



# The 5-Year Wilkinson Microwave Anisotropy Probe (*WMAP*) Observations: Cosmological Interpretation

**Eiichiro Komatsu** (Texas Cosmology Center, UT Austin)  
Particle Physics Seminar, BNL, March 11, 2009

# Texas Cosmology Center (TCC)

## The University of Texas Austin

- The new Cosmology Center, founded in January 2009, at the University of Texas at Austin!
- [www.tcc.utexas.edu](http://www.tcc.utexas.edu)

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#### *Astronomy*

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Karl Gebhardt  
Gary Hill  
Eiichiro Komatsu (Director)  
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Paul Shapiro

#### *Physics*

Duane Dicus  
Jacques Distler  
Willy Fischler  
Vadim Kaplunovsky  
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Steven Weinberg

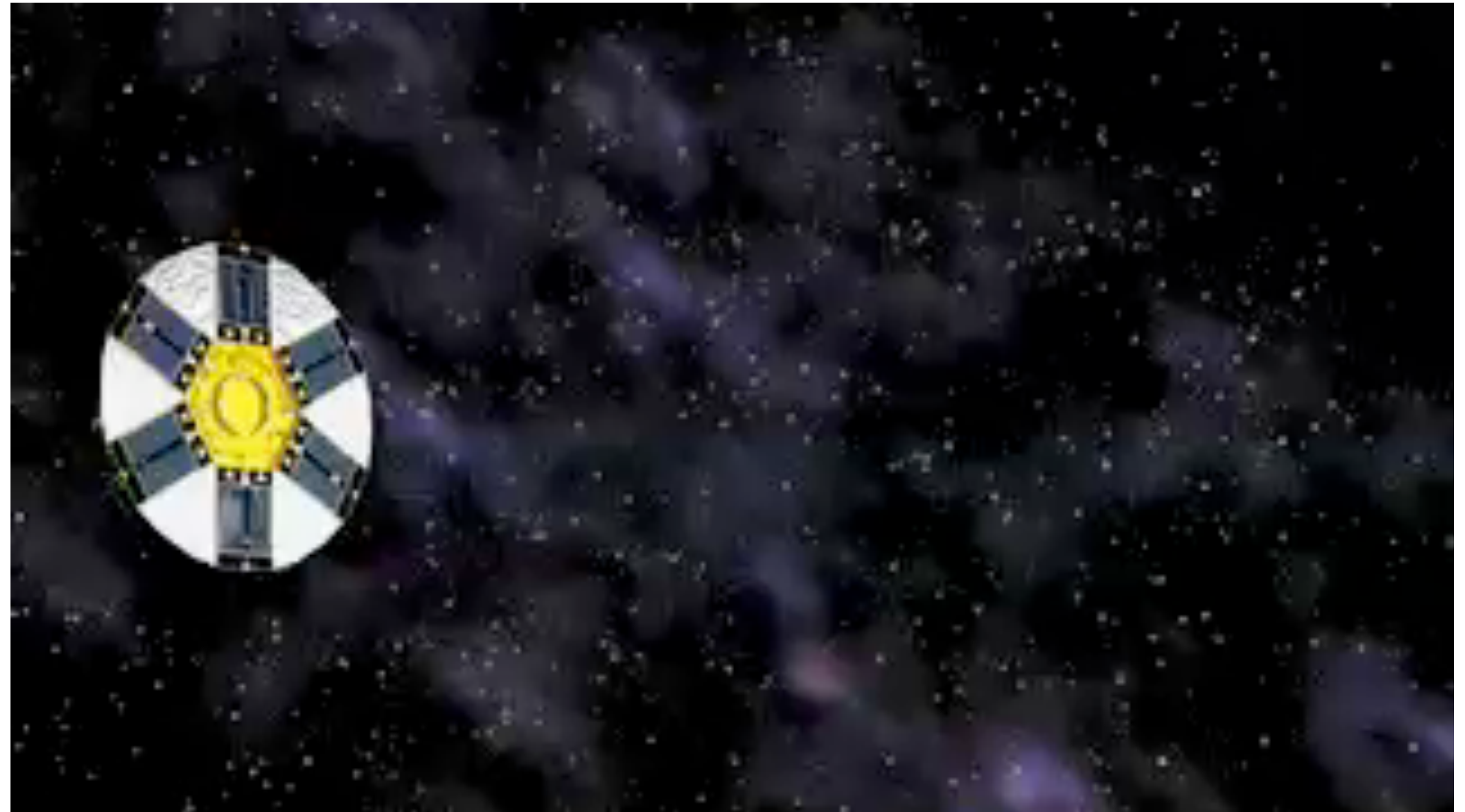
# WMAP at Lagrange 2 (L2) Point

June 2001:  
WMAP launched!

February 2003:  
The first-year data  
release

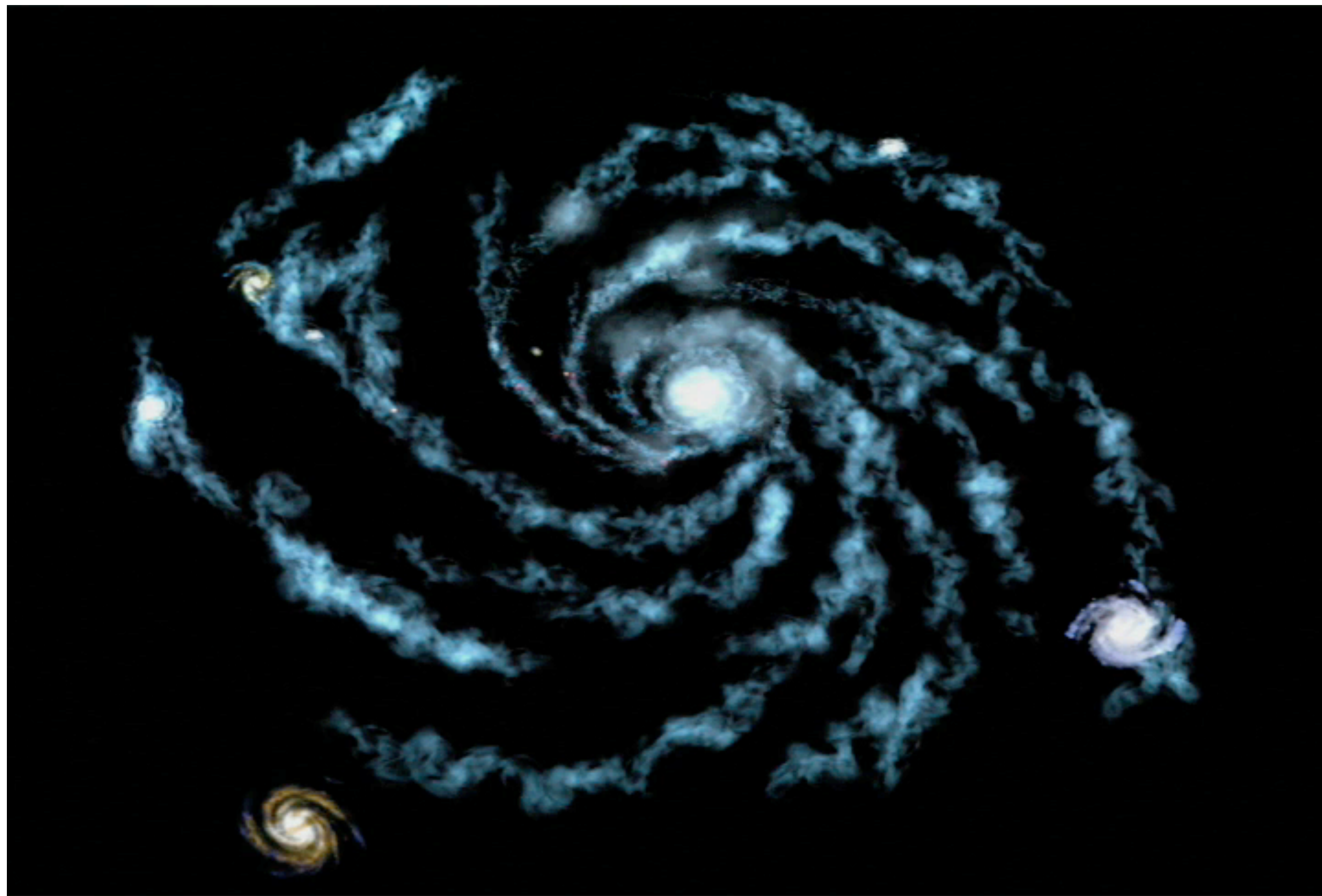
March 2006:  
The three-year data  
release

**March 2008:  
The five-year  
data release**



- L2 is a million miles from Earth
- WMAP leaves Earth, Moon, and Sun behind it to avoid radiation from them

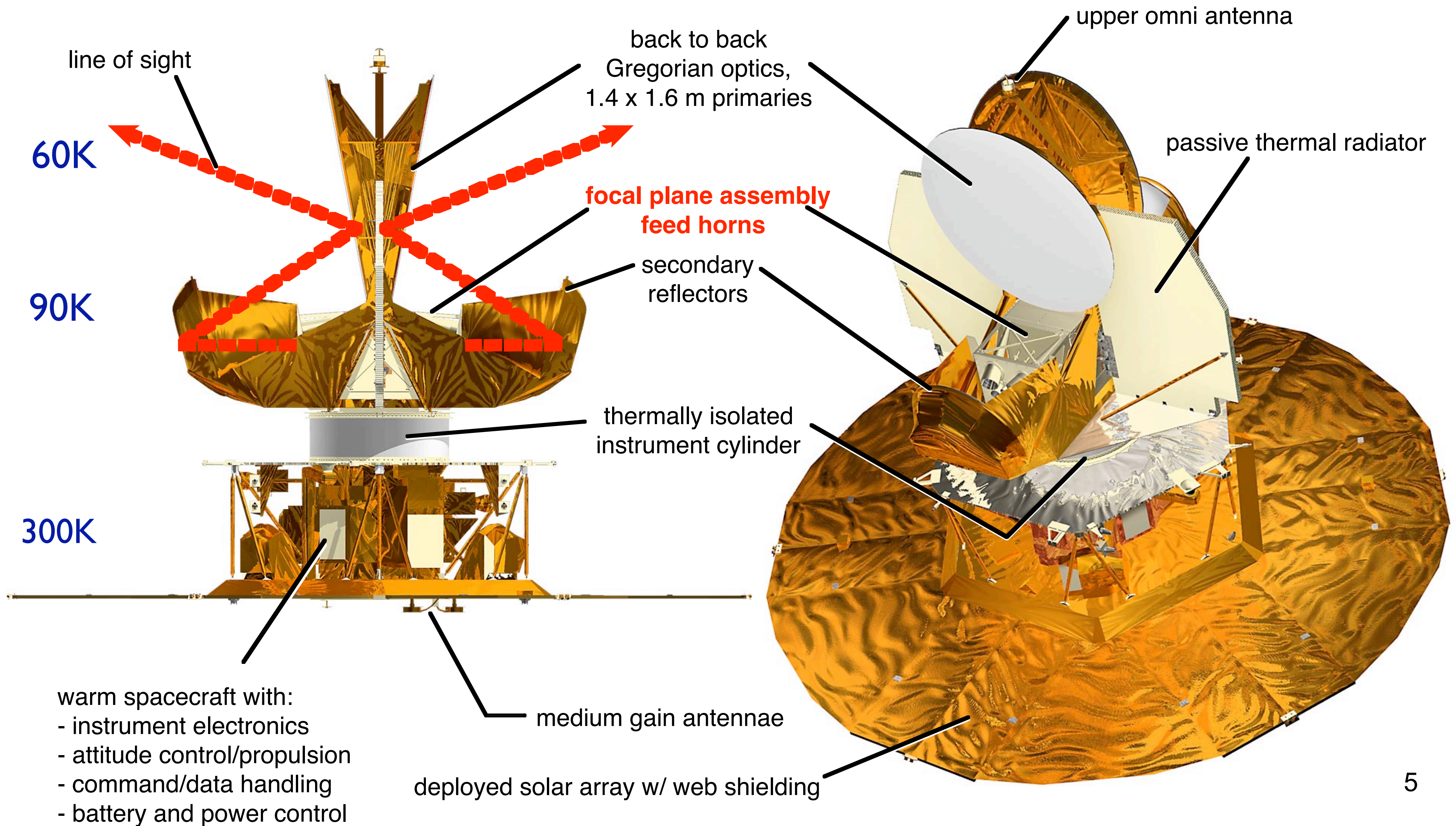
# WMAP Measures Microwaves From the Universe



- The mean temperature of photons in the Universe today is 2.725 K
- WMAP is capable of measuring the temperature *contrast* down to better than **one part in millionth**<sup>4</sup>

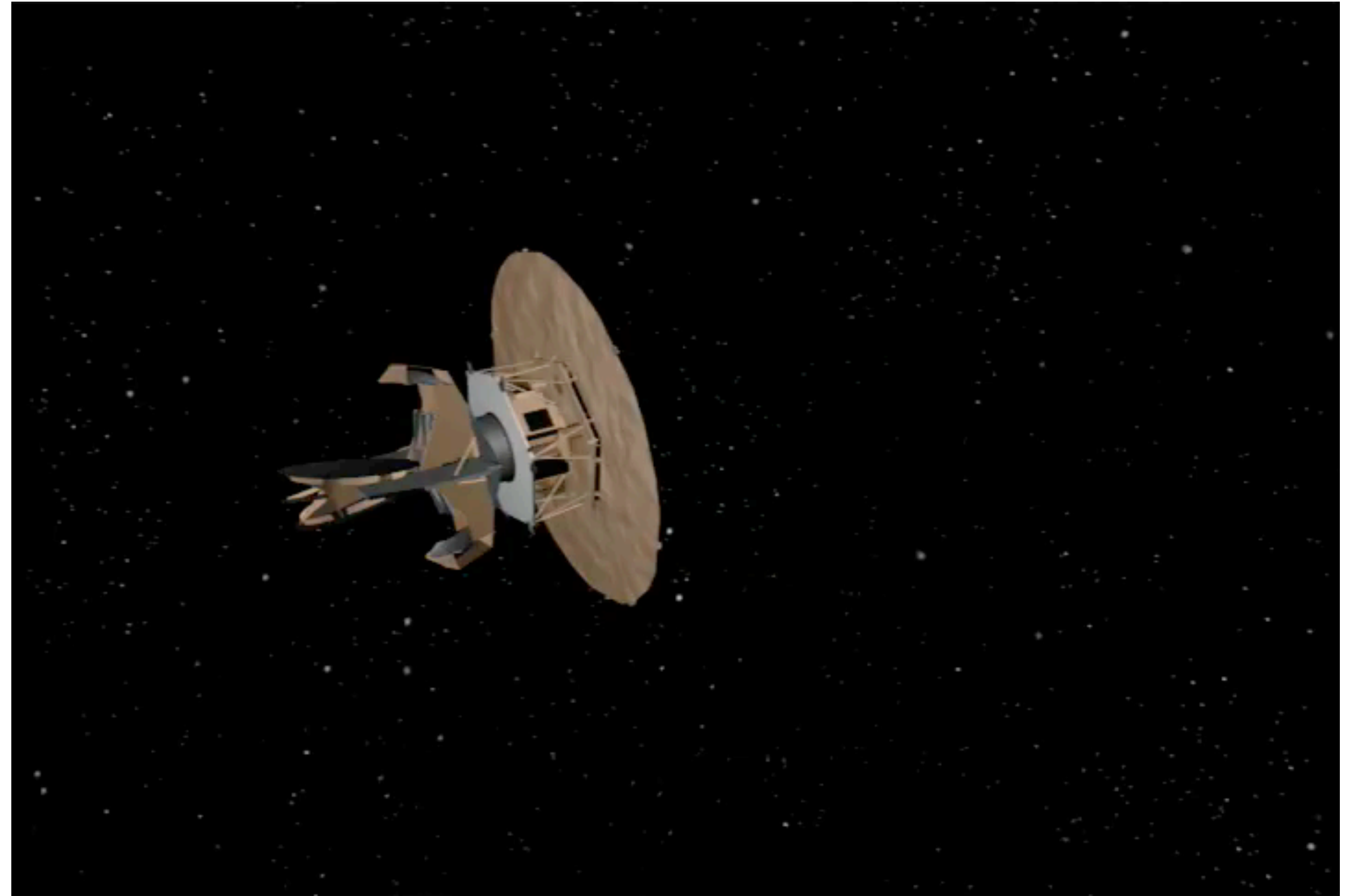
# WMAP Spacecraft

## Radiative Cooling: No Cryogenic System

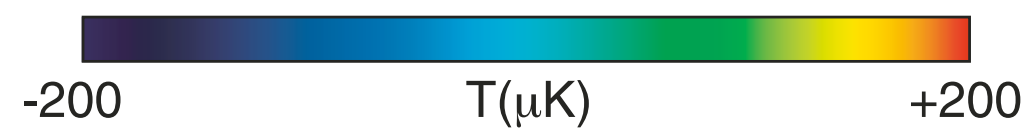
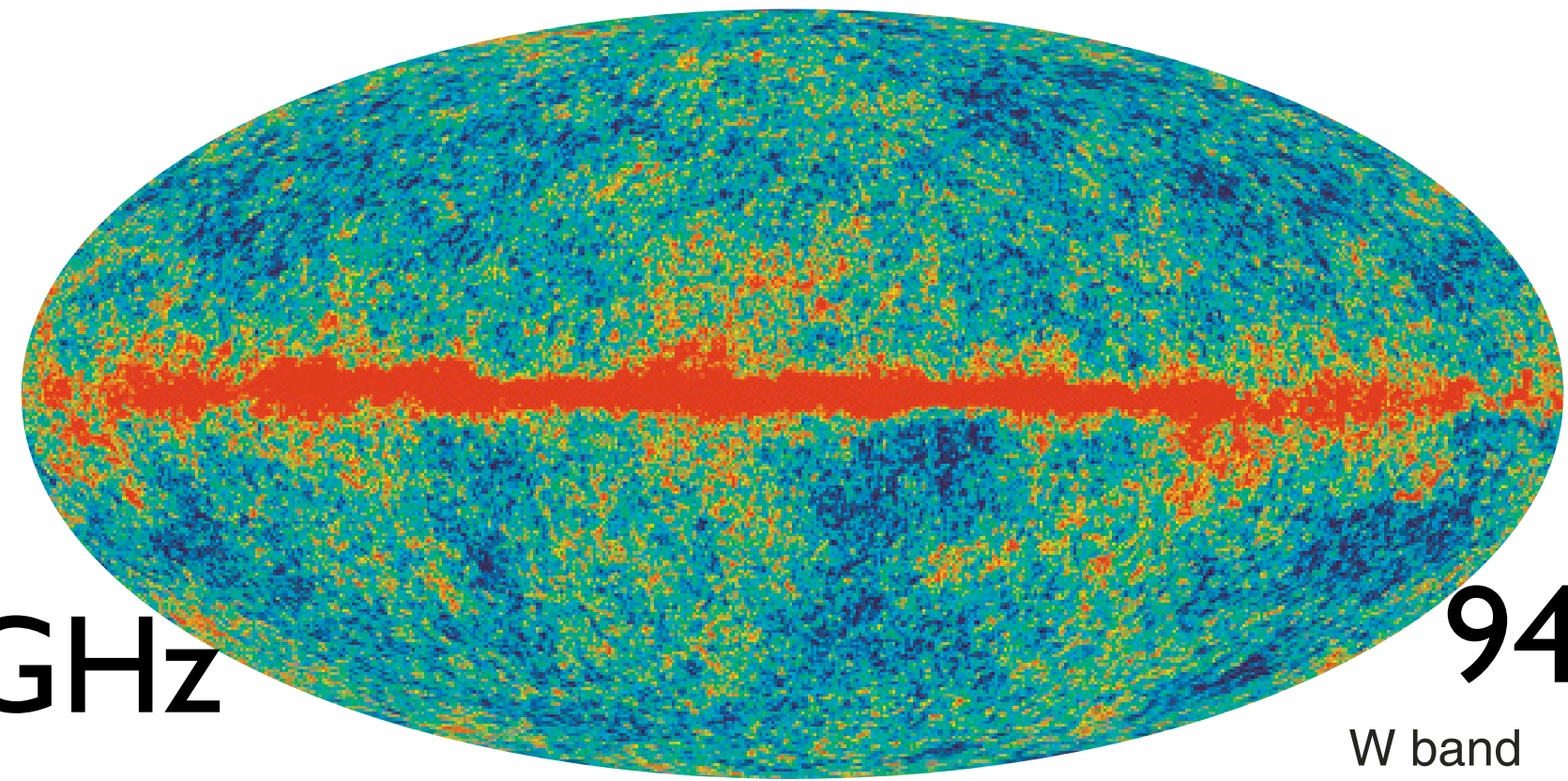
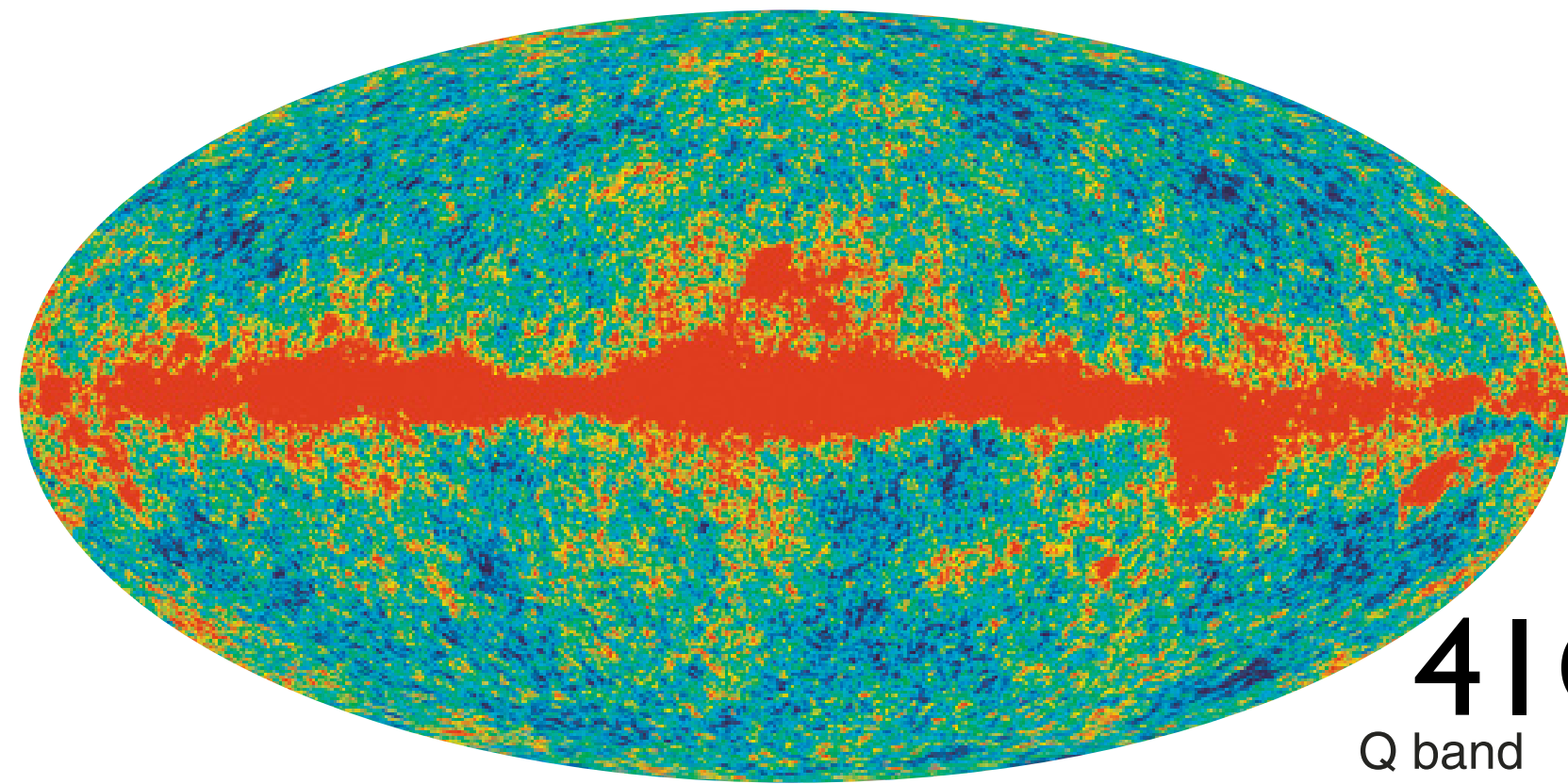
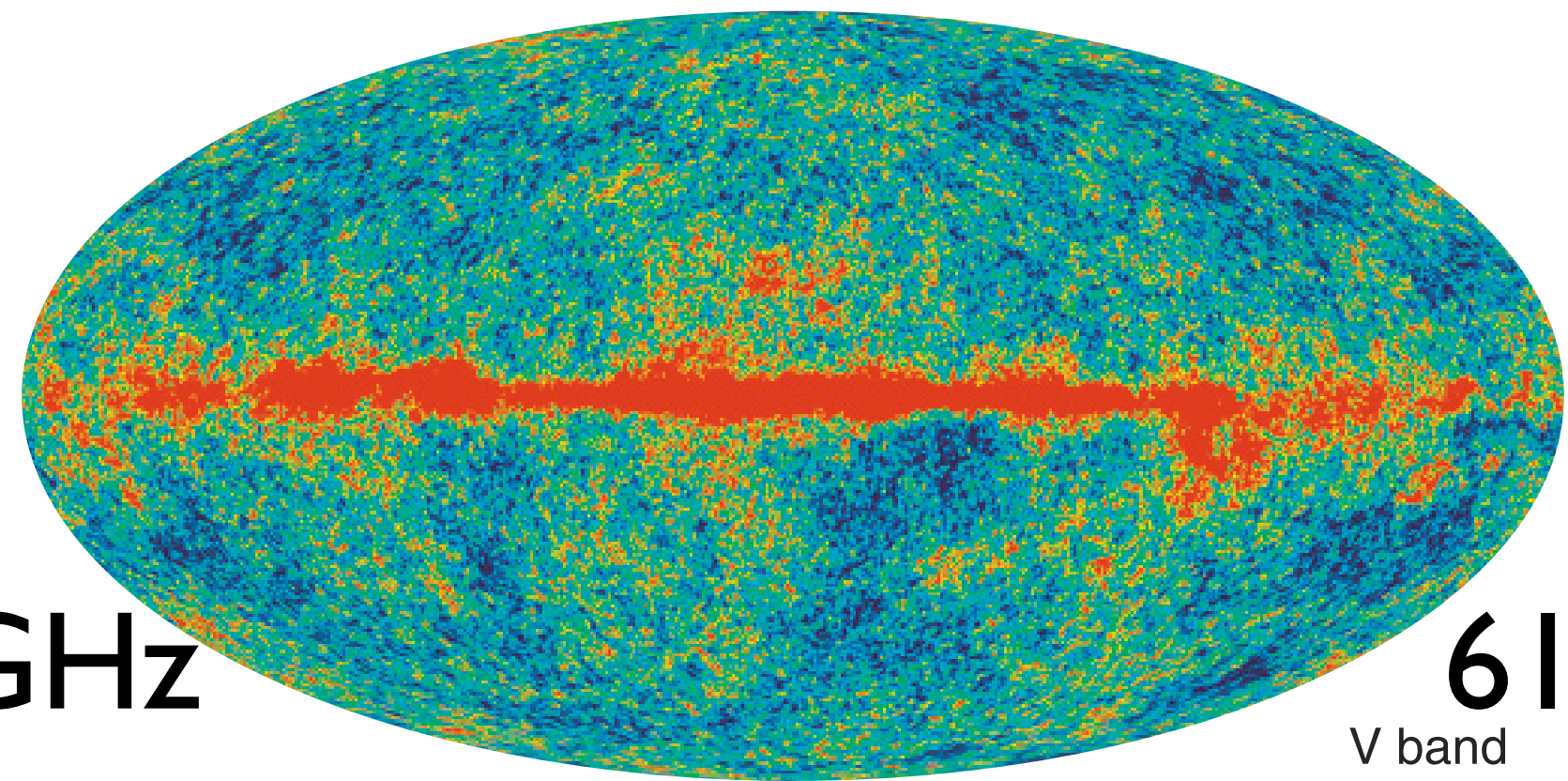
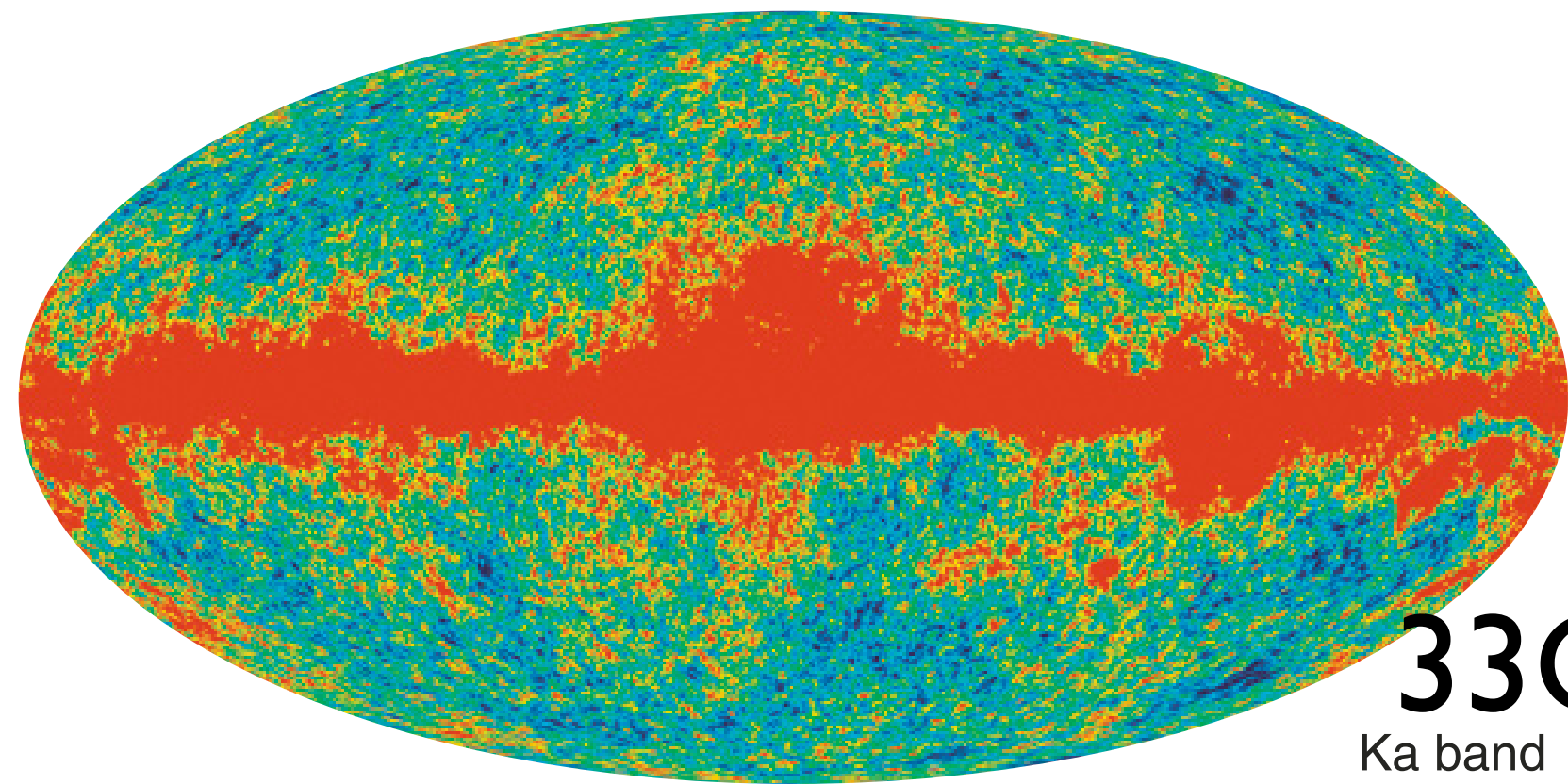
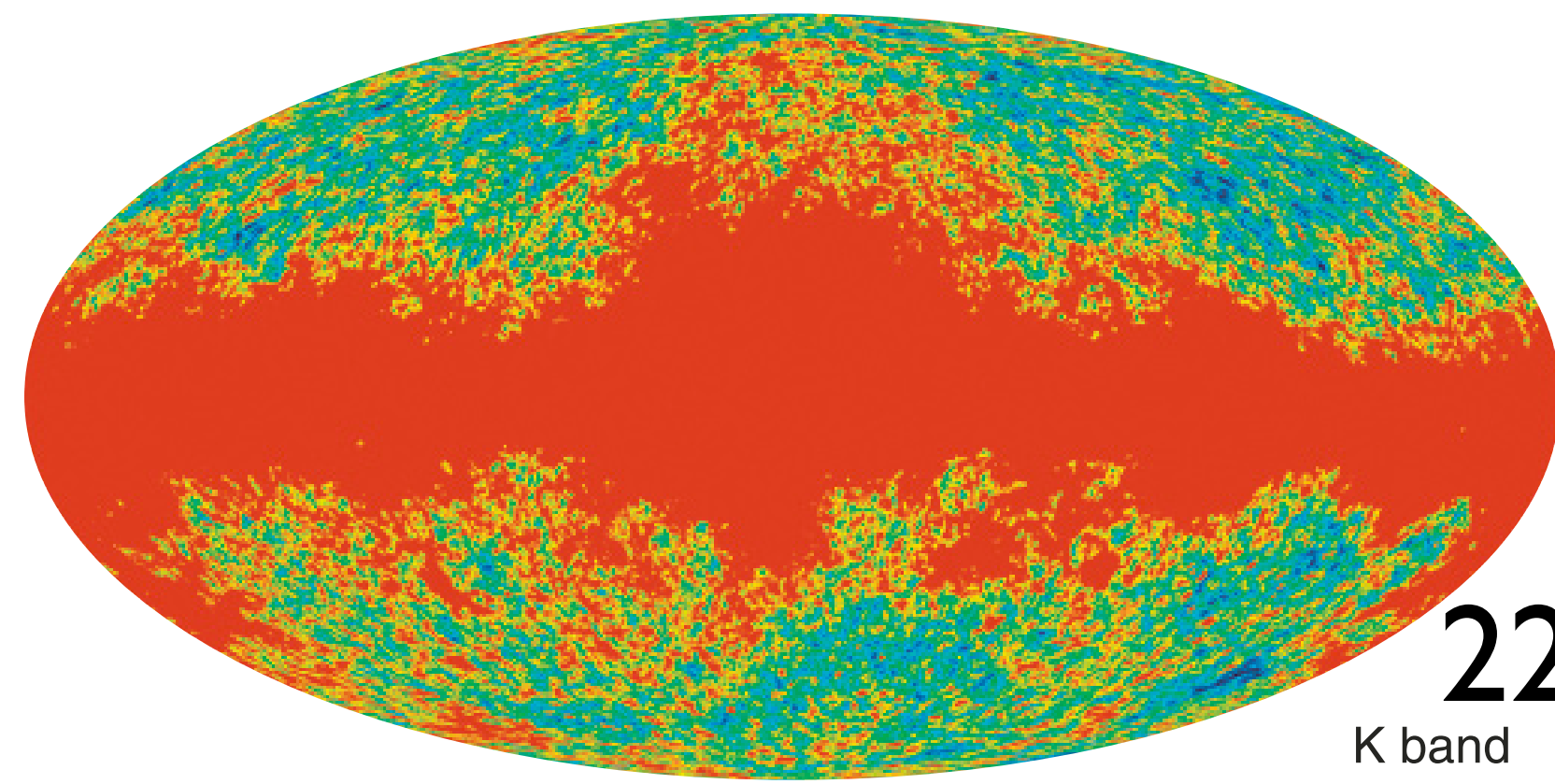


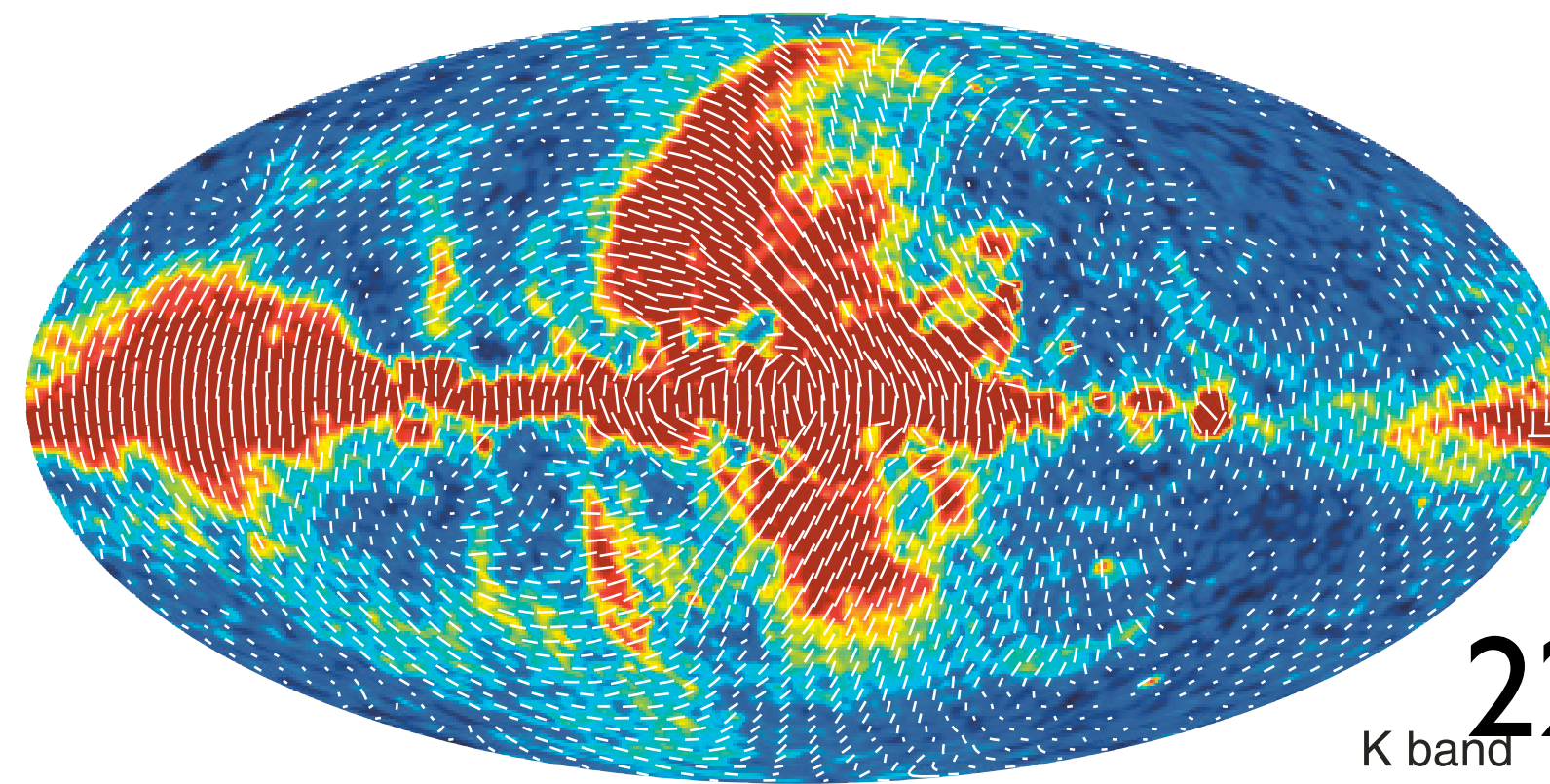
# Journey Backwards in Time

- The Cosmic Microwave Background (**CMB**) is *the fossil light from the Big Bang*
- This is the oldest light that one can ever hope to measure
- CMB is a direct image of the Universe when the Universe was only 380,000 years old

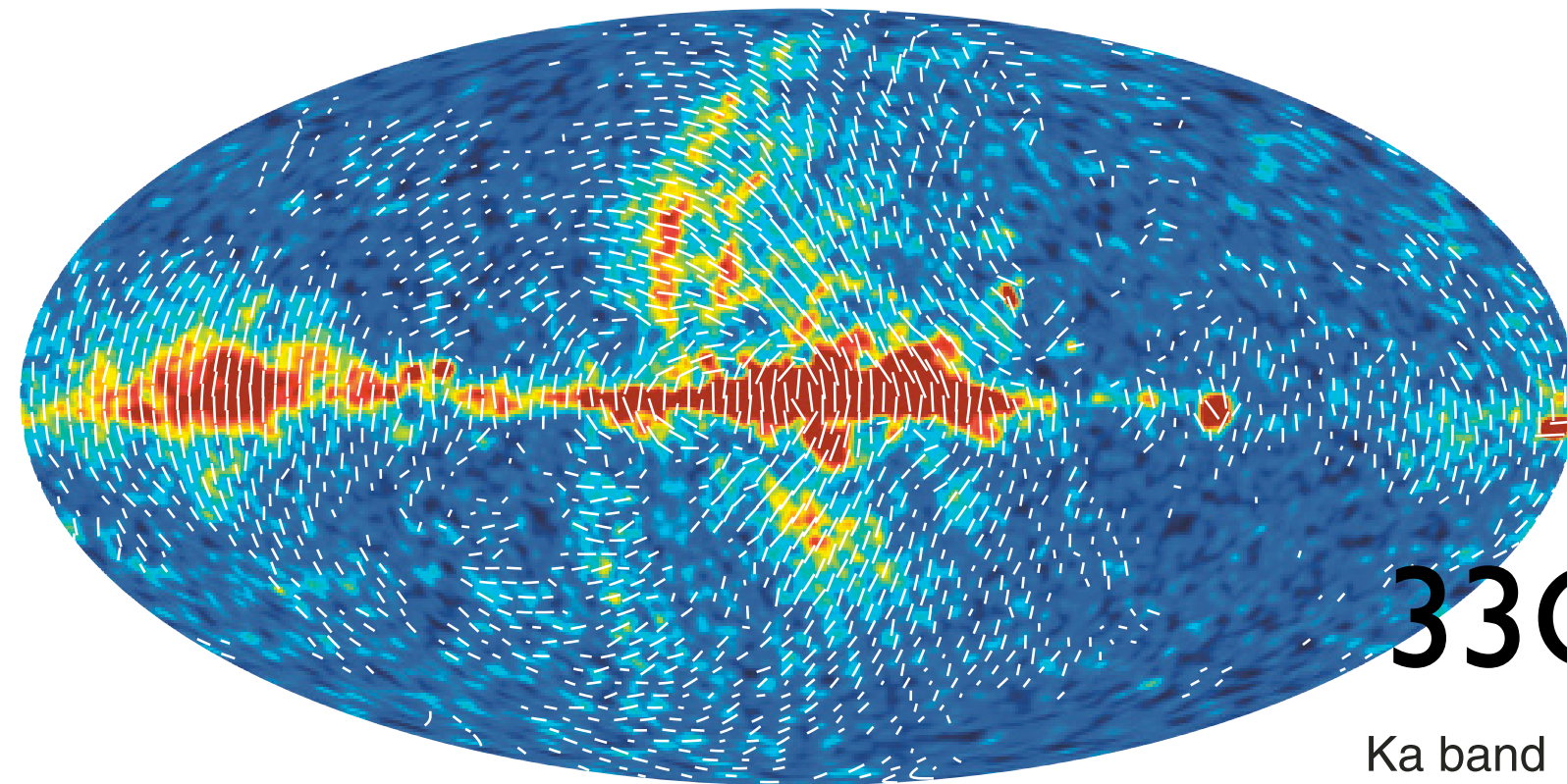
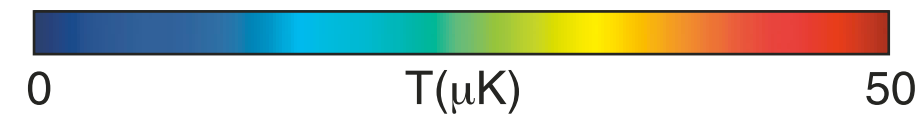


- CMB photons, after released from the cosmic plasma “soup,” traveled for **13.7 billion years** to reach us.
- CMB collects information about the Universe as it travels through it.

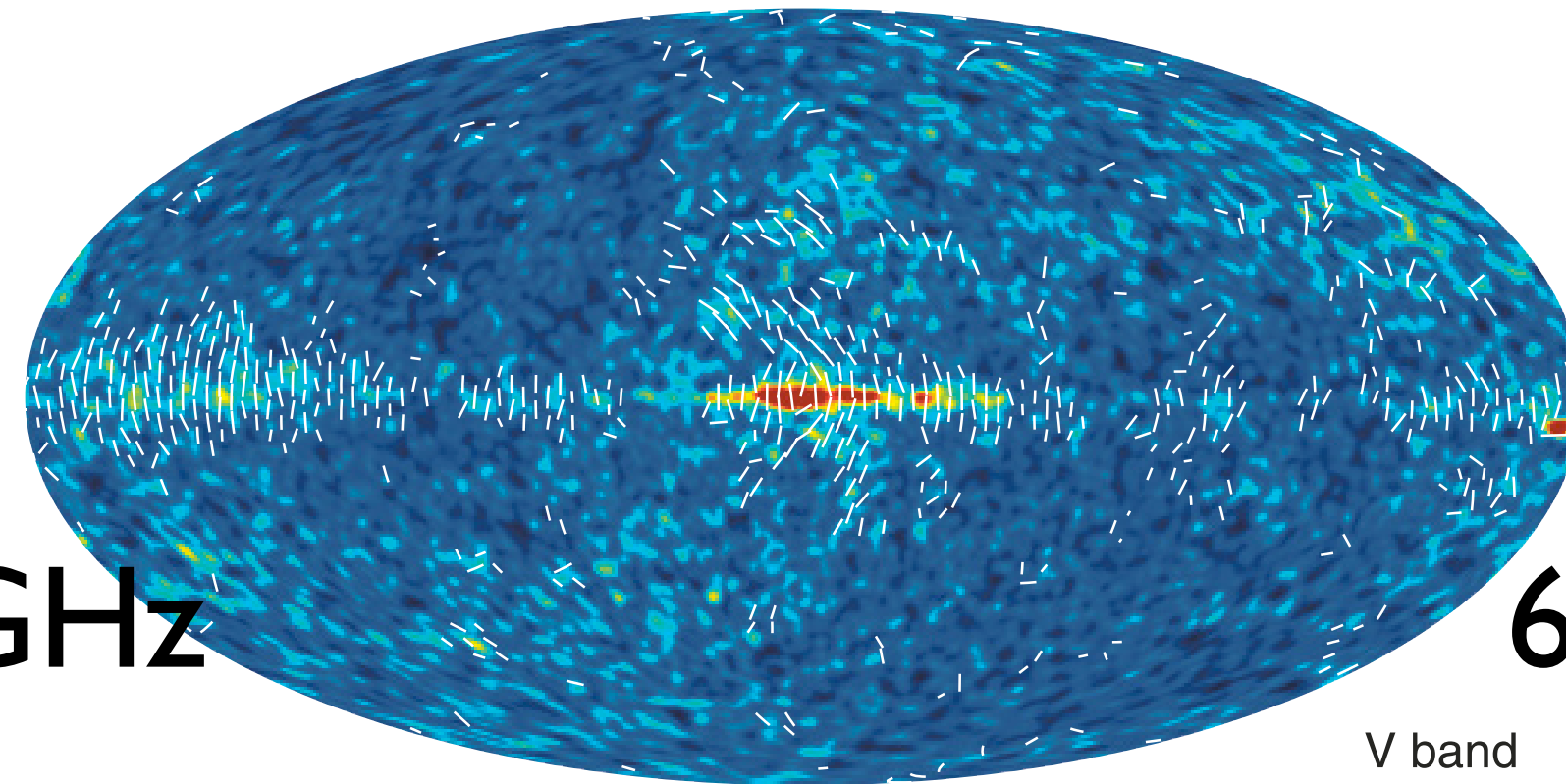




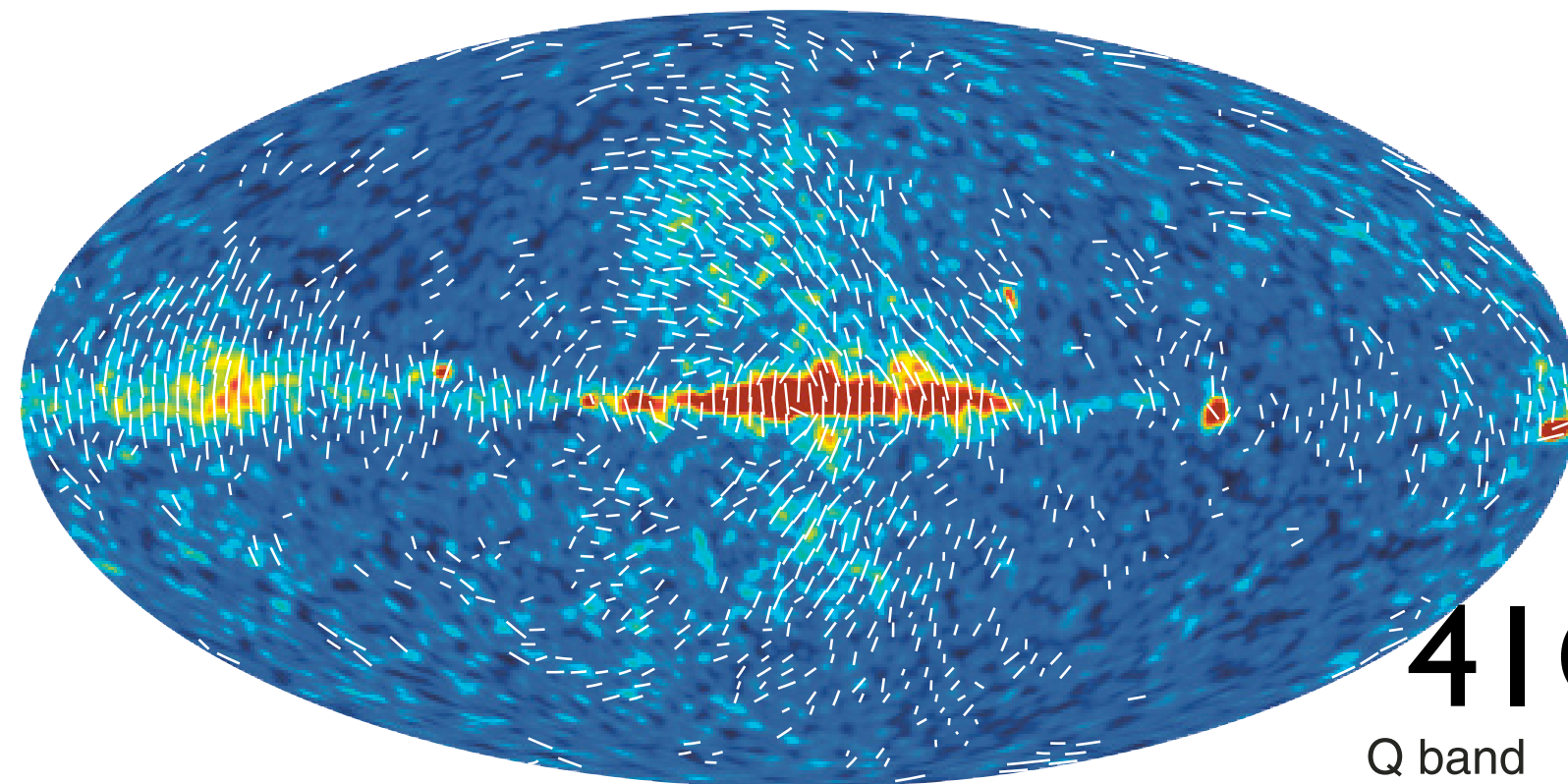
**22GHz**  
K band



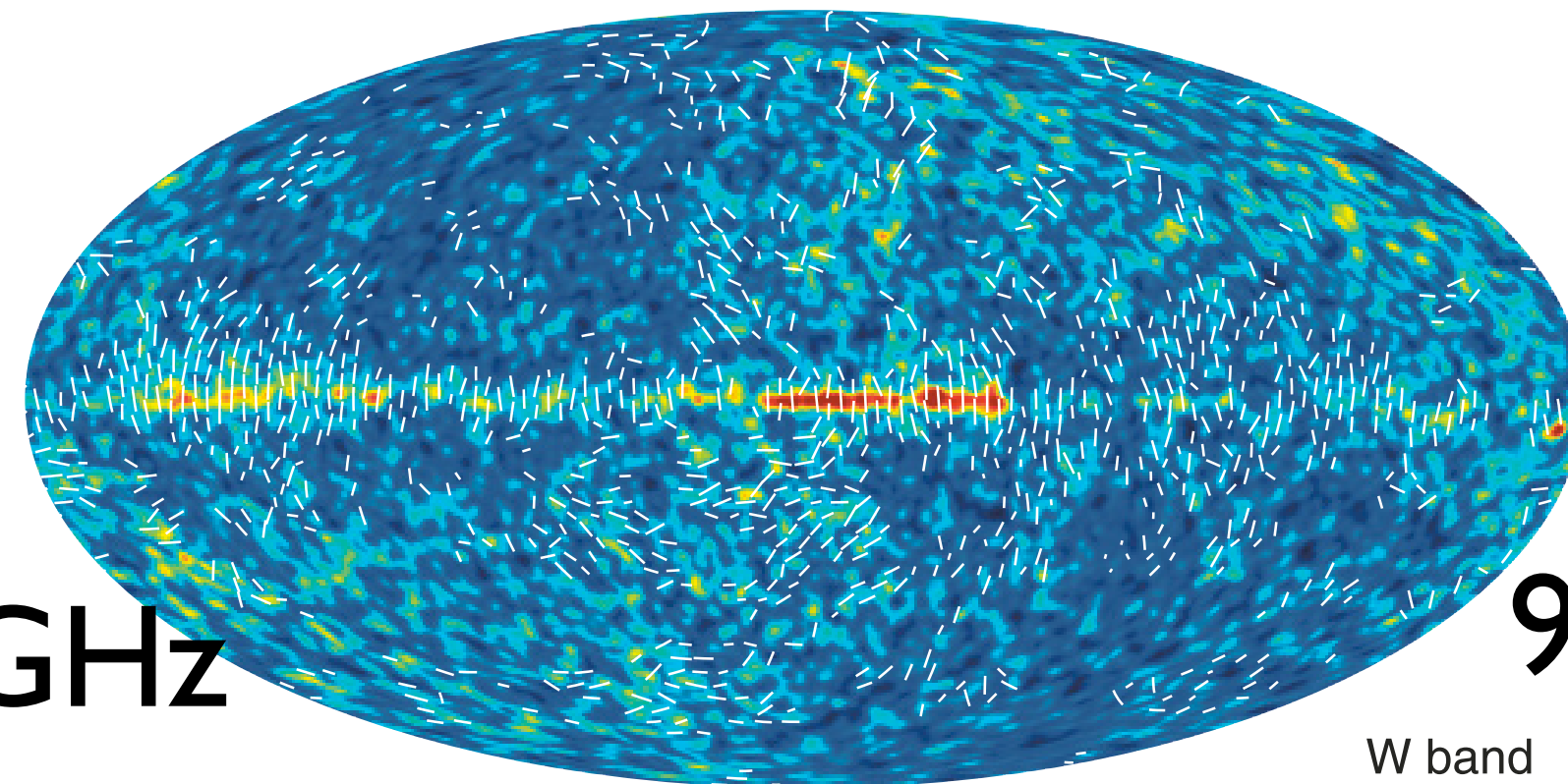
**33GHz**  
Ka band



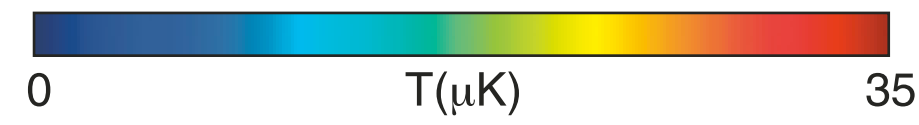
**61GHz**  
V band



**41GHz**  
Q band



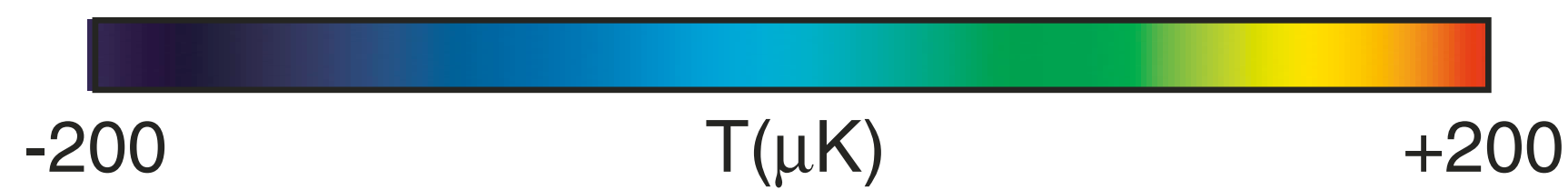
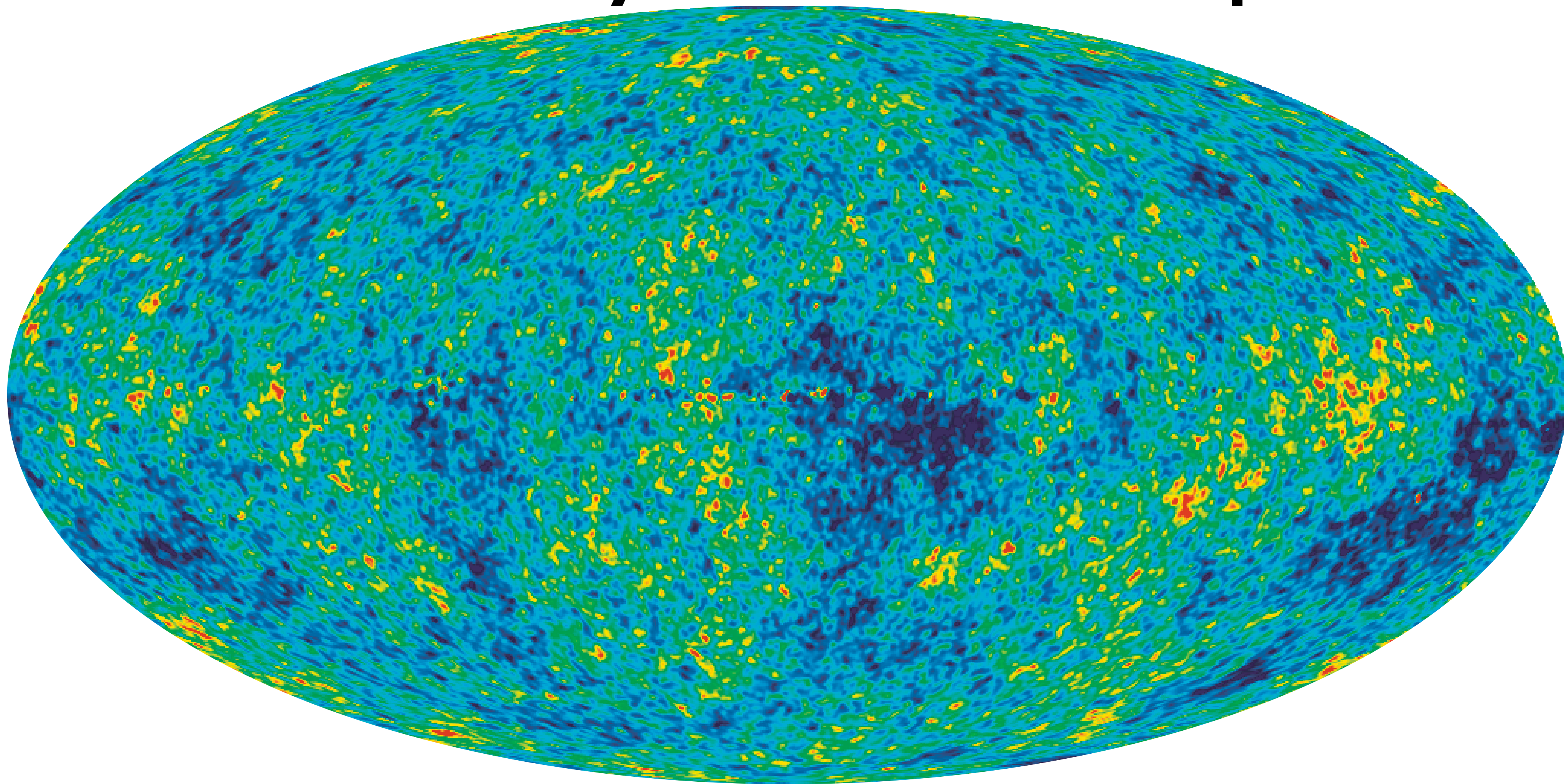
**94GHz**  
W band





# Galaxy-cleaned Map

*Hinshaw et al.*



WMAP 5-year

# WMAP 5-Year Papers

- **Hinshaw et al.**, “*Data Processing, Sky Maps, and Basic Results*” [ApJS, 180, 225 \(2009\)](#)
- **Hill et al.**, “*Beam Maps and Window Functions*” [ApJS, 180, 246](#)
- **Gold et al.**, “*Galactic Foreground Emission*” [ApJS, 180, 265](#)
- **Wright et al.**, “*Source Catalogue*” [ApJS, 180, 283](#)
- **Nolta et al.**, “*Angular Power Spectra*” [ApJS, 180, 296](#)
- **Dunkley et al.**, “*Likelihoods and Parameters from the WMAP data*” [ApJS, 180, 306](#)
- **Komatsu et al.**, “*Cosmological Interpretation*” [ApJS, 180, 330](#)<sub>10</sub>

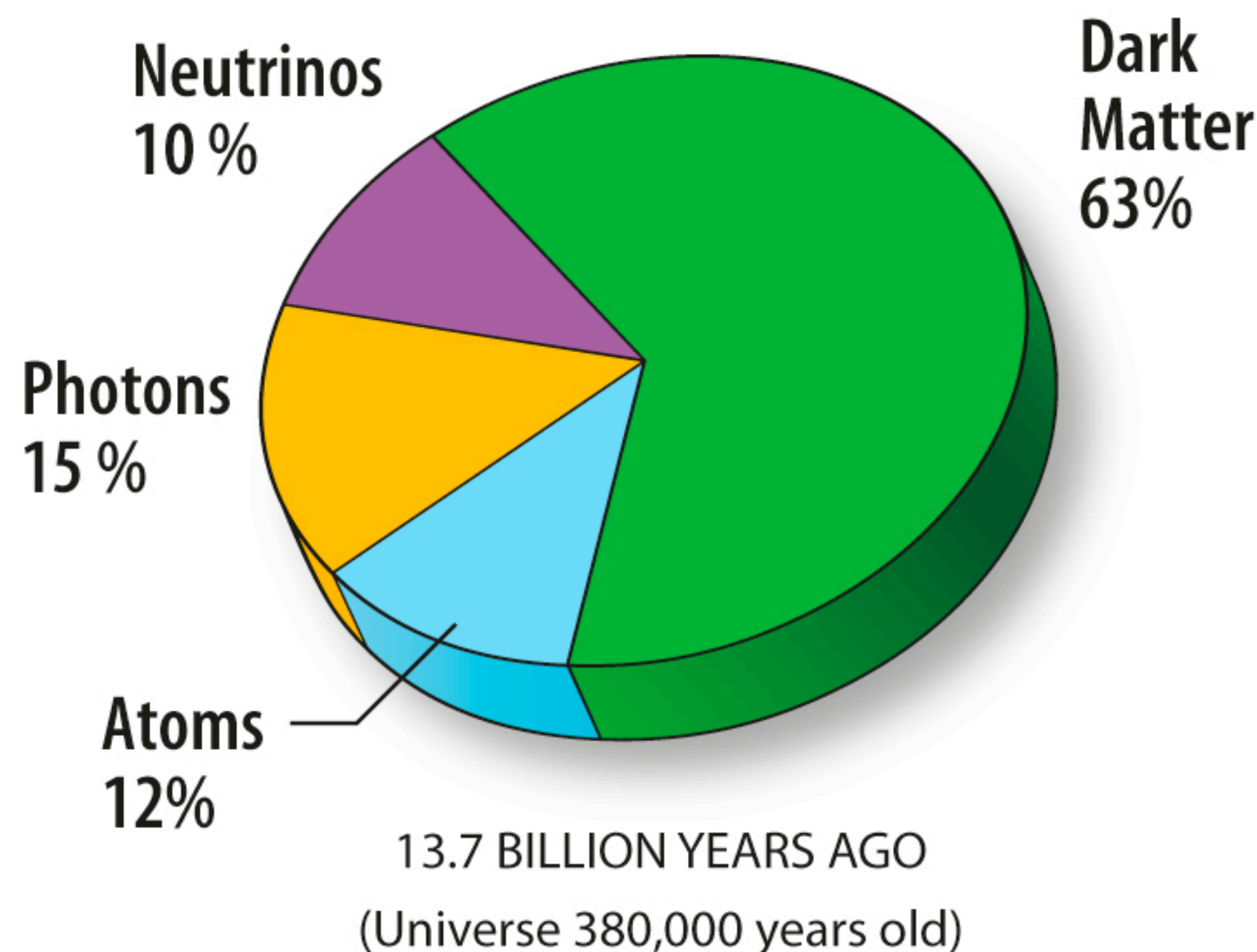
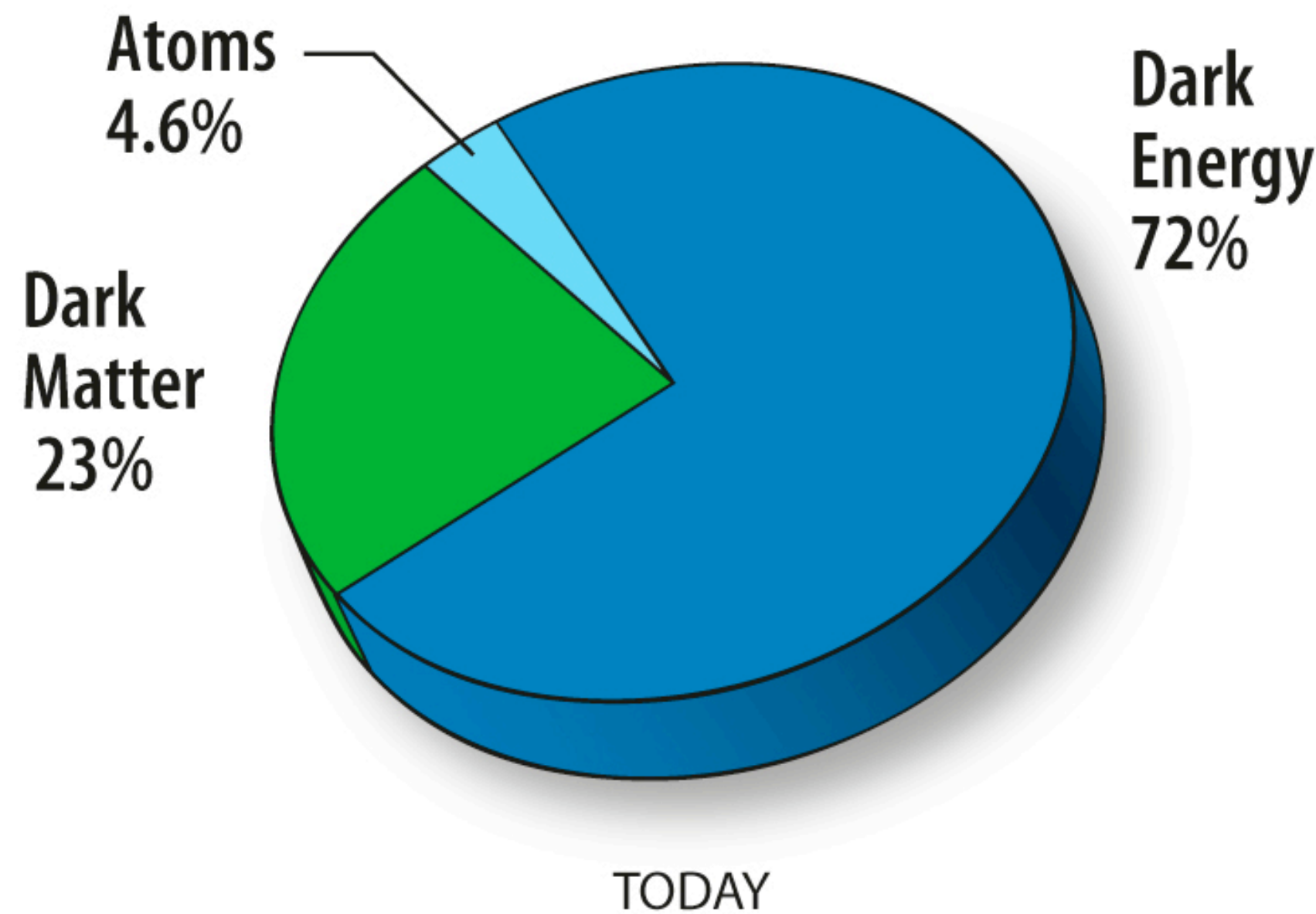
# WMAP 5-Year Science Team

- C.L. Bennett
- G. Hinshaw
- N. Jarosik
- S.S. Meyer
- L. Page
- D.N. Spergel
- E.L. Wright
- M.R. Greason
- M. Halpern
- R.S. Hill
- A. Kogut
- M. Limon
- N. Odegard
- G.S. Tucker
- J. L. Weiland
- E. Wollack
- J. Dunkley
- B. Gold
- E. Komatsu
- D. Larson
- M.R.olta

Special  
Thanks to  
**WMAP**  
**Graduates!**

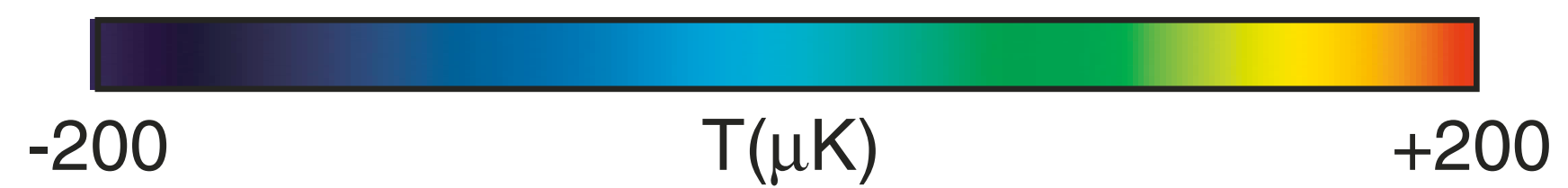
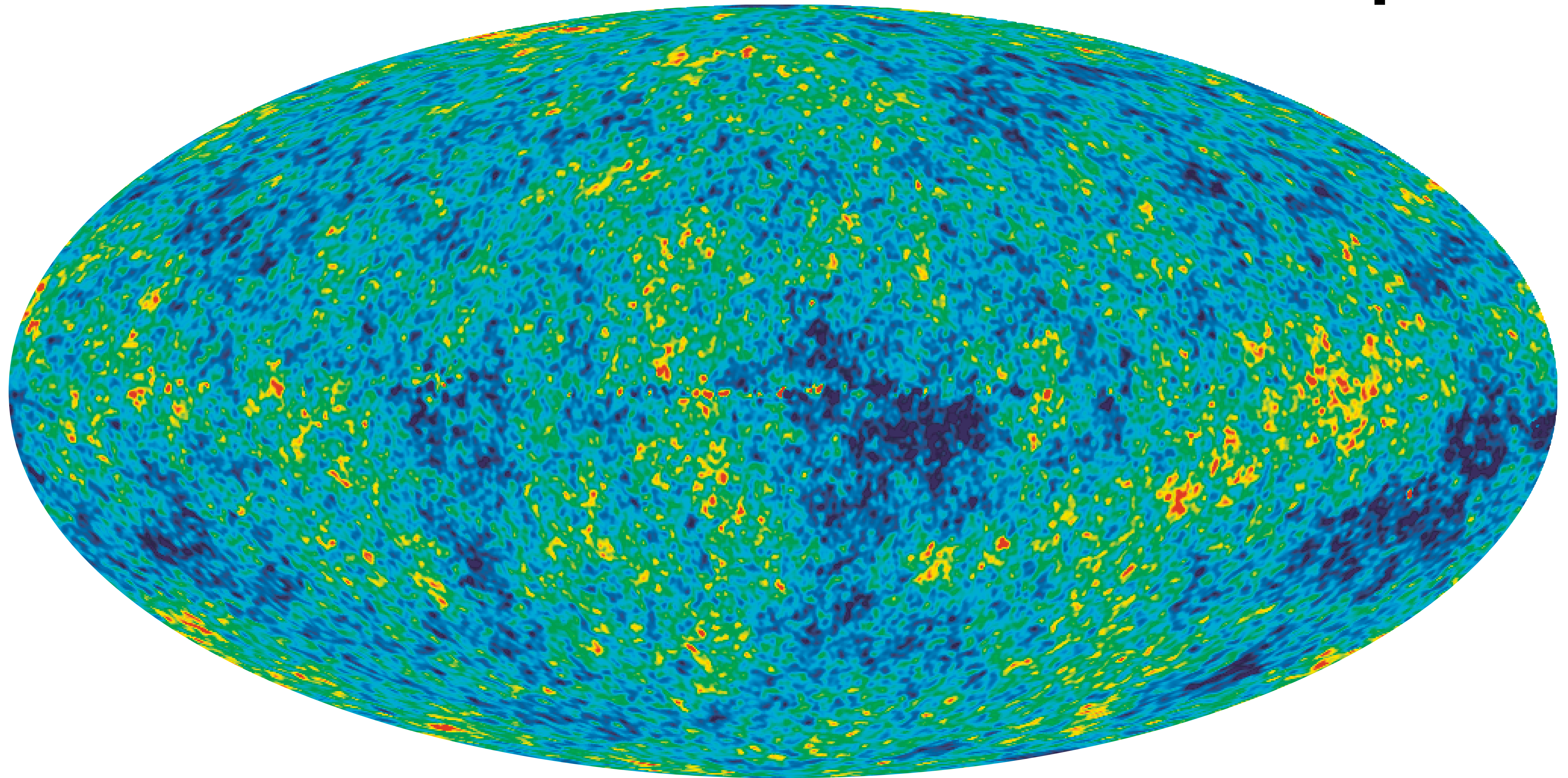
- C. Barnes
- R. Bean
- O. Dore
- H.V. Peiris
- L. Verde

# ~WMAP 5-Year~ Pie Chart Update!



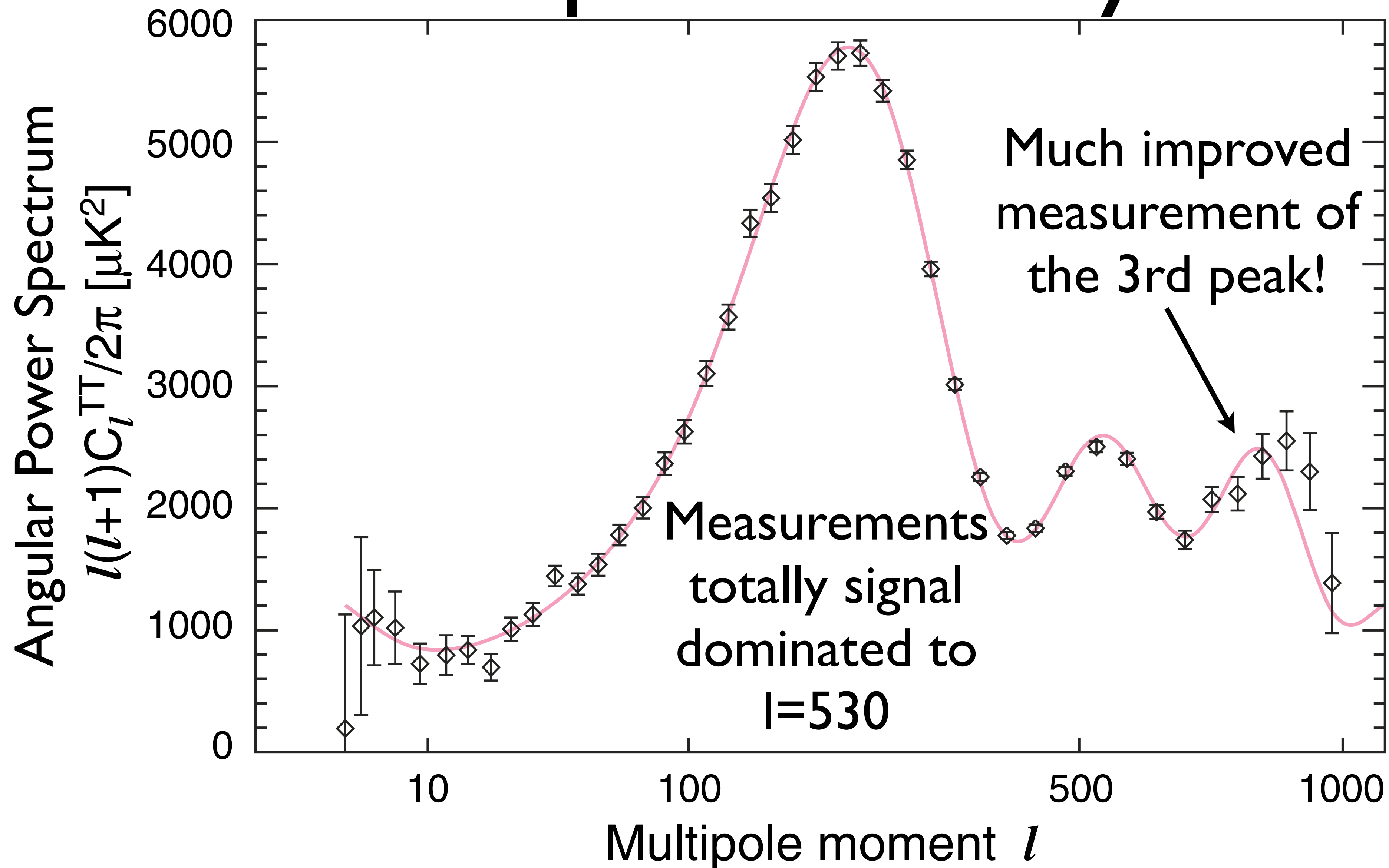
- Universe today
  - Age: **13.72 +/- 0.12 Gyr**
  - Atoms: **4.56 +/- 0.15 %**
  - Dark Matter: **22.8 +/- 1.3%**
  - Vacuum Energy: **72.6 +/- 1.5%**
- When CMB was released 13.7 B yrs ago
  - A significant contribution from the *cosmic neutrino background*

# How Did We Use This Map?

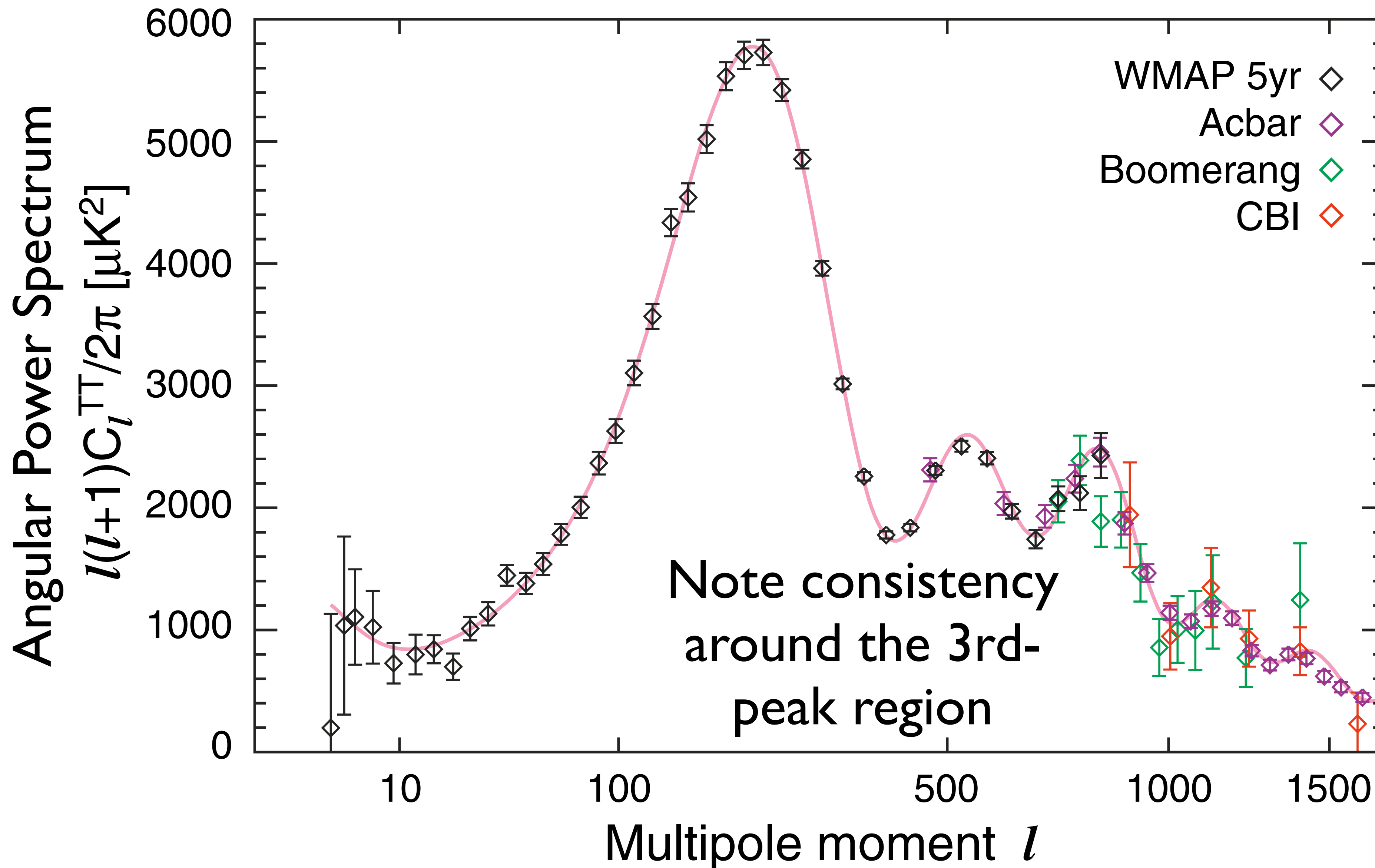


WMAP 5-year

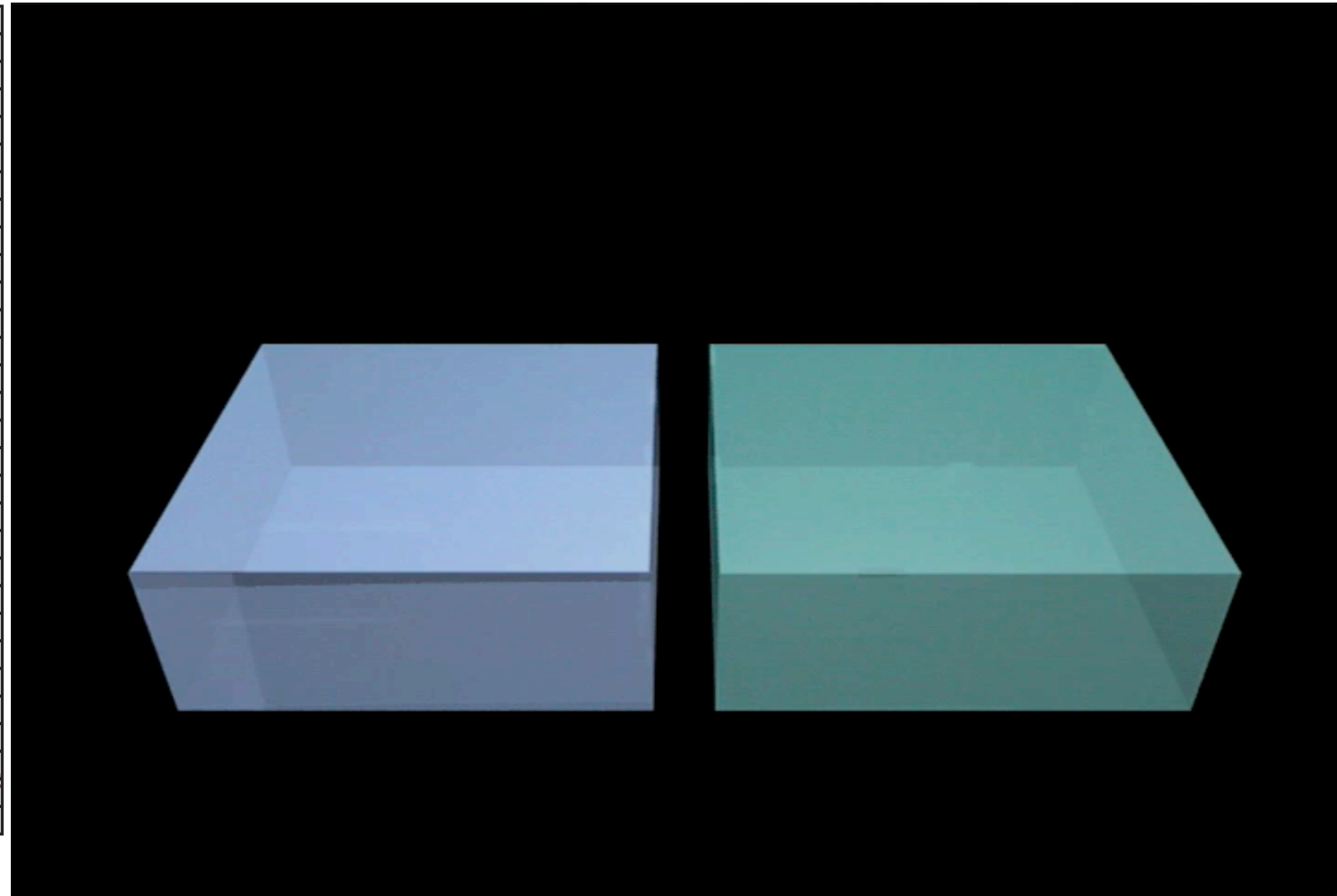
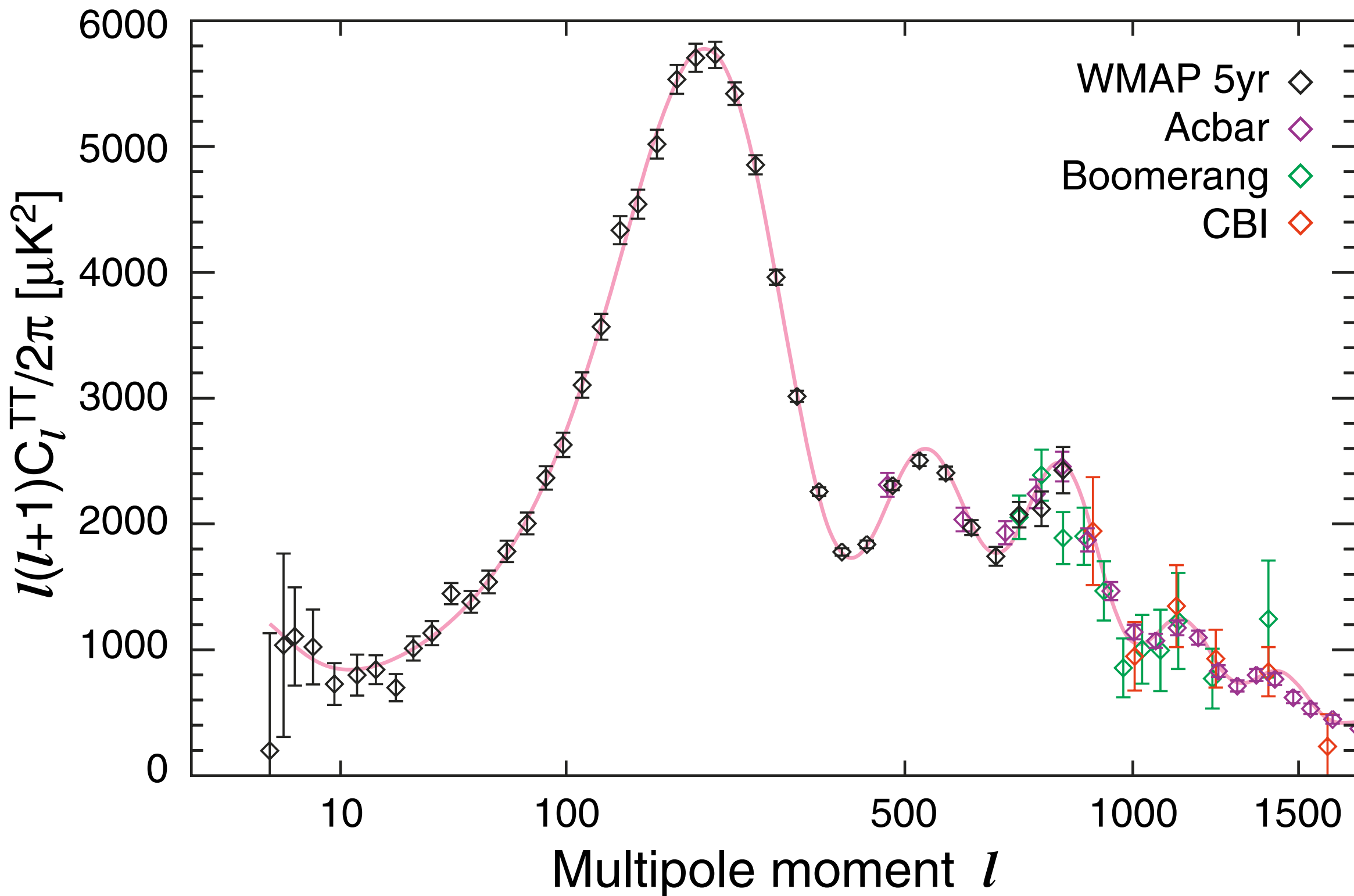
# The Spectral Analysis



# The Cosmic Sound Wave



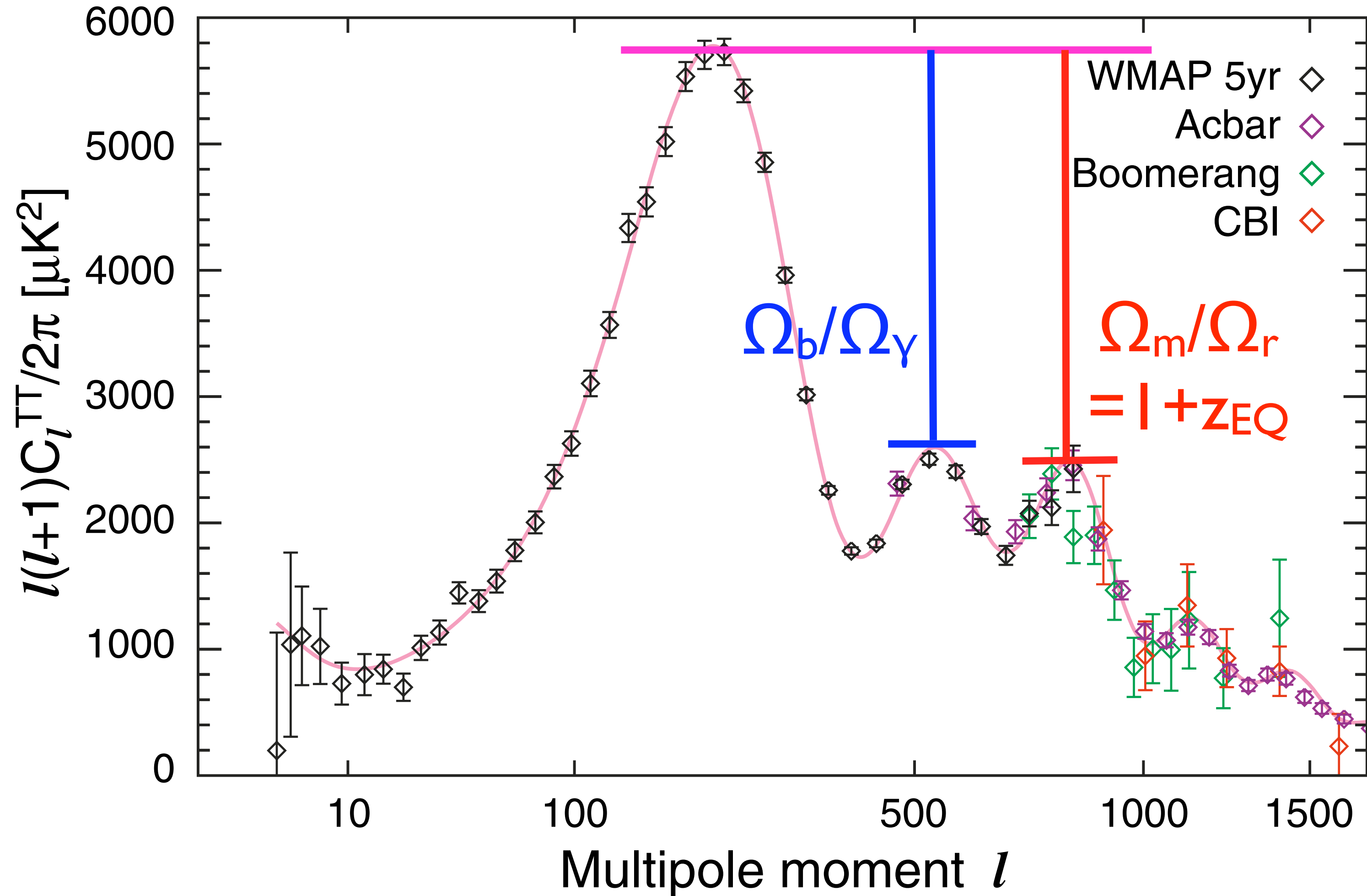
# The Cosmic Sound Wave



- We measure the composition of the Universe by analyzing the wave form of the cosmic sound waves.



# CMB to $\Omega_b h^2$ & $\Omega_m h^2$



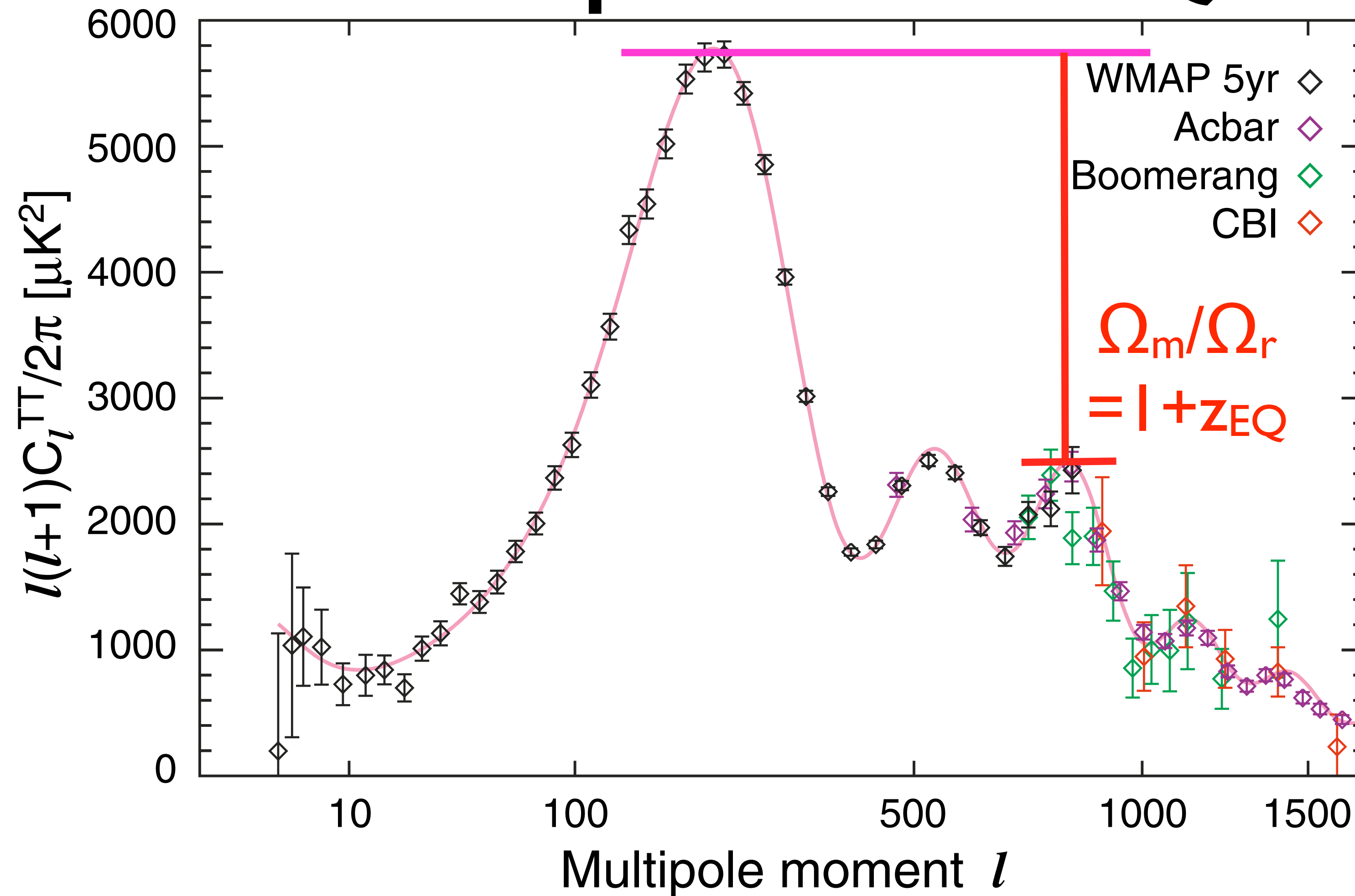
- $l$ -to-2: baryon-to-photon;  $l$ -to-3: matter-to-radiation ratio
- $\Omega_\gamma = 2.47 \times 10^{-5} h^{-2}$  &  $\Omega_r = \Omega_\gamma + \Omega_\nu = 1.69 \Omega_\gamma = 4.17 \times 10^{-5} h^{-2}$

# Effective Number of Neutrino Species, $N_{\text{eff}}$

- For relativistic neutrinos, the energy density is given by
  - $\rho_\nu = N_{\text{eff}} (7\pi^2/120) T_\nu^4$
  - where  $N_{\text{eff}}=3.04$  for the standard model, and  $T_\nu=(4/11)^{1/3}T_{\text{photon}}$
- Adding more relativistic neutrino species (or any other relativistic components) delays the epoch of the matter-radiation equality, as

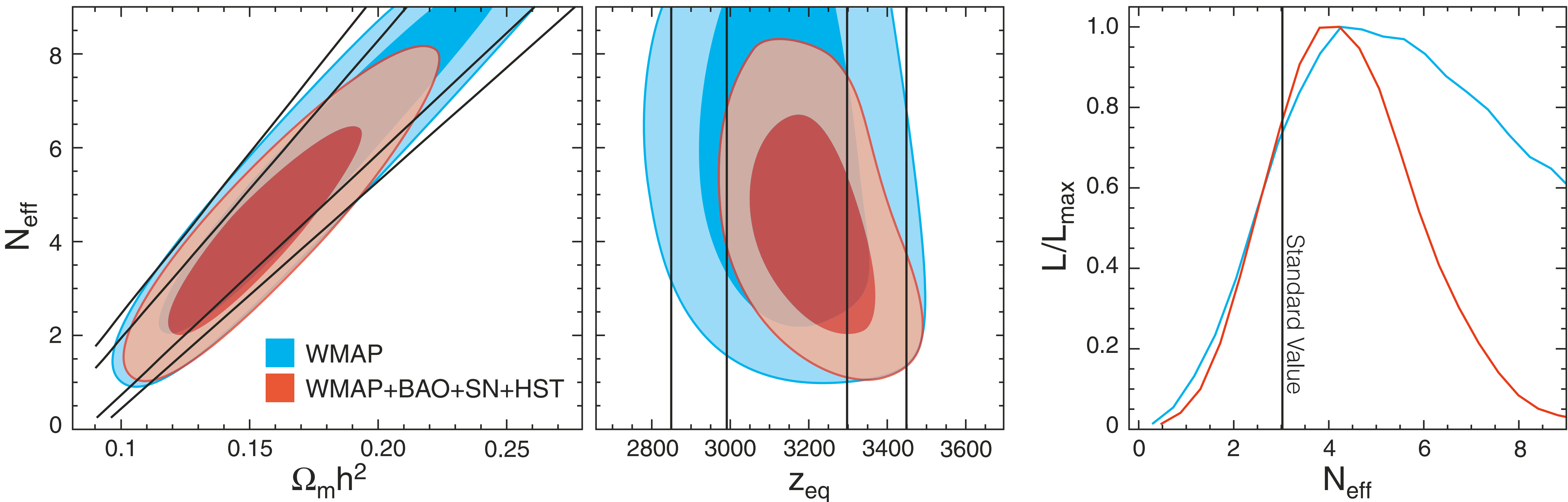
$$1+z_{\text{EQ}} = (\Omega_m h^2 / 2.47 \times 10^{-5}) / (1 + 0.227 N_{\text{eff}})$$

# 3rd-peak to $z_{\text{EQ}}$



- It is  $z_{\text{EQ}}$  that is observable from CMB.
- If we fix  $N_{\text{eff}}$ , we can determine  $\Omega_m h^2$ ; otherwise...

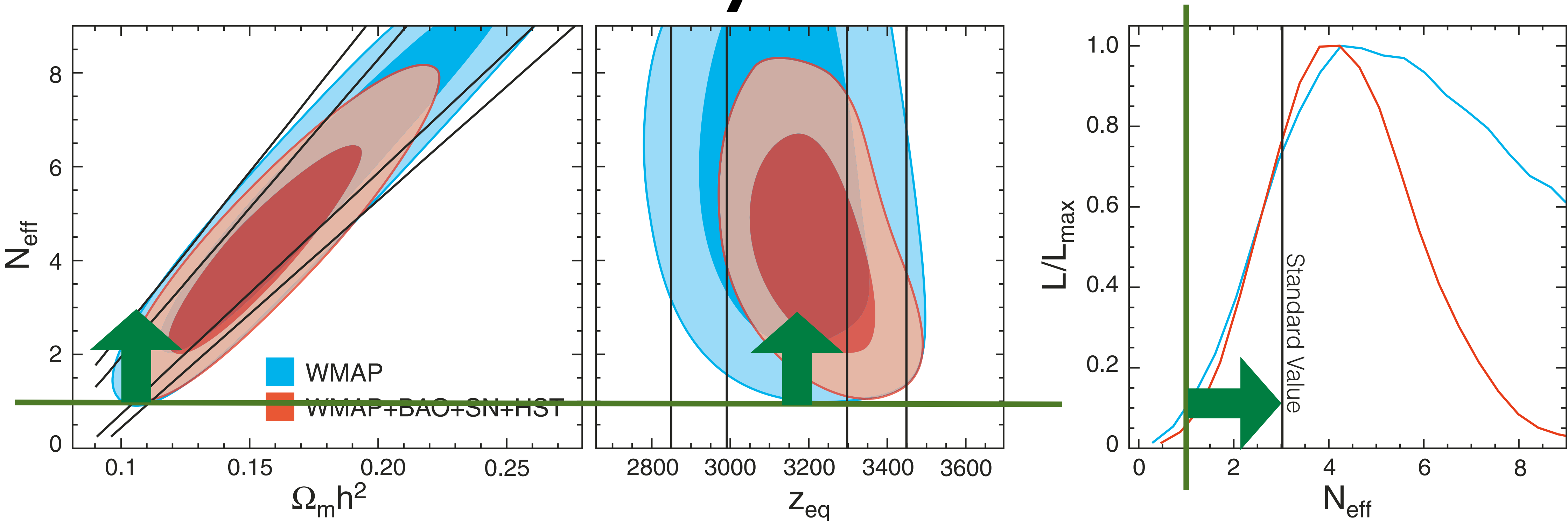
# $N_{\text{eff}}-\Omega_m h^2$ Degeneracy



- $N_{\text{eff}}$  and  $\Omega_m h^2$  are degenerate.
- Adding information on  $\Omega_m h^2$  from the distance measurements (BAO, SN, HST) breaks the degeneracy:

•  **$N_{\text{eff}} = 4.4 \pm 1.5$  (68%CL)**

# WMAP-only Lower Limit

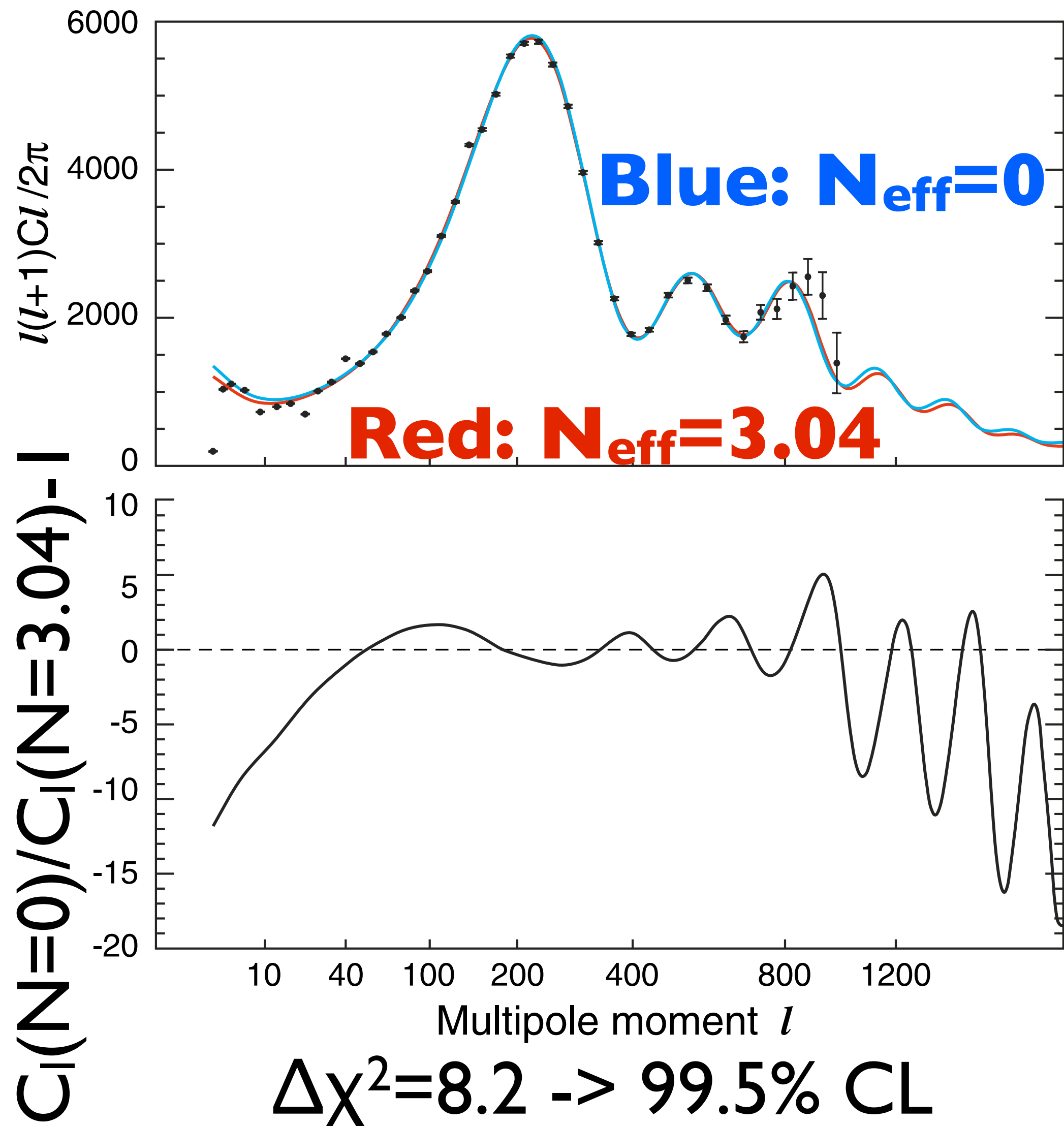


- $N_{\text{eff}}$  and  $\Omega_m h^2$  are degenerate - but, look.
- **WMAP-only lower limit is not  $N_{\text{eff}}=0$**
- $N_{\text{eff}} > 2.3$  (95%CL) [Dunkley et al.]

# Cosmic Neutrino Background

- How do neutrinos affect the CMB?
  - *Neutrinos add to the radiation energy density*, which delays the epoch at which the Universe became matter-dominated. The larger the number of neutrino species is, the later the matter-radiation equality,  $z_{\text{equality}}$ , becomes.
    - This effect can be mimicked by lower matter density.
  - *Neutrino perturbations* affect metric perturbations as well as the photon-baryon plasma, through which CMB anisotropy is affected.

# CNB As Seen By WMAP



- Multiplicative phase shift is due to the change in  $z_{\text{equality}}$ 
  - Degenerate with  $\Omega_m h^2$
- Additive phase shift is due to neutrino perturbations
  - **No degeneracy** (Bashinsky & Seljak 2004)

# Cosmic/Laboratory Consistency

- From WMAP( $z=1090$ )+BAO+SN
  - $N_{\text{eff}} = 4.4 \pm 1.5$
- From the Big Bang Nucleosynthesis ( $z=10^9$ )
  - $N_{\text{eff}} = 2.5 \pm 0.4$  (Gary Steigman)
- From the decay width of Z bosons measured in lab
  - $N_{\text{neutrino}} = 2.984 \pm 0.008$  (LEP)

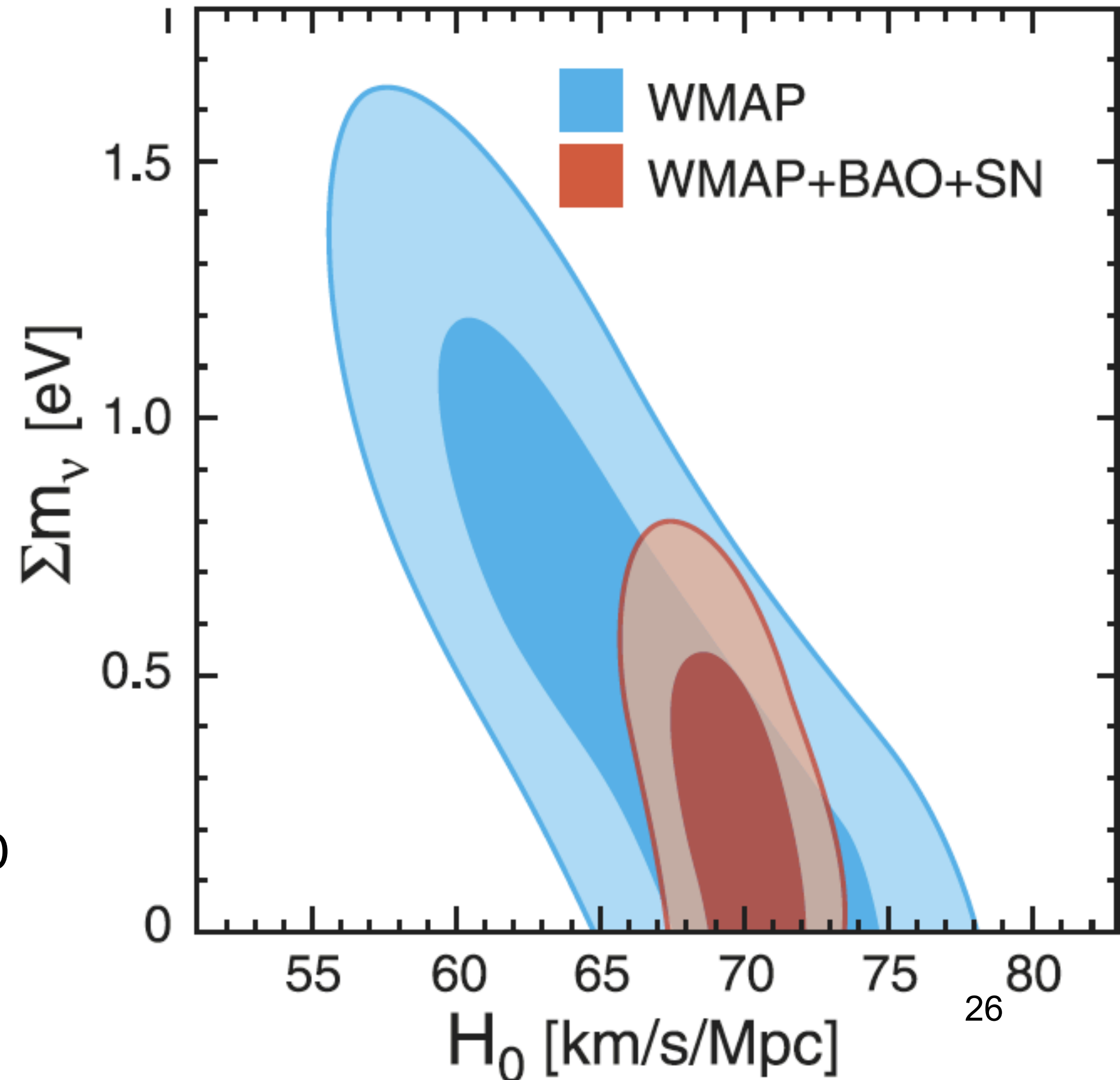


# $\Sigma m_\nu$ from CMB alone

- There is a simple limit by which one can constrain  $\Sigma m_\nu$  using the primary CMB from  $z=1090$  alone (ignoring gravitational lensing of CMB by the intervening mass distribution)
- When all of neutrinos were lighter than  $\sim 0.6$  eV, they were still relativistic at the time of photon decoupling at  $z=1090$  (photon temperature  $3000\text{K}=0.26\text{eV}$ ).
  - $\langle E_\nu \rangle = 3.15(4/11)^{1/3} T_{\text{photon}} = 0.58$  eV
- Neutrino masses didn't matter if they were relativistic!
- For degenerate neutrinos,  $\Sigma m_\nu = 3.04 \times 0.58 = 1.8$  eV
  - **If  $\Sigma m_\nu \ll 1.8\text{eV}$ , CMB alone cannot see it**

# CMB + $H_0$ Helps

- WMAP 5-year alone:  
 $\Sigma m_\nu < 1.3 \text{ eV}$  (95%CL)
- WMAP+BAO+SN:  
 **$\Sigma m_\nu < 0.67 \text{ eV}$  (95%CL)**
- Where did the improvement comes from? It's the present-day Hubble expansion rate,  $H_0$



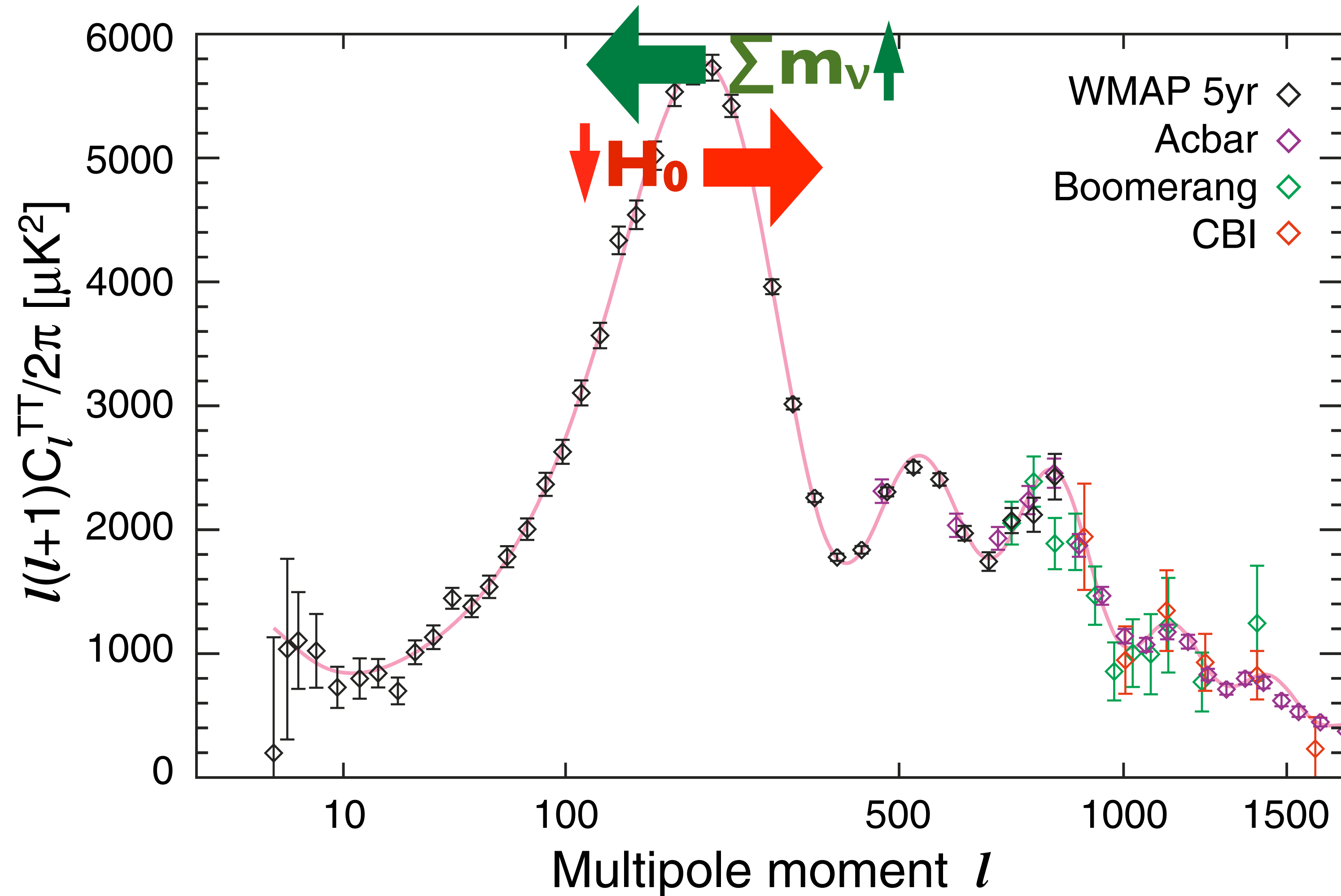
# Neutrino Subtlety

- For  $\sum m_\nu \ll 1.8\text{eV}$ , neutrinos were relativistic at  $z=1090$
- But, we know that  $\sum m_\nu > 0.05\text{eV}$  from neutrino oscillation experiments
- This means that **neutrinos are definitely non-relativistic today!**
- So, today's value of  $\Omega_m$  is the sum of baryons, CDM, and neutrinos:  $\Omega_m h^2 = (\Omega_b + \Omega_c) h^2 + 0.0106(\sum m_\nu / 1\text{eV})$

# Matter-Radiation Equality

- However, since neutrinos were relativistic before  $z=1090$ , the matter-radiation equality is determined by:
  - $1+z_{\text{EQ}} = (\Omega_b + \Omega_c)h^2 / 4.17 \times 10^{-5}$  (observable by CMB)
- Now, recall  $\Omega_m h^2 = (\Omega_b + \Omega_c)h^2 + 0.0106(\sum m_\nu / \text{eV})$ 
  - For a given  $\Omega_m h^2$  constrained by BAO+SN, adding  $\sum m_\nu$  makes  $(\Omega_b + \Omega_c)h^2$  smaller  $\rightarrow$  smaller  $z_{\text{EQ}}$   $\rightarrow$   
**Radiation Era lasts longer**
- **This effect shifts the first peak to a lower multipole**

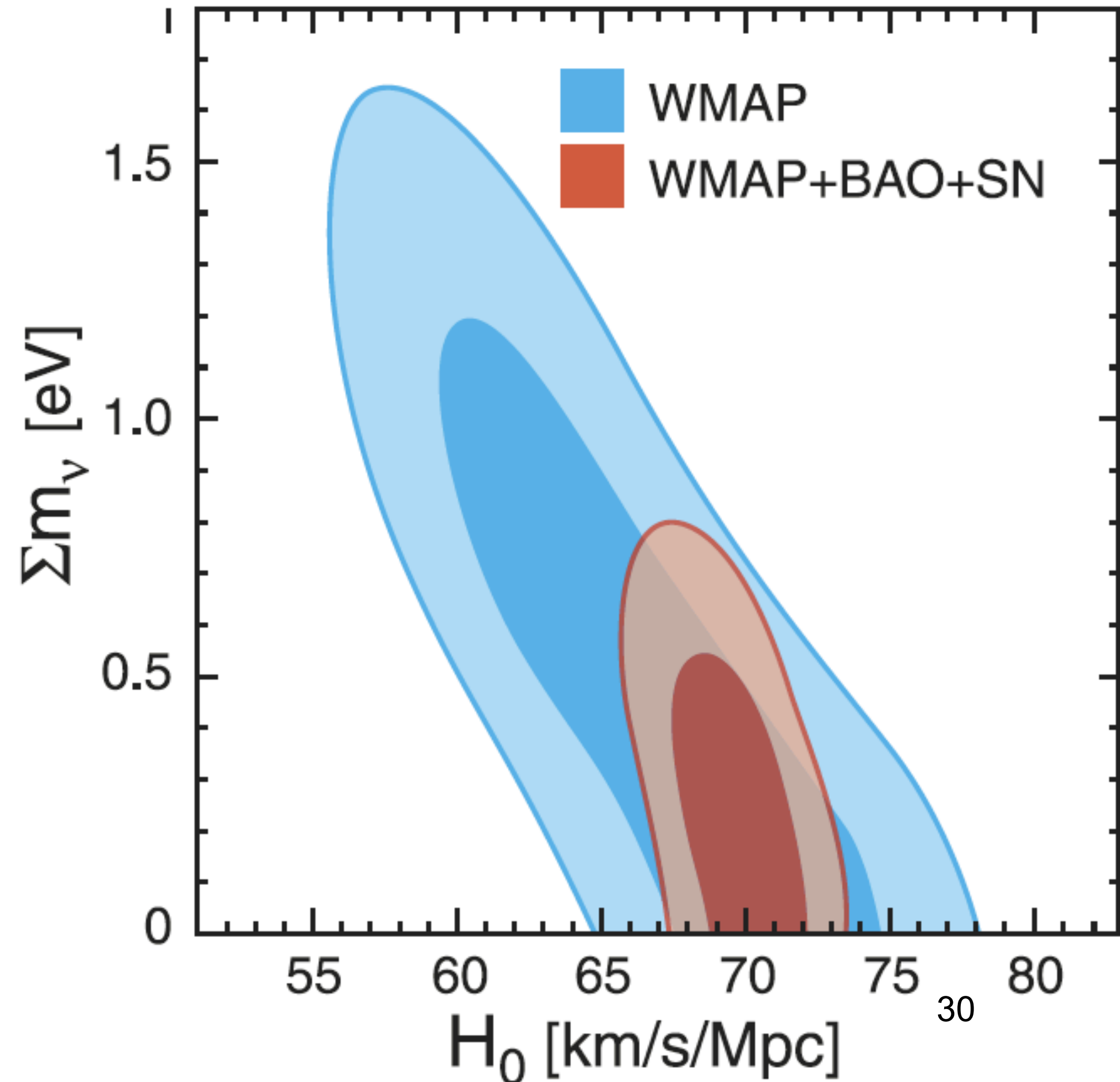
# $\Sigma m_\nu$ : Shifting the Peak To Low- $l$



- But, lowering  $H_0$  shifts the peak in the opposite direction. So...

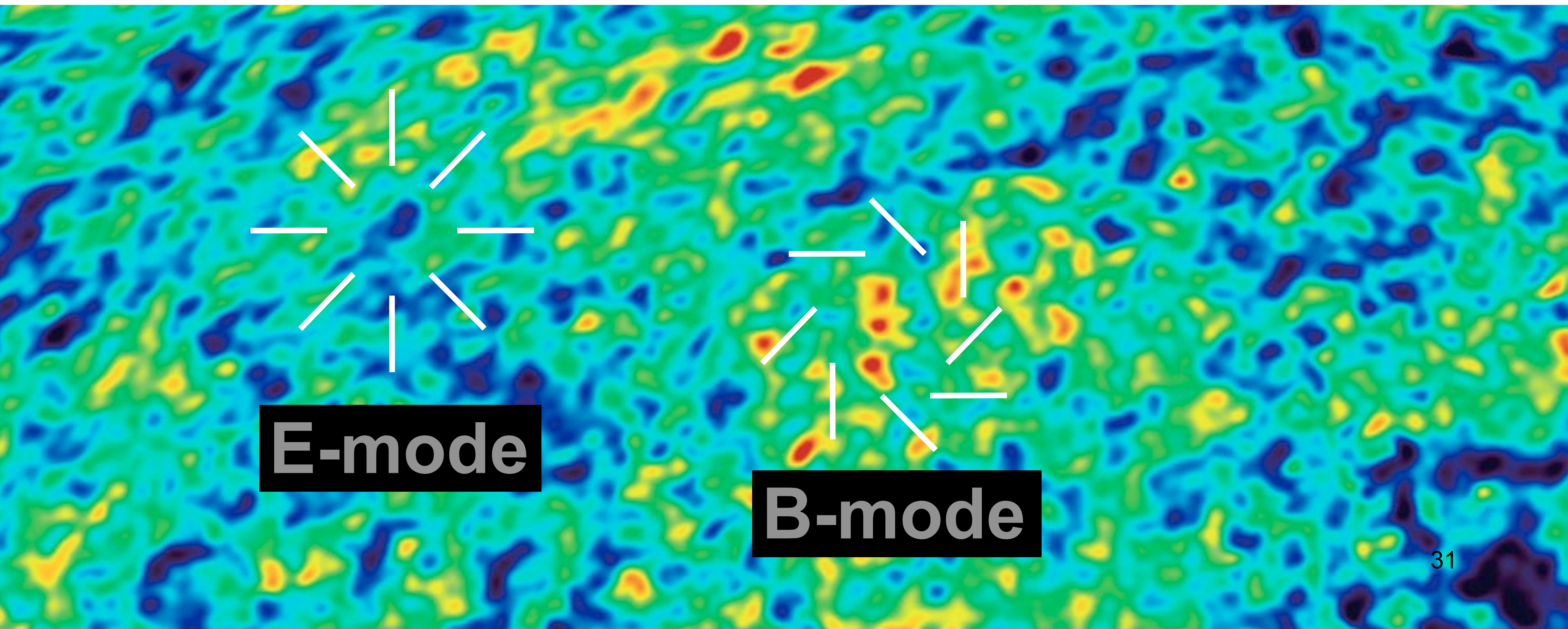
# Shift of Peak Absorbed by $H_0$

- Here is a catch:
  - **Shift of the first peak to a lower multipole can be canceled by lowering  $H_0$ !**
- Same thing happens to curvature of the universe: making the universe positively curved shifts the first peak to a lower multipole, but this effect can be canceled by lowering  $H_0$ .
- So, 30% positively curved universe is consistent with the WMAP data, IF  $H_0=30\text{km/s/Mpc}$

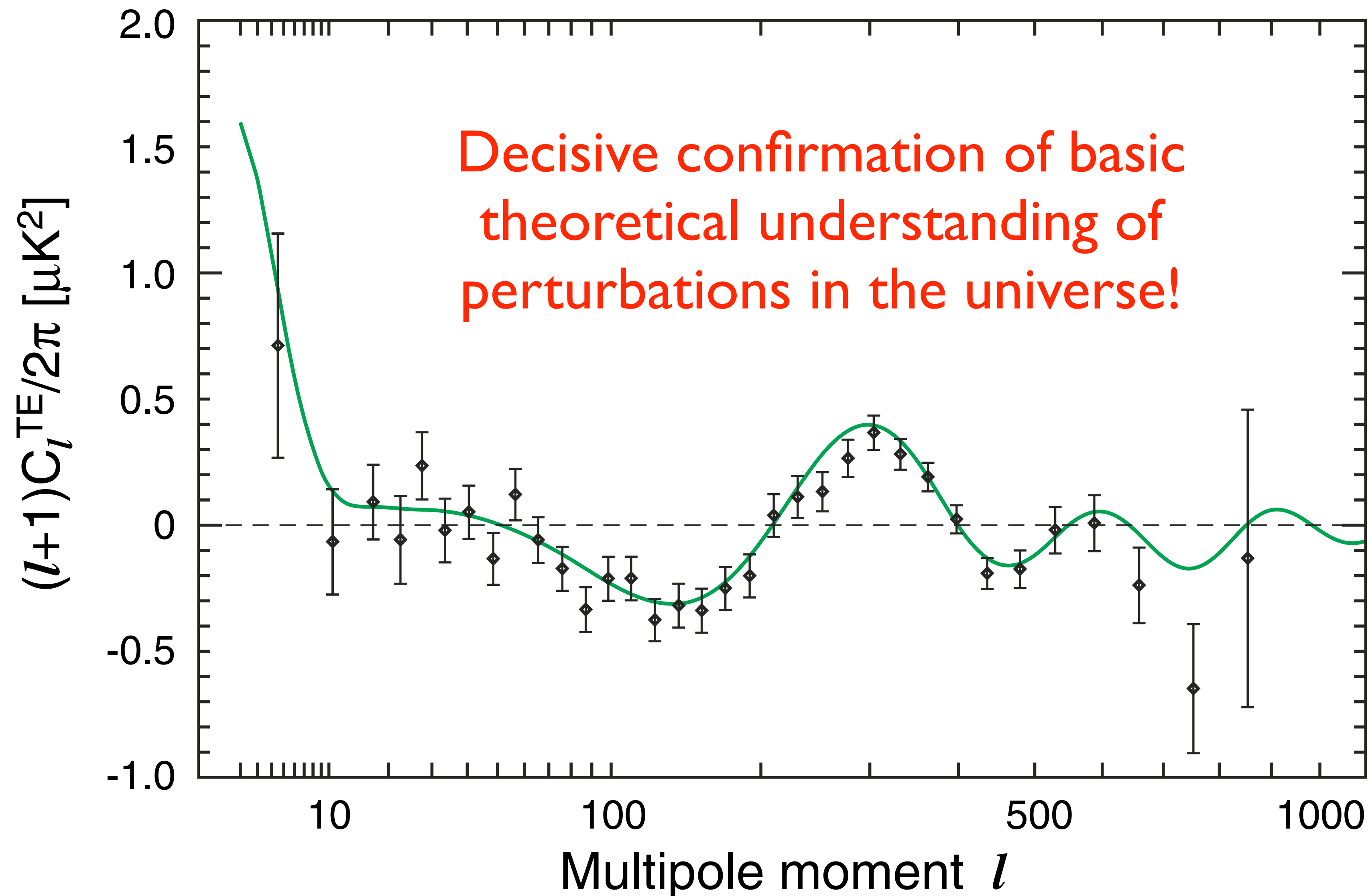


# *How About Polarization?*

- Polarization is a rank-2 tensor field.
- One can decompose it into a divergence-like “E-mode” and a vorticity-like “B-mode”.



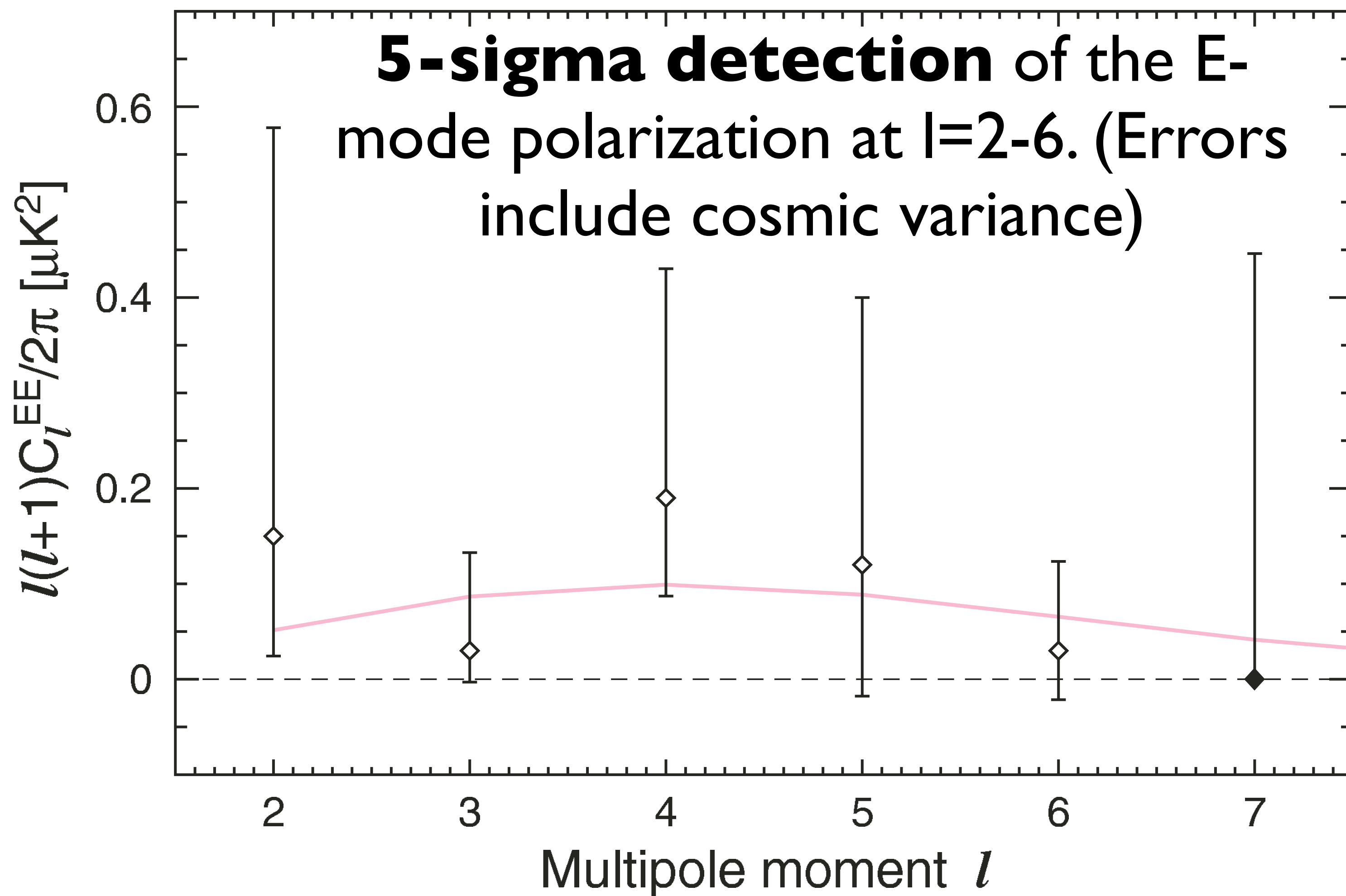
# 5-Year TxE Power Spectrum





# 5-Year E-Mode Polarization Power Spectrum at Low $l$

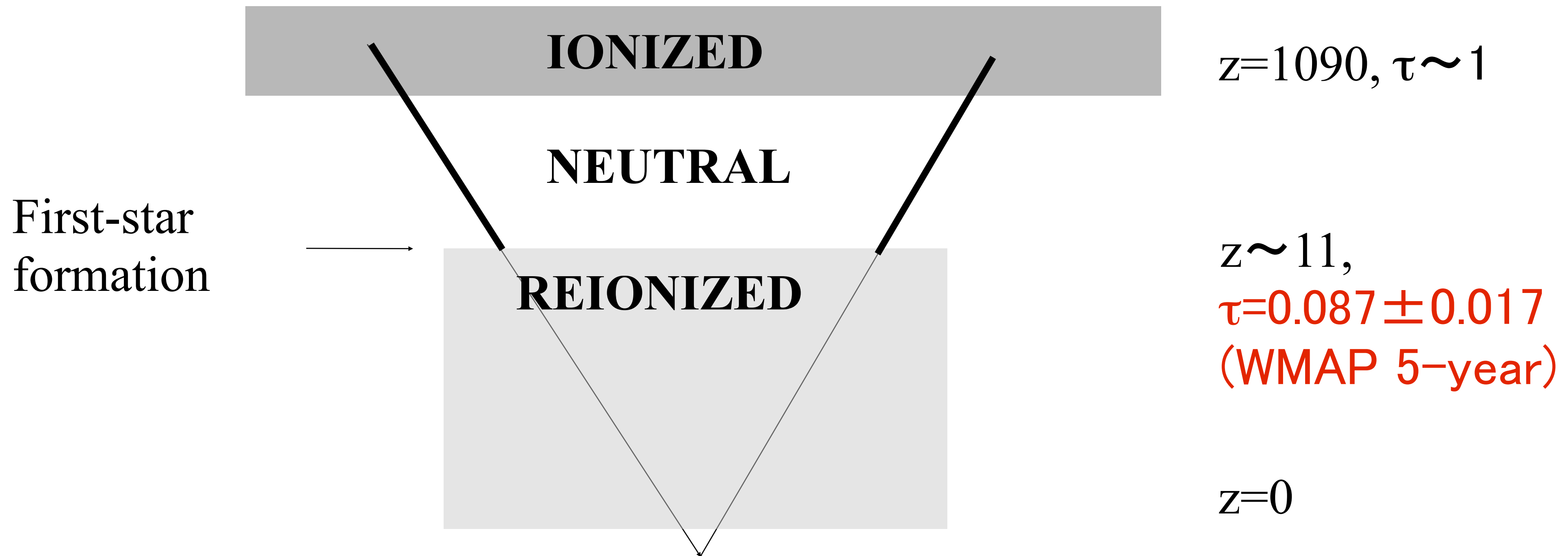
E-Mode Angular Power Spectrum



Black Symbols are upper limits

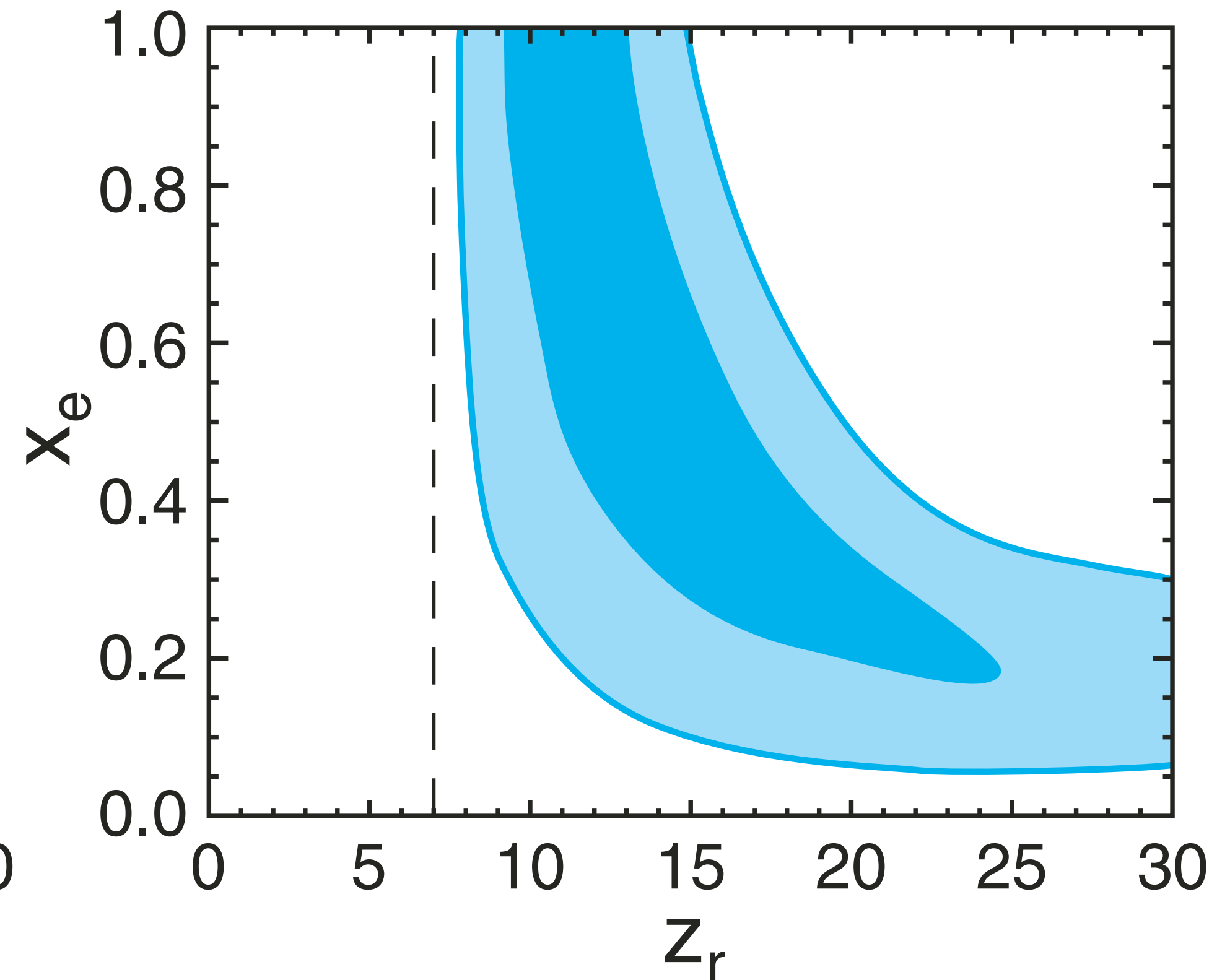
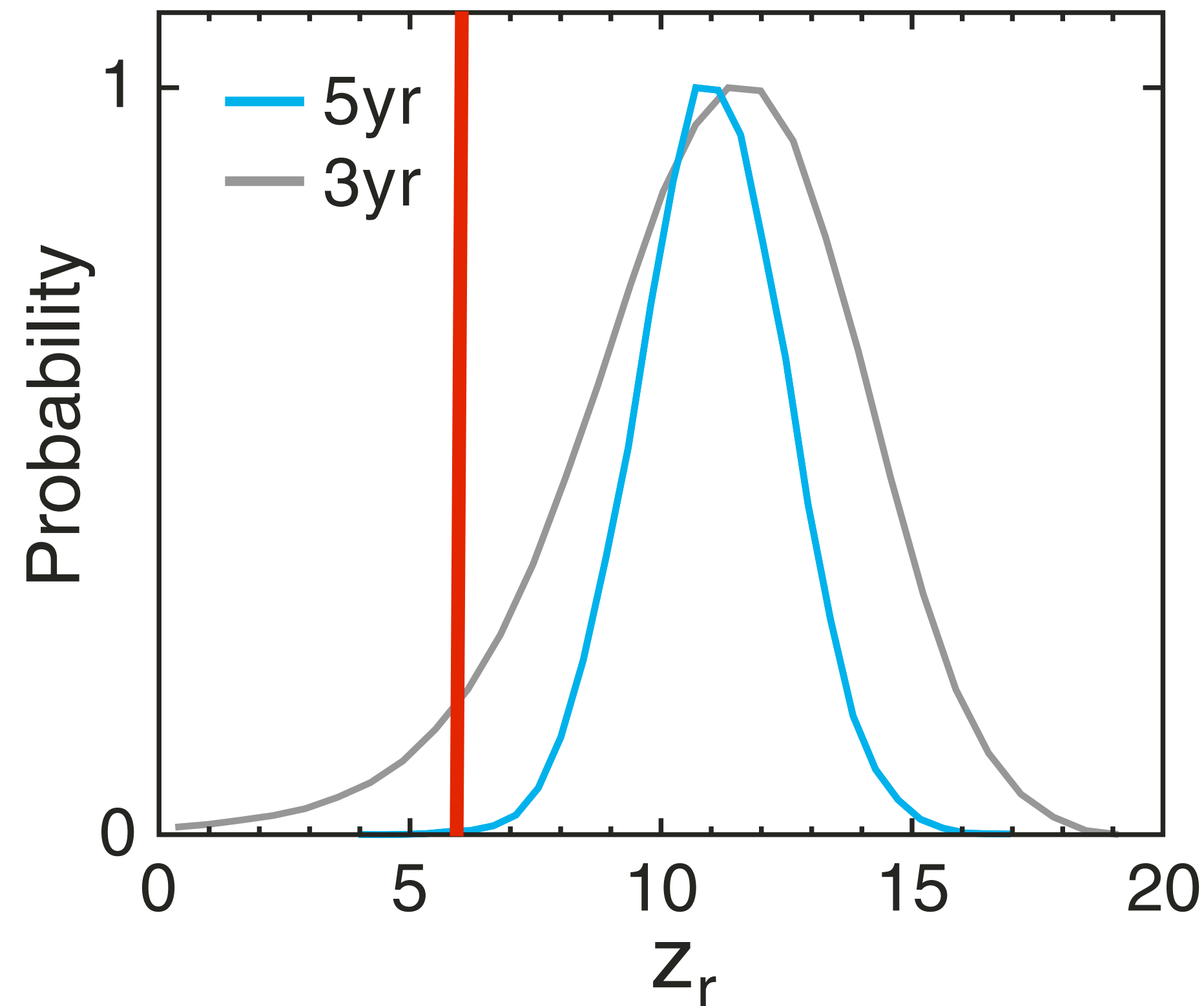
# Polarization From Reionization

- CMB was emitted at  $z=1090$ .
- Some fraction ( $\sim 9\%$ ) of CMB was re-scattered in a reionized universe: *erased temperature anisotropy, but created polarization.*
- The reionization redshift of  $\sim 11$  would correspond to 400 million years after the Big-Bang.



# $z_{\text{reion}}=6$ Is Excluded

*Dunkley et al.*

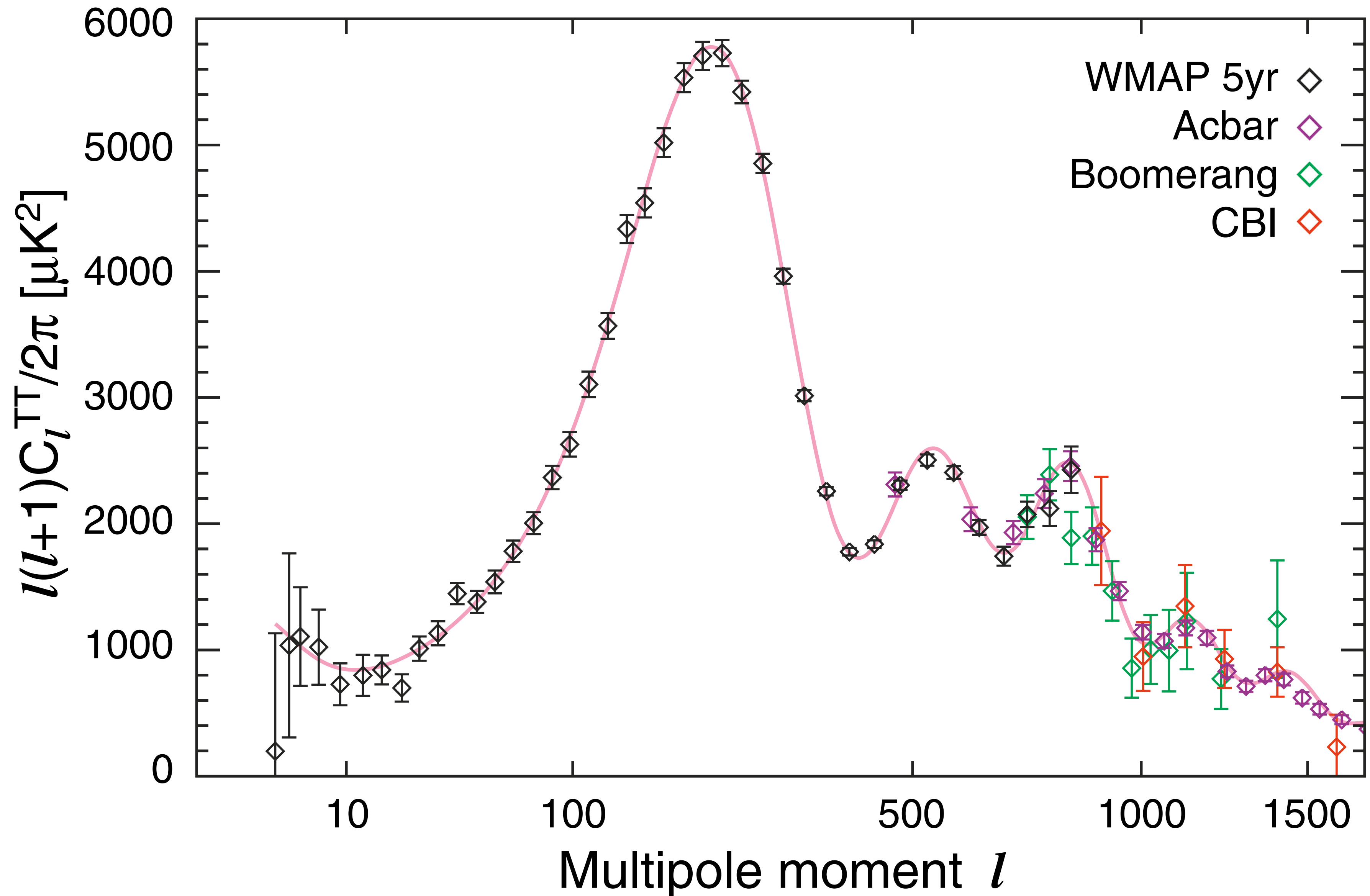


- Assuming an instantaneous reionization from  $x_e=0$  to  $x_e=1$  at  $z_{\text{reion}}$ , we find  $z_{\text{reion}}=11.0 \pm 1.4$  (68 % CL).
- The reionization was not an instantaneous process at  $z \sim 6$ . (The 3-sigma lower bound is  $z_{\text{reion}} > 6.7$ .)

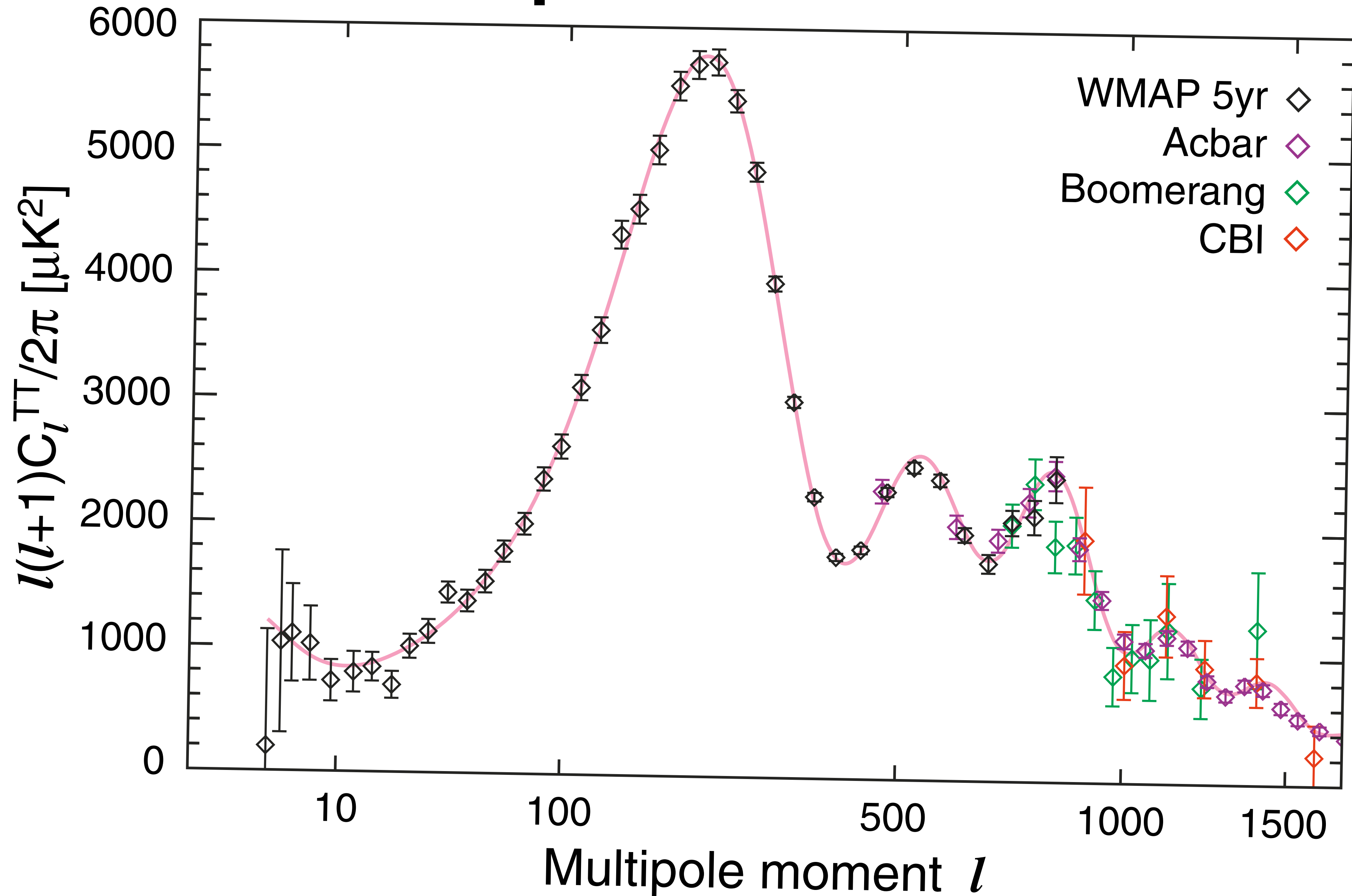
# B-modes

- No detection of B-mode polarization yet.
- I will come back to this later.

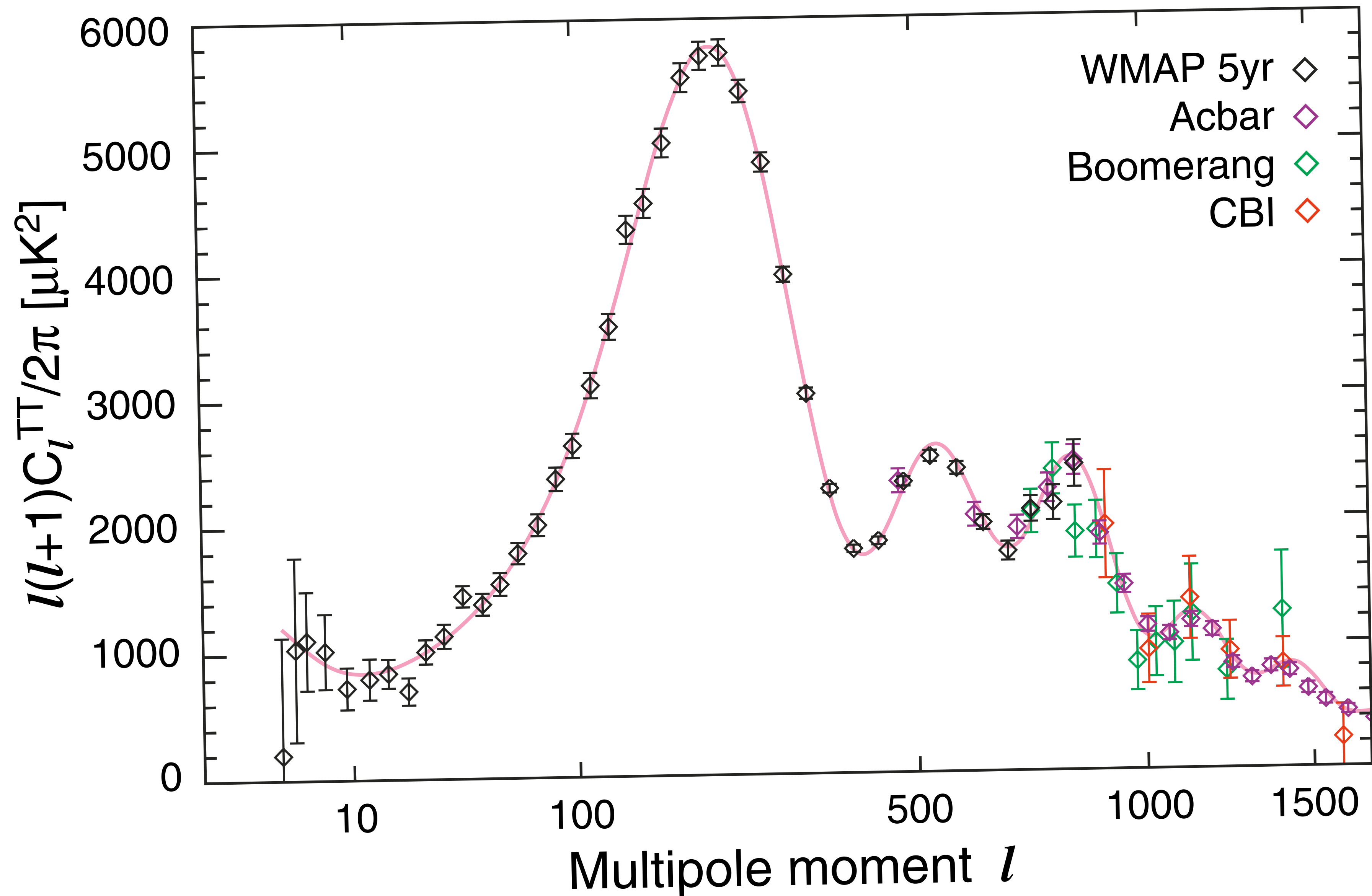
# *Tilting*=Primordial Shape->Inflation



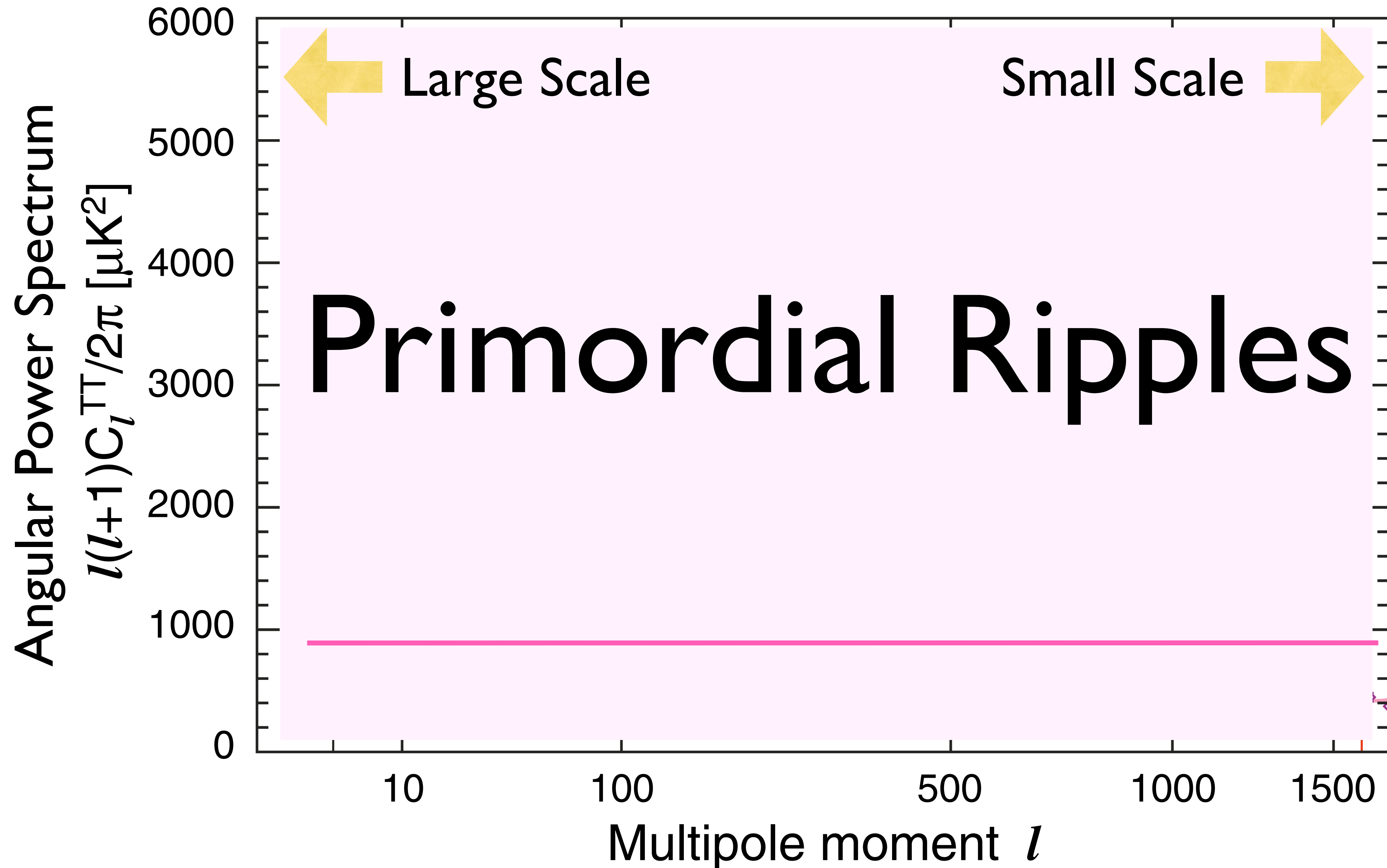
# “Red” Spectrum: $n_s < 1$



# “Blue” Spectrum: $n_s > 1$

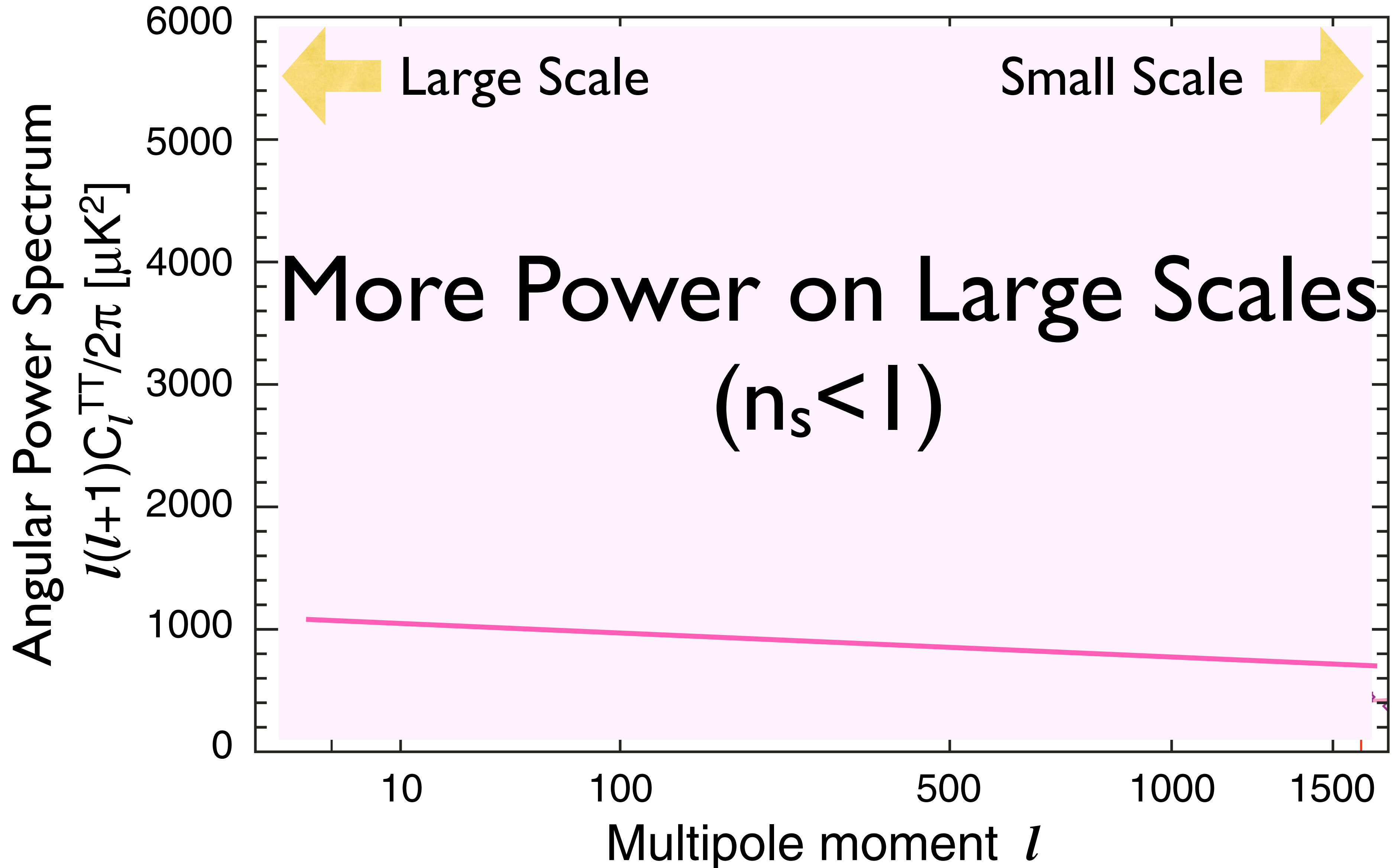


# Getting rid of the Sound Waves

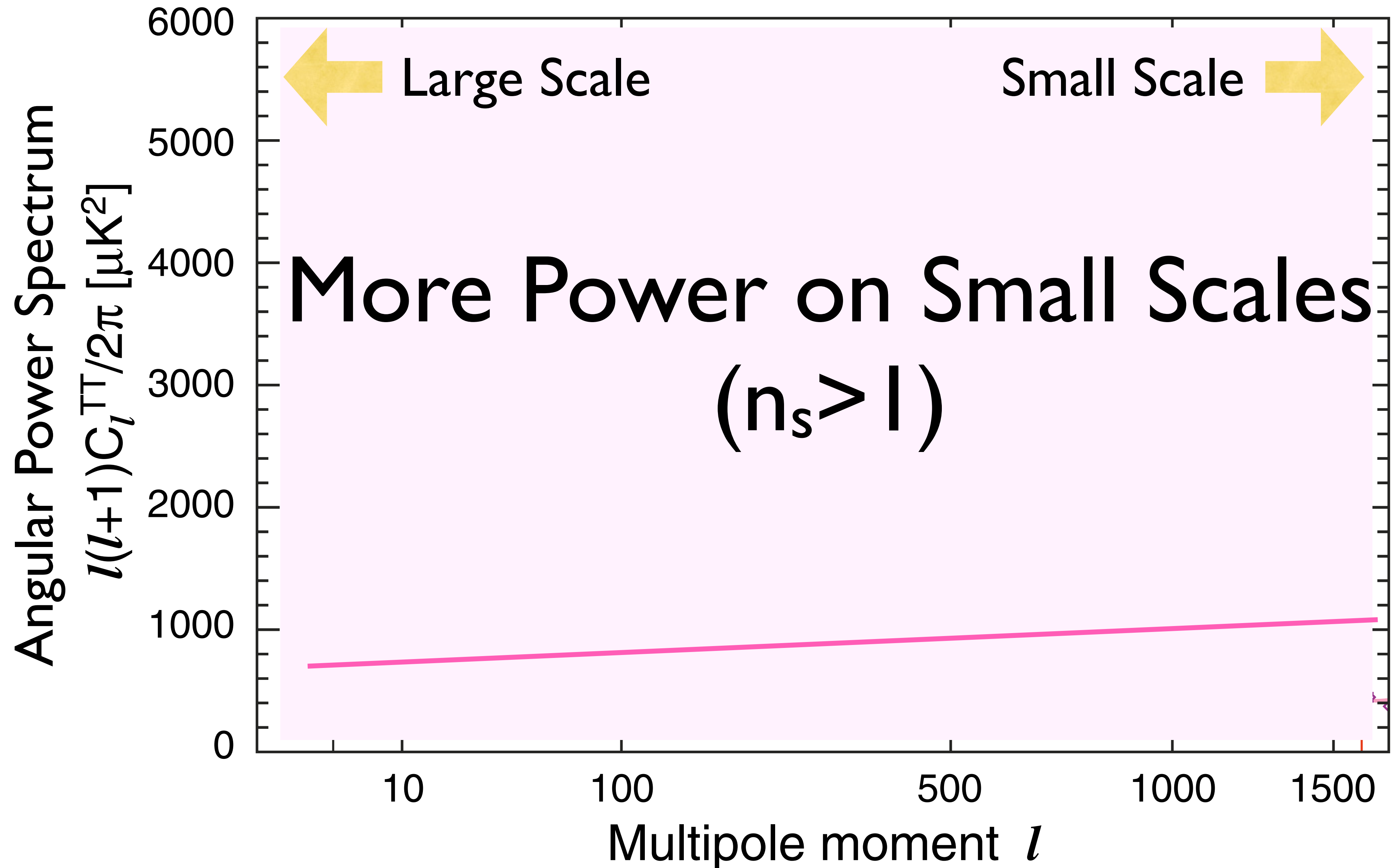




# The Early Universe Could Have Done This Instead



...or, This.

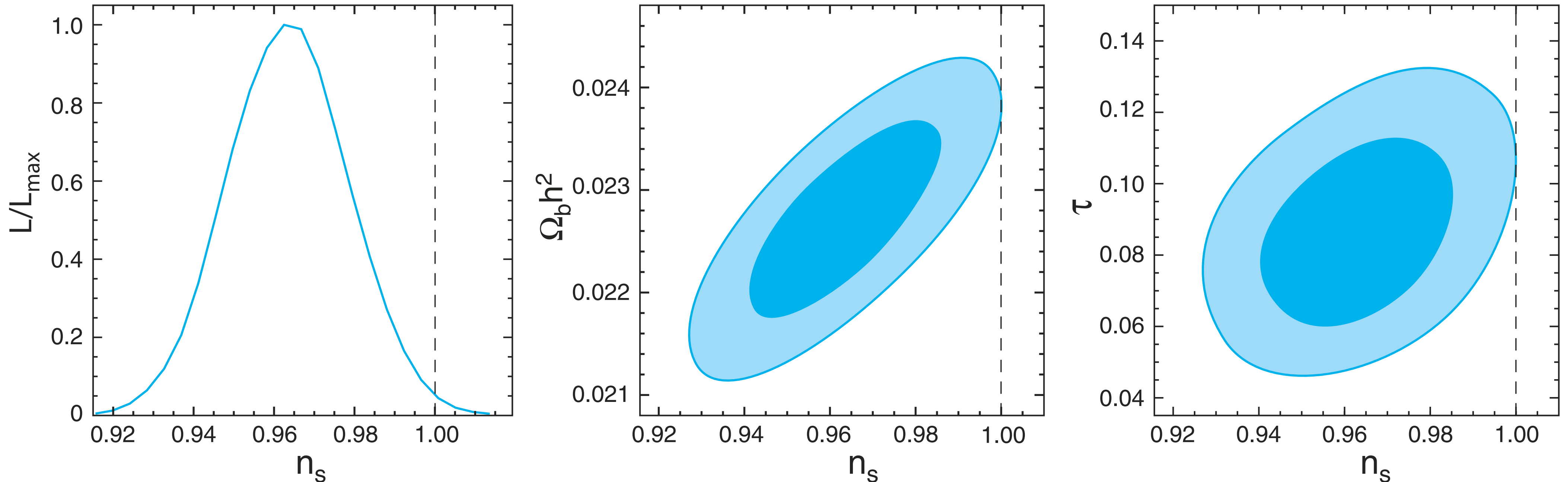


# Expectations From 1970's: $n_s=1$

- Metric perturbations in  $g_{ij}$  (let's call that “curvature perturbations”  $\Phi$ ) is related to  $\delta$  via
  - $k^2\Phi(k)=4\pi G\rho a^2\delta(k)$
- Variance of  $\Phi(x)$  in position space is given by
  - $\langle\Phi^2(x)\rangle=\int\ln k \mathbf{k}^3|\Phi(\mathbf{k})|^2$
  - In order to avoid the situation in which curvature (geometry) diverges on small or large scales, a “scale-invariant spectrum” was proposed:  $\mathbf{k}^3|\Phi(\mathbf{k})|^2 = \text{const.}$
  - This leads to the expectation:  $\mathbf{P}(\mathbf{k})=|\delta(k)|^2=\mathbf{k}^{n_s}$  ( $n_s=1$ )
    - *Harrison 1970; Zel'dovich 1972; Peebles&Yu 1970*

# Is $n_s$ different from ONE?

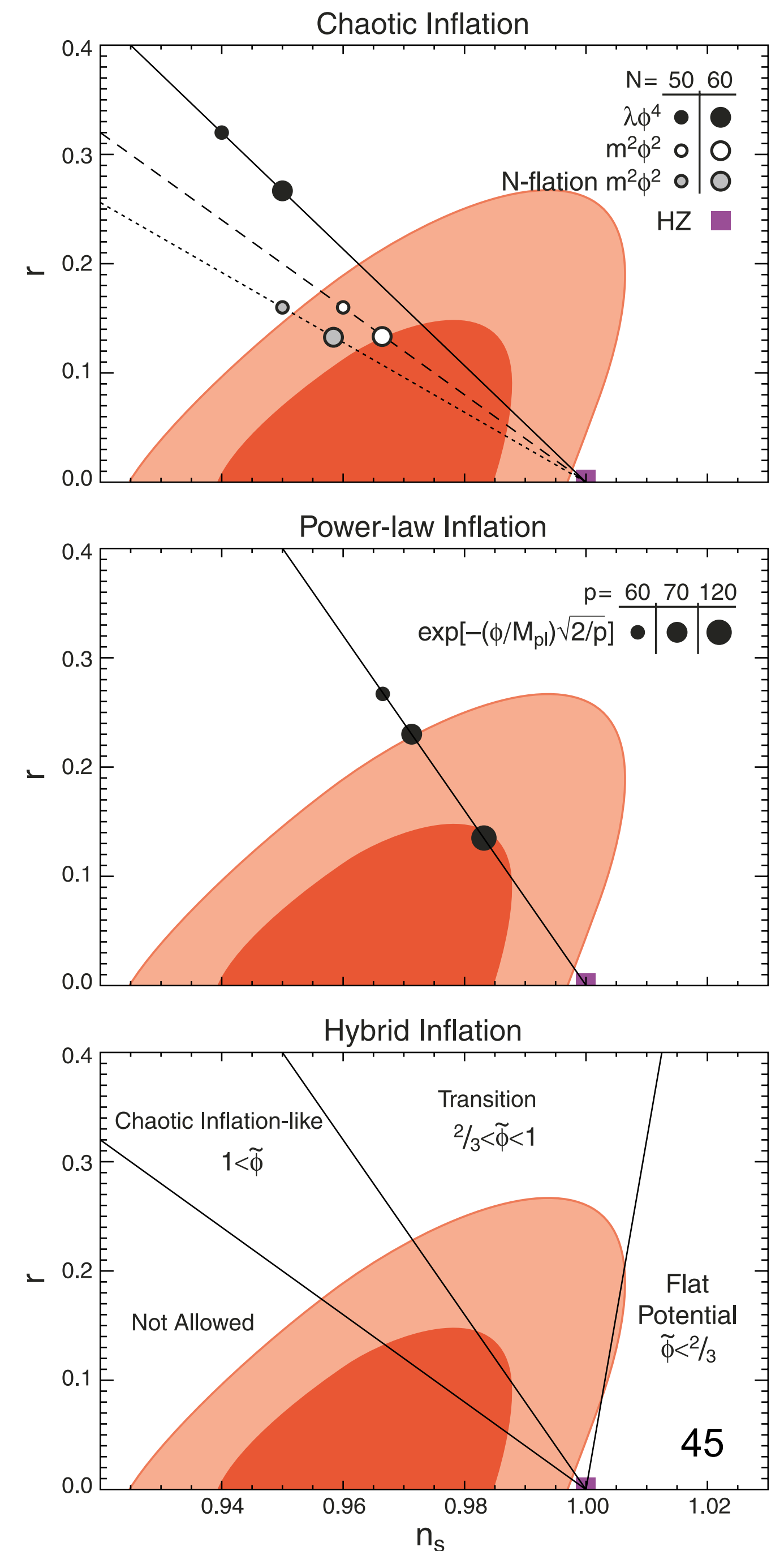
*Komatsu et al.*



- WMAP-alone:  $n_s = \mathbf{0.963}$  (+0.014) (-0.015) (Dunkley et al.)
  - 2.5-sigma away from  $n_s = 1$ , “scale invariant spectrum”
- $n_s$  is degenerate with  $\Omega_b h^2$ ; thus, we can't really improve upon  $n_s$  further unless we improve upon  $\Omega_b h^2$

# Deviation from $n_s=1$

- This was expected by many inflationary models
- In  $n_s$ - $r$  plane (where  $r$  is called the “tensor-to-scalar ratio,” which is  $P(k)$  of gravitational waves divided by  $P(k)$  of density fluctuations) **many inflationary models are compatible with the current data**
- Many models have been excluded also

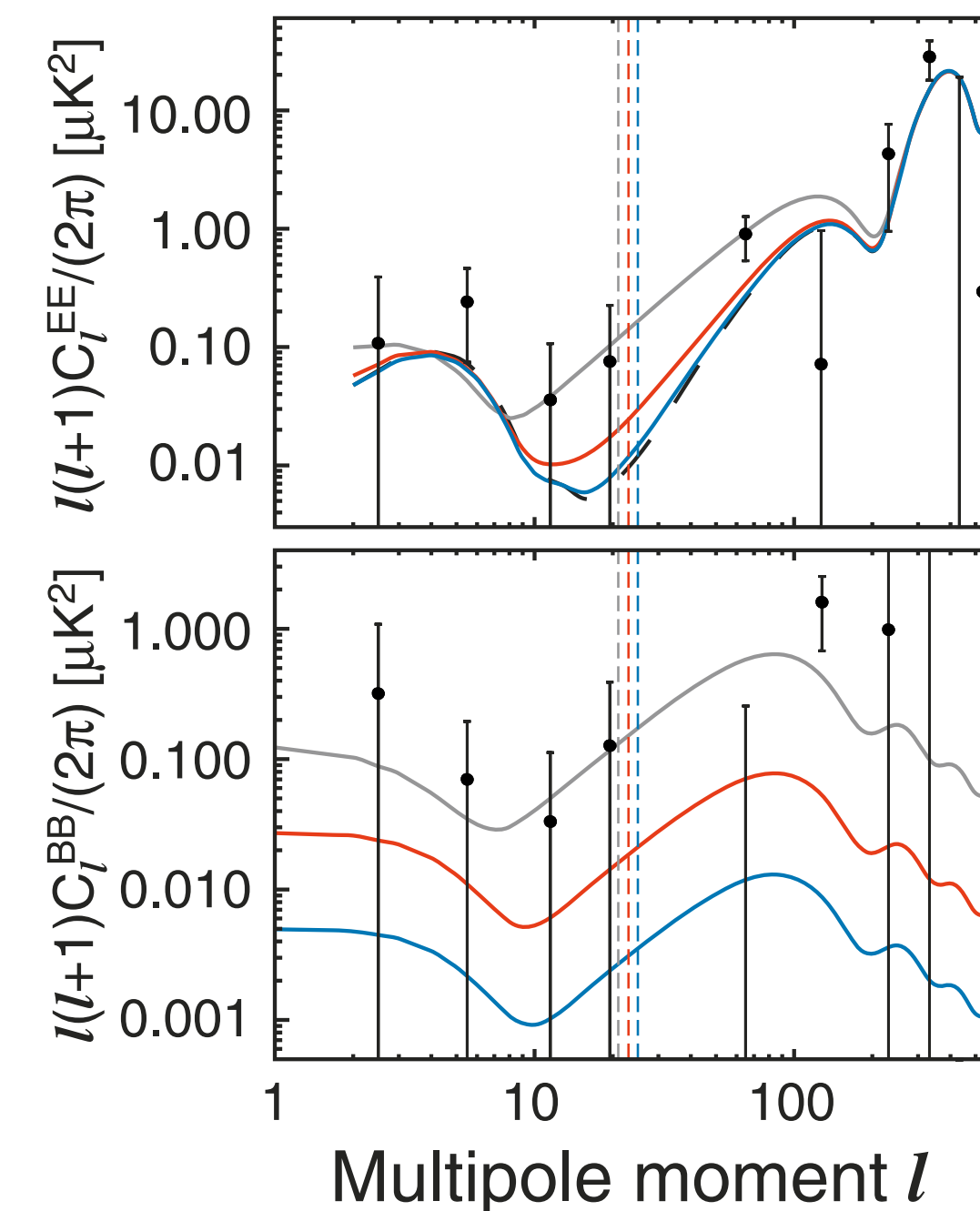
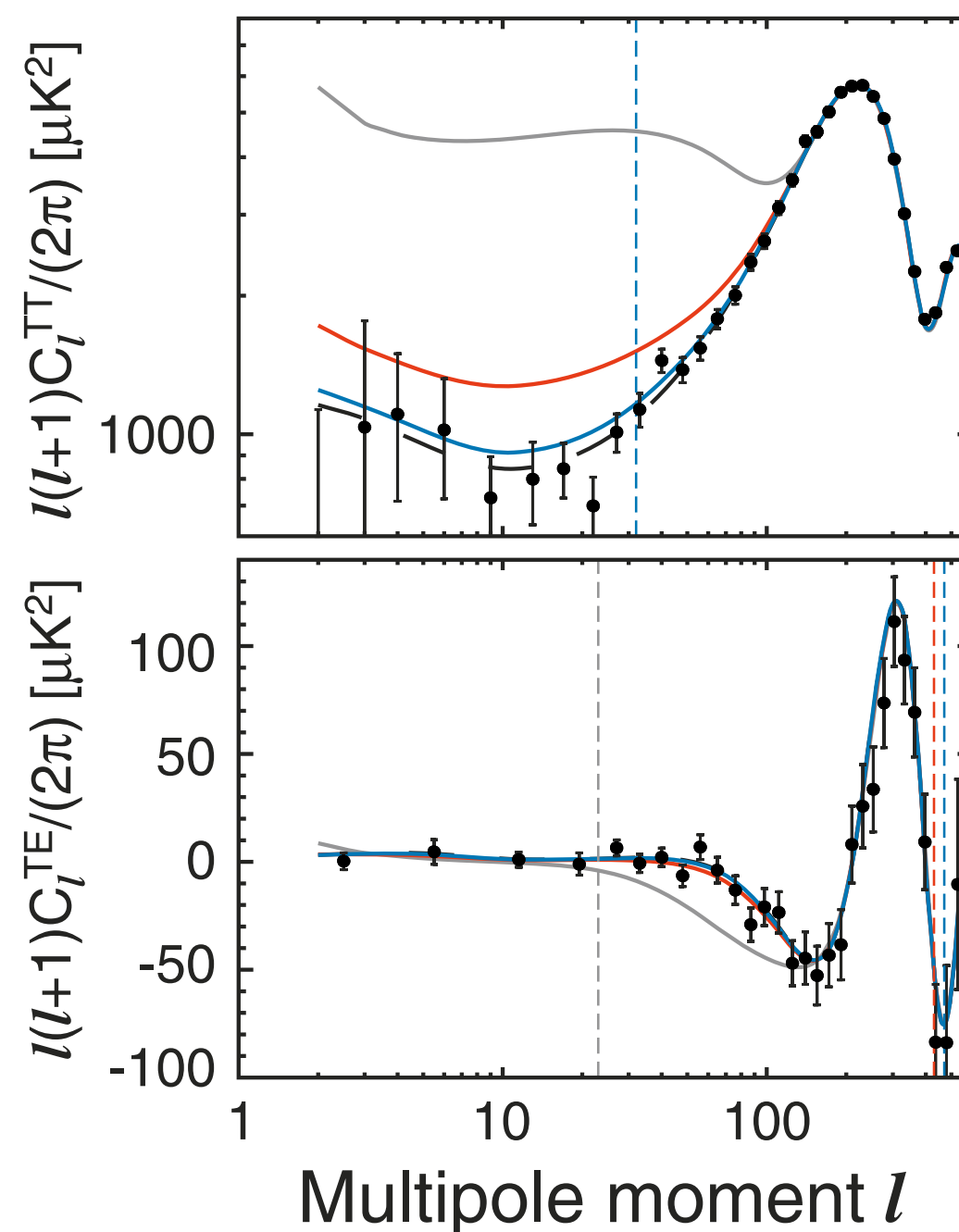
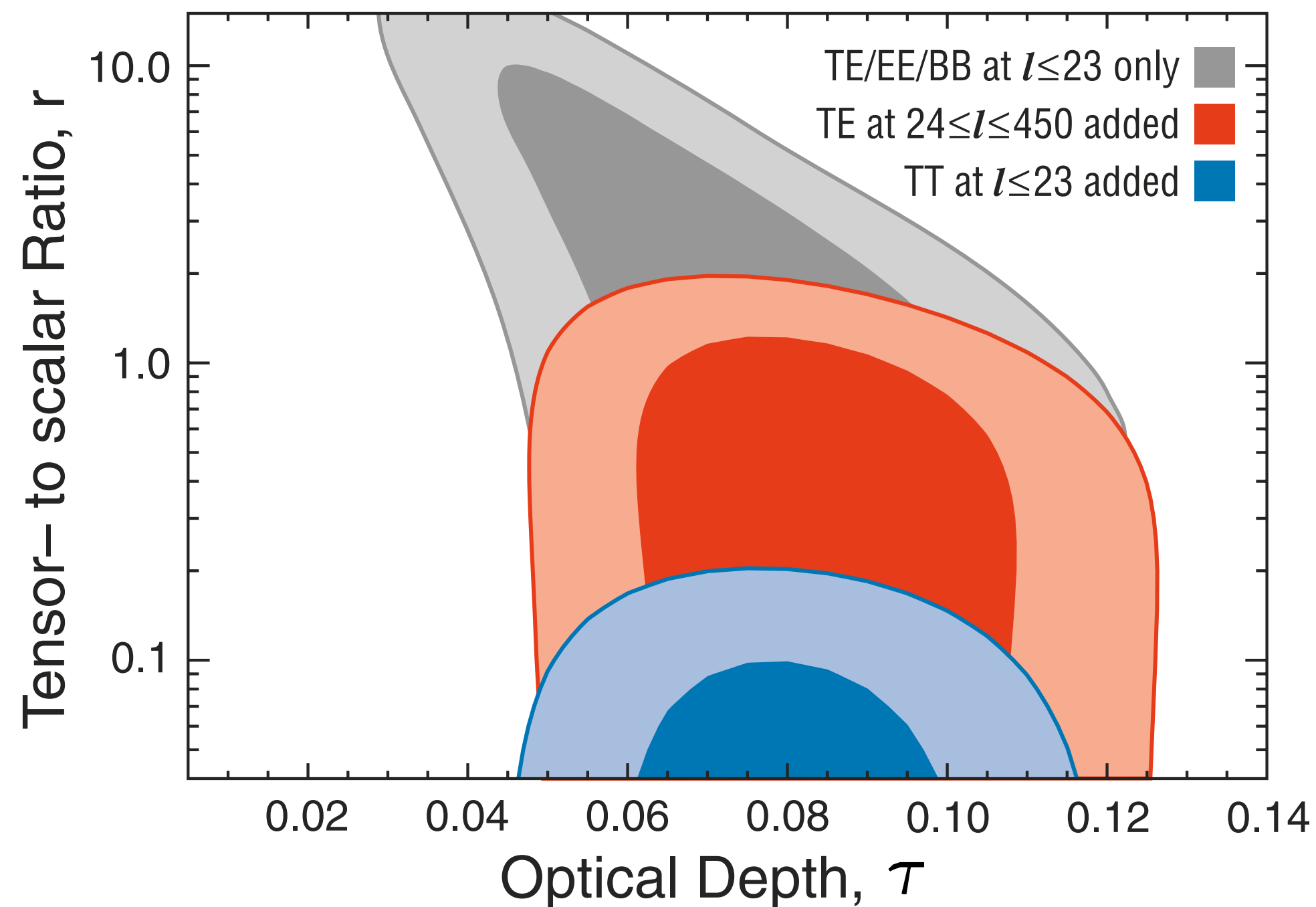


# Searching for Primordial Gravitational Waves in CMB

- Not only do inflation models produce density fluctuations, but also primordial gravitational waves
- Some predict the observable amount ( $r > 0.01$ ), some don't
- Current limit:  **$r < 0.22$**  (95%CL)
- Alternative scenarios (e.g., New Ekpyrotic) don't
- A powerful probe for testing inflation and testing specific models: next "Holy Grail" for CMBist

# How GW Affects CMB

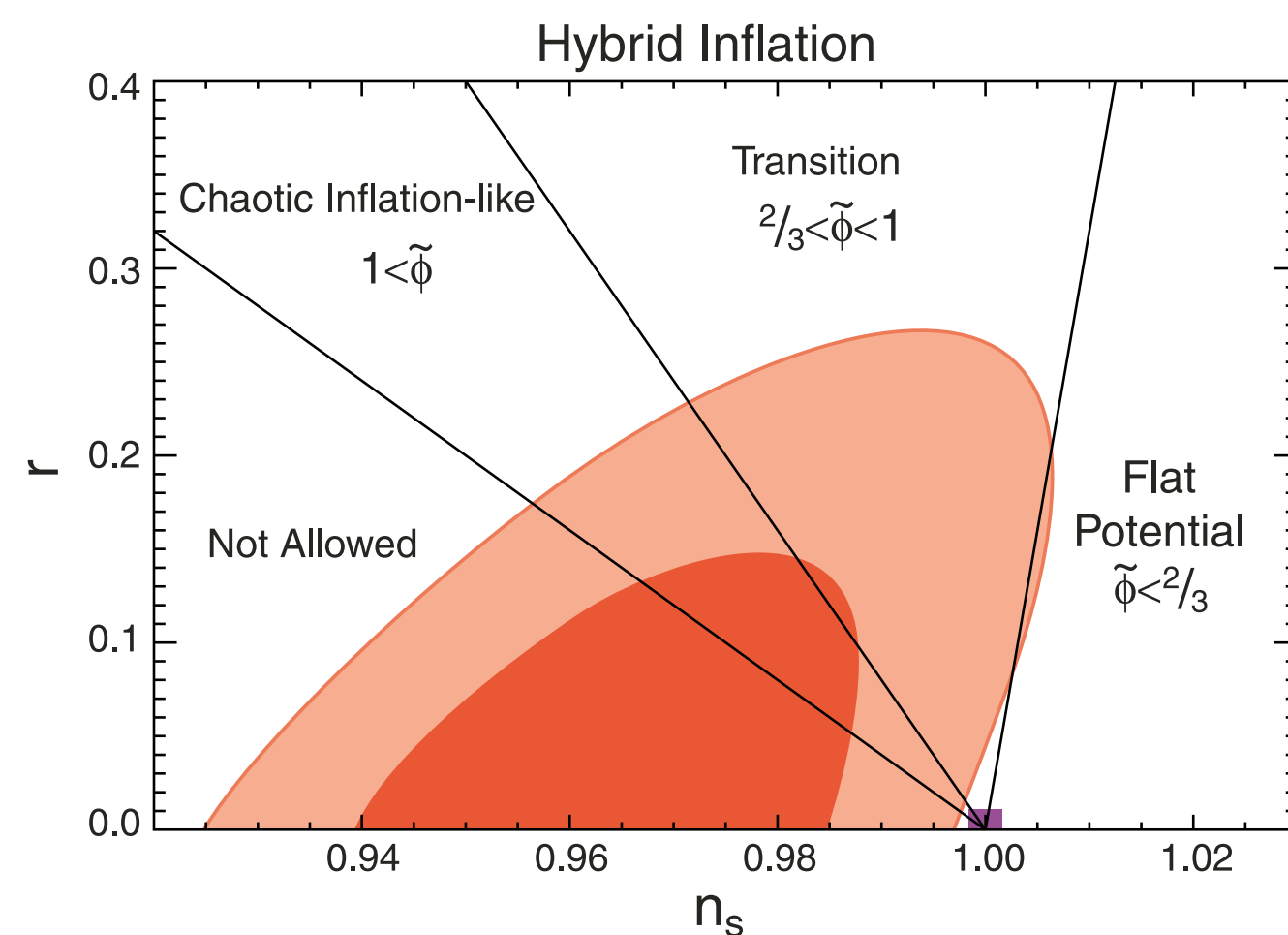
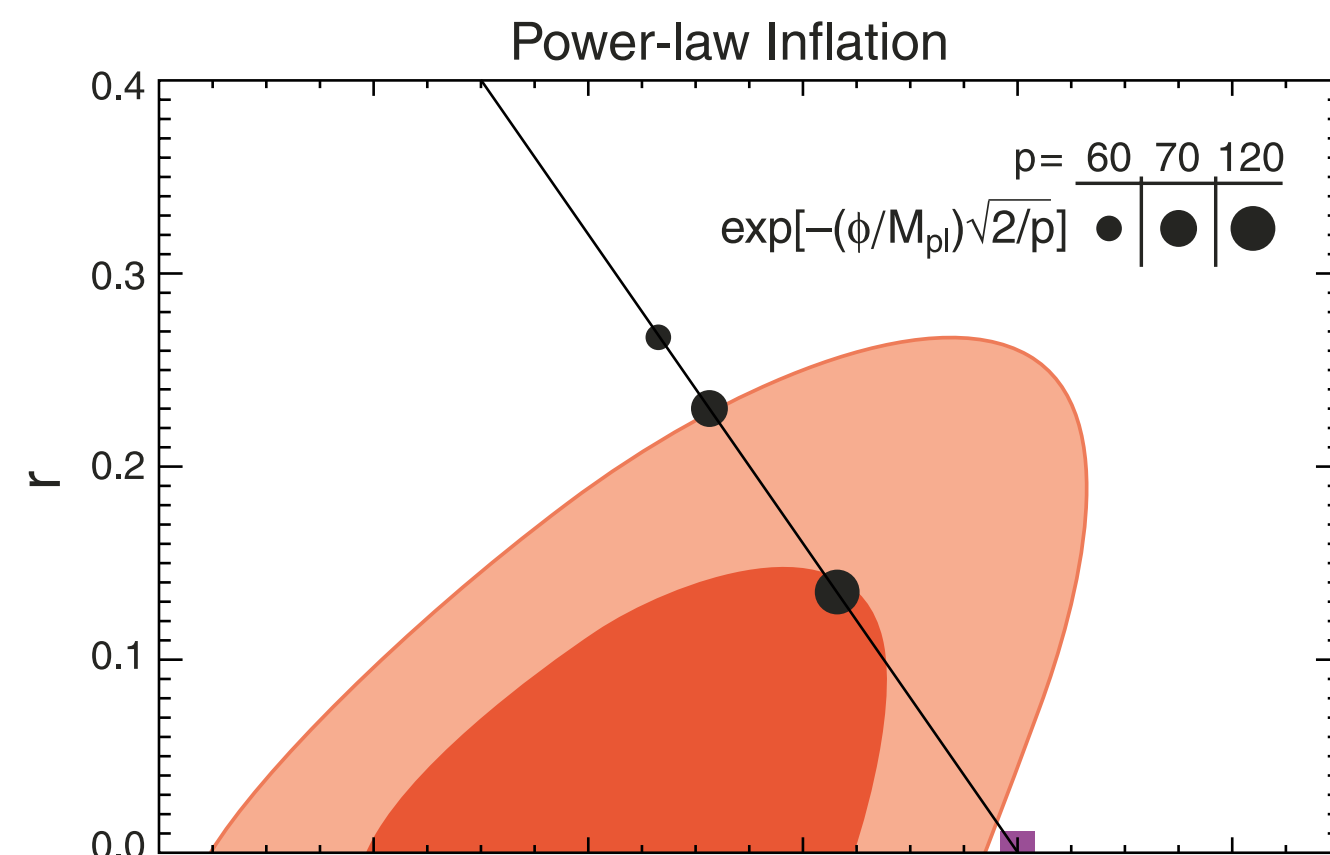
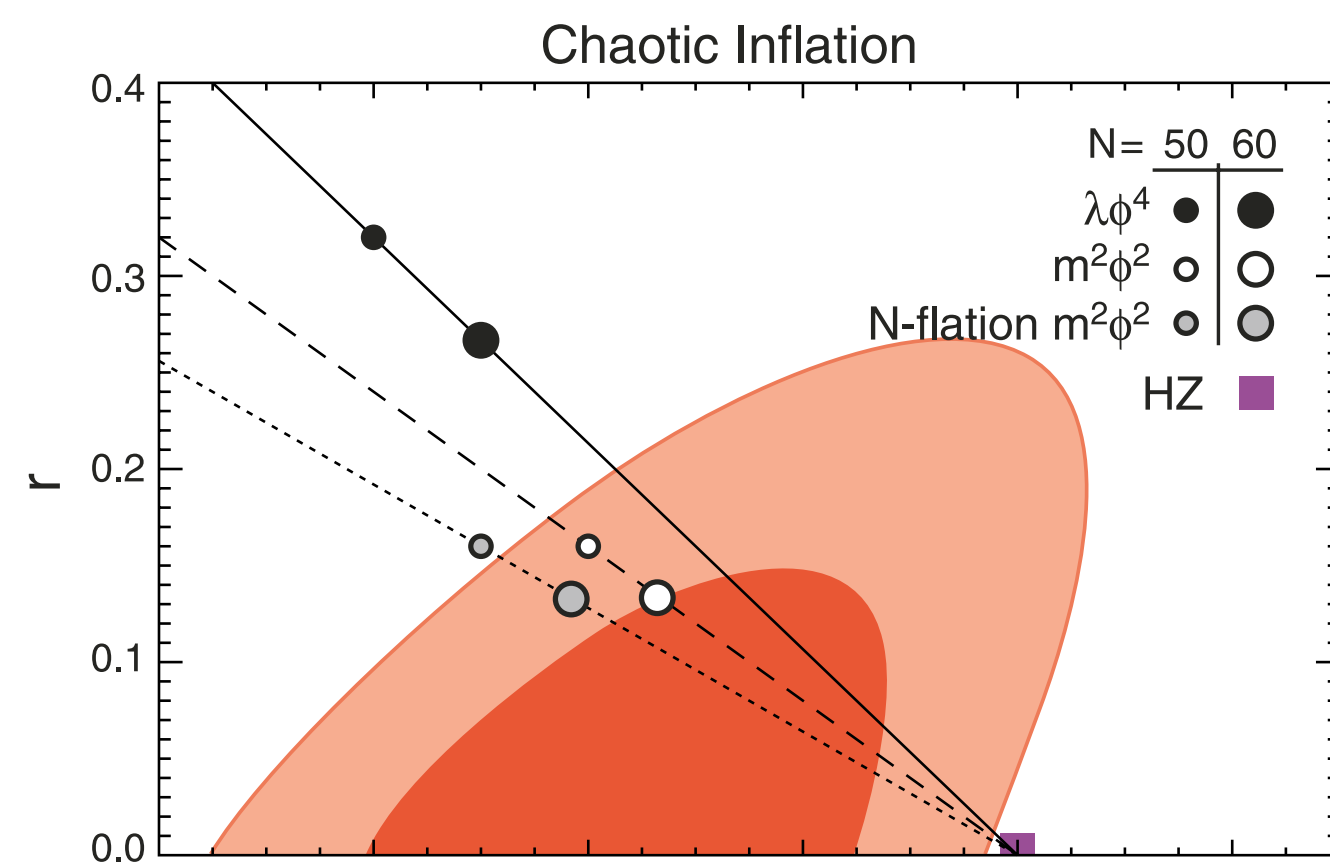
*Komatsu et al.*



- If all the other parameters ( $n_s$  in particular) are fixed...
  - Low- $l$  polarization gives  $r < 20$  (95% CL)
  - + high- $l$  polarization gives  $r < 2$  (95% CL)
  - + low- $l$  temperature gives  $r < 0.2$  (95% CL)

# Lowering a “Limbo Bar”

- $\lambda\varphi^4$  is totally out. (unless you invoke, e.g., non-minimal coupling, to suppress  $r$ ...)
- $m^2\varphi^2$  is within 95% CL.
  - Future WMAP data would be able to push it to outside of 95% CL, if  $m^2\varphi^2$  is not the right model.
- N-flation  $m^2\varphi^2$  (Easter&McAllister) is being pushed out
- PL inflation [ $a(t)\sim t^p$ ] with  $p<60$  is out.
- A blue index ( $n_s>1$ ) region of hybrid inflation is disfavored





# Gaussianity

- In the simplest model of inflation, the distribution of primordial fluctuations is close to a Gaussian with random phases.
- The level of non-Gaussianity predicted by the simplest model is well below the current detection limit.
- A convincing detection of primordial non-Gaussianity will rule out most of inflation models in the literature.
  - **Detection of non-Gaussianity would be a breakthrough in cosmology**

# Getting the Most Out of Fluctuations, $\delta(\mathbf{x})$

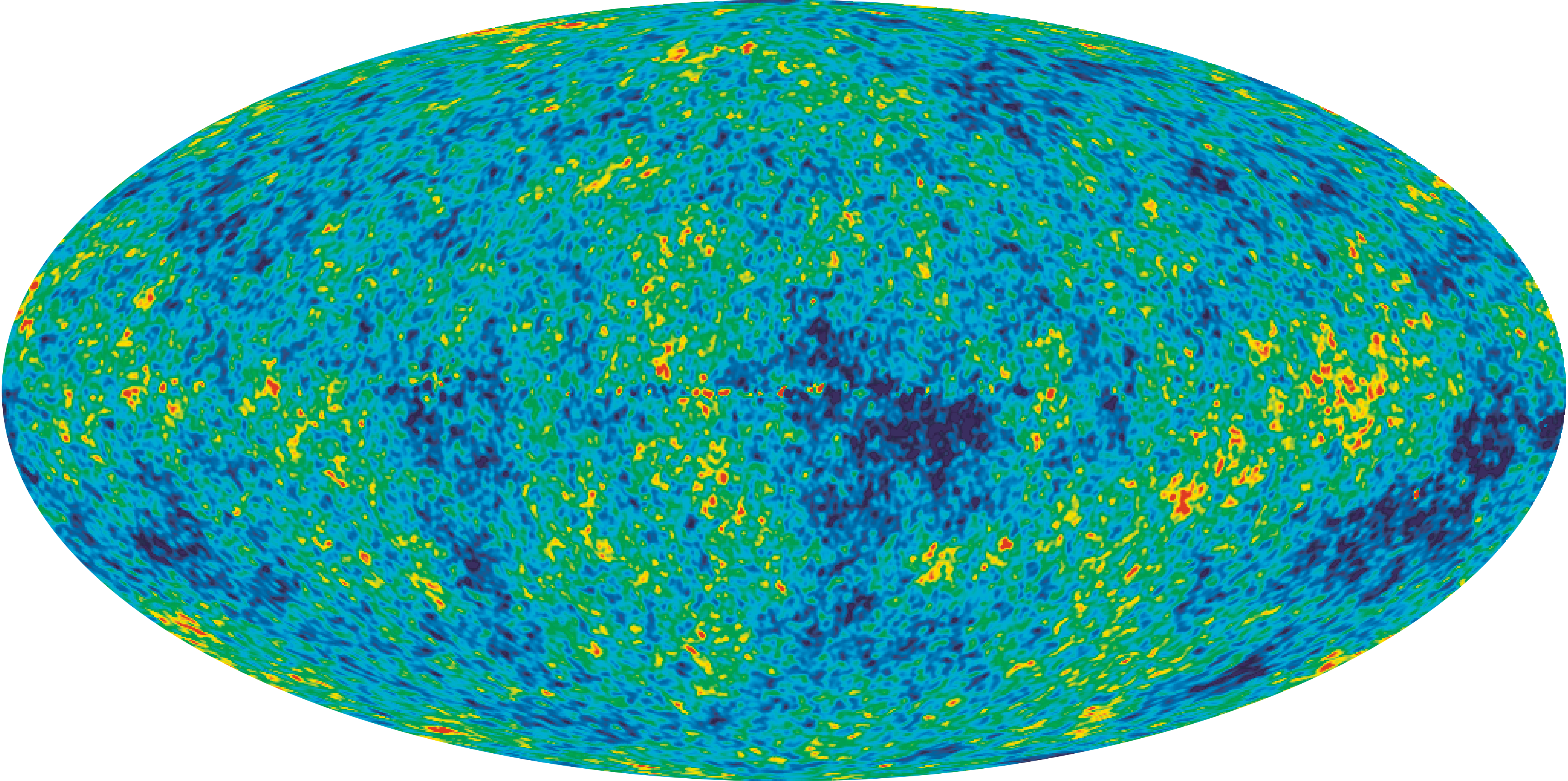
- In Fourier space,  $\delta(\mathbf{k}) = A(\mathbf{k})\exp(i\varphi_{\mathbf{k}})$ 
  - **Power:**  $P(\mathbf{k}) = \langle |\delta(\mathbf{k})|^2 \rangle = A^2(\mathbf{k})$
  - **Phase:**  $\varphi_{\mathbf{k}}$
- We can use the observed distribution of...
  - matter (e.g., galaxies, gas)
  - radiation (e.g., Cosmic Microwave Background)
- to learn about both  $P(\mathbf{k})$  and  $\varphi_{\mathbf{k}}$ .

# What About Phase, $\varphi_k$

- There were expectations also:
  - Random phases! (Peebles, ...)
- Collection of random, uncorrelated phases leads to the most famous probability distribution of  $\delta$ :

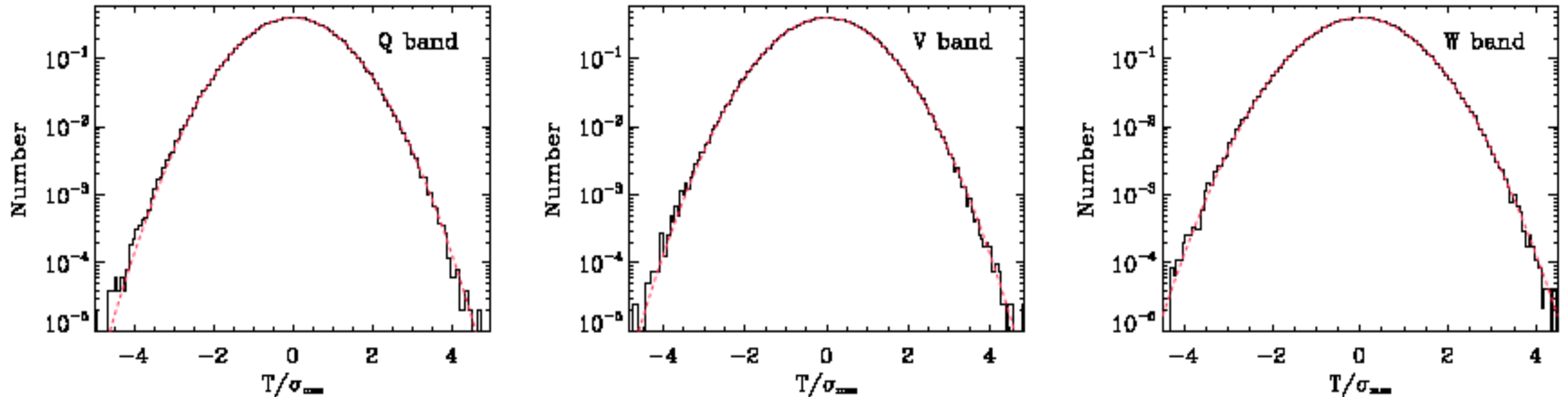
# **Gaussian Distribution**

# Gaussian?



WMAP 5-year

# Take One-point Distribution Function



- The one-point distribution of WMAP map looks pretty Gaussian.
  - Left to right: Q (41GHz), V (61GHz), W (94GHz).
- Deviation from Gaussianity is small, if any.

# Inflation Likes This Result

- According to inflation (Guth & Yi; Hawking; Starobinsky; Bardeen, Steinhardt & Turner), CMB anisotropy was created from **quantum fluctuations of a scalar field in Bunch-Davies vacuum** during inflation
- Successful inflation (with the expansion factor more than  $e^{60}$ ) *demands* the scalar field be almost interaction-free
- The wave function of free fields in the ground state is a Gaussian!

# But, Not Exactly Gaussian

- Of course, there are always corrections to the simplest statement like this
- For one, inflaton field **does** have interactions. They are simply weak – of order the so-called slow-roll parameters,  $\epsilon$  and  $\eta$ , which are  $O(0.01)$

# Simplified Treatment

- Let's try to capture field interactions, or whatever non-linearities that might have been there during inflation, by the following simple, order-of-magnitude form (*Komatsu & Spergel 2001*):

- $\Phi(\mathbf{x}) = \Phi_{\text{gaussian}}(\mathbf{x}) + f_{\text{NL}}[\Phi_{\text{gaussian}}(\mathbf{x})]^2$

Earlier work on this form:  
Salopek&Bond (1990); Gangui  
et al. (1994); Verde et al. (2000);  
Wang&Kamionkowski (2000)

- One finds  $f_{\text{NL}} = \mathcal{O}(0.01)$  from inflation (*Maldacena 2003*;  
*Acquaviva et al. 2003*)
- **This is a powerful prediction of inflation**



# Why Study Non-Gaussianity?

- Because a detection of  $f_{\text{NL}}$  has a best chance of **ruling out the largest class of inflation models.**
- Namely, it will rule out inflation models based upon
  - a single scalar field with
  - the canonical kinetic term that
  - rolled down a smooth scalar potential slowly, and
  - was initially in the Bunch-Davies vacuum.
- ***Detection of non-Gaussianity would be a major breakthrough in cosmology.***

# Tool: Bispectrum

- **Bispectrum = Fourier Trans. of 3-pt Function**
- **The bispectrum vanishes** for Gaussian fluctuations with random phases.
- Any non-zero detection of the bispectrum indicates the presence of (some kind of) non-Gaussianity.
- A sensitive tool for finding non-Gaussianity.

# No Detection at $>95\%CL$

- $-9 < f_{NL} < 111$  (95% CL)
- $f_{NL} = 51 \pm 30$  (68% CL)
- Latest reanalysis:  $f_{NL} = 38 \pm 20$  (68% CL) [Smith et al.]
- These numbers mean that the primordial curvature perturbations are Gaussian to **0.1% level**.
  - This result provides the strongest evidence for quantum origin of primordial fluctuations during inflation.

# Summary

- The WMAP 5-year data indicate that the simplest cosmological model that fits that the data has 6 parameters: the amplitude of fluctuations, baryon density, dark matter density, dark energy density, the optical depth, and  $n_s$ .
- Other parameters are consistent with the standard values:  $N_V=4.4\pm 1.5$ ,  $\sum m_\nu < 0.67\text{eV}$ , ...
- No detection of gravitational waves ( $r < 0.22$ ) or non-Gaussianity ( $f_{NL}=38\pm 20$ ) **yet**
- I didn't have time to talk about it, but the spatial geometry of the universe is flat to 1%, and the dark energy is consistent with C.C. to 10%.

# Looking Ahead...

- With more WMAP observations, exciting discoveries may be waiting for us. Two examples for which we might be seeing some hints from the 5-year data:
  - Non-Gaussianity: If  $f_{\text{NL}} \sim 40$ , we will see it at  $\sim 2.5$  sigma level with 9 years of data.
  - Gravitational waves ( $r$ ) and tilt ( $n_s$ ) :  $m^2\varphi^2$  can be pushed out of the favorable parameter region
    - More, maybe seeing a hint of it if  $m^2\varphi^2$  is indeed the correct model?!