

WMAP 5-Year Results: Implications for Inflation

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University of Texas at Austin
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WMAP 5-Year Papers

- **Hinshaw et al.**, “*Data Processing, Sky Maps, and Basic Results*” [0803.0732](#)
- **Hill et al.**, “*Beam Maps and Window Functions*” [0803.0570](#)
- **Gold et al.**, “*Galactic Foreground Emission*” [0803.0715](#)
- **Wright et al.**, “*Source Catalogue*” [0803.0577](#)
- **Nolta et al.**, “*Angular Power Spectra*” [0803.0593](#)
- **Dunkley et al.**, “*Likelihoods and Parameters from the WMAP data*” [0803.0586](#)
- **Komatsu et al.**, “*Cosmological Interpretation*” [0803.0547](#)

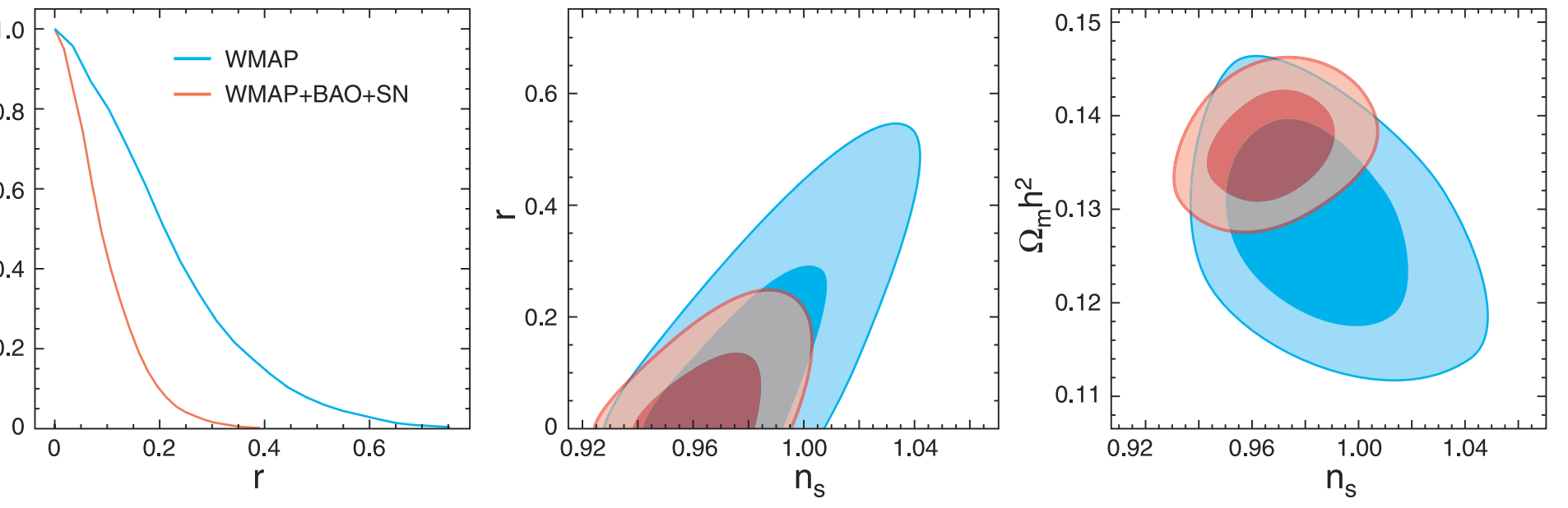
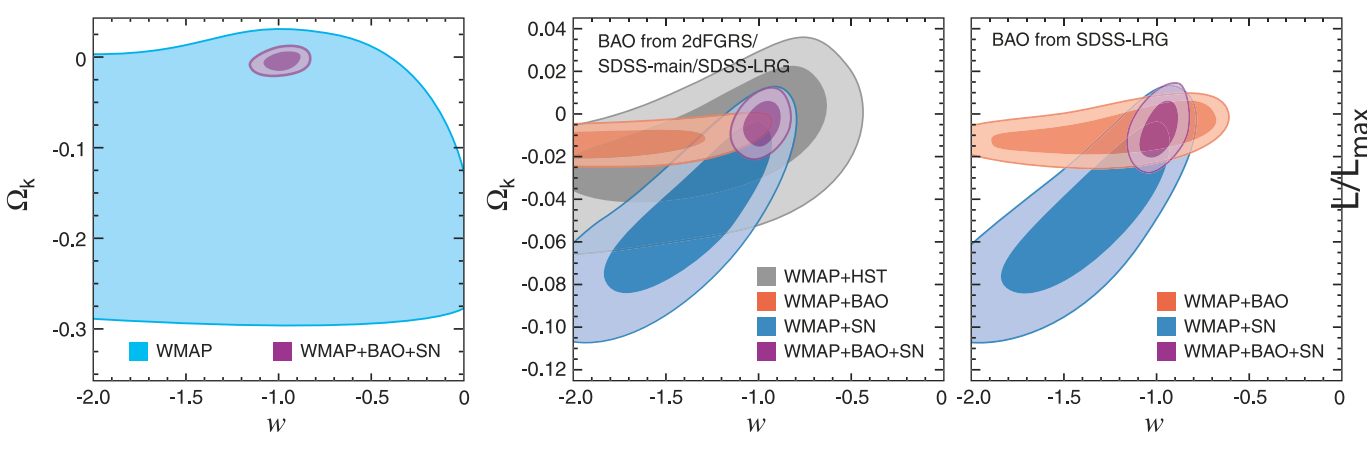
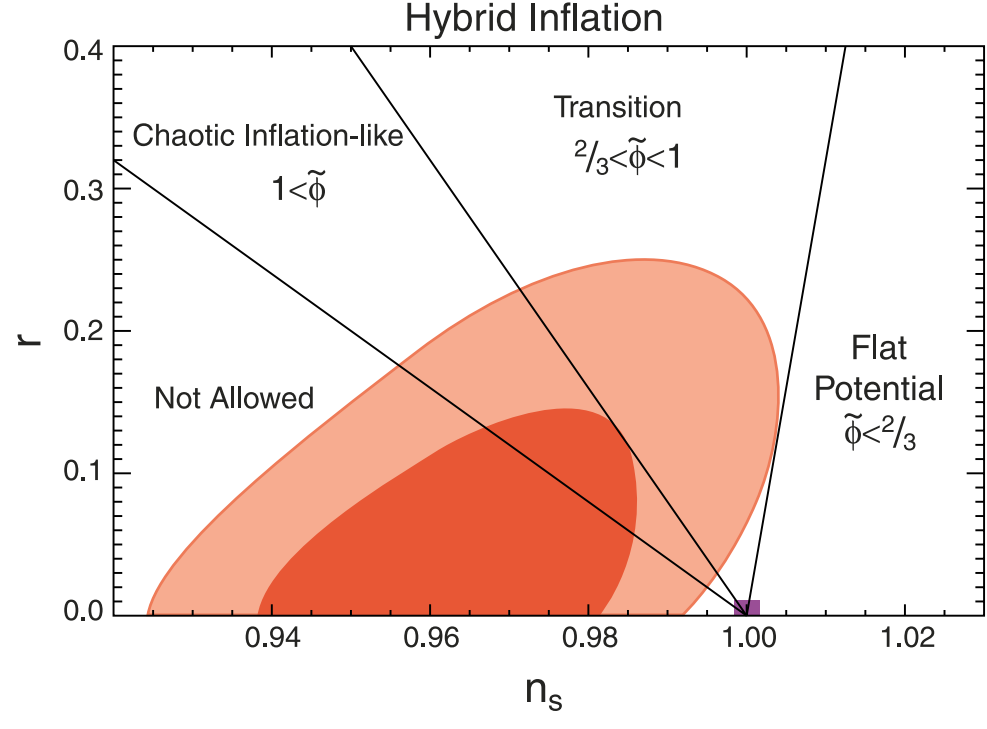
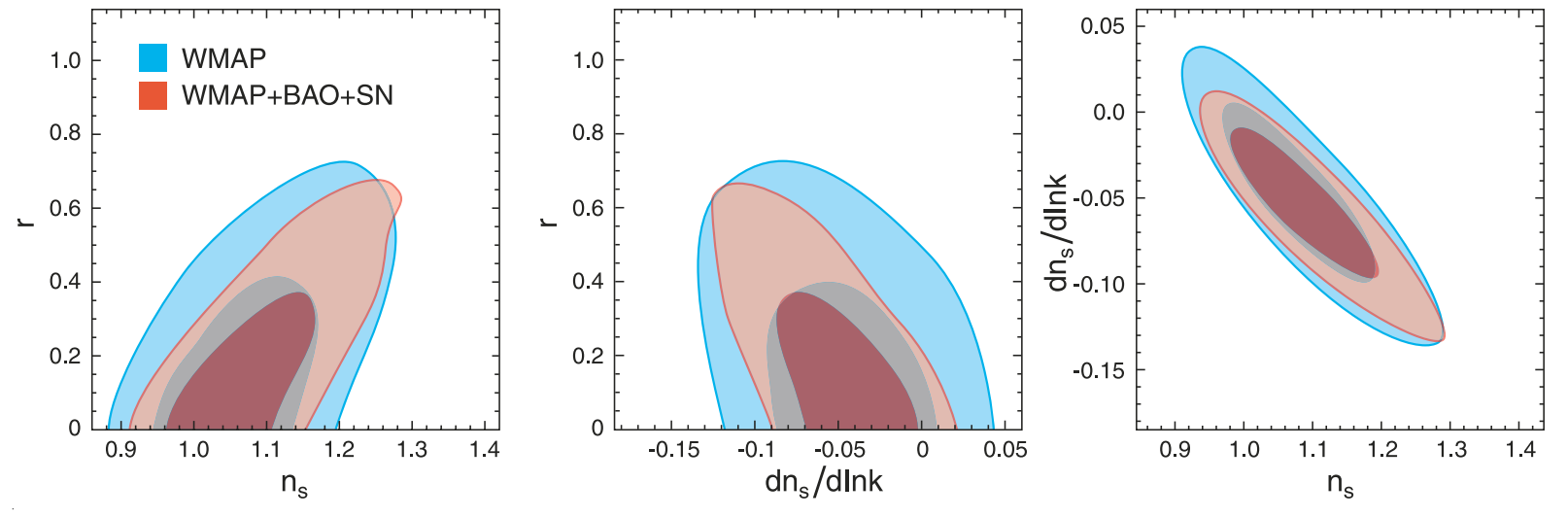
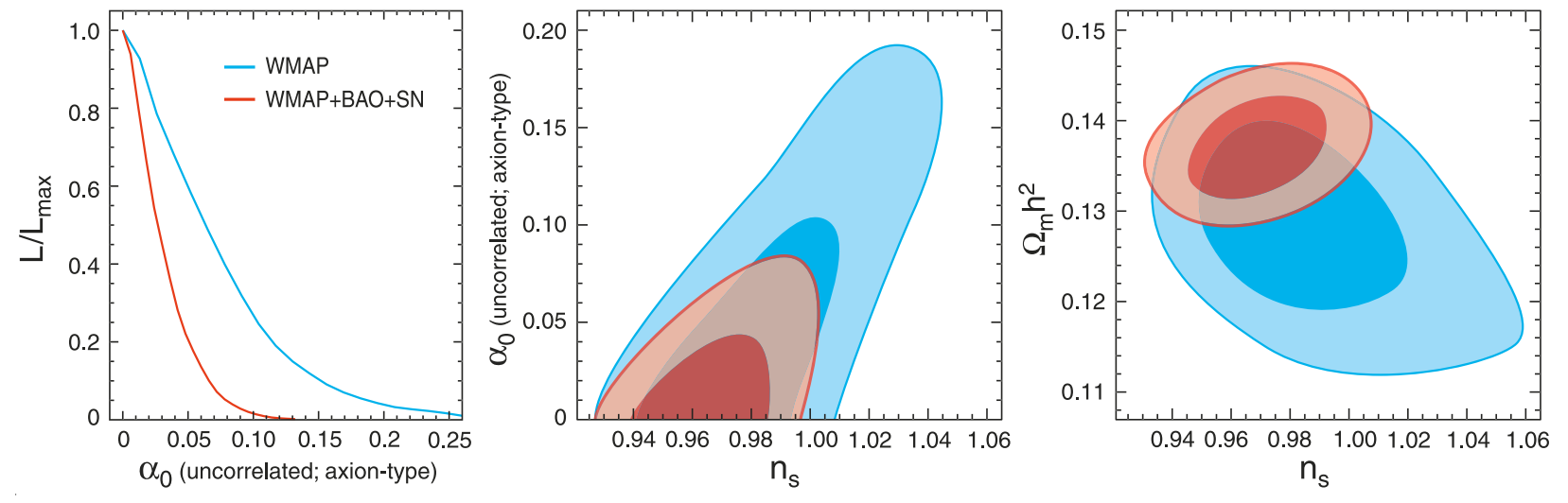
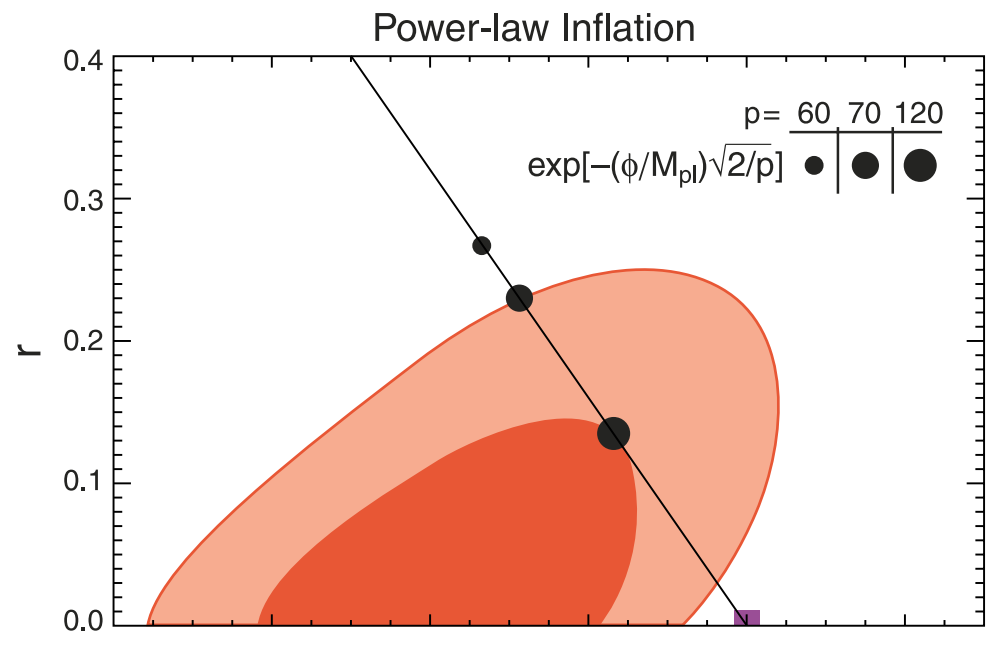
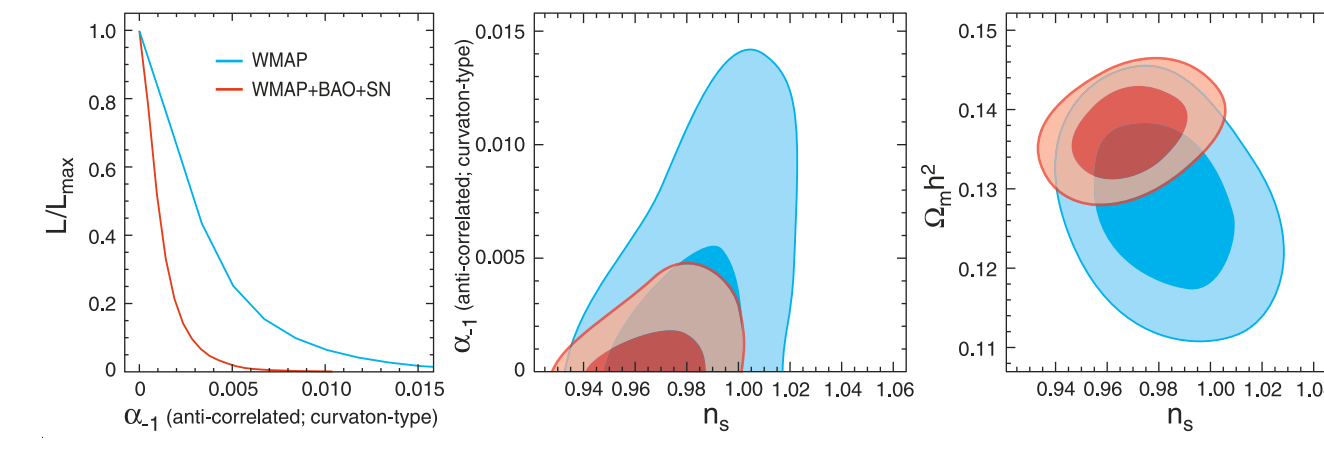
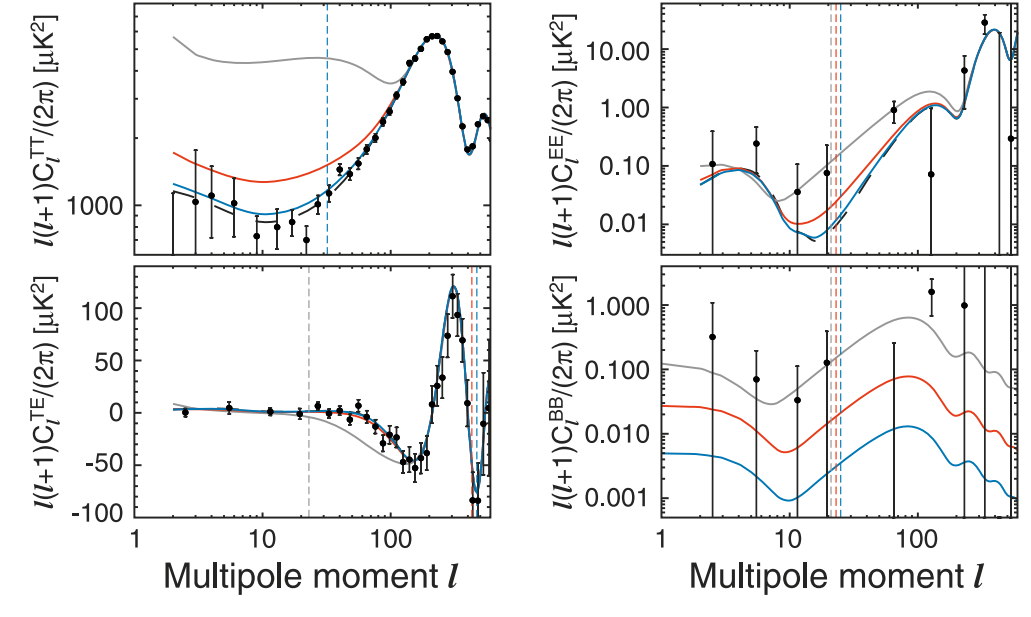
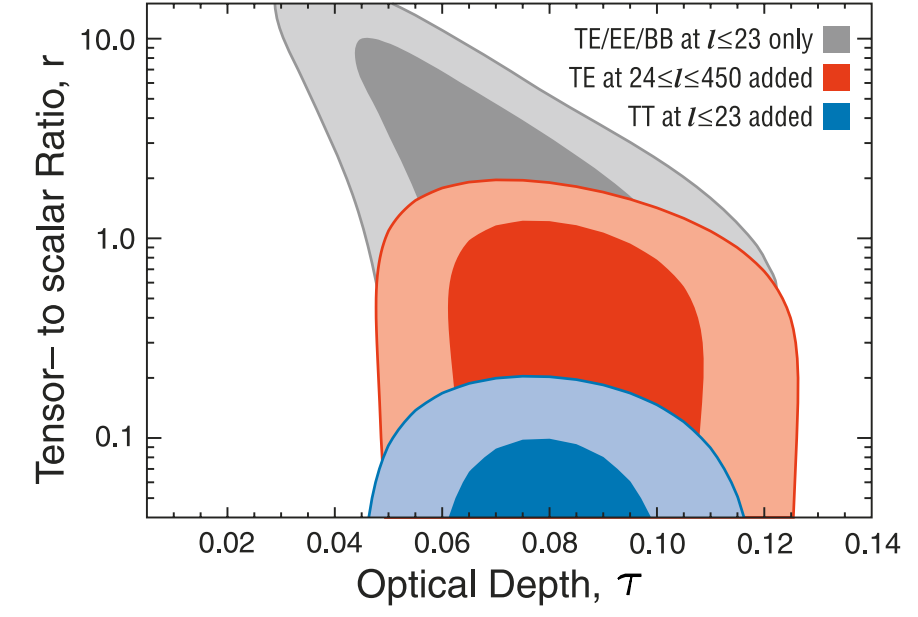
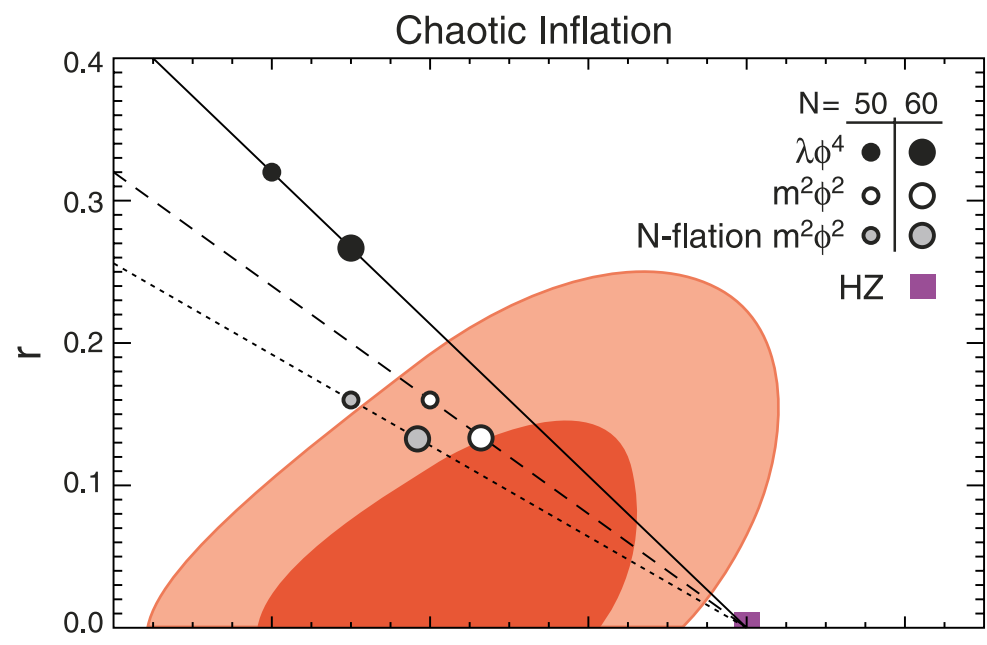
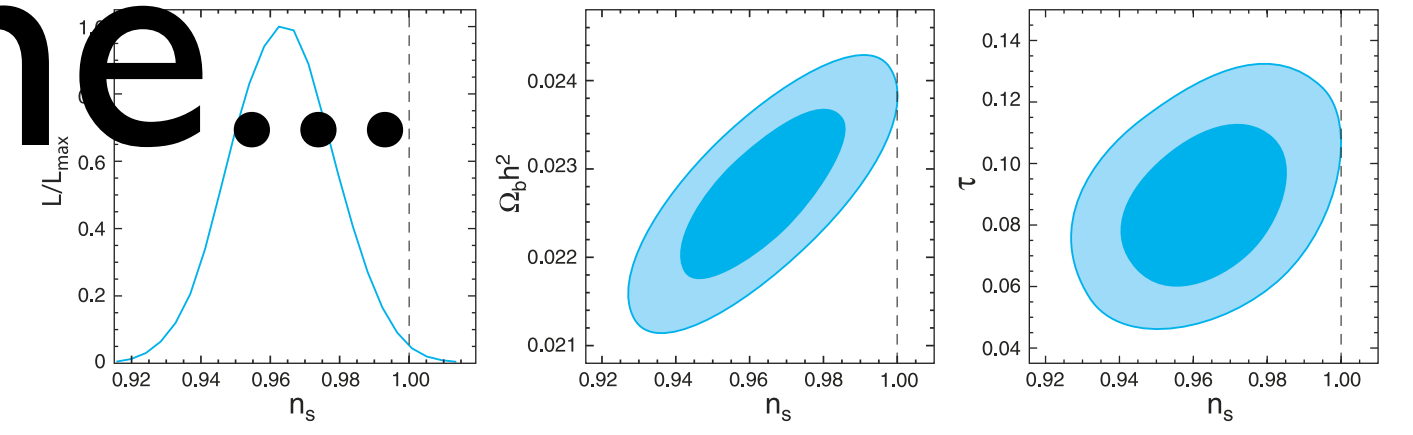
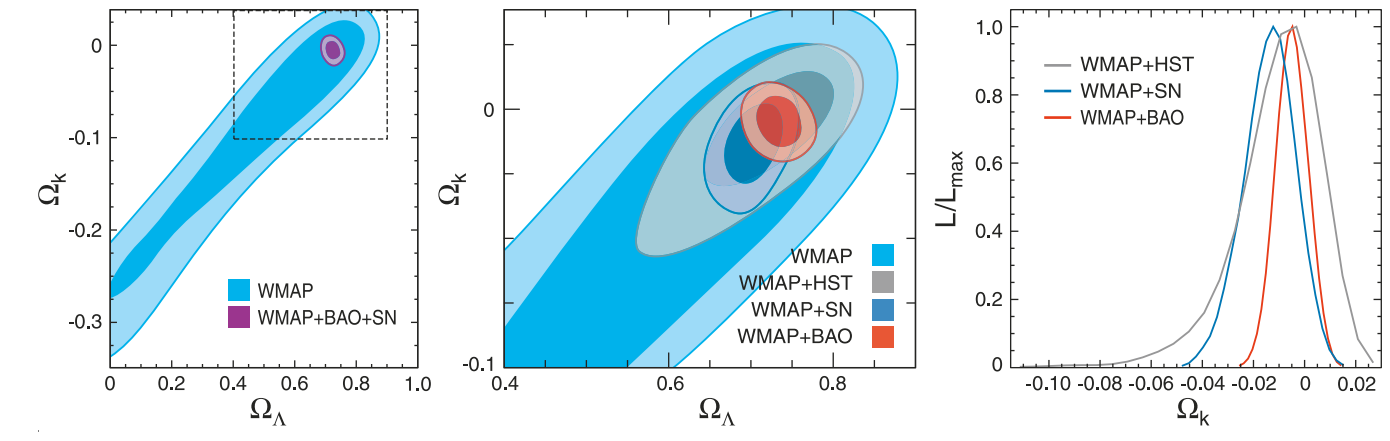
WMAP 5-Year Science Team

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- L. Page
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- J. Dunkley
- B. Gold
- E. Komatsu
- D. Larson
- M.R.olta

Special
Thanks to
WMAP
Graduates!

- C. Barnes
- R. Bean
- O. Dore
- H.V. Peiris
- L. Verde

Plots to come...



Some numbers to come...

- $n_s=0.960 (+ 0.014) (-0.013)$ for $r=0$
- $r < 0.20$ (95% CL); $n_s=0.968 (+/- 0.015)$
- $-0.0181 < \Omega_k < 0.0071$ (95% CL) for $w=-1$
- $-0.0175 < \Omega_k < 0.0085$ (95% CL) for $w \neq -1$
- Entropy perturbation (axion) $< 8.6\%$ (95% CL)
- Entropy perturbation (curvaton) $< 2.0\%$ (95% CL)
- $-9 < f_{NL}(\text{local}) < 111$ (95% CL)
- $-151 < f_{NL}(\text{equilateral}) < 253$ (95% CL)

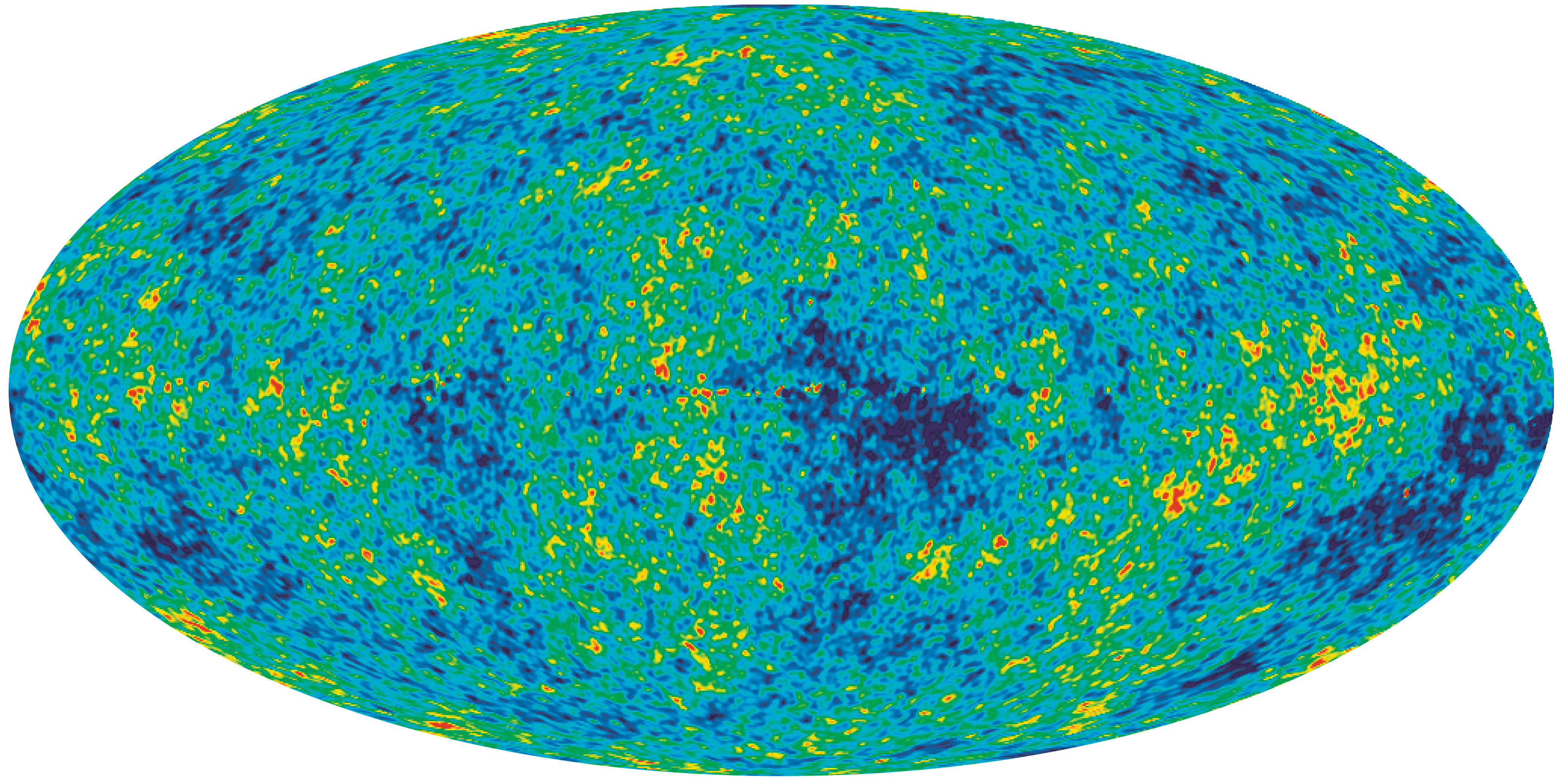
Is Yours A Good Model?

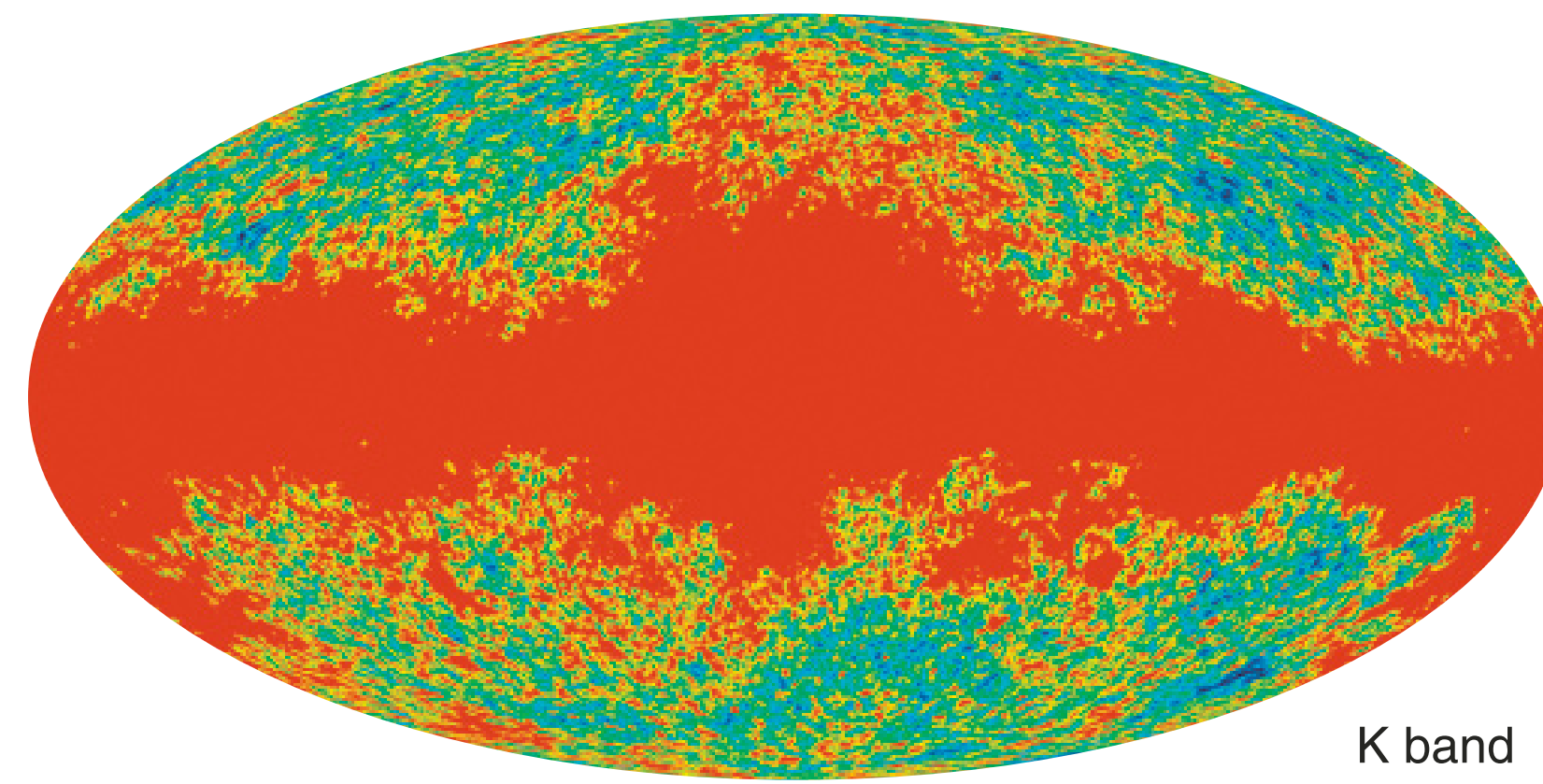
Check List

- Is the observable universe flat?
- Are the primordial fluctuations adiabatic?
- Are the primordial fluctuations nearly Gaussian?
- Is the power spectrum nearly scale invariant?
- Is the amplitude of gravitational waves reasonable?

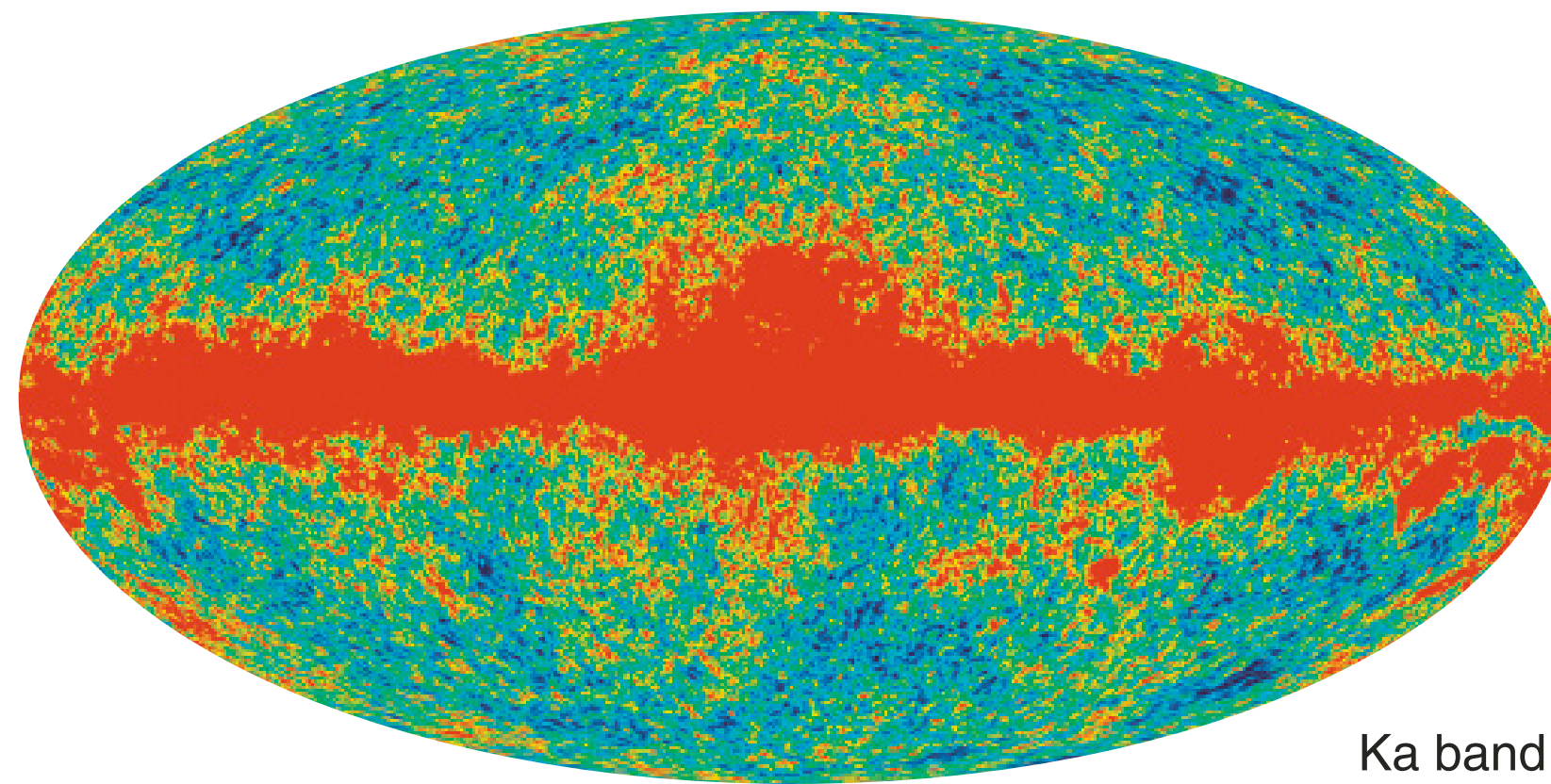
WMAP 5-Year Data

Hinshaw et al.

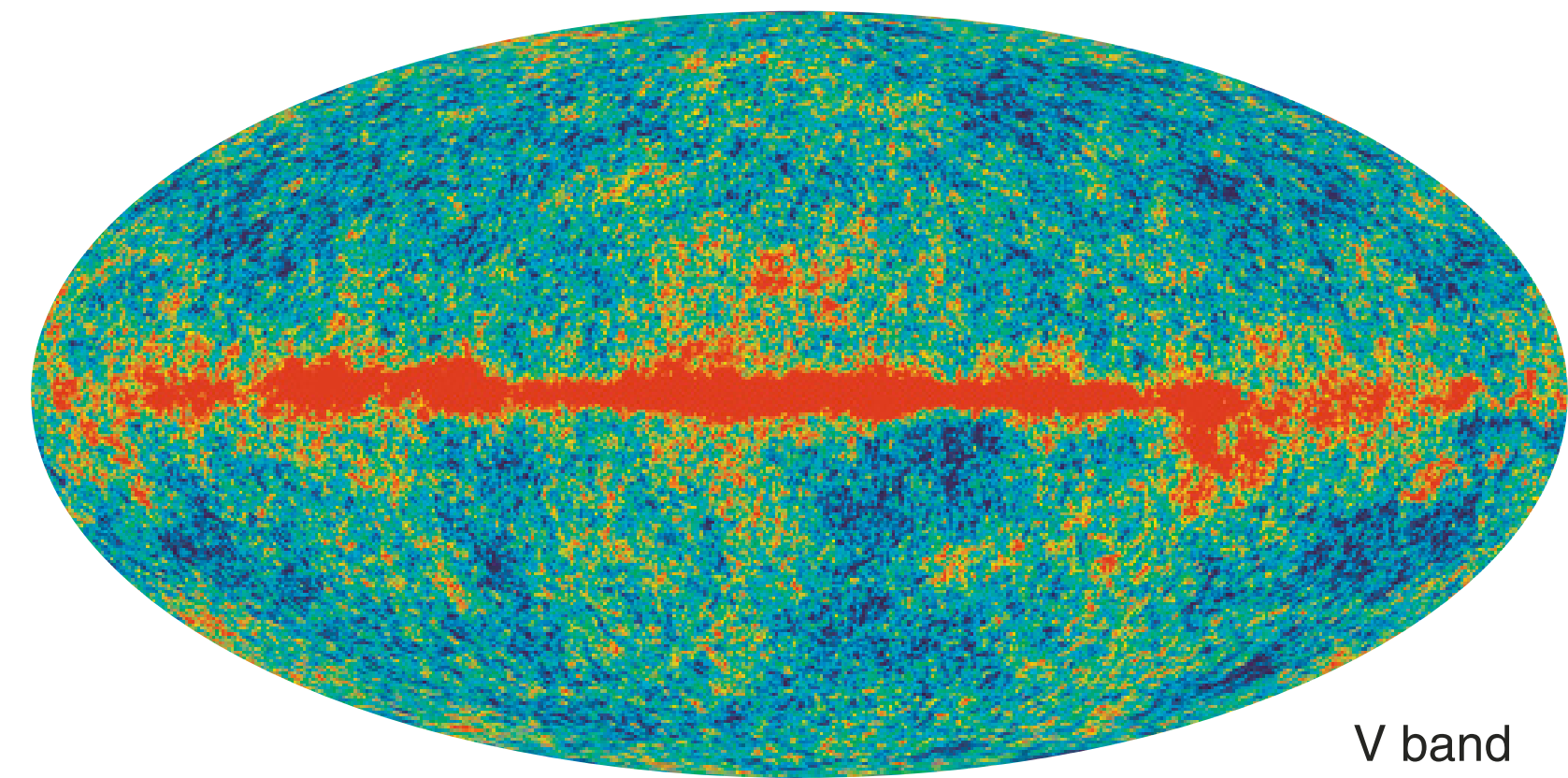




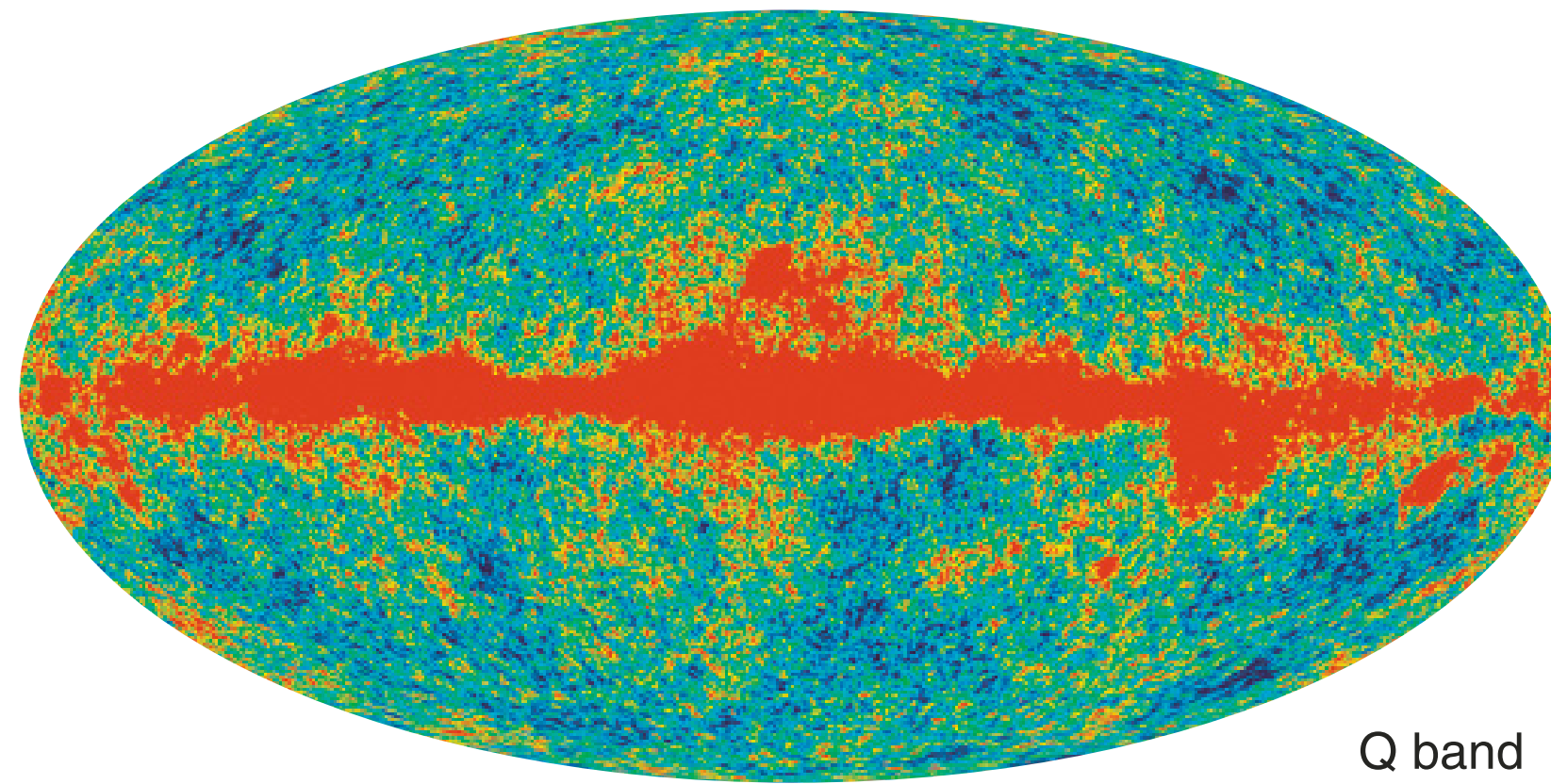
K band



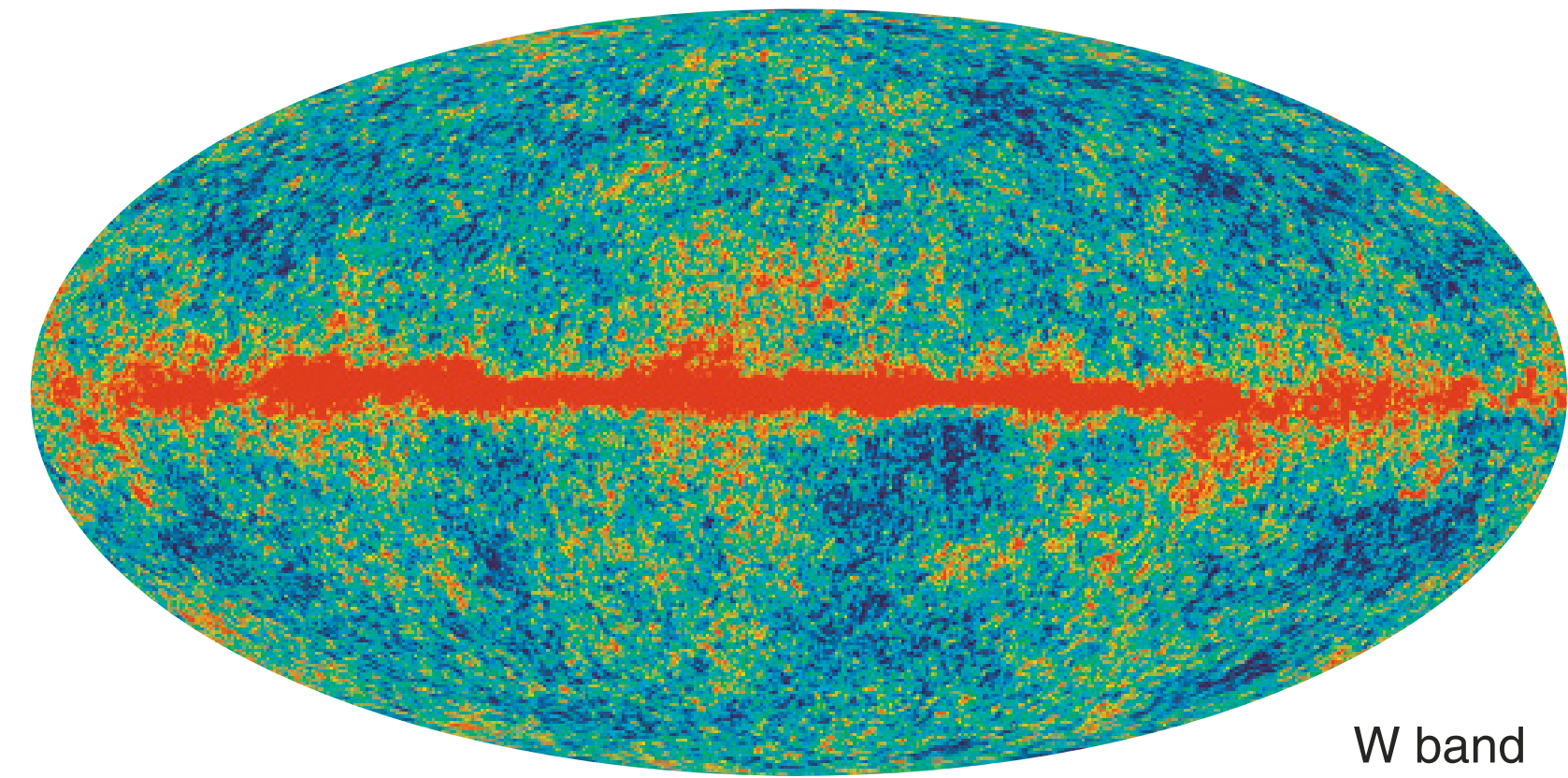
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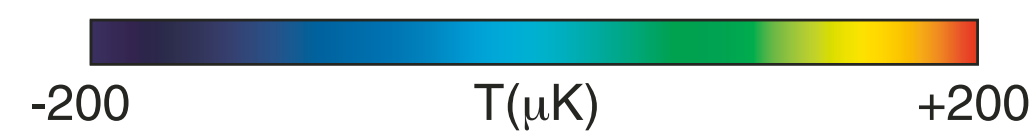
V band



Q band



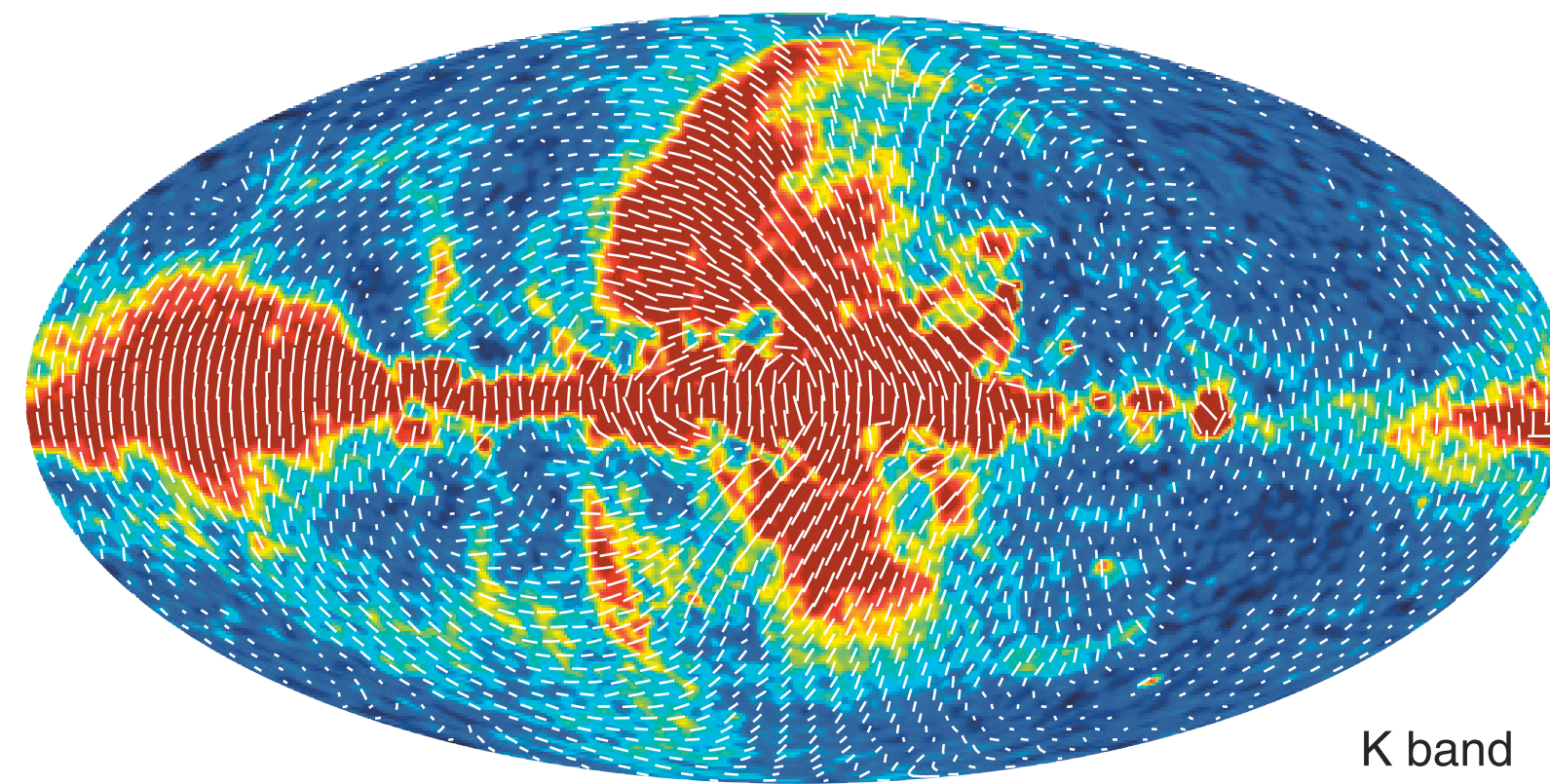
W band



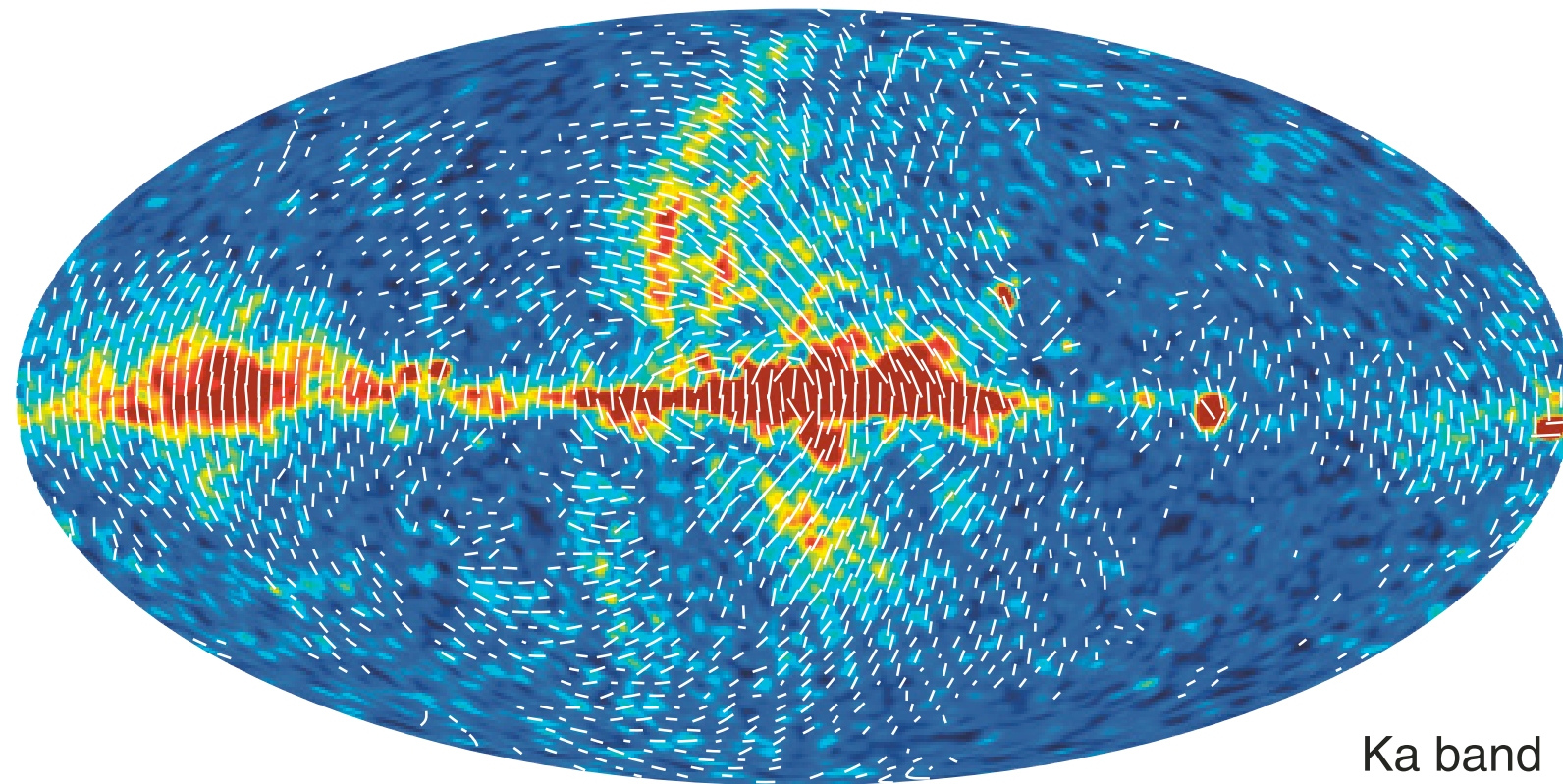
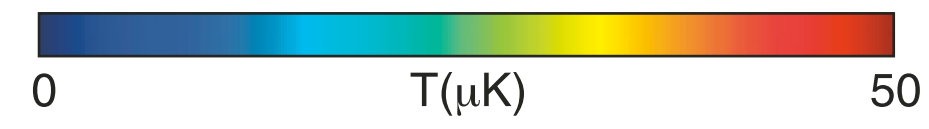
-200

$T(\mu\text{K})$

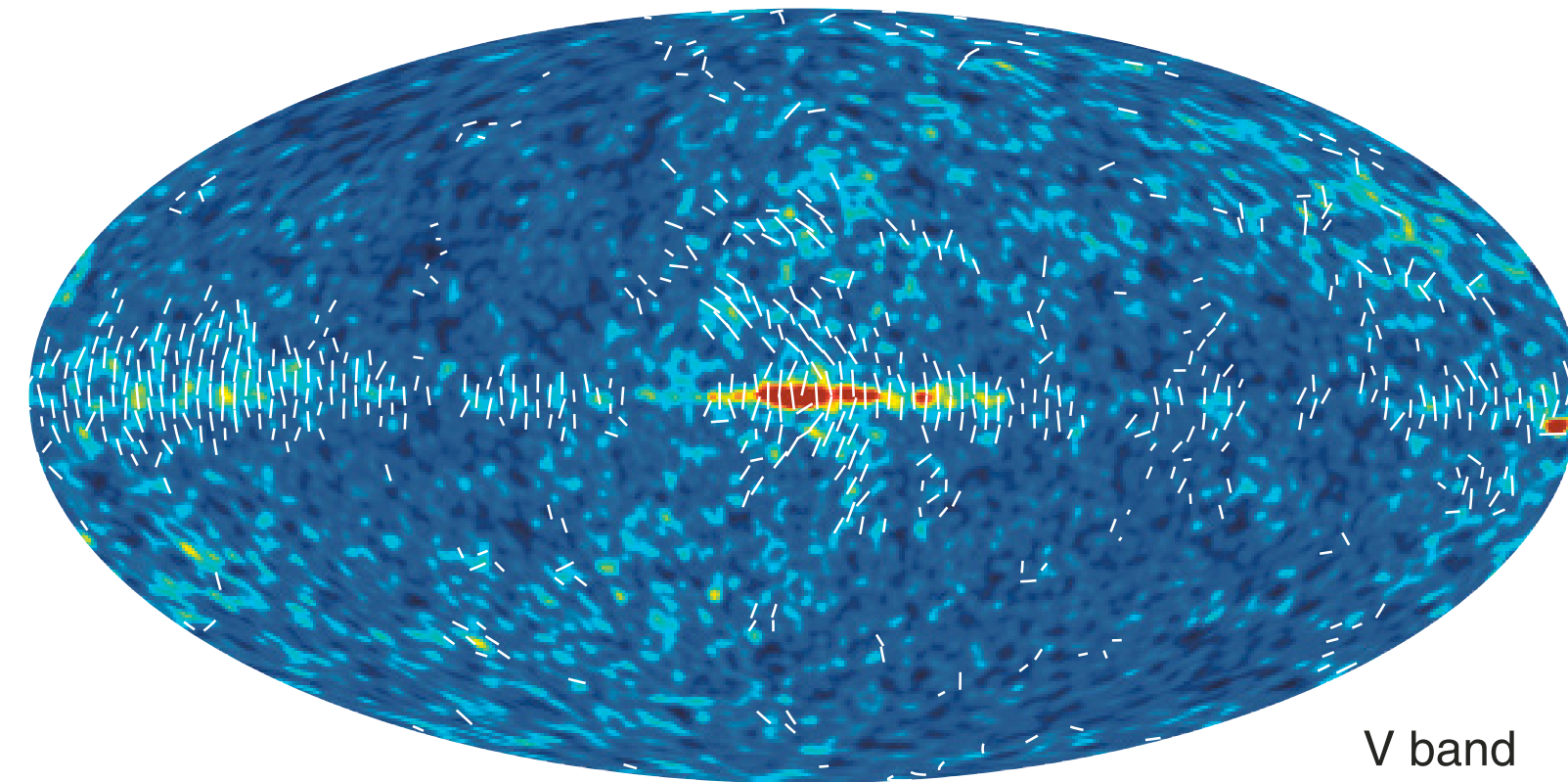
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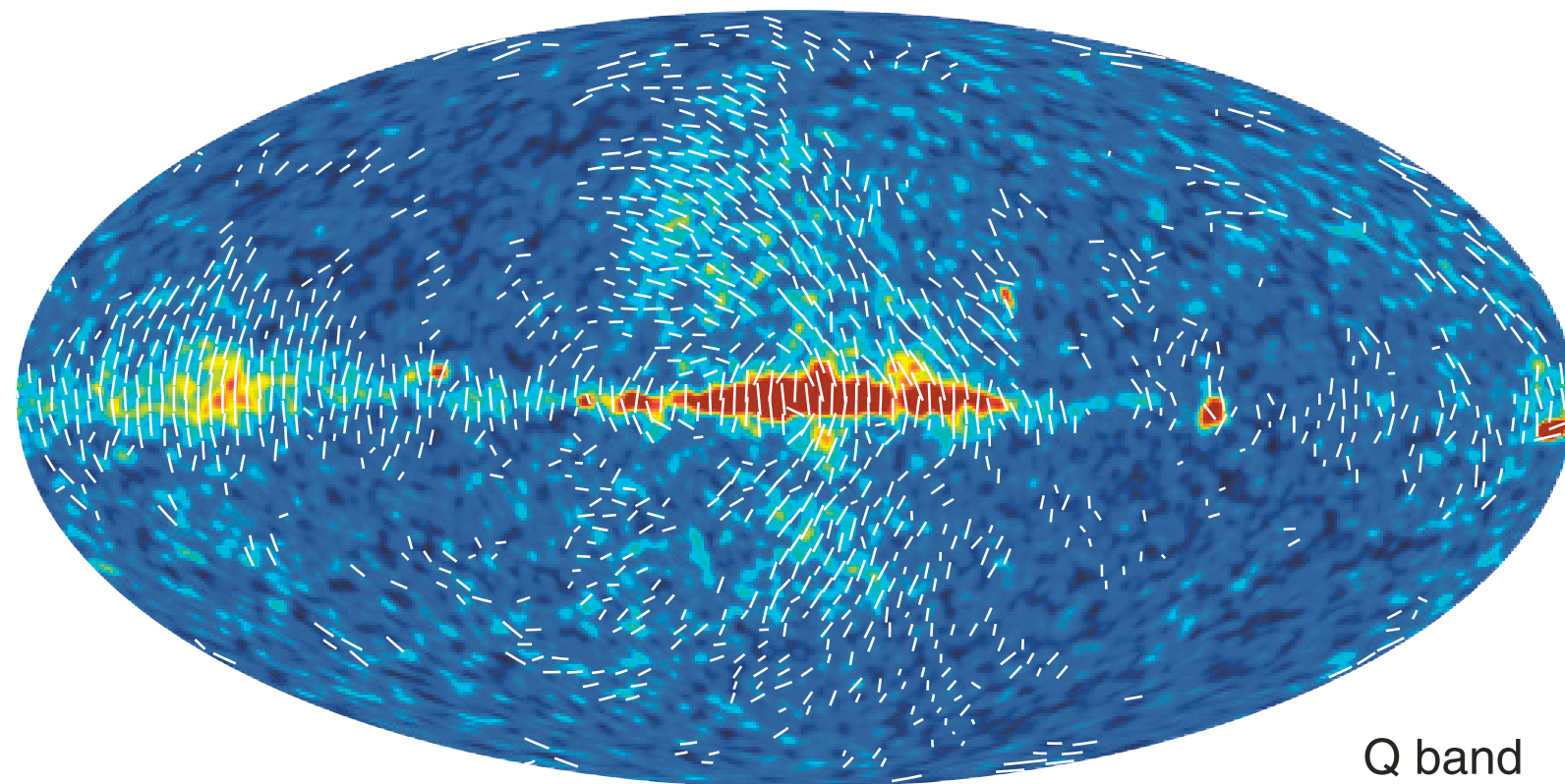
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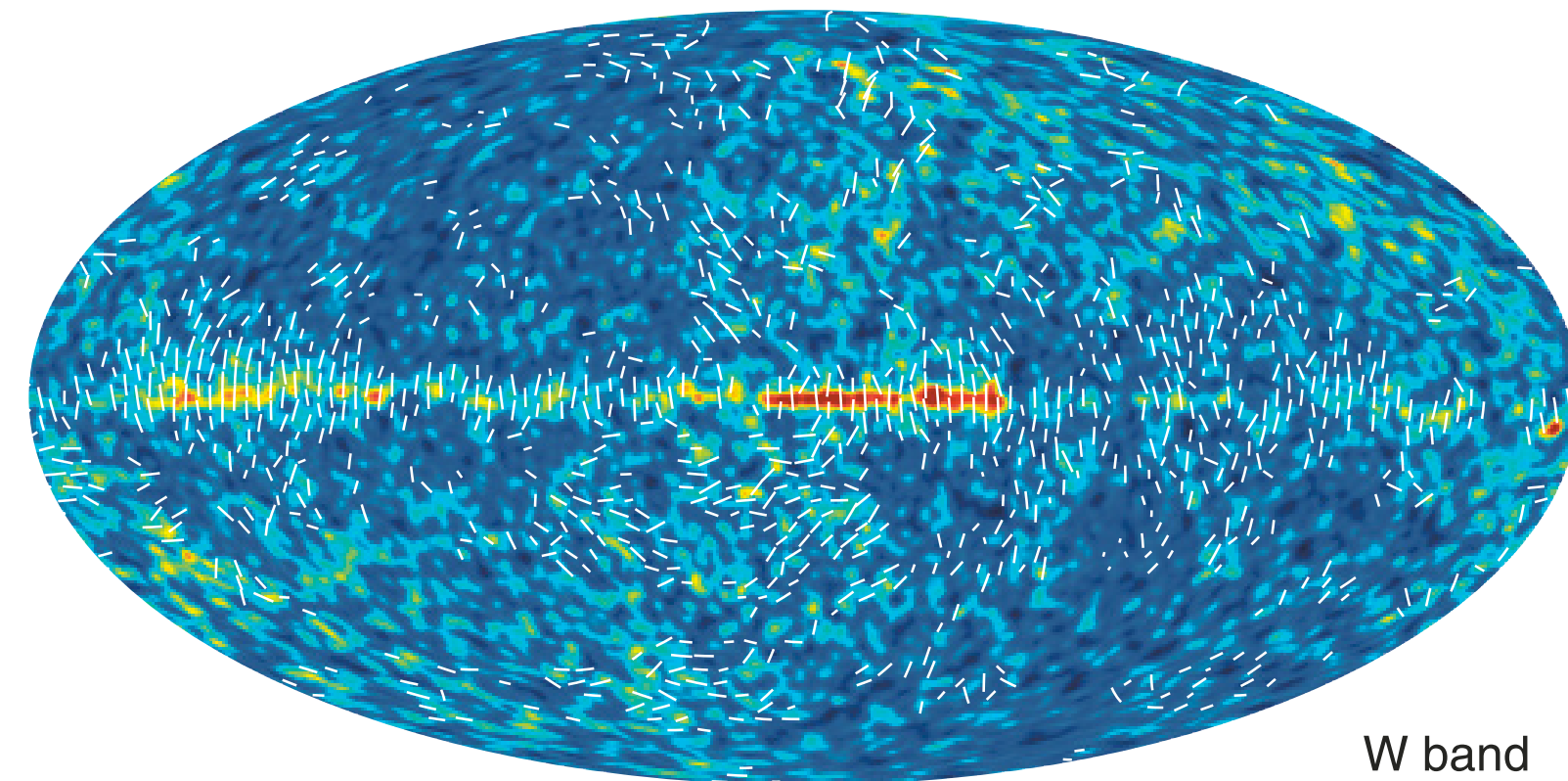
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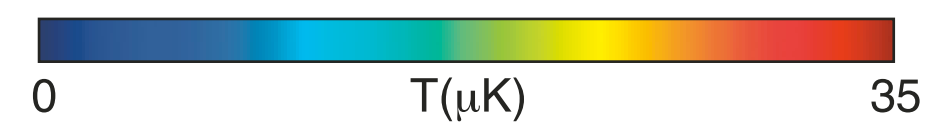
V band



Q band



W band

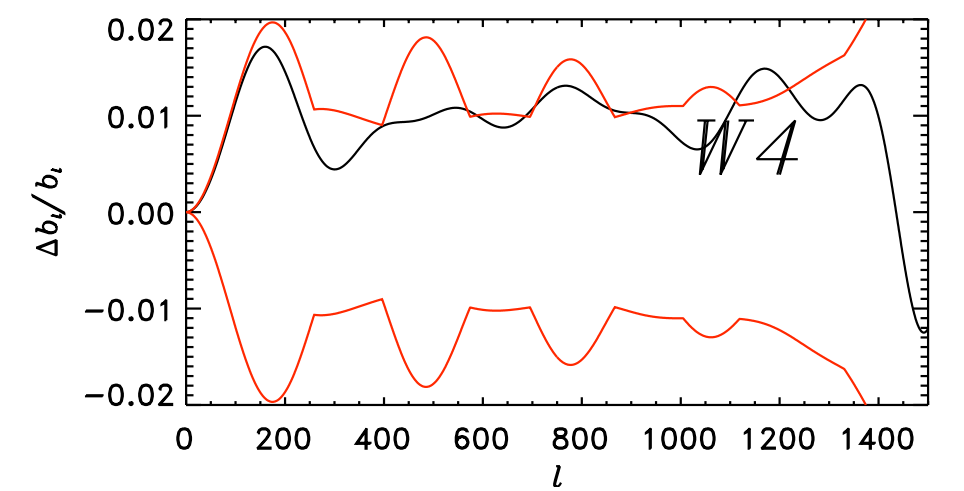
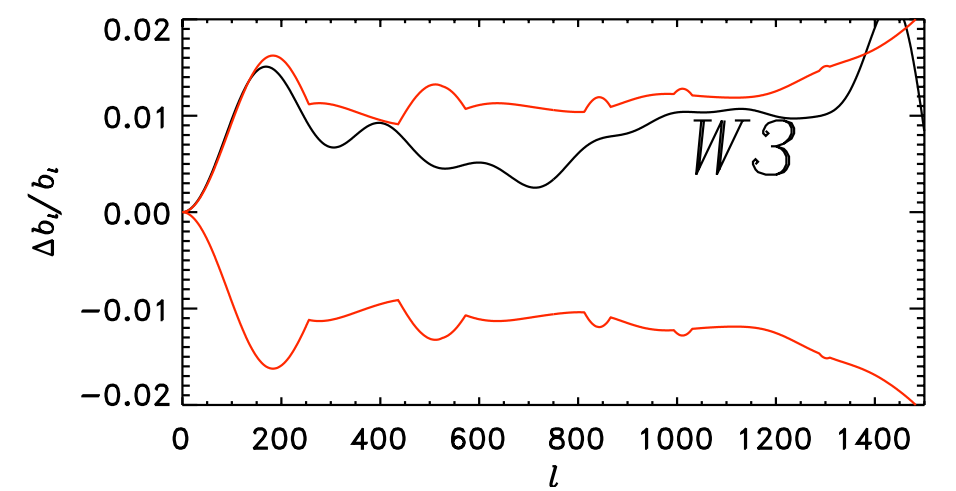
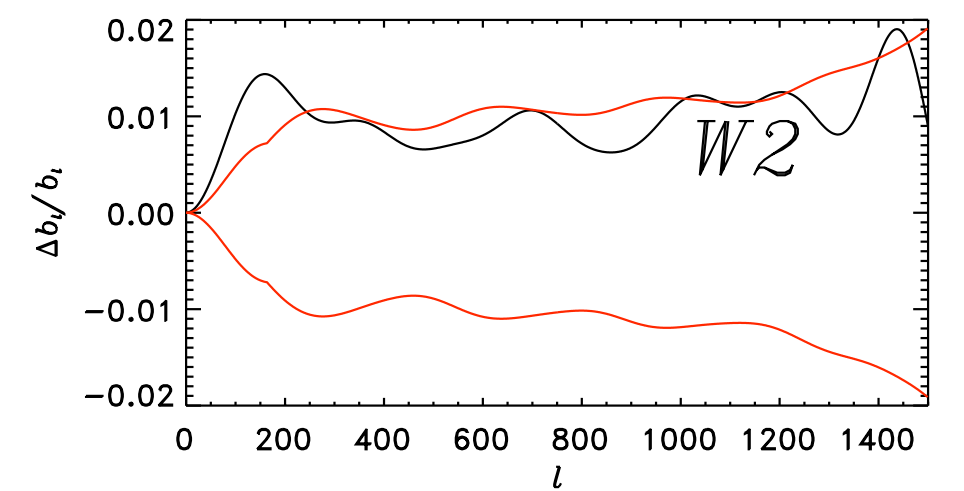
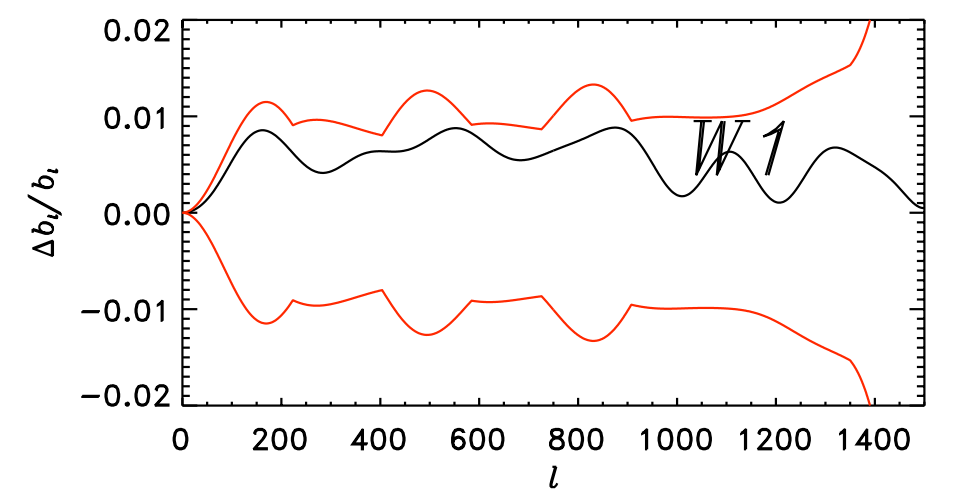
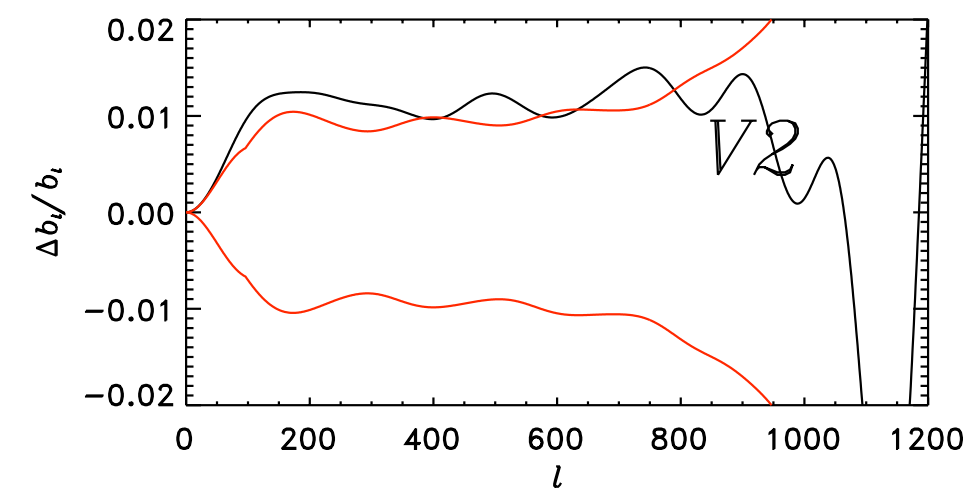
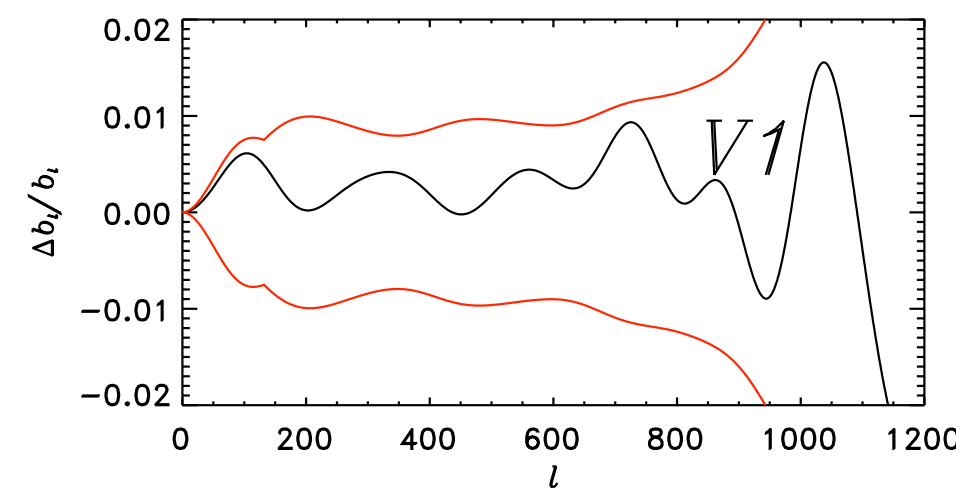
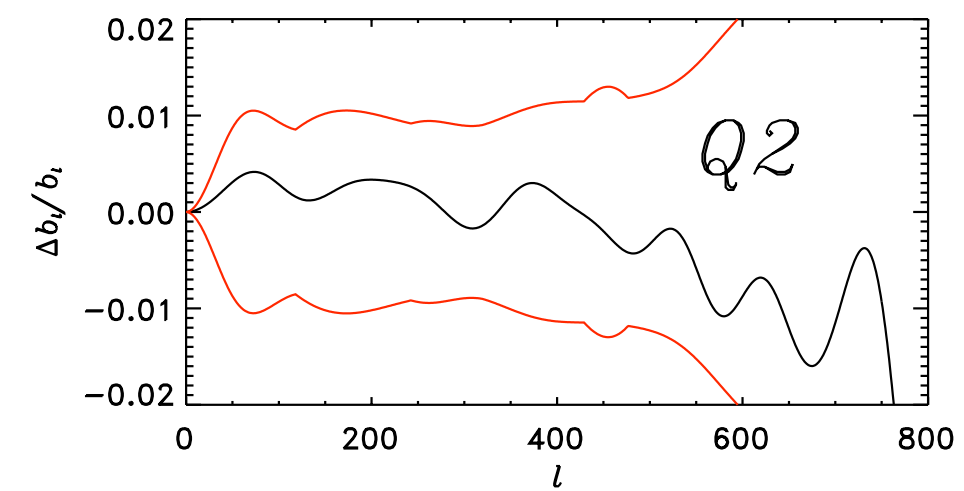
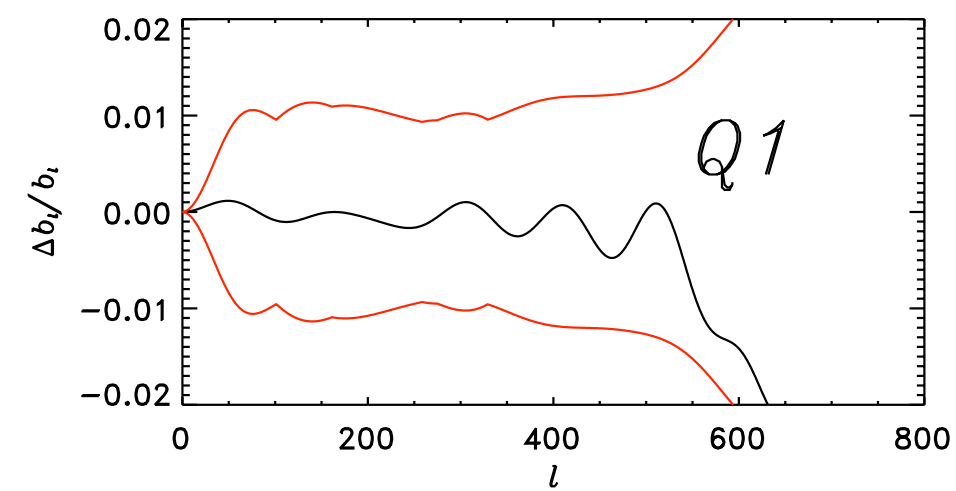
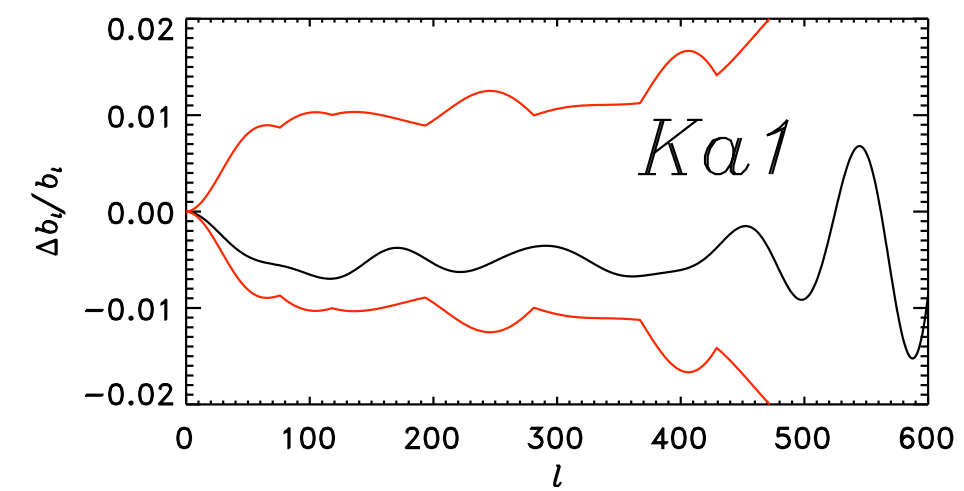
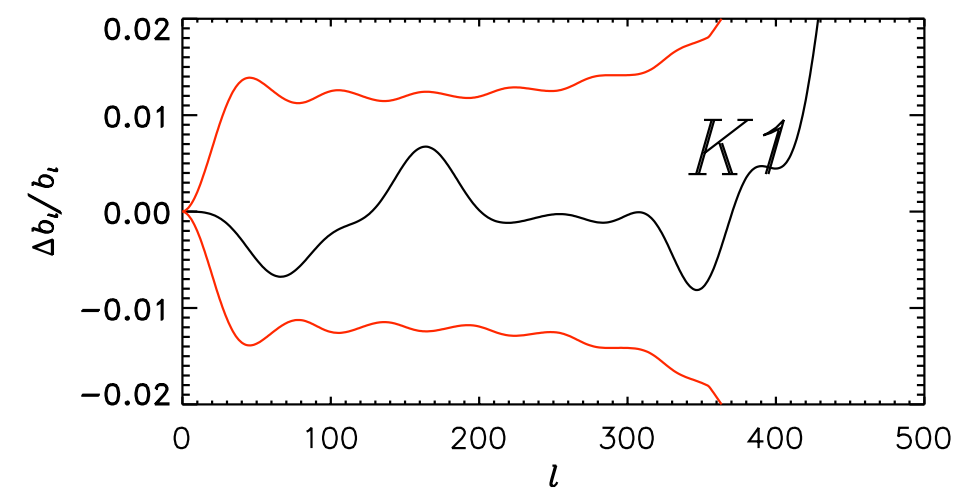


Improved Data/Analysis

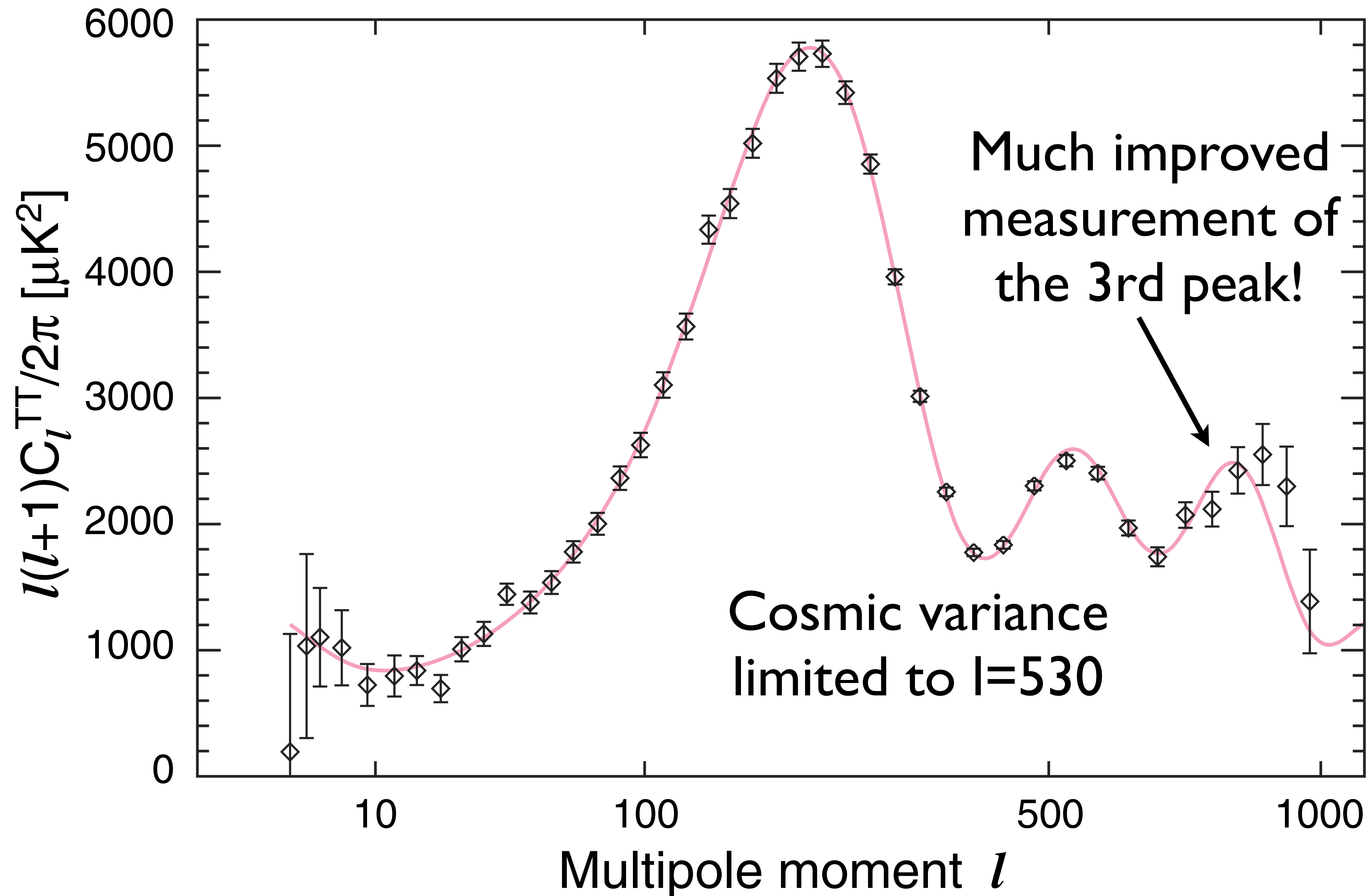
- Improved Beam Model
 - 5 years of the Jupiter data, combined with the extensive physical optics modeling, reduced the beam uncertainty by a factor of 2 to 4.
- Improved Calibration
 - Improved algorithm for the gain calibration from the CMB dipole reduced the calibration error from 0.5% to 0.2%
- More Polarization Data Usable for Cosmology
 - We use the polarization data in Ka band. (We only used Q and V bands for the 3-year analysis.)

New Beam

- The difference between the 5-year beam and the 3-year beam (shown in black) is within ~ 1 sigma of **the 3-year beam errors (shown in red)**
- We use V and W bands to measure the temperature power spectrum, C_l
 - Power spectrum depends on the beam²
 - **The 5-year C_l is $\sim 2.5\%$ larger than the 3-year C_l at $l > 200$**

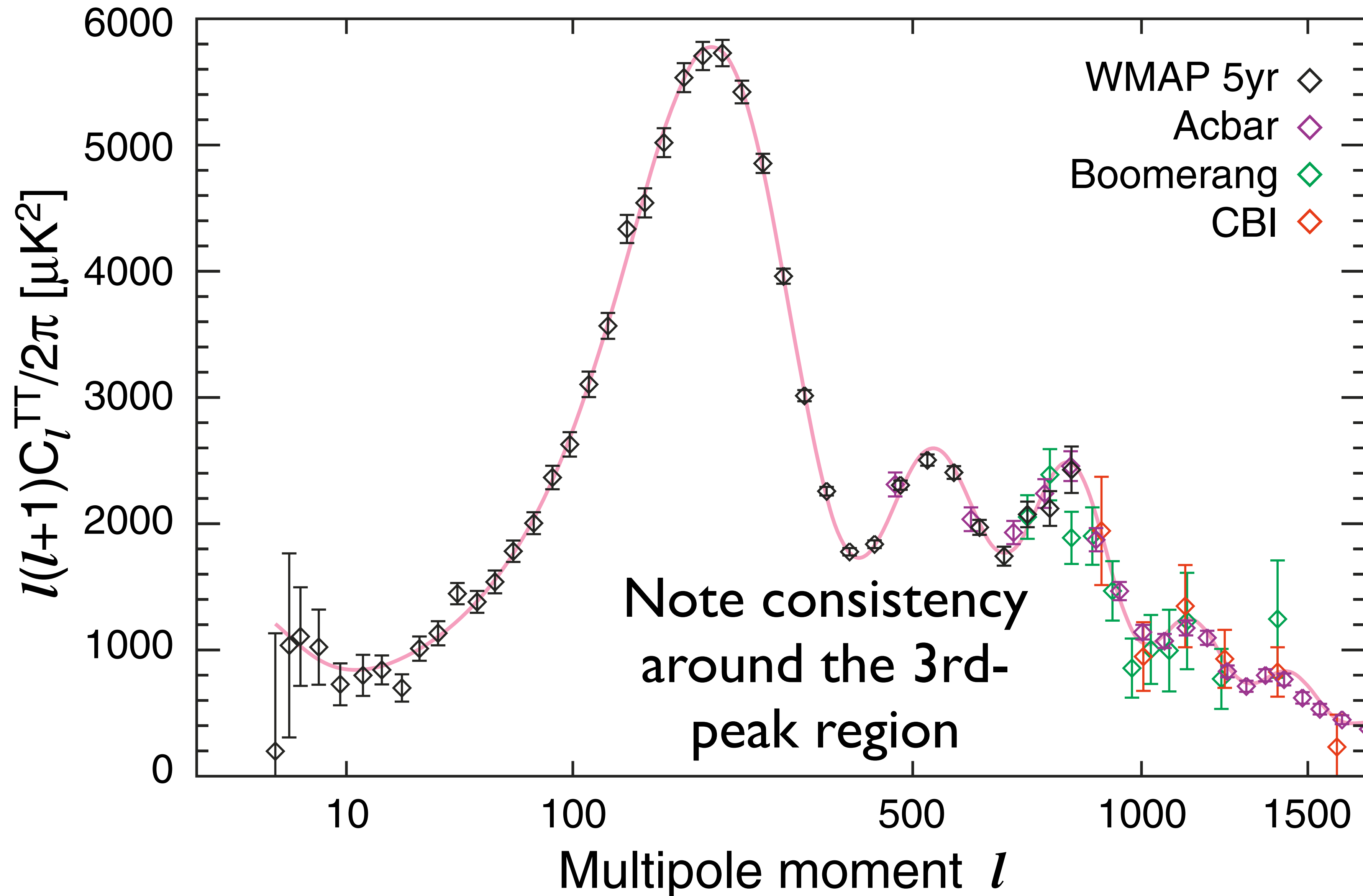


The 5-Year C_l

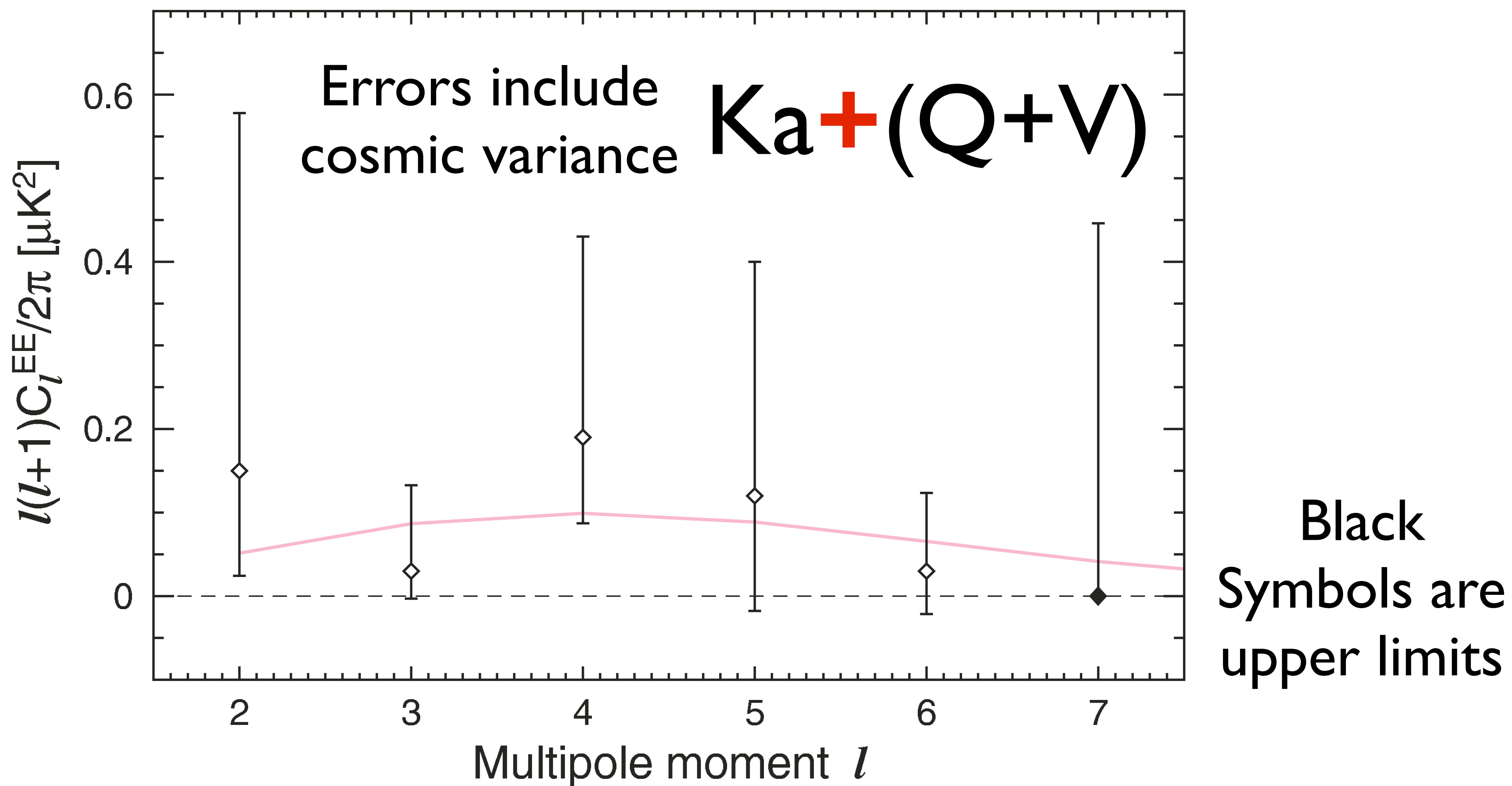


The 5-Year C_l

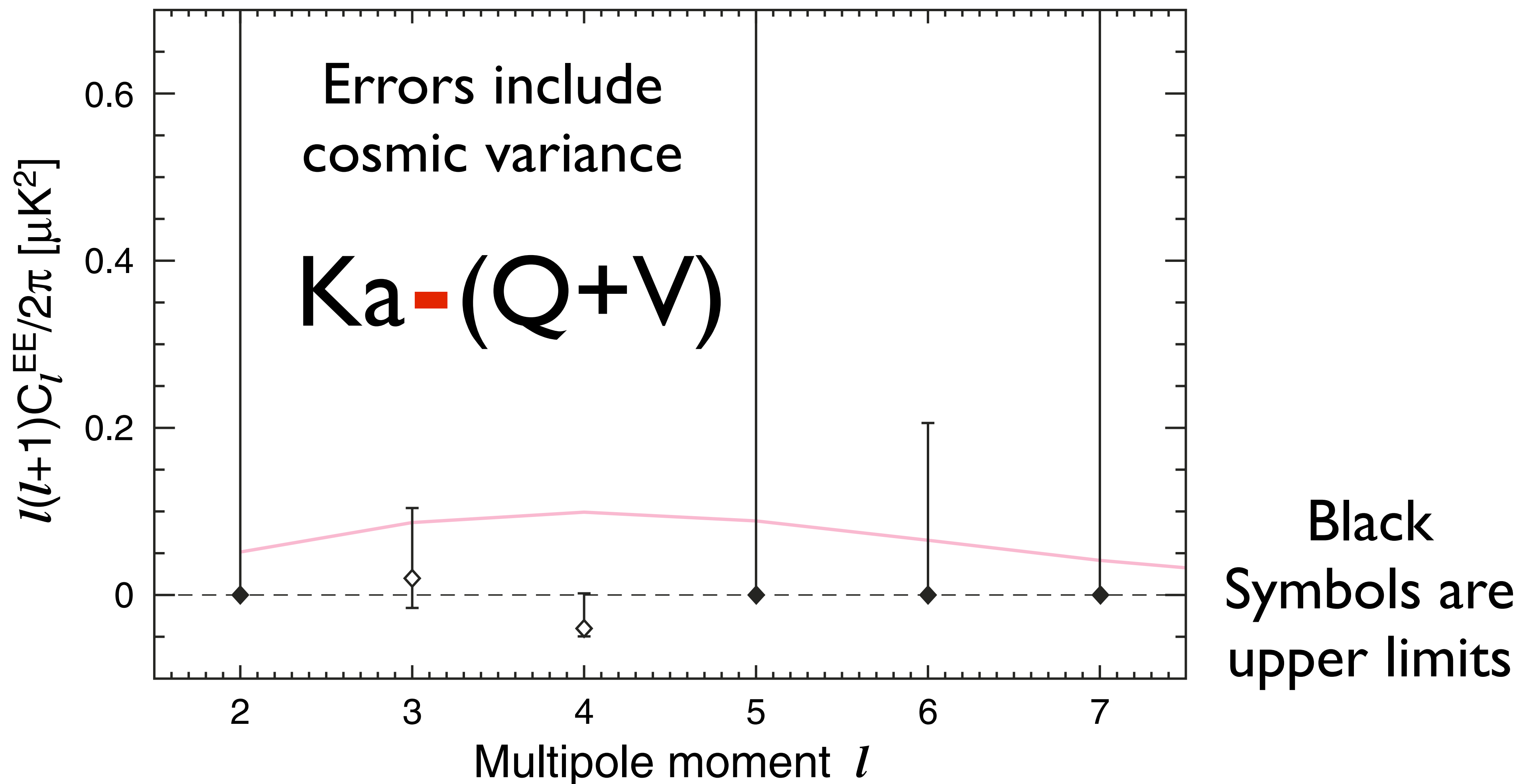
Nolta et al.



Adding Polarization in Ka: OK? Look at C_l^{EE}

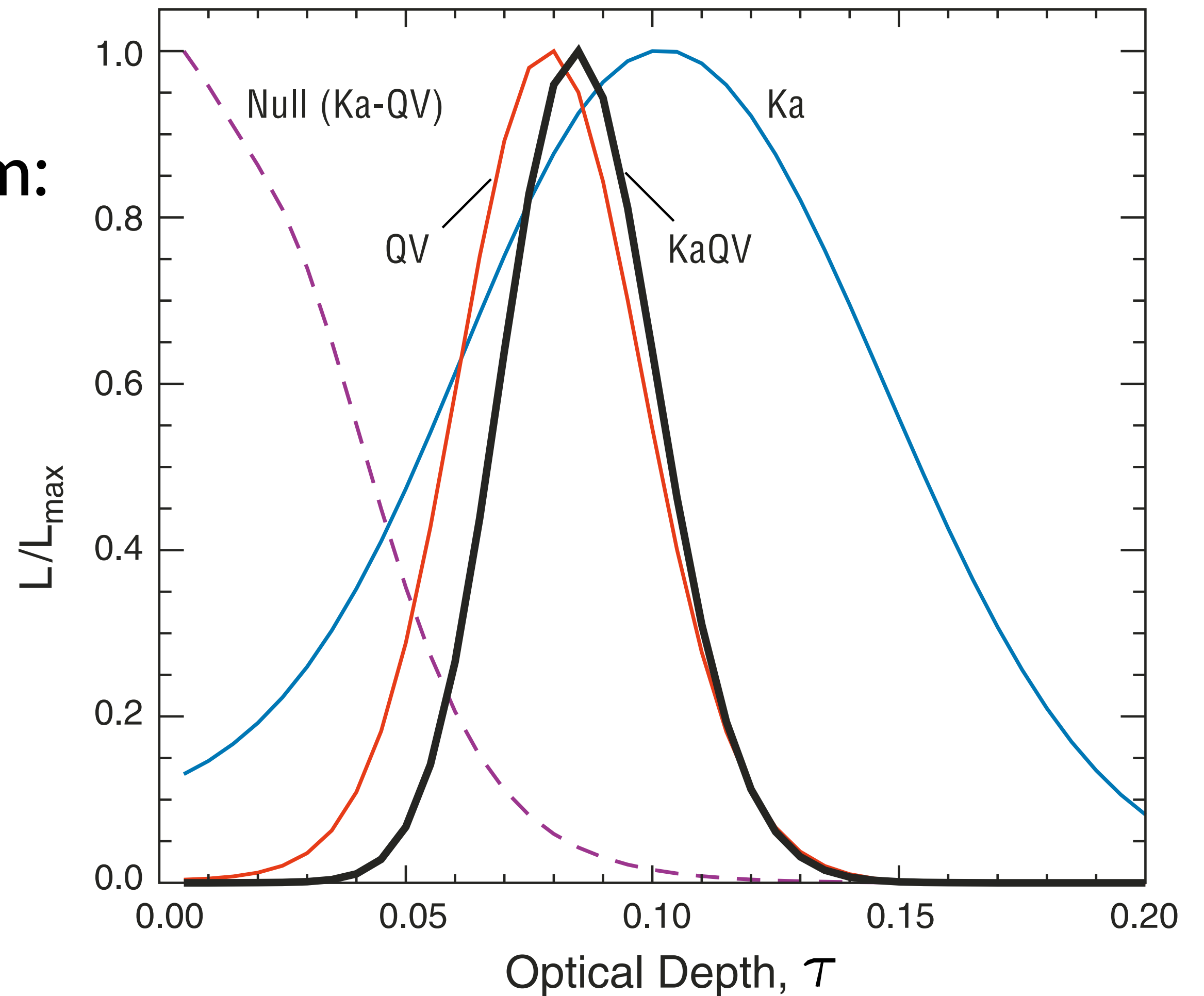


Adding Polarization in Ka: Passed the Null Test

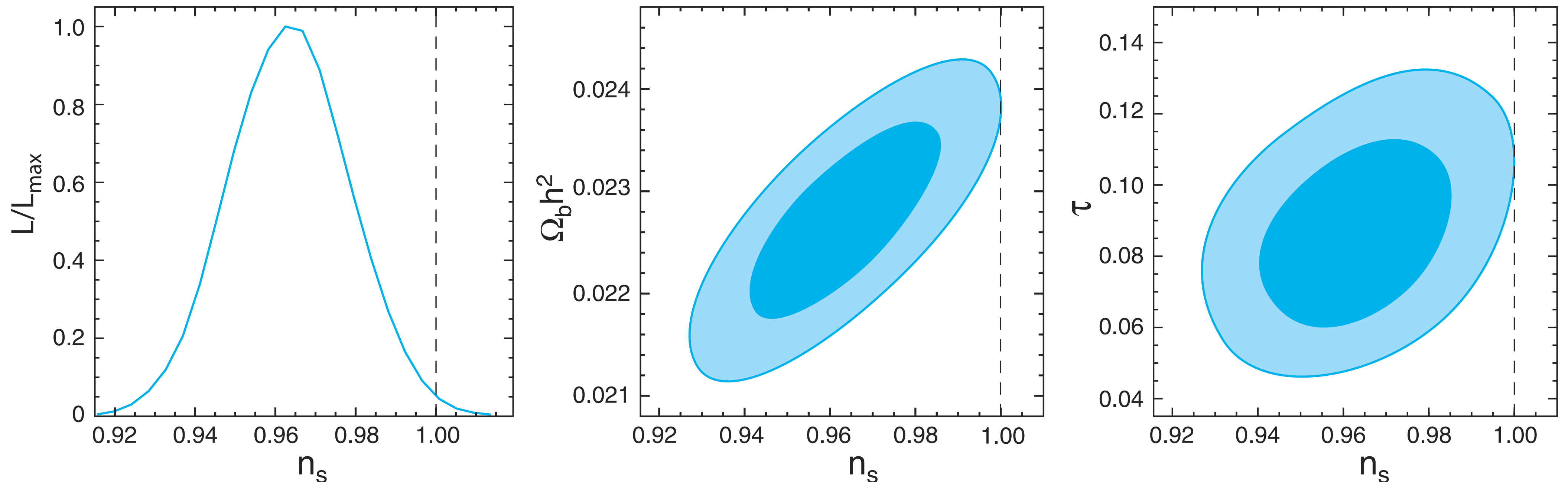


Adding Polarization in Ka: Passed the Null Test!!

- Optical Depth measured from the EE power spectrum:
- $\tau(5\text{yr}) = 0.087 \pm 0.017$
- $\tau(3\text{yr}) = 0.089 \pm 0.030$
(Page et al.; QV only)
- 3-sigma to 5-sigma!
- Tau from the null map (Ka-QV) is consistent with zero



Tau: (Once) Important for n_s *Komatsu et al.*



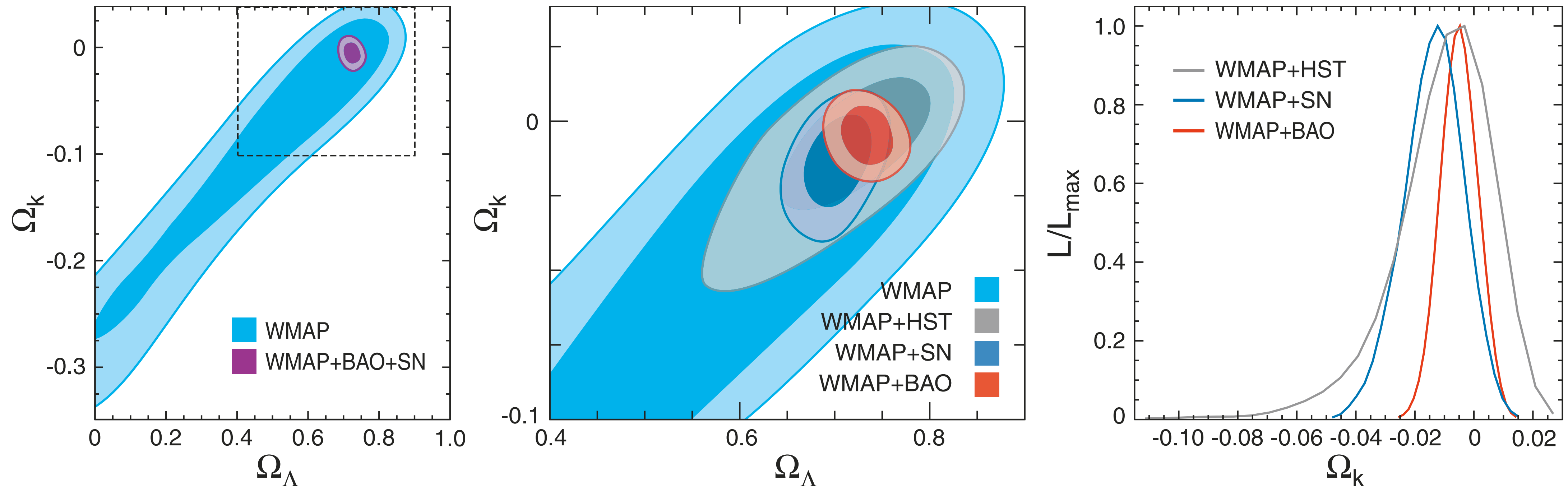
- With the 5-year determination of the optical depth (τ), the most dominant source of degeneracy is now $\Omega_b h^2$, rather than τ .
- WMAP-alone: $n_s = 0.963 (+0.014) (-0.015)$ (Dunkley et al.)
 - 2.5-sigma away from $n_s = 1$

How Do We Test Early Universe Models?

- The WMAP data alone can put tight limits on most of the items in the check list. (For the WMAP-only limits, see Dunkley et al.)
- However, we can improve the limits on many of these items by adding the extra information from the distance measurements:
 - *Luminosity Distances* from Type Ia Supernovae (SN)
 - *Angular Diameter Distances* from the Baryon Acoustic Oscillations (BAO) in the distribution of galaxies

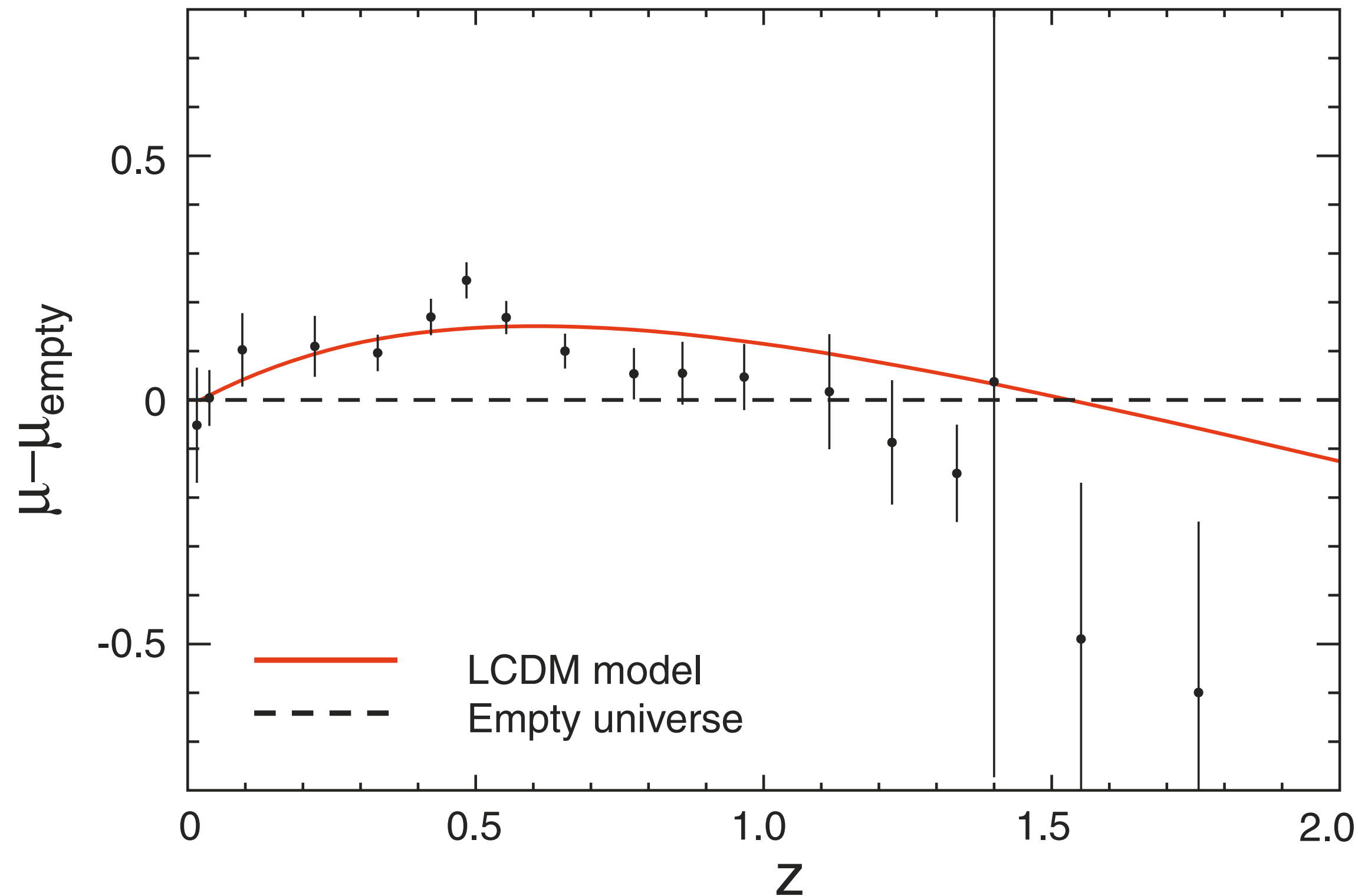
Example: Flatness

Komatsu et al.



- WMAP measures the angular diameter distance to the decoupling epoch at $z=1090$.
- The distance depends on curvature AND other things, like the energy content; thus, we need more than one distance indicators, in order to constrain, e.g., Ω_m and H_0

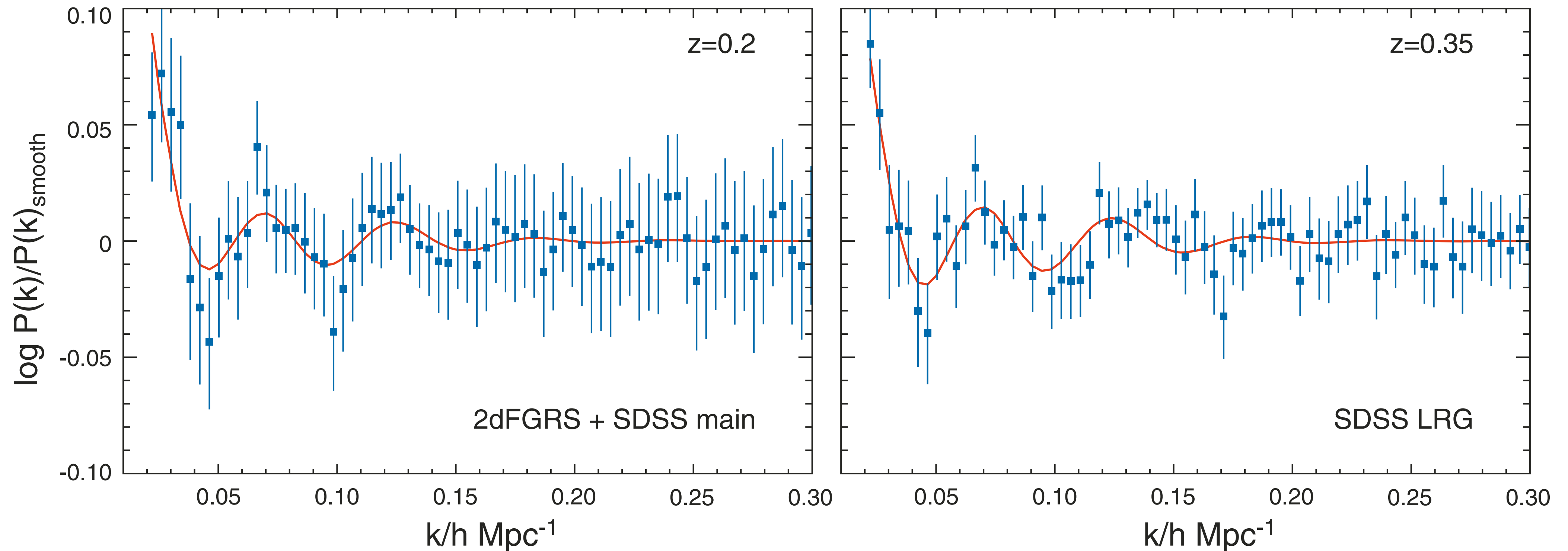
Type Ia Supernova (SN) Data



From these measurements, we get the **relative** luminosity distances between Type Ia SNe. Since we marginalize over the absolute magnitude, the current SN data are insensitive to the **absolute distances**.

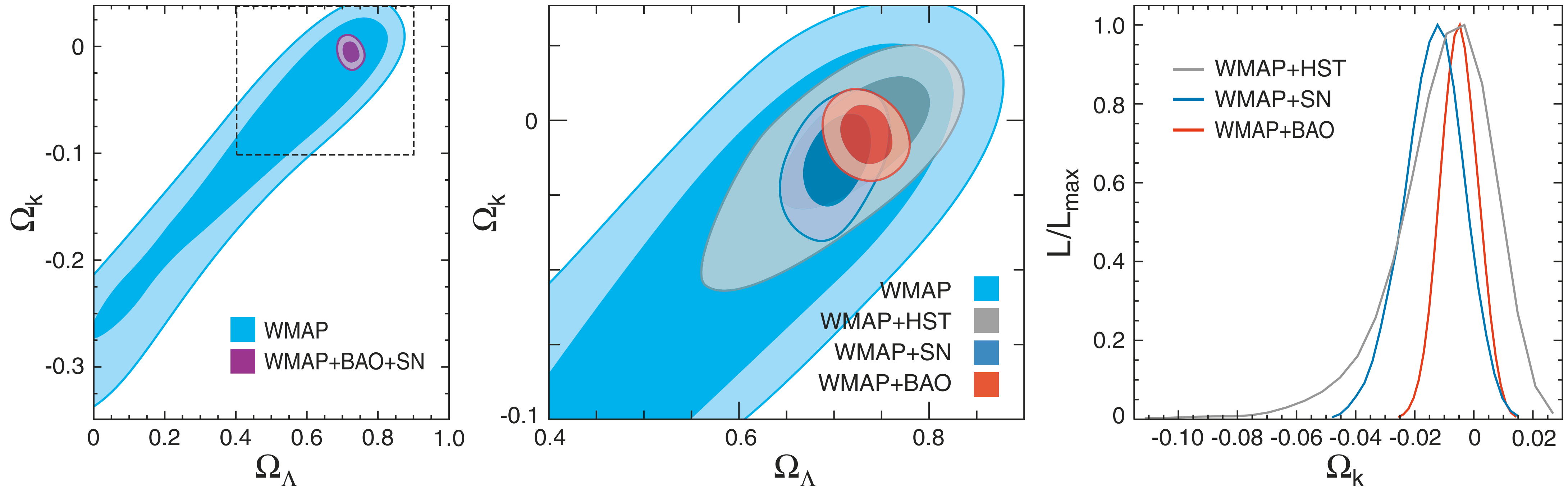
- Riess et al. (2004; 2006) HST data
- Astier et al. (2006) Supernova Legacy Survey (SNLS)
- Wood-Vasey et al. (2007) ESSENCE data

BAO in Galaxy Distribution *Dunkley et al.*



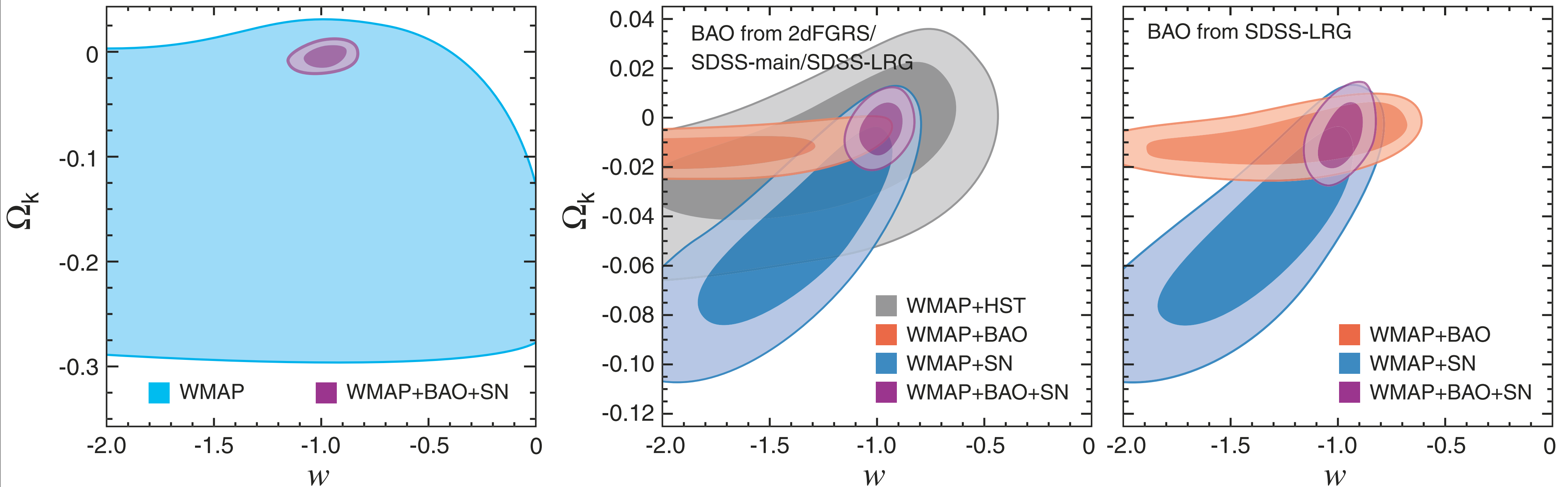
- BAO measured from SDSS (main samples and LRGs) and 2dFGRS (Percival et al. 2007)
- Just like the acoustic oscillations in CMB, the galaxy BAOs can be used to measure the **absolute** distances

As a result..



- **$-0.0181 < \Omega_k < 0.0071$** (95% CL) for $w=-1$
- The constraint driven mostly by WMAP+BAO
- BAOs are more powerful than SNe in pinning down curvature, as they are **absolute** distance indicators.

What if $w \neq -1$...



- WMAP+BAO \rightarrow Curvature
- WMAP+SN \rightarrow w
- WMAP+BAO+SN \rightarrow Simultaneous limit
- $-0.0175 < \Omega_k < 0.0085$; $-0.11 < w < 0.14$ (95% CL)

Fun Numbers to Quote...

- The curvature radius of the universe is given, by definition, by
 - $R_{\text{curv}} = 3h^{-1}\text{Gpc} / \text{sqrt}(\Omega_k)$
 - For negatively curved space ($\Omega_k > 1$): $R > 33h^{-1}\text{Gpc}$
 - For positively curved space ($\Omega_k > 1$): $R > 23h^{-1}\text{Gpc}$
- The particle horizon today is $9.7h^{-1}\text{Gpc}$
 - The observable universe is pretty flat! (Fun to teach this in class)

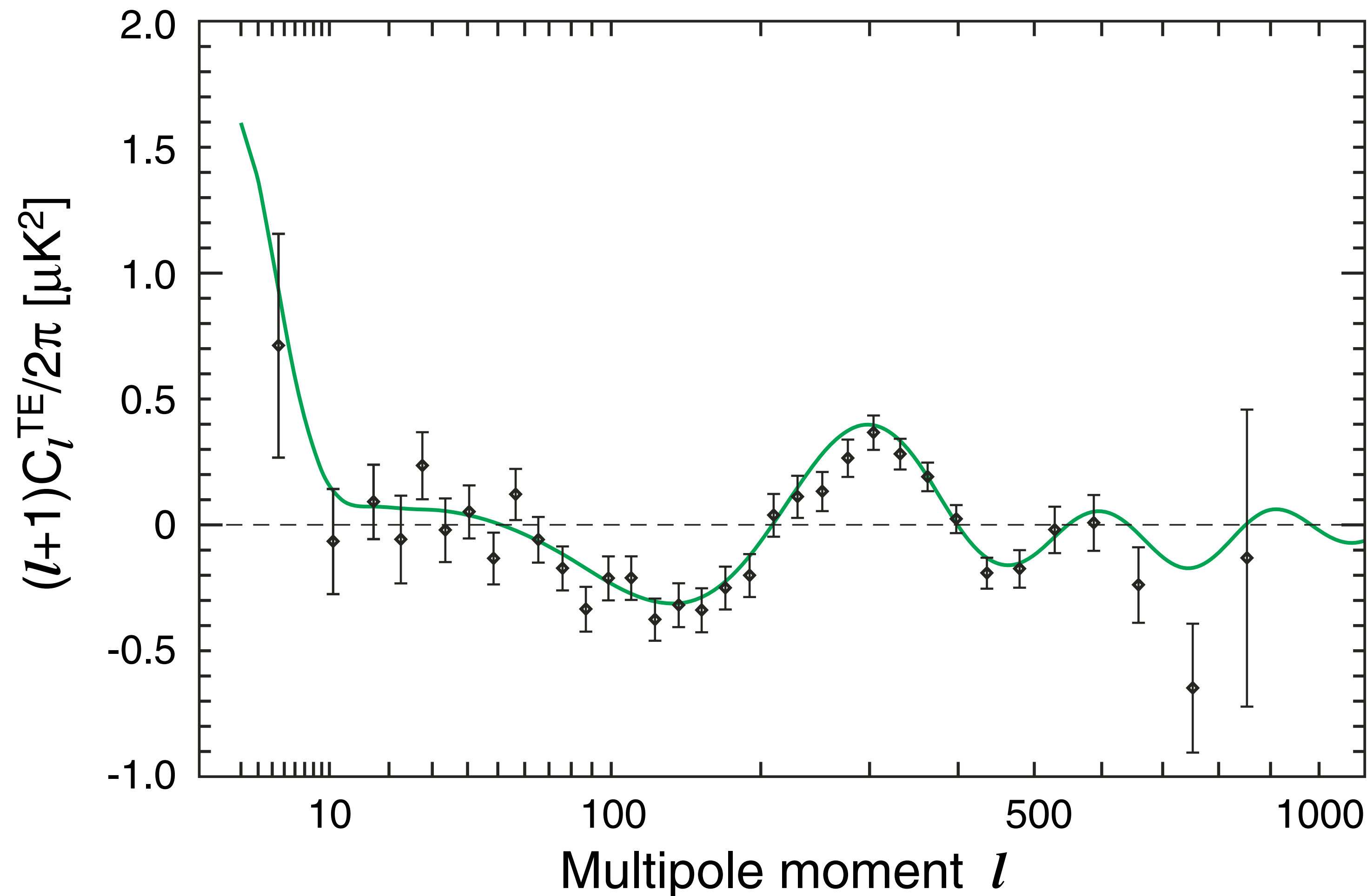
Implications for Inflation?

- Details aside...
 - Q. How long should inflation have lasted to explain the observed flatness of the universe?
 - A. **$N_{\text{total}} > 36 + \ln(T_{\text{reheating}}/1 \text{ TeV})$**
 - A factor of 10 improvement in Ω_k will raise this lower limit by 1.2.
 - Lower if the reheating temperature was $< 1 \text{ TeV}$
- This is the check list #1

Check List #2: Adiabaticity

- The adiabatic relation between radiation and matter:
 - $3\delta\rho_{\text{radiation}}/(4\rho_{\text{radiation}}) = \delta\rho_{\text{matter}}/\rho_{\text{matter}}$
- *Deviation from adiabaticity*: A simple-minded quantification
 - Fractional deviation of A from B = $(A-B) / [(A+B)/2]$
 - $\delta_{\text{adi}} = [3\delta\rho_{\text{radiation}}/(4\rho_{\text{radiation}}) - \delta\rho_{\text{matter}}/\rho_{\text{matter}}] / \{ [3\delta\rho_{\text{radiation}}/(4\rho_{\text{radiation}}) + \delta\rho_{\text{matter}}/\rho_{\text{matter}}] / 2 \}$
 - Call this the “**adiabaticity deviation parameter**”
 - “Radiation and matter obey the adiabatic relation to $(100\delta_{\text{adi}})\%$ level.”

WMAP 5-Year TE Power Spectrum



- The negative TE at $l \sim 100$ is the distinctive signature of super-horizon adiabatic perturbations (Spergel & Zaldarriaga 1997)
- Non-adiabatic perturbations would fill in the trough, and shift the zeros.

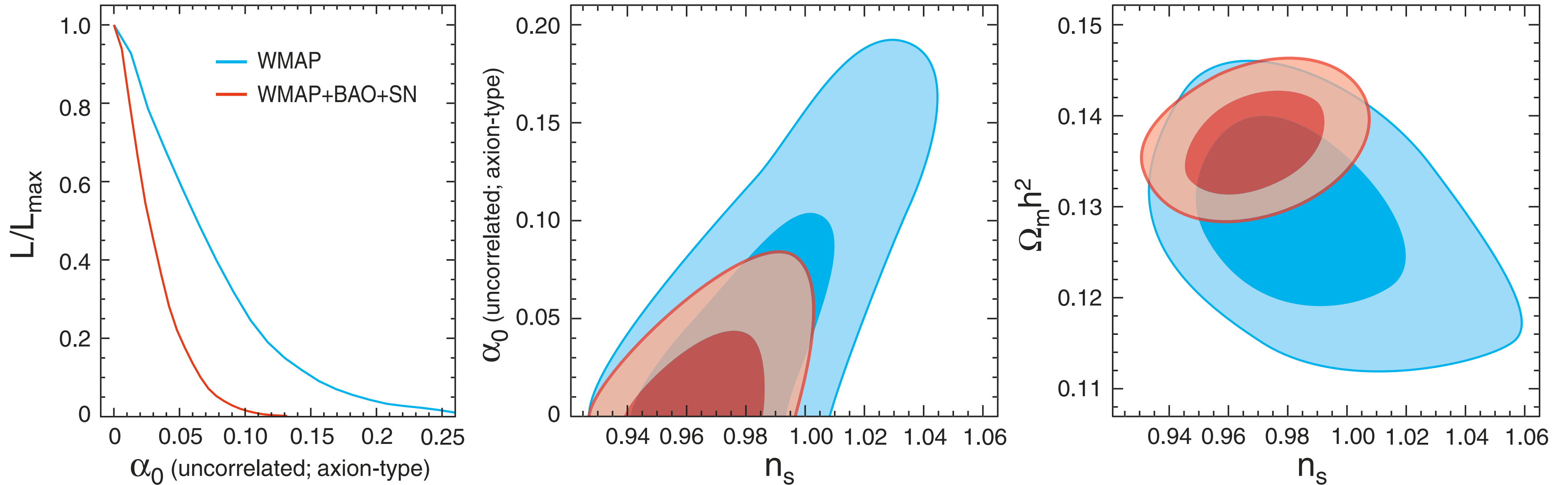
Entropy and curvature perturbations

- Usually, we use the entropy perturbations and curvature perturbations when we talk about adiabaticity.
 - (Entropy Pert.) = $3\delta\rho_{\text{radiation}}/(4\rho_{\text{radiation}}) - \delta\rho_{\text{matter}}/\rho_{\text{matter}}$
 - (Curvature Pert.) = $\delta\rho_{\text{matter}}/(3\rho_{\text{matter}}) = \delta\rho_{\text{radiation}}/(4\rho_{\text{radiation}})$
- Let's take the ratio, square it, and call it α :
 - $\alpha = (\text{Entropy})^2/(\text{Curvature})^2 = 9\delta_{\text{adi}}^2$
 - This parameter, α , has often been used in the literature.

Two Scenarios

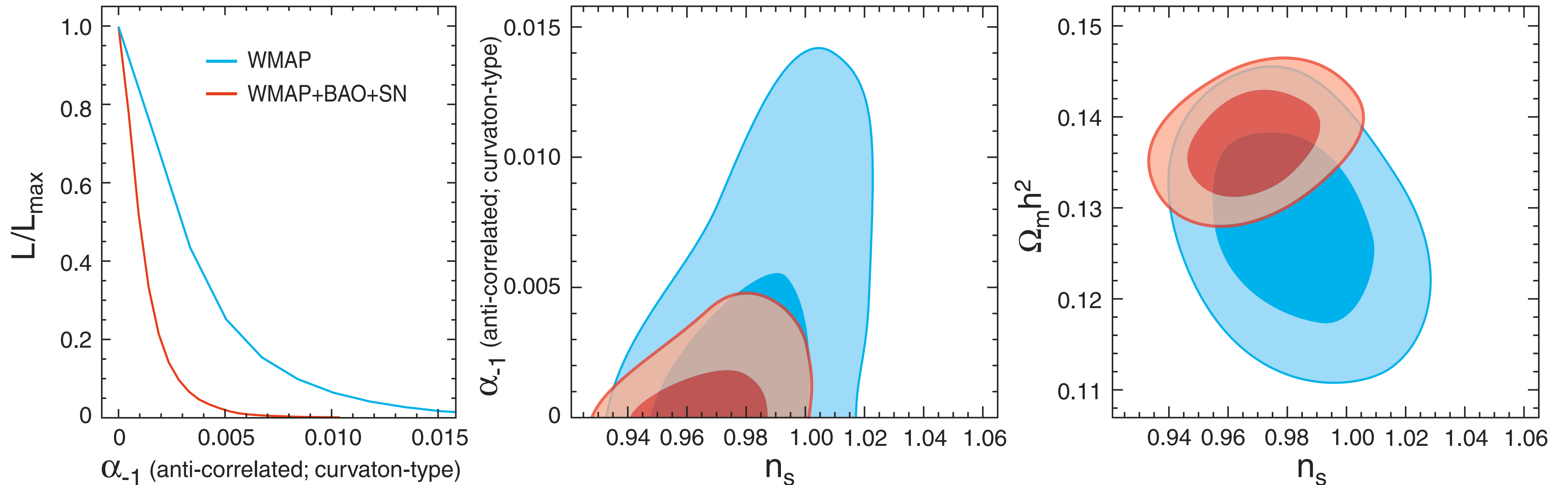
- To make the argument concrete, we take two concrete examples for entropy perturbations.
- (i) “***Axion Type***” Entropy perturbations and curvature perturbations are **uncorrelated**.
- (ii) “***Curvaton Type***” Entropy perturbations and curvature perturbations are **anti-correlated**. (or correlated, depending on the sign convention)
- In both scenarios, the entropy perturbation raises the temperature power spectrum at $l < 100$
 - Therefore, *both contributions are degenerate with n_s* .
How do we break the degeneracy? BAO&SN.

Axion Type



- $\alpha_{\text{axion}} < 0.16$ [WMAP-only; 95% CL]
- $\alpha_{\text{axion}} < 0.067$ [WMAP+BAO+SN; 95% CL]
- CMB and axion-type dark matter are adiabatic to **8.6%**

Curvaton Type



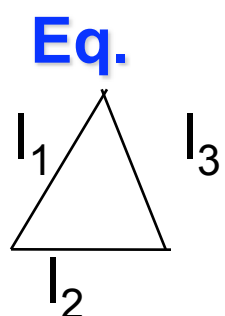
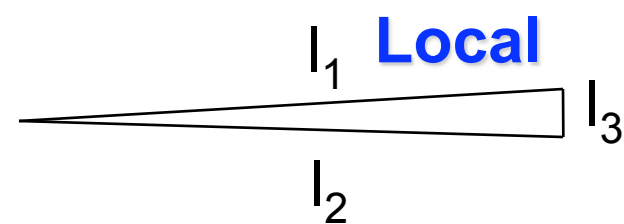
- $\alpha_{\text{curvaton}} < 0.011$ [WMAP-only; 95% CL]
- $\alpha_{\text{curvaton}} < 0.0037$ [WMAP+BAO+SN; 95% CL]
- CMB and axion-type dark matter are adiabatic to **2.0%**

Check list #3: Gaussianity

- Since there is a workshop focused on non-Gaussianity immediately following this one, I would defer detailed discussions on non-Gaussianity to that workshop.
- Let me just present results here.

Angular Bispectrum

- Non-zero bispectrum means the detection of non-Gaussianity. It's always easy to look for deviations from zero!
- There are many triangles to look for, but...
 - Will focus on two classes
 - “Squeezed” parameterized by $f_{\text{NL}}^{\text{local}}$
 - “Equilateral” parameterized by $f_{\text{NL}}^{\text{equil}}$



No Detection at $\geq 95\%$ CL

- $-9 < f_{\text{NL}}(\text{local}) < 111$ (95% CL)
- $-151 < f_{\text{NL}}(\text{equilateral}) < 253$ (95% CL)
- These numbers mean that the primordial curvature perturbations are Gaussian to **0.1% level!**
- These numbers are based upon the new Galaxy mask (KQ75) and after correcting for the point-source contamination.

The other mask?

Komatsu et al.

- The new mask, KQ75, cuts more sky than the masks used in the previous (1-yr and 3-yr) analysis. When we used the previous mask, Kp0, instead, we found:
- $6.5 < f_{\text{NL}}(\text{local}) < 110.5$ (95% CL) for Kp0 mask
 - A “hint” for $f_{\text{NL}}(\text{local}) > 0$ at 2.3 sigma. The error is smaller because Kp0 cuts less sky (76.5% retained) than KQ75 (71.8% retained)
 - To see if $f_{\text{NL}}(\text{local}) > 0$ persists with KQ75, we definitely need more data. More years of WMAP observations are needed.
- For more information, please come to the next workshop...

Check List #4: Scale Invariance

- For a power-law power spectrum (no $dn_s/d\ln k$):
 - WMAP-only: $n_s=0.963$ (+0.014) (-0.015)
 - WMAP+BAO+SN: $n_s=0.960$ (+0.014) (-0.013)
 - **2.9 sigma away from $n_s=1$**
 - No dramatic improvement from the WMAP-only result because neither BAO nor SN is sensitive to $\Omega_b h^2$

Running Index?

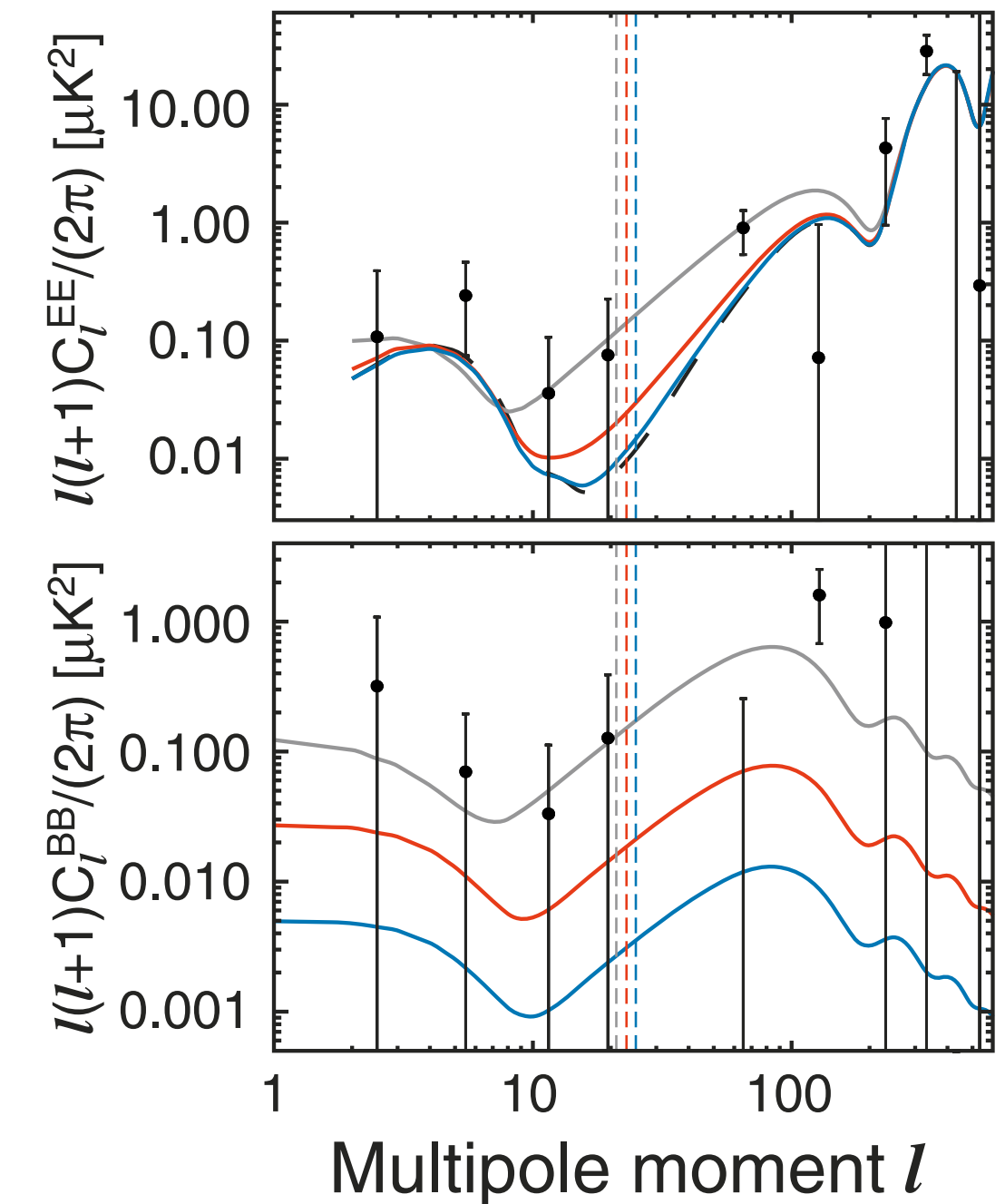
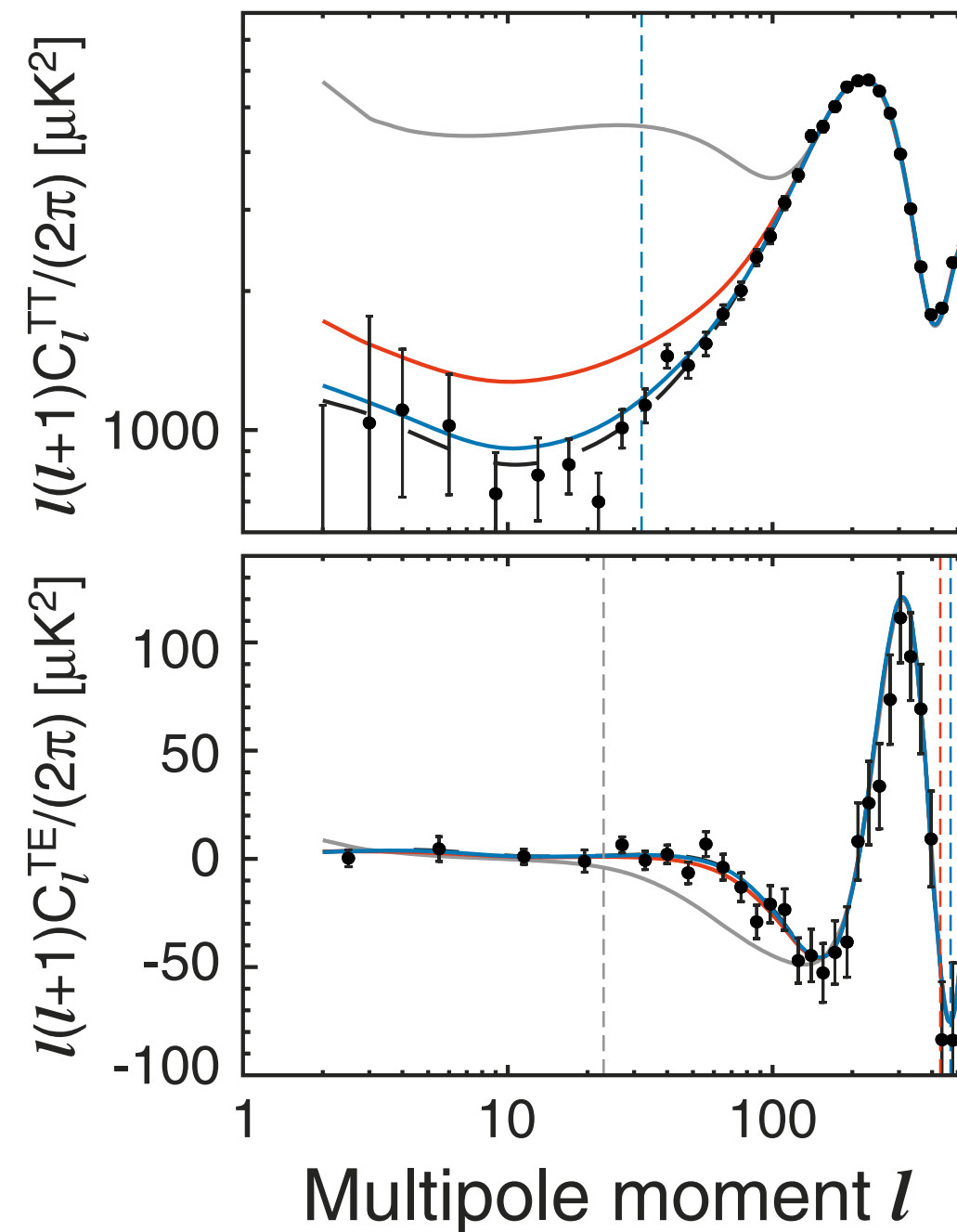
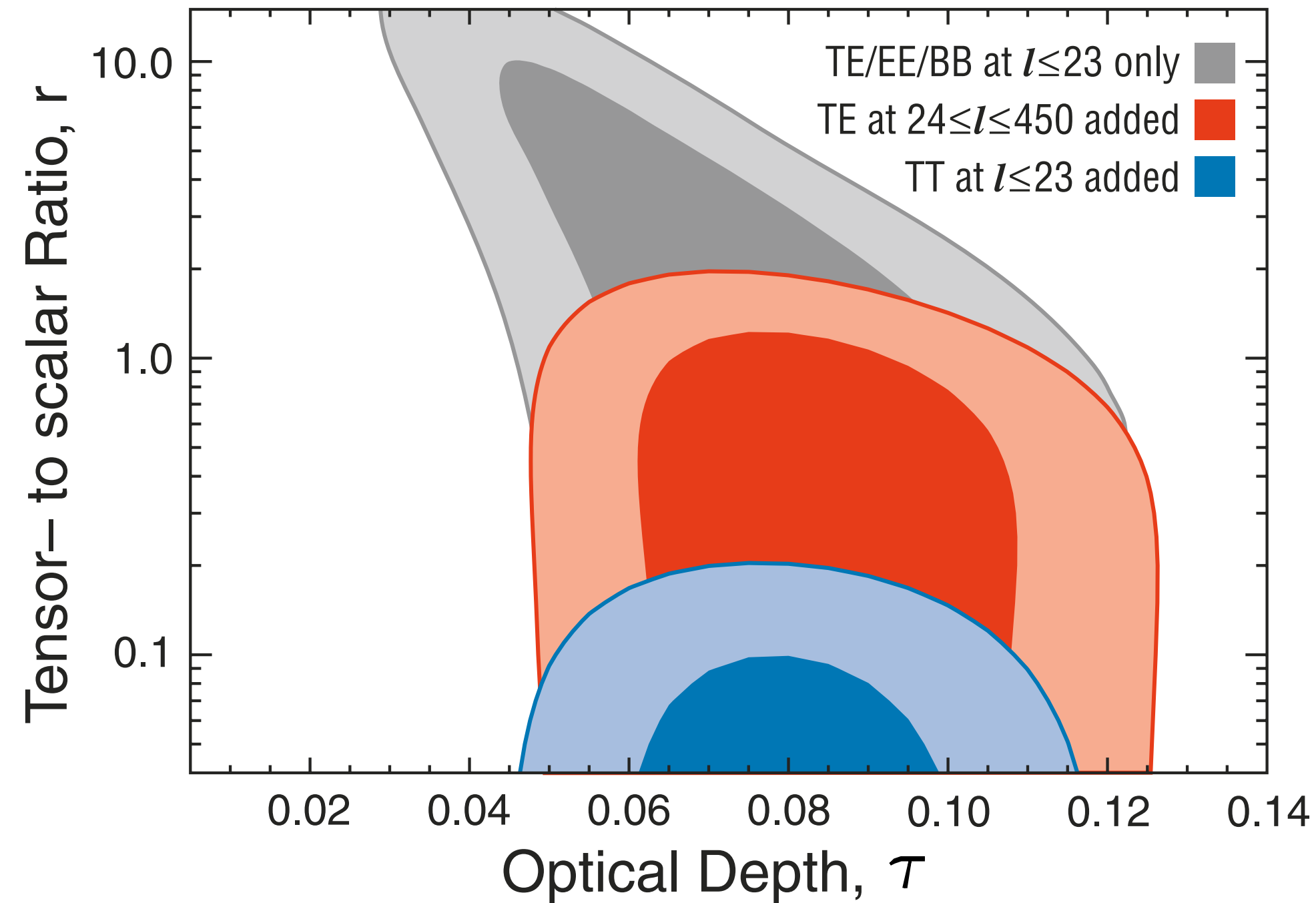
- No significant running index is observed.
 - WMAP-only: $dn_s/d\ln k = -0.037 \pm 0.028$
 - WMAP+BAO+SN: $dn_s/d\ln k = -0.032 (+0.021) (-0.020)$
- **A power-law spectrum is a good fit.**
- Note that $dn_s/d\ln k \sim O(0.001)$ is expected from simple inflation models (like $m^2\varphi^2$), but we are not there yet.

Check List #5: Gravitational Waves

- How do WMAP data constrain the amplitude of primordial gravitational waves?

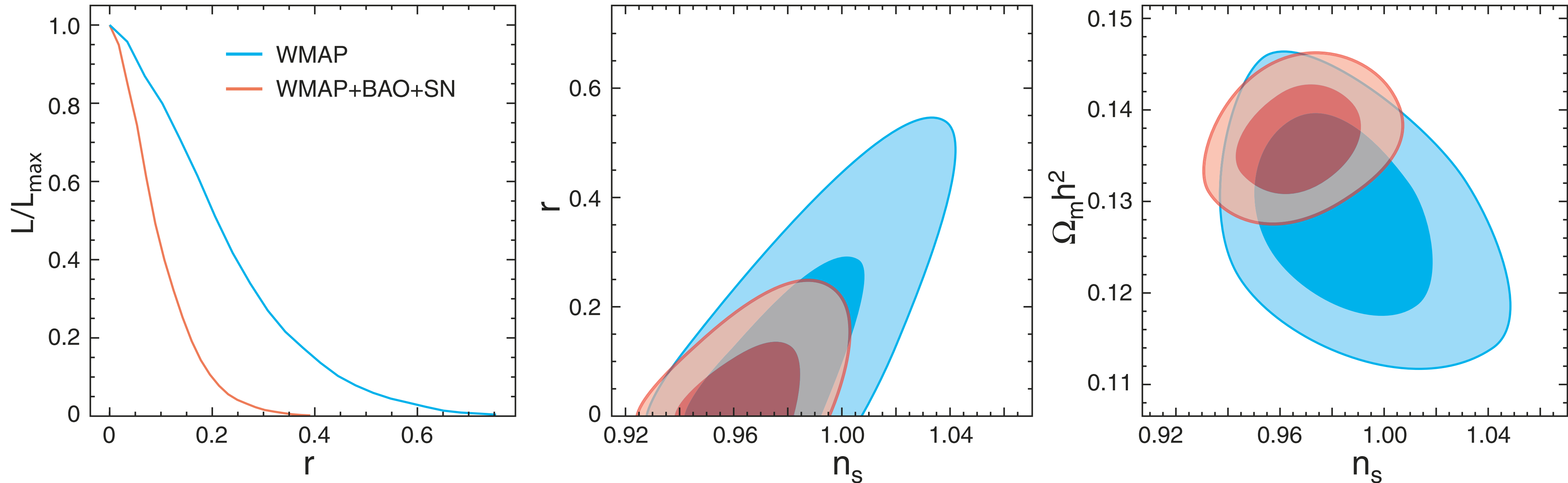
Pedagogical Explanation

Komatsu et al.



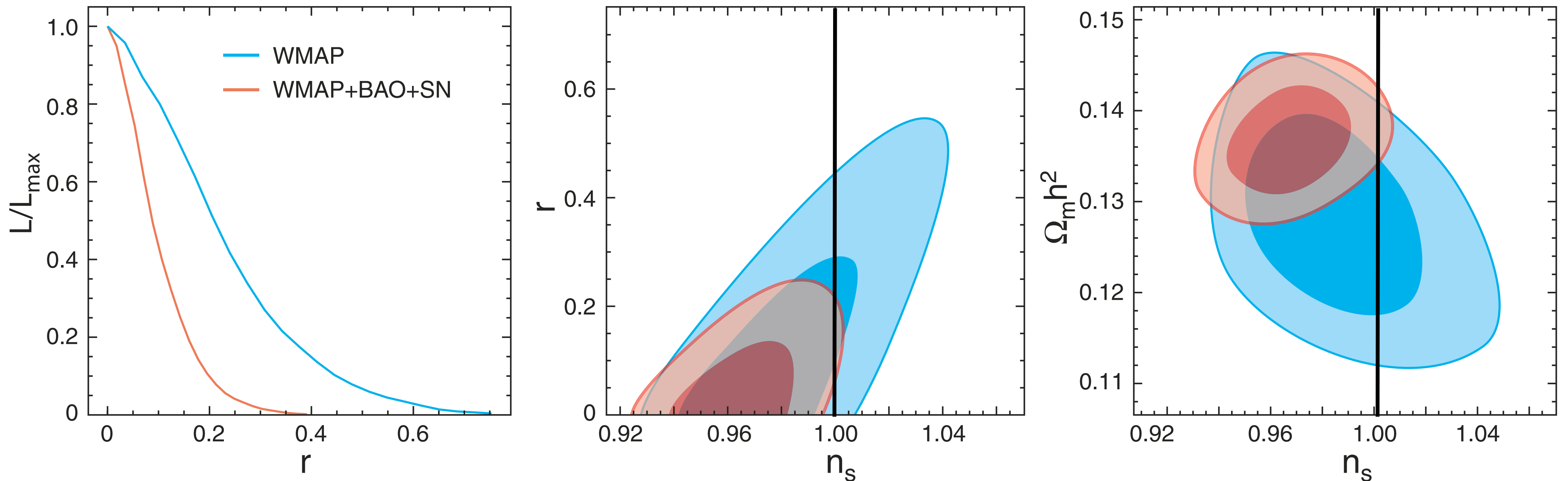
- If all the other parameters (n_s in particular) are fixed...
 - Low- l polarization gives $r < 20$ (95% CL)
 - + high- l polarization gives $r < 2$ (95% CL)
 - + low- l temperature gives $r < 0.2$ (95% CL)

Real Life: Killer Degeneracy



- Since the limit on r relies on the low- l temperature, it is strongly degenerate with n_s .
- The degeneracy can be broken partially by BAO&SN
- $r < 0.43$ (WMAP-only) \rightarrow **$r < 0.20$** (WMAP+BAO+SN)

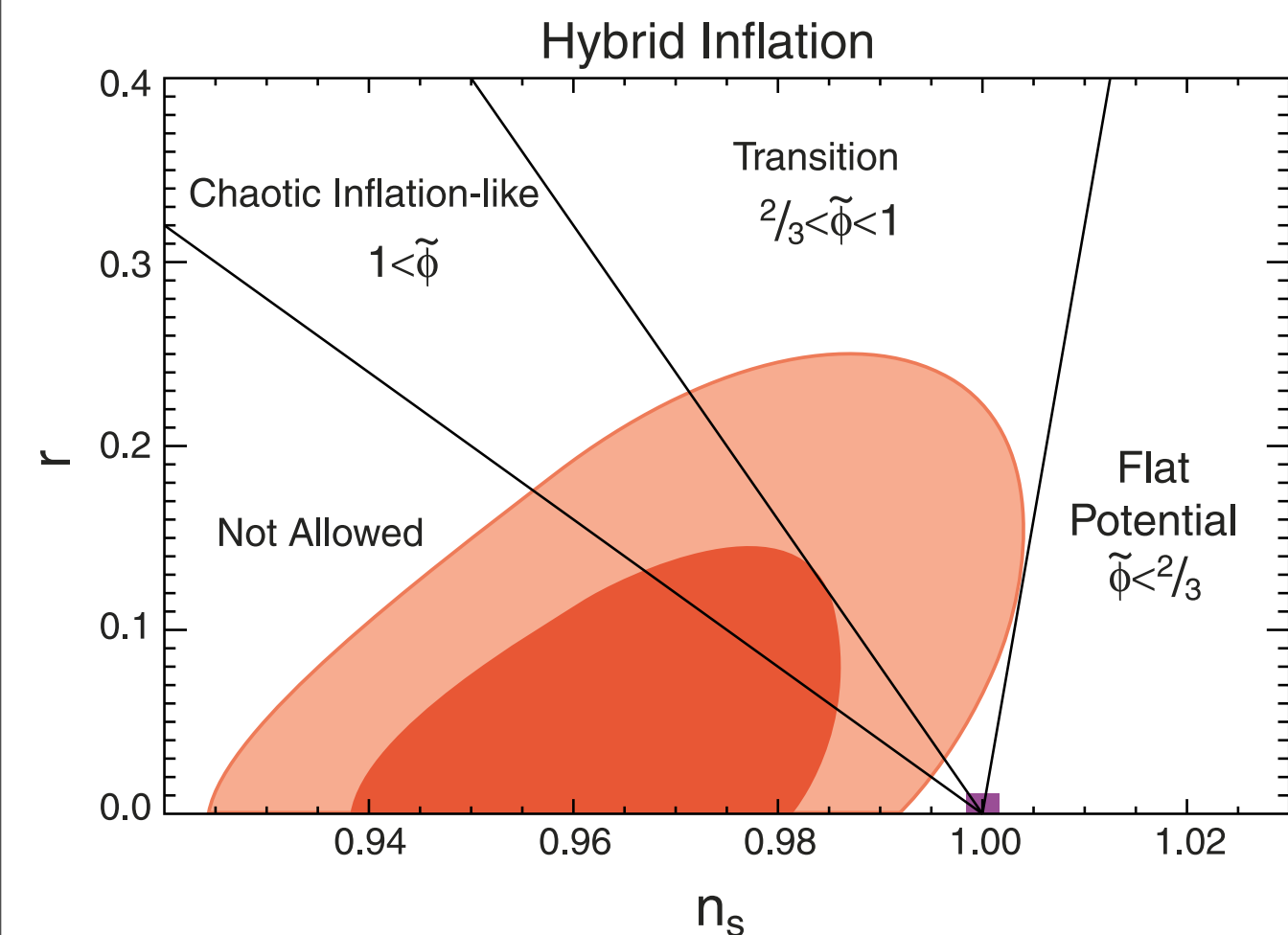
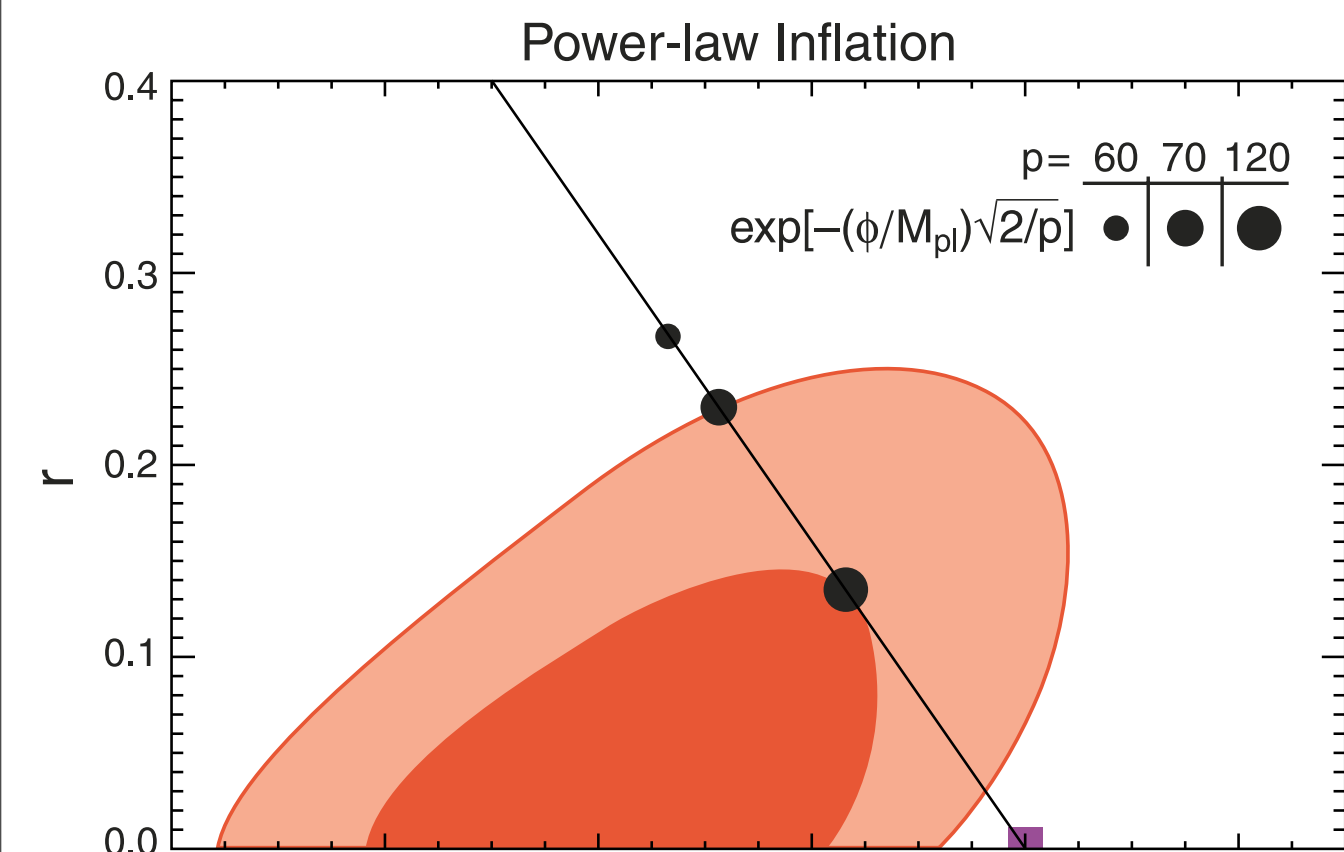
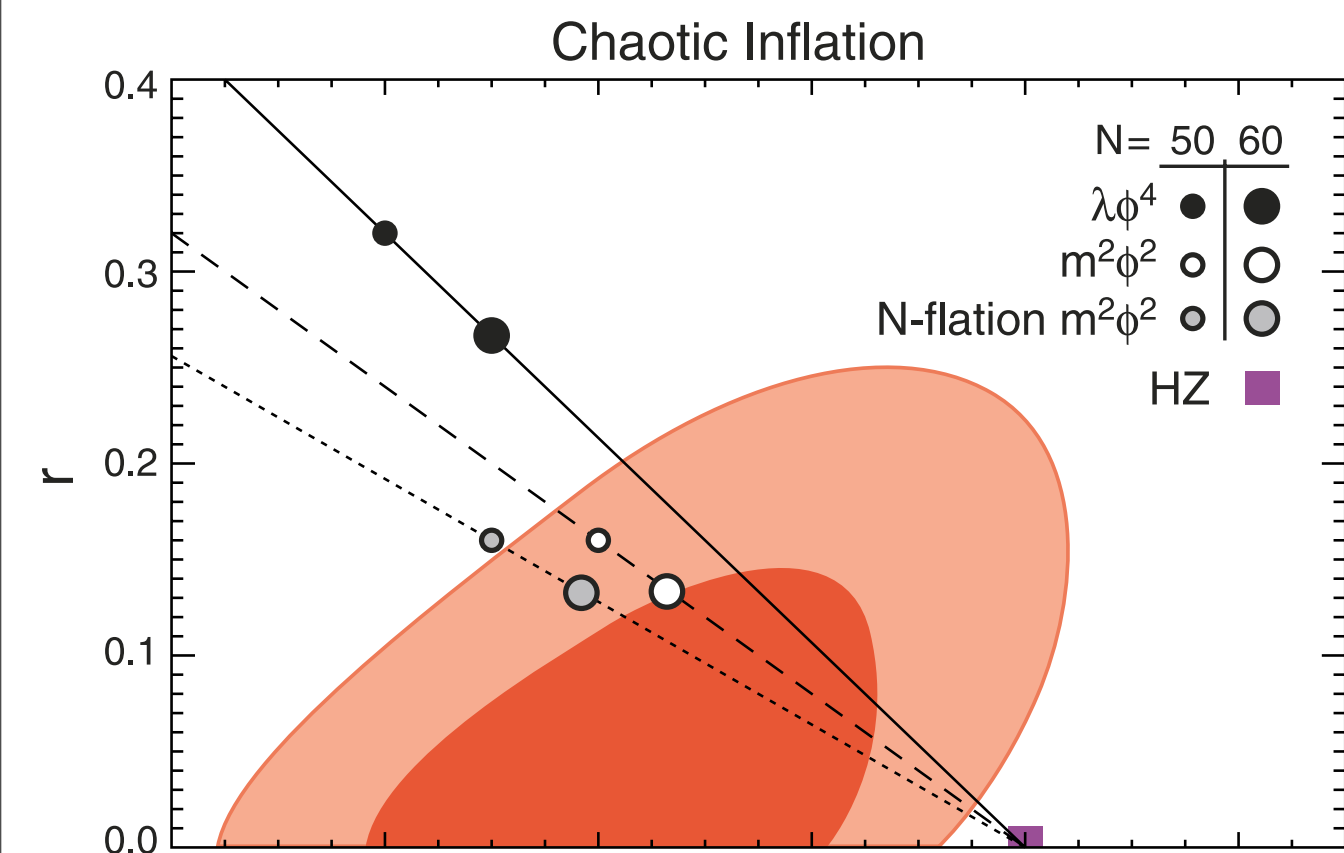
$n_s > 1.0$ is Disfavored, Regardless of r



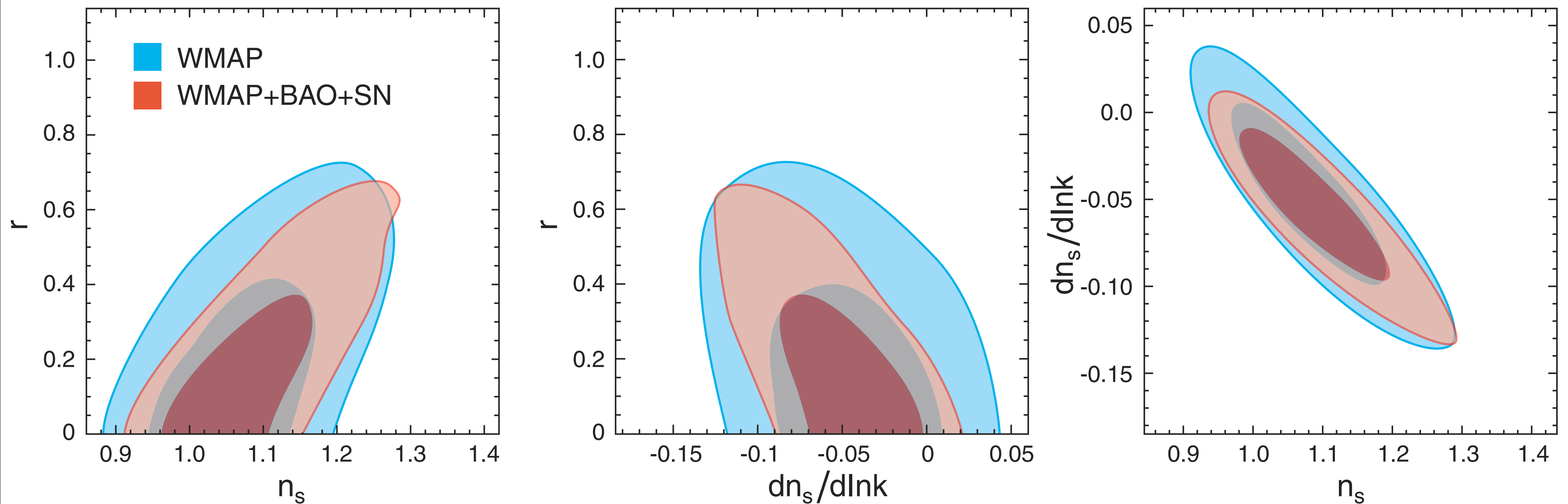
- The maximum n_s we find at 95% CL is **$n_s = 1.005$ for $r = 0.16$.**

Lowering a “Limbo Bar”

- $\lambda\varphi^4$ is totally out. (unless you invoke, e.g., non-minimal coupling, to suppress r ..)
- $m^2\varphi^2$ is within 95% CL.
 - Future WMAP data would be able to push it to outside of 95% CL, if $m^2\varphi^2$ is not the right model.
- N-flation $m^2\varphi^2$ (Easter&McAllister) is being pushed out
- PL inflation [$a(t)\sim t^p$] with $p<60$ is out.
- A blue index ($n_s>1$) region of hybrid inflation is disfavored



How About Putting Everything (n_s , r , $dn_s/d\ln k$) In?



- Then of course, constraints are weakened.. BAO&SN do not help much anymore.

Your Score Card?

- **Flatness:** $-0.0175 < \Omega_k < 0.0085$ (not assuming $w=-1$!)
- **Non-adiabaticity:** $<8.6\%$ (axion DM); $<2.0\%$ (curvaton DM)
- **Non-Gaussianity:** $-9 < \text{Local} < 111$; $-151 < \text{Equilateral} < 253$
- **Tilt** (for $r=0$): $n_s=0.960 (+0.014) (-0.013)$ [68% CL]
- **Running** (for $r=0$): $-0.0728 < dn_s/d\ln k < 0.0087$
- **Gravitational waves:** $r < 0.20$
 - $n_s=0.968 (+/- 0.015)$ [68% CL]
 - $n_s > 1$ disfavored at 95% CL

Looking Ahead...

- With more WMAP observations, exciting discoveries may be waiting for us. Two examples for which we might be seeing some hints from the 5-year data:
 - Non-Gaussianity: If $f_{\text{NL}} \sim 60$, we will see it at the 3 sigma level with 9 years of data.
 - Gravitational waves (r) and tilt (n_s) : $m^2\phi^2$ can be pushed out of the favorable parameter region
 - $n_s > 1$ will probably be ruled out regardless of r .

What else is there in the Interpretation Paper

- Not just inflation...
- Fun stuff about dark energy
 - User-friendly “WMAP distance priors”
- Cosmic parity violation (upper limits, of course)
 - Scientific use of the TB and EB correlations
 - Now implemented in the delivered likelihood code
- Neutrinos!