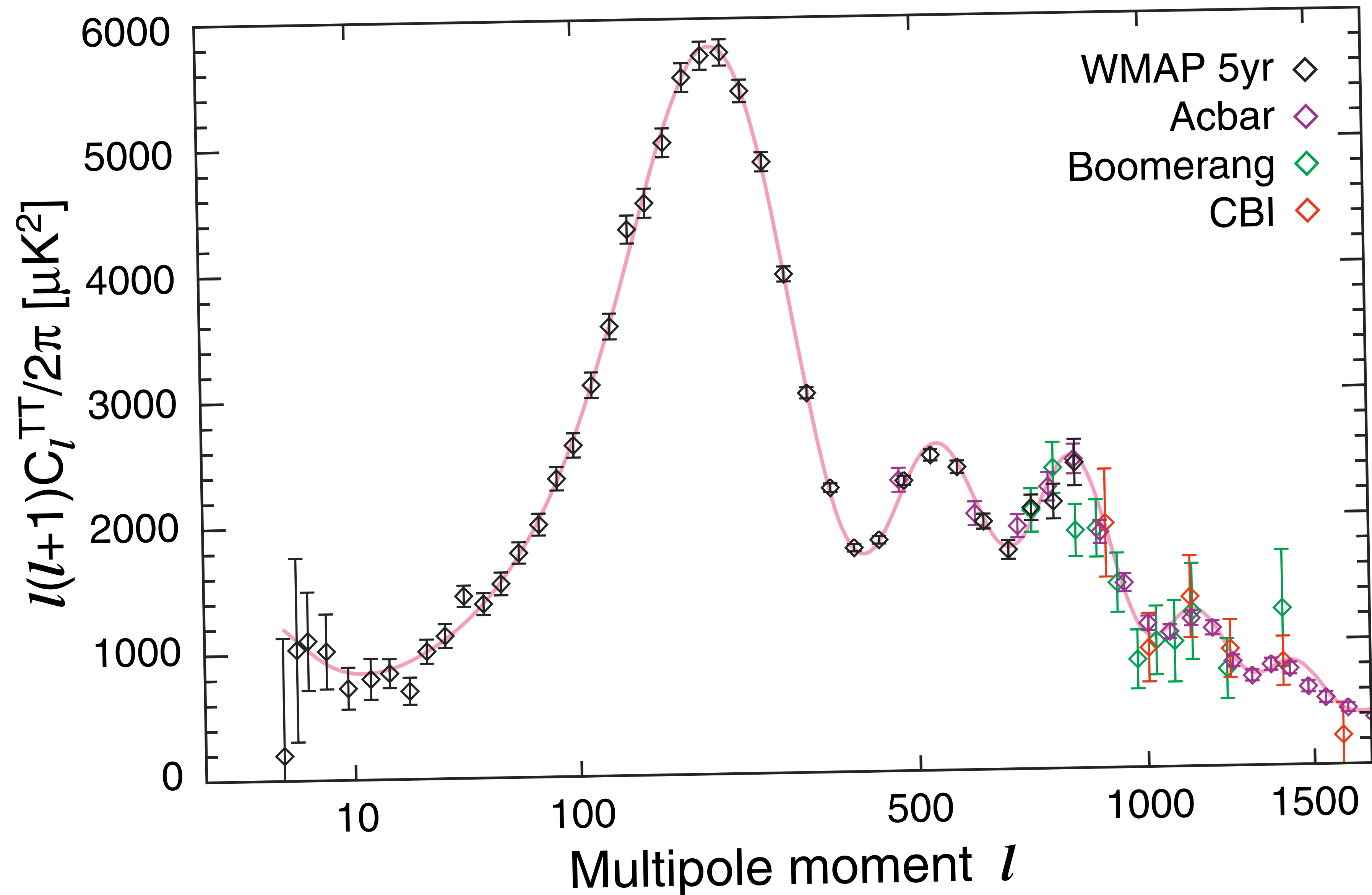
Check List #4: Scale Invariance



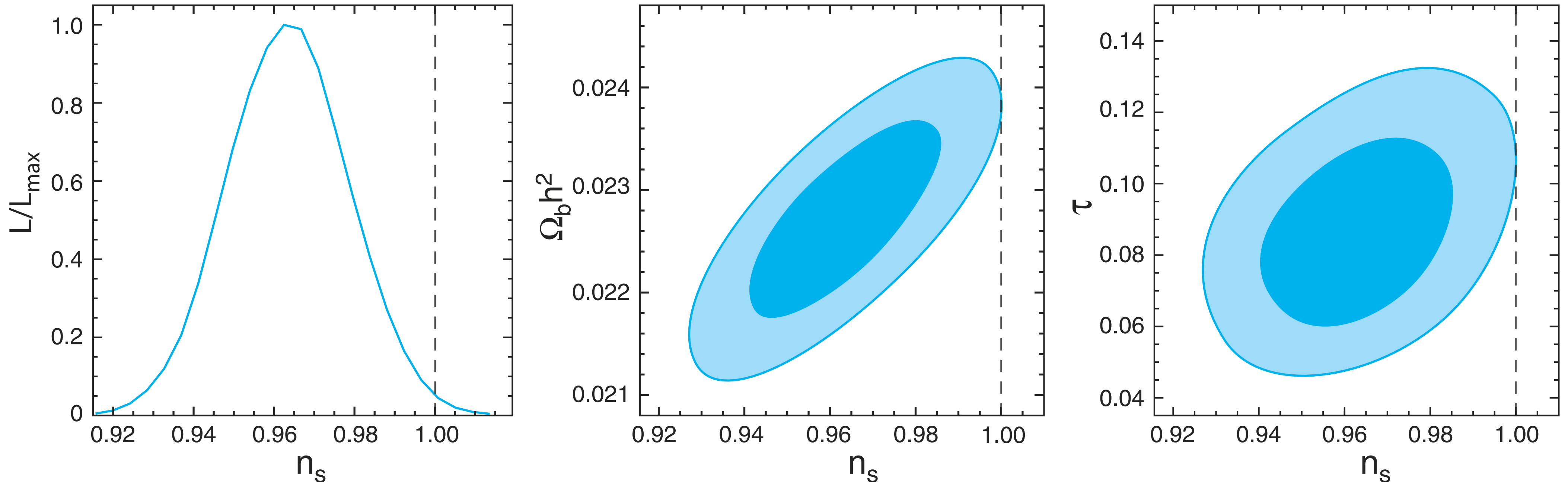
“Red” Spectrum: $n_s < 1$



“Blue” Spectrum: $n_s > 1$



Is n_s different from ONE?



- WMAP-alone: $n_s = \mathbf{0.963}$ (+0.014) (-0.015) (Dunkley et al.)
 - 2.5-sigma away from $n_s = 1$, “scale invariant spectrum”
- n_s is degenerate with $\Omega_b h^2$; thus, we can't really improve upon n_s further unless we improve upon $\Omega_b h^2$

This One Just In!

Pettini et al. 0805.0594

- The accuracy of $\Omega_b h^2$ inferred from the [D/H] measurement of the most-metal poor Damped Lyman-alpha system (towards QSO Q0913+072) is comparable to WMAP!

- $\Omega_b h^2(\text{DLA}) = 0.0213 \pm 0.0010$ from $\log(\text{D}/\text{H}) = -4.55 \pm 0.03$

- $\Omega_b h^2(\text{WMAP}) = 0.0227 \pm 0.0006$

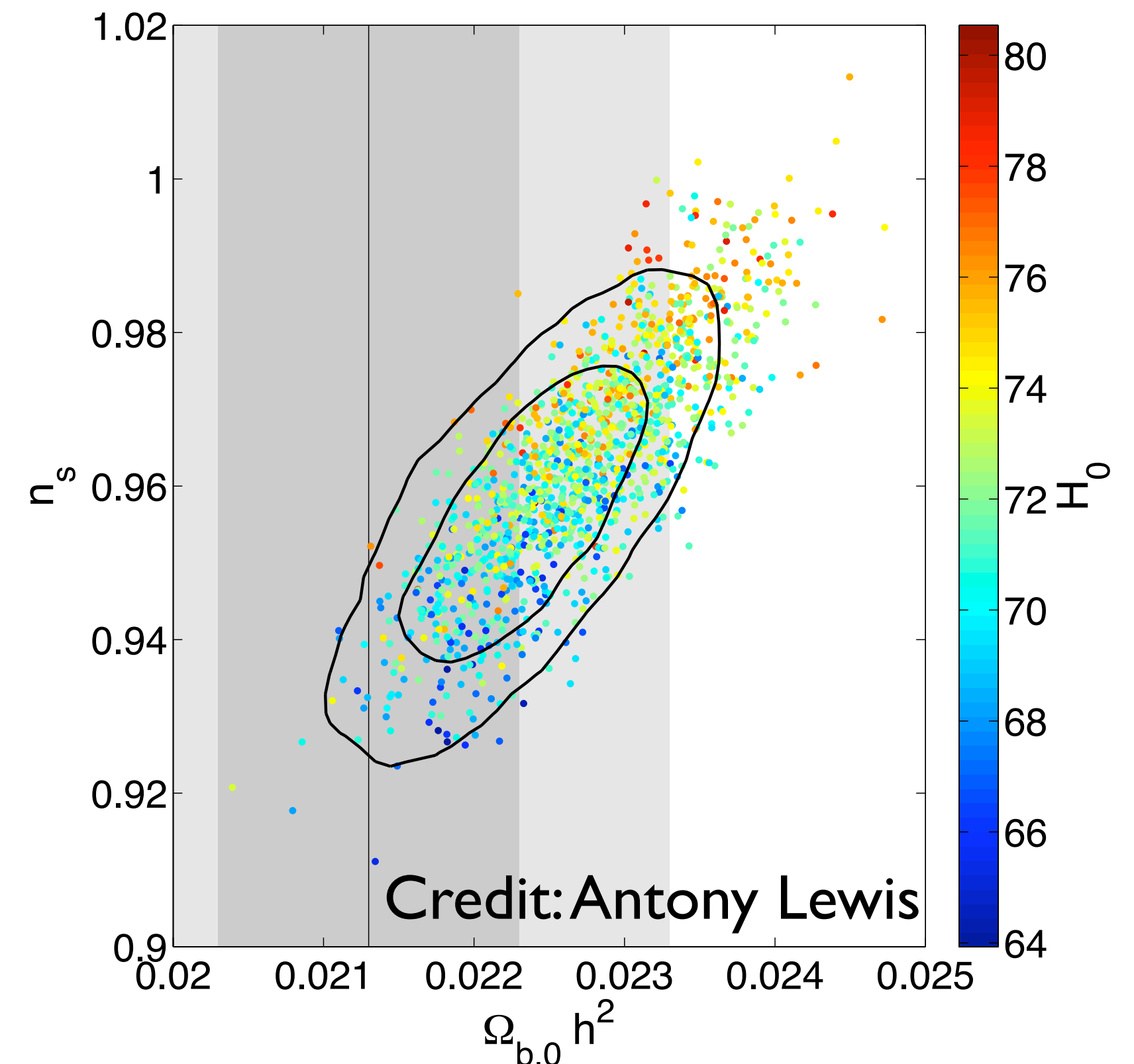
- $\Omega_b h^2(\text{DLA})$ is totally independent of n_s

- *Degeneracy reduced!*

- $n_s(\text{DLA} + \text{WMAP}) = \mathbf{0.956 \pm 0.013}$

- **3.4-sigma away from 1**

- $n_s(\text{WMAP}) = 0.963 (+0.014) (-0.015)$

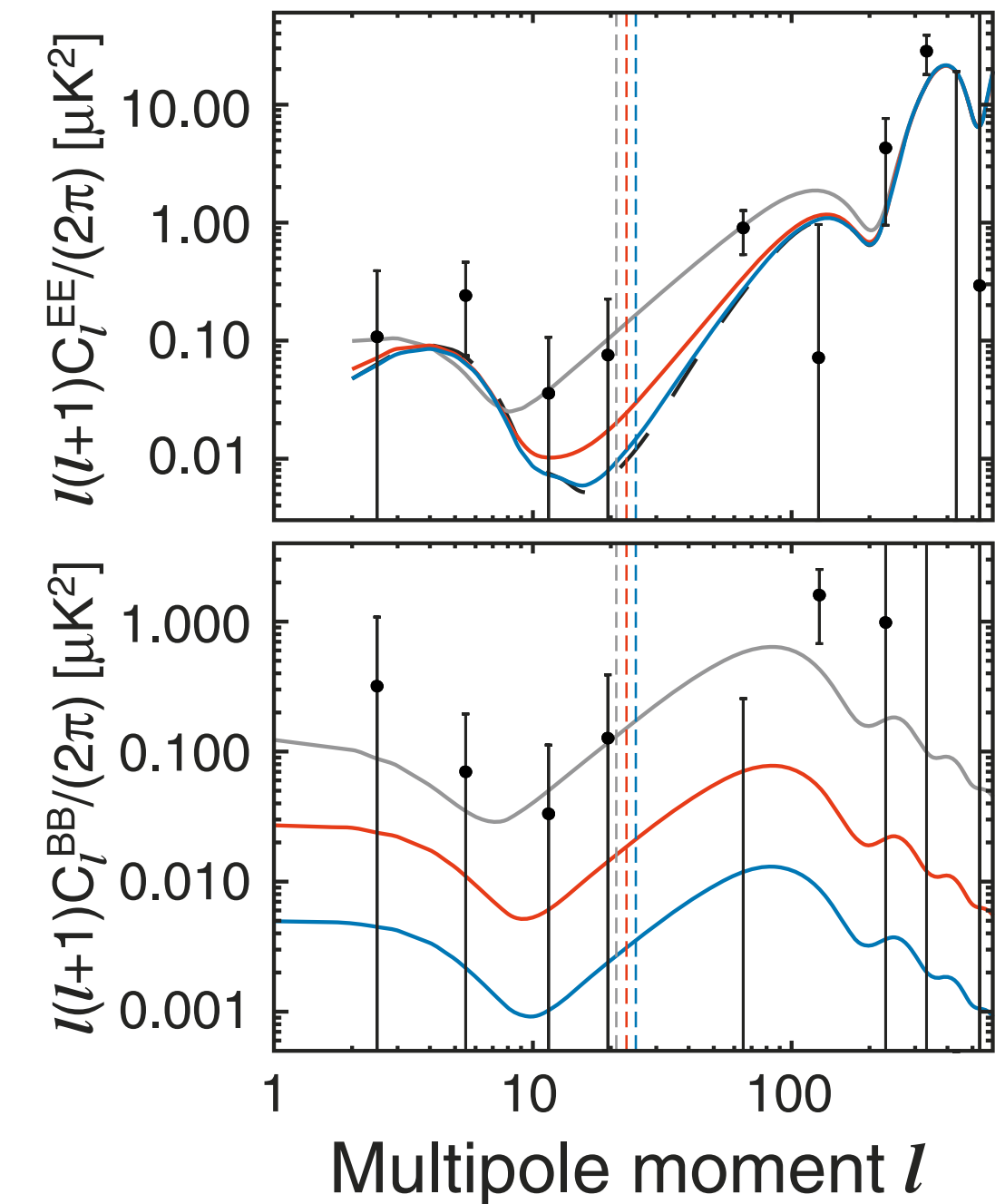
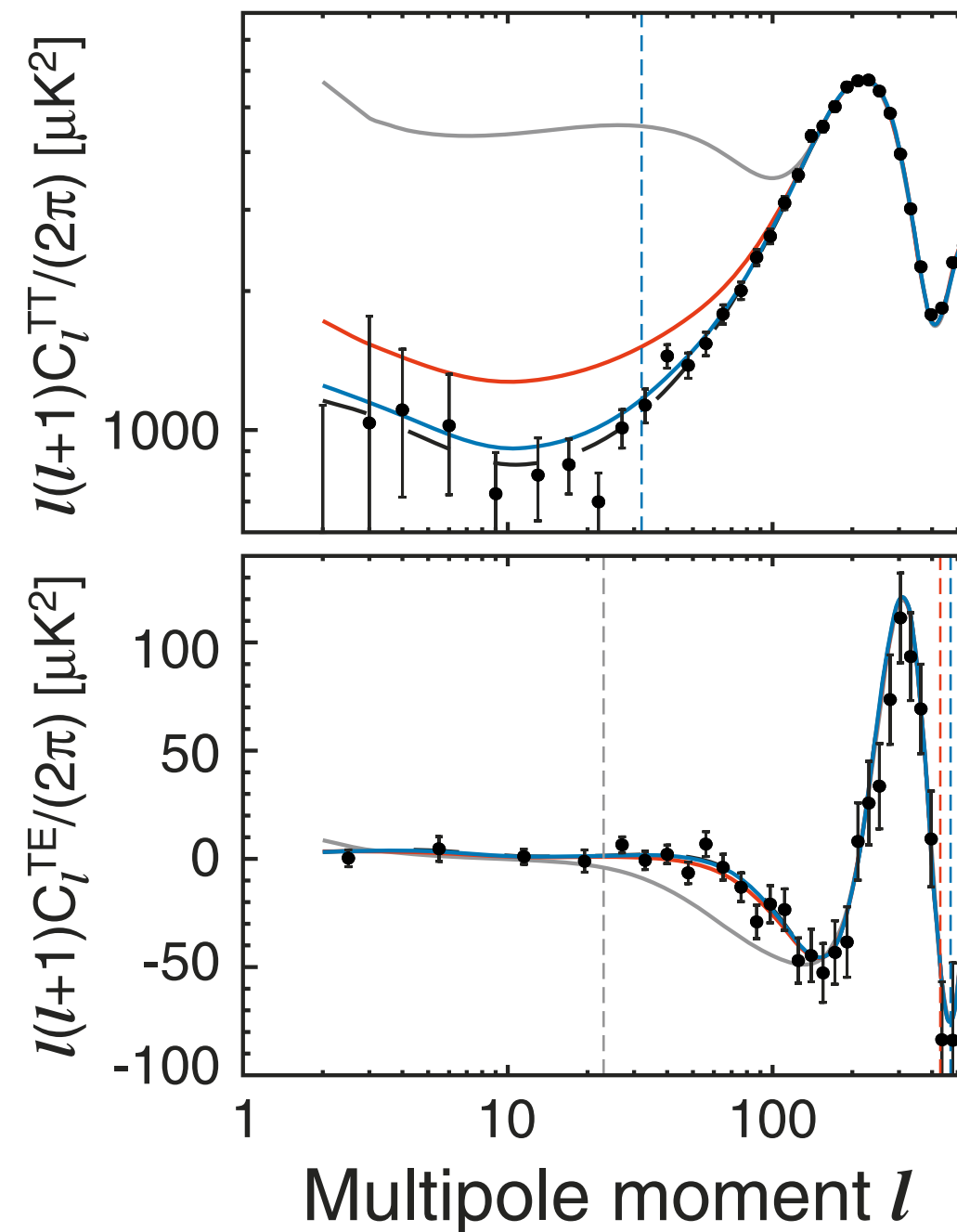
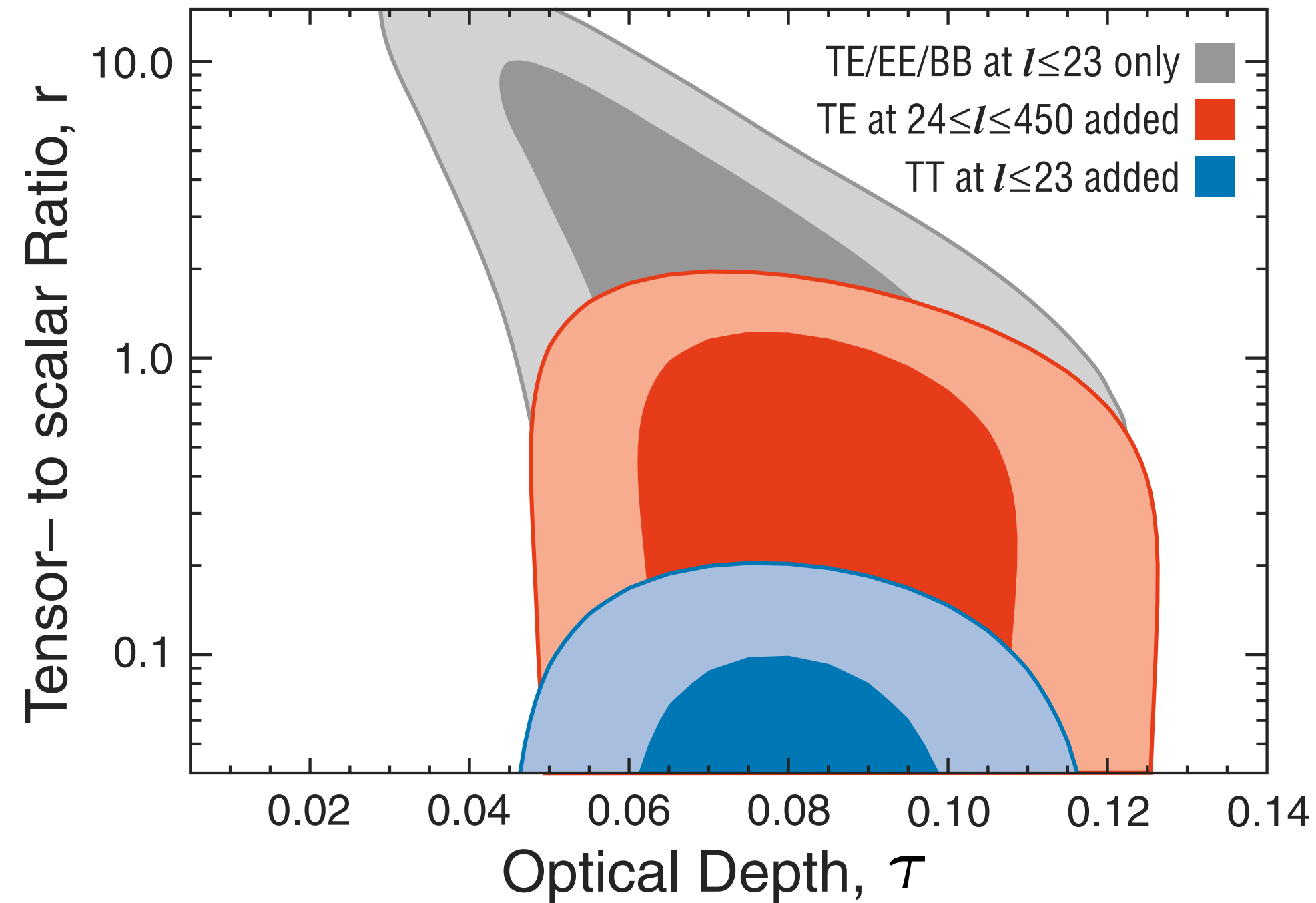


Check List #5: Gravitational Waves

- How do WMAP data constrain the amplitude of primordial gravitational waves?
- We use “ r ” to parameterize the amplitude of GWs relative to the density fluctuations (or the scalar curvature (metric) perturbations)
 - When $r=1$, we have equal amount of scalar and tensor metric perturbations.

Pedagogical Explanation

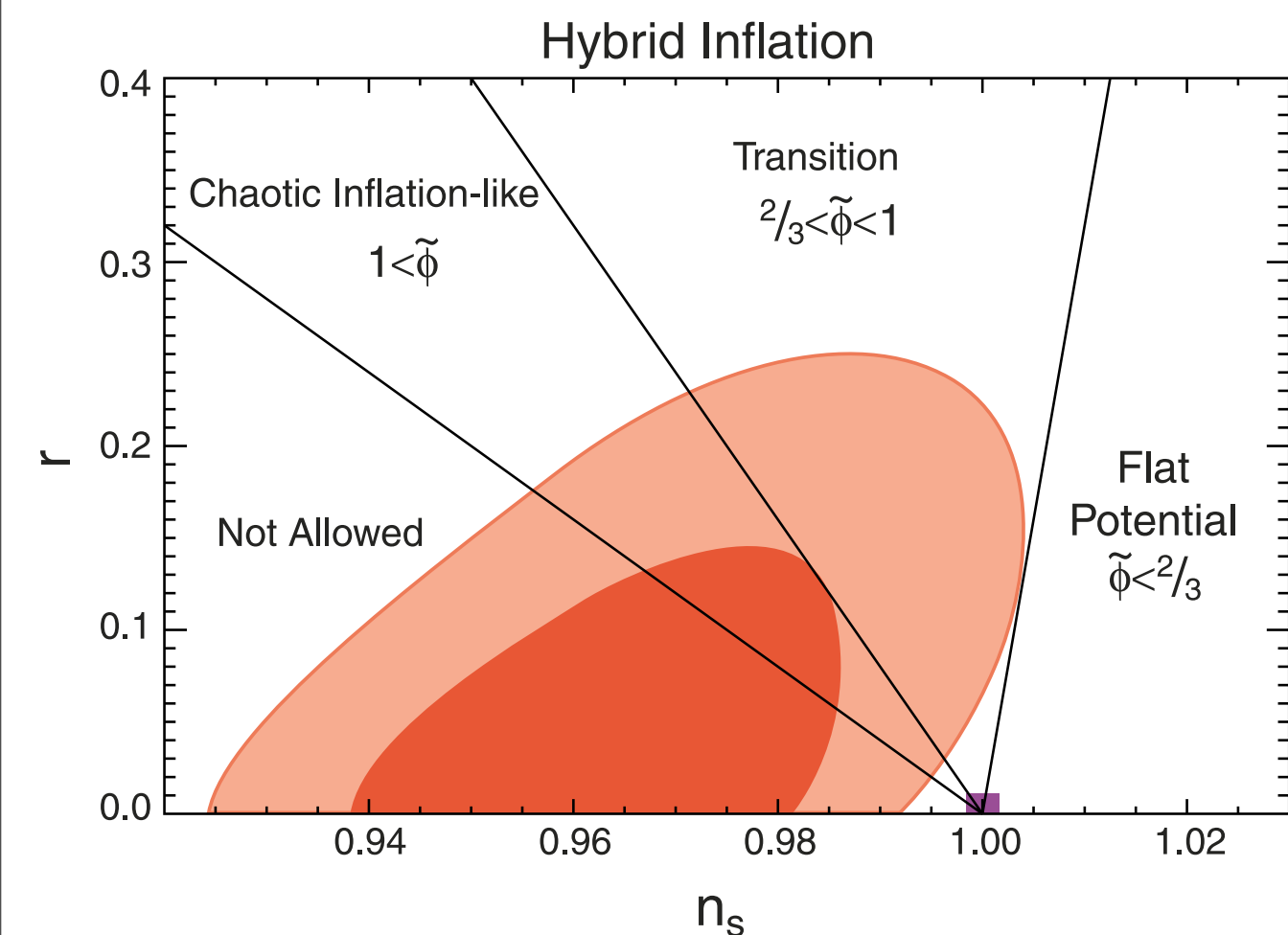
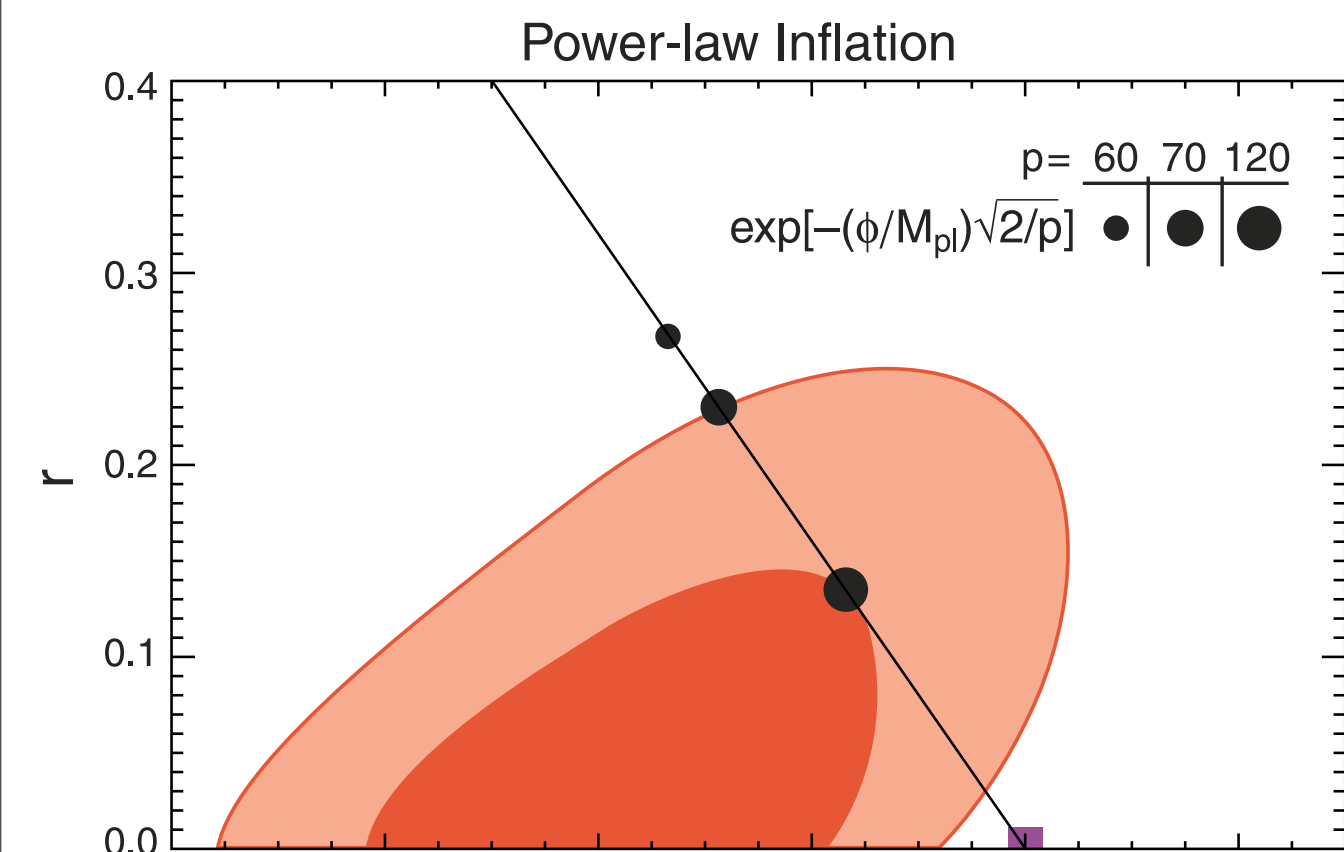
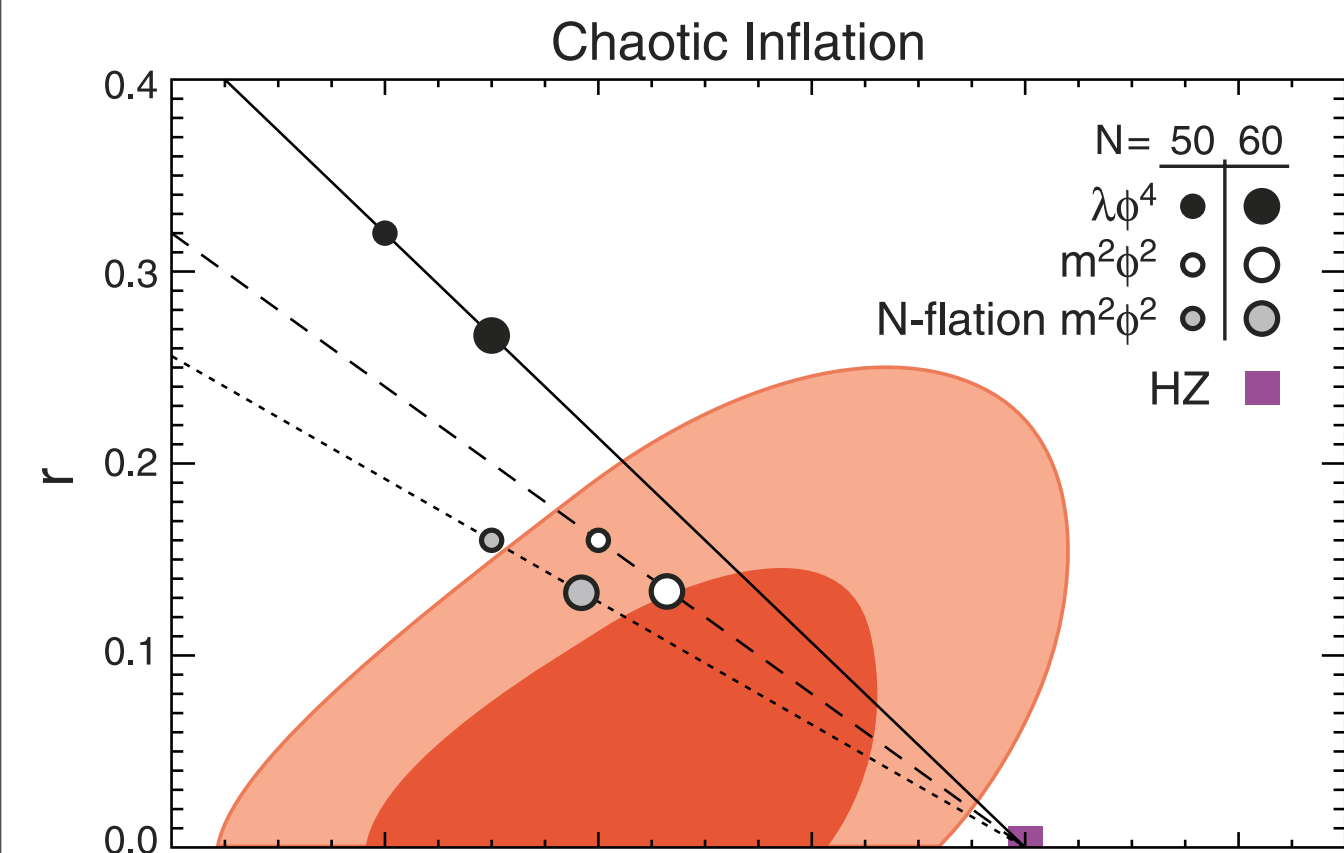
Komatsu et al.



- If all the other parameters (n_s in particular) are fixed...
 - Low- l polarization gives $r < 20$ (95% CL)
 - + high- l polarization gives $r < 2$ (95% CL)
 - + low- l temperature gives $r < 0.2$ (95% CL)

Lowering a “Limbo Bar”

- $\lambda\varphi^4$ is totally out. (unless you invoke, e.g., non-minimal coupling, to suppress r ..)
- $m^2\varphi^2$ is within 95% CL.
 - Future WMAP data would be able to push it to outside of 95% CL, if $m^2\varphi^2$ is not the right model.
- N-flation $m^2\varphi^2$ (Easter&McAllister) is being pushed out
- PL inflation [$a(t)\sim t^p$] with $p<60$ is out.
- A blue index ($n_s>1$) region of hybrid inflation is disfavored



Grading Inflation

- **Flatness:** $-0.0175 < \Omega_k < 0.0085$ (not assuming $w=-1$!)
- **Non-adiabaticity:** $<8.6\%$ (axion DM); $<2.0\%$ (curvaton DM)
- **Non-Gaussianity:** $-9 < \text{Local} < 111$; $-151 < \text{Equilateral} < 253$
- **Tilt** (for $r=0$): $n_s=0.960 (+0.014) (-0.013)$ [68% CL]
- **Gravitational waves:** **$r < 0.20$**
 - $n_s=0.968 (+/- 0.015)$ [68% CL]
 - **$n_s > 1$ disfavored at 95% CL regardless of r**

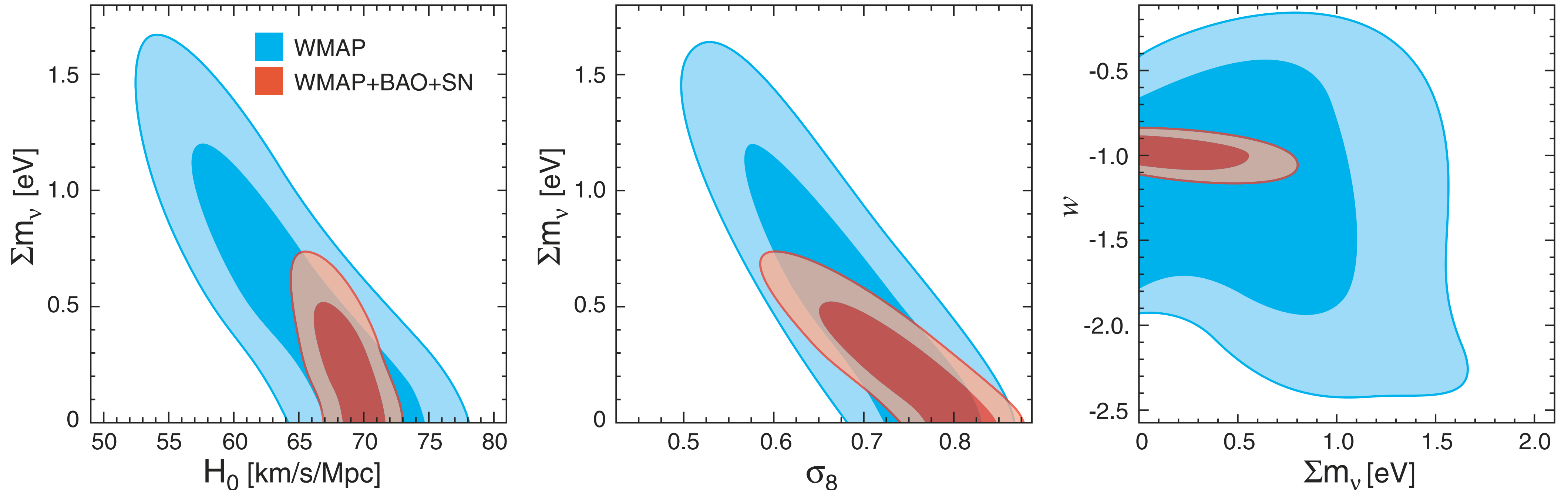
Summary

- A simple, yet *mysterious* Λ CDM still fits the WMAP data, as well as the other astrophysical data sets.
- **We did everything we could do to find deviations from Λ CDM, but failed.**
 - Bad news... we still don't know what DE or DM is.
- Significant improvements in limits on the deviations
 - Most notably, $r < 0.2$ (95% CL), and $n_s > 1$ is now disfavored regardless of r .
 - Good News: Many popular inflation models have been either ruled out, or being in danger!
- Significant improvements in Λ CDM parameters.

Looking Ahead...

- With more WMAP observations, exciting discoveries may be waiting for us. Two examples for which we might be seeing some hints from the 5-year data:
 - **Non-Gaussianity**: If $f_{\text{NL}} \sim 50$, we will see it at the 3 sigma level with 9 years of data.
 - **Gravitational waves** (r) and tilt (n_s) : $m^2\varphi^2$ can be pushed out of the favorable parameter region
 - $n_s > 1$ would be convincingly ruled out regardless of r .

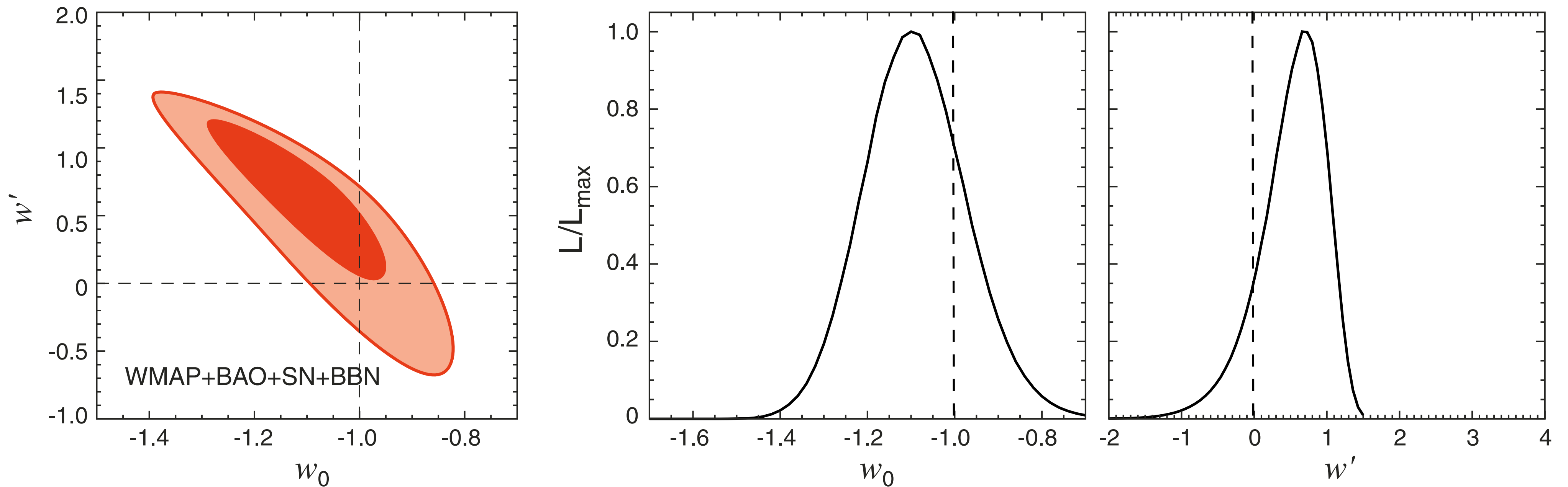
Neutrino Mass



- The local distance measurements (BAO) help determine the neutrino mass by giving H_0 .
- **$\text{Sum}(m_\nu) < 0.61 \text{ eV}$** (95% CL) -- independent of the normalization of the large scale structure.

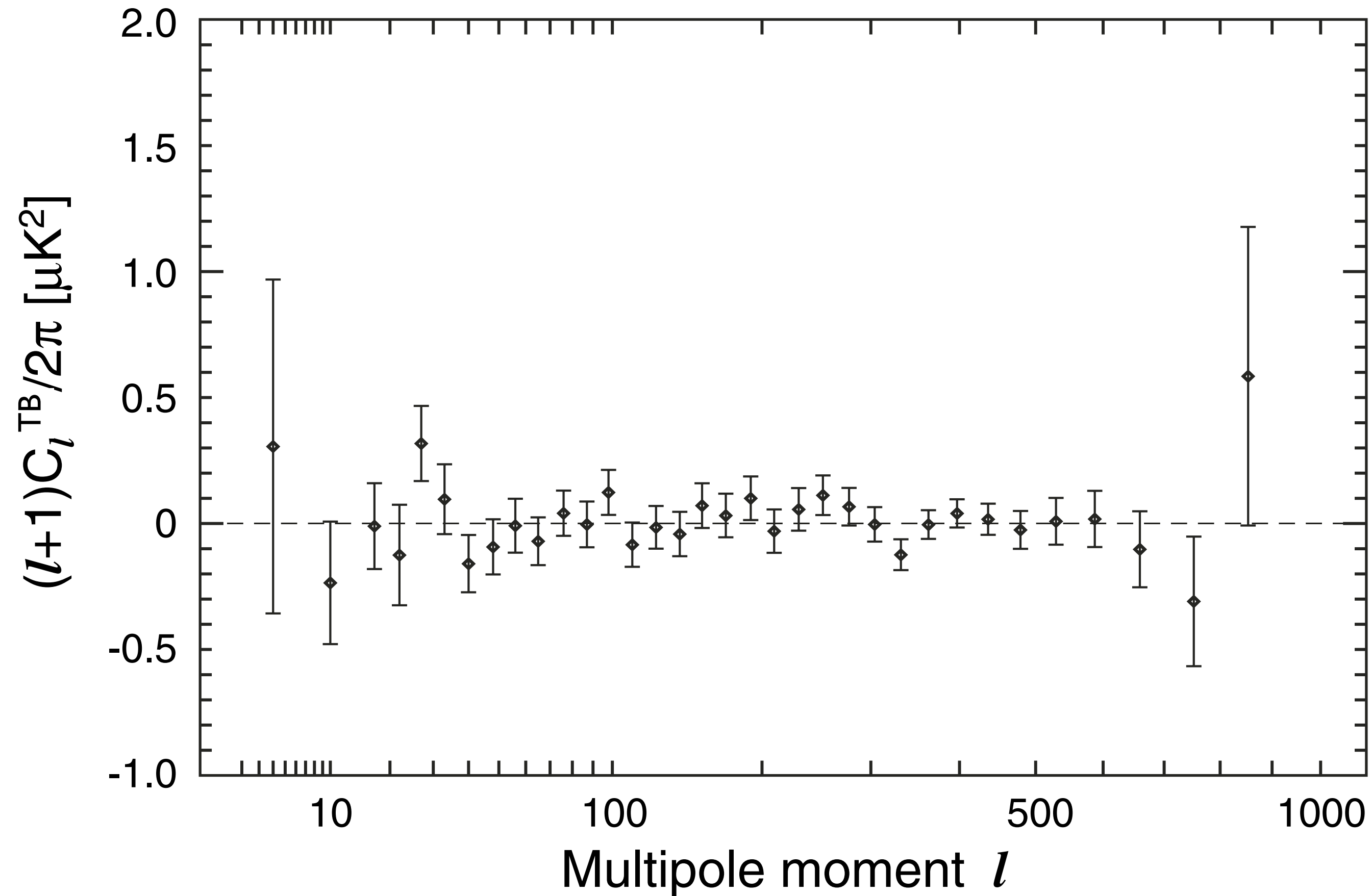
Dark Energy EOS:

$$w(z) = w_0 + w'z / (1+z)$$



- Dark energy is pretty consistent with cosmological constant: $w_0 = -1.09 \pm 0.12$ & $w' = 0.52 \pm 0.46$ (68%CL)

Probing Parity Violation



- Parity violating interactions that rotate the polarization angle of CMB can produce TB and EB correlations.

E \rightarrow B

$$C_l^{TE,obs} = C_l^{TE} \cos(2\Delta\alpha),$$

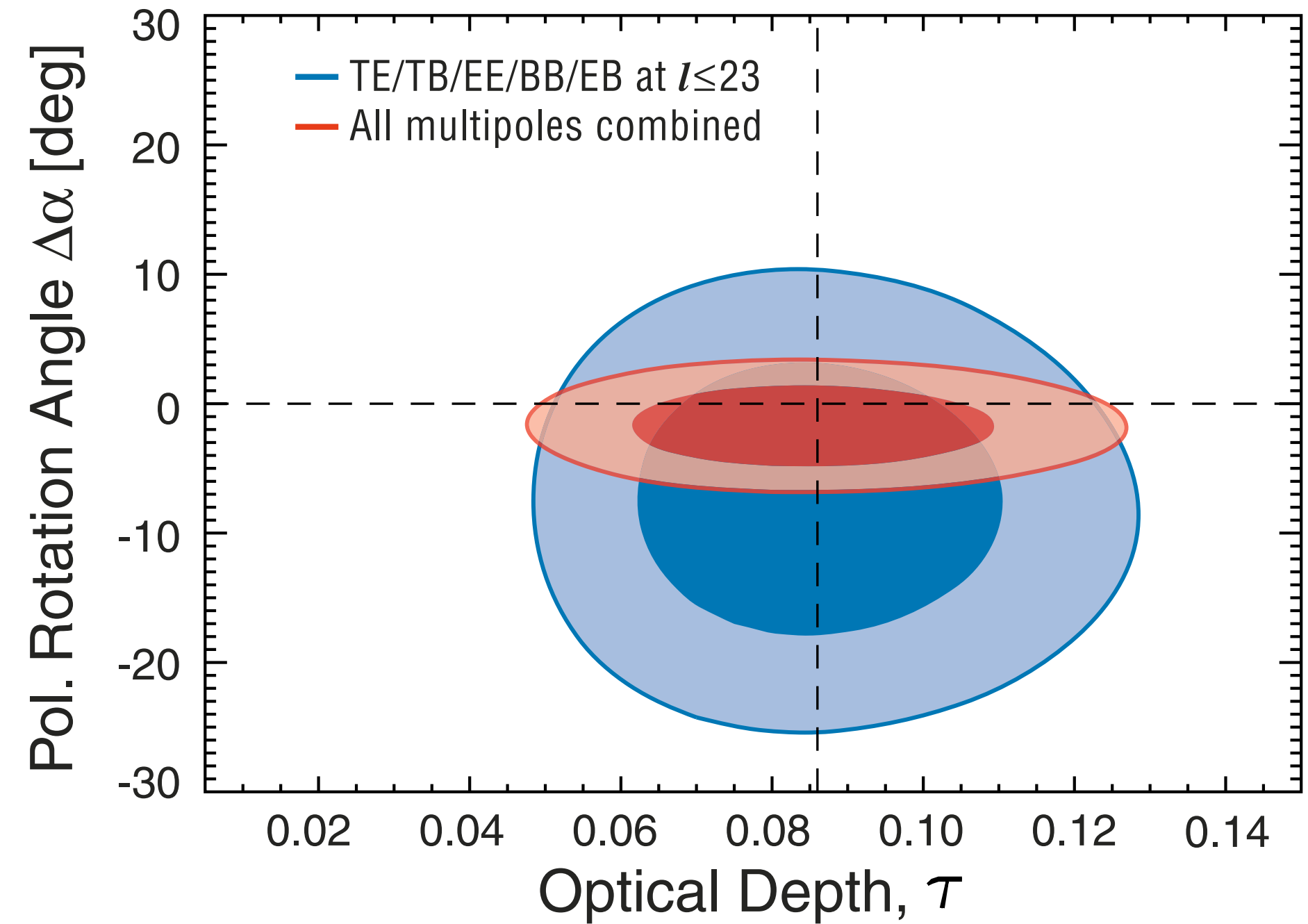
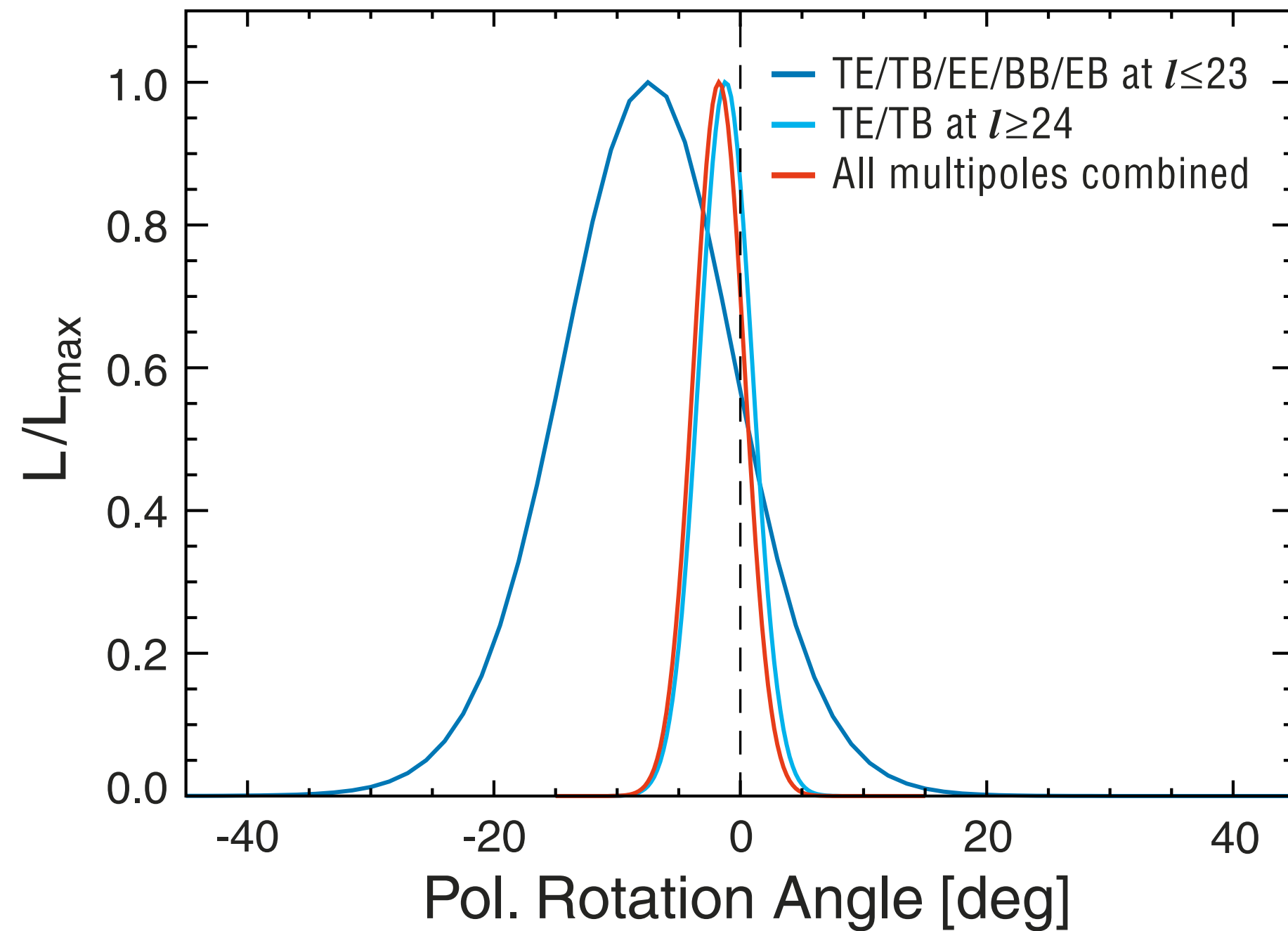
$$C_l^{TB,obs} = C_l^{TE} \sin(2\Delta\alpha),$$

$$C_l^{EE,obs} = C_l^{EE} \cos^2(2\Delta\alpha),$$

$$C_l^{BB,obs} = C_l^{EE} \sin^2(2\Delta\alpha),$$

$$C_l^{EB,obs} = \frac{1}{2} C_l^{EE} \sin(4\Delta\alpha).$$

- These are simpler relations when there was no primordial B-mode polarization.
- How much rotation would WMAP allow?



- **$\Delta\alpha = (-1.7 \pm 2.1)$ degrees (68% CL)**
- Comparable to the astrophysical constraint from quasars and radio galaxies
 - $\Delta\alpha = (-0.6 \pm 1.5)$ degrees (68% CL) (Carroll 1998)
- But, note the difference in path length!