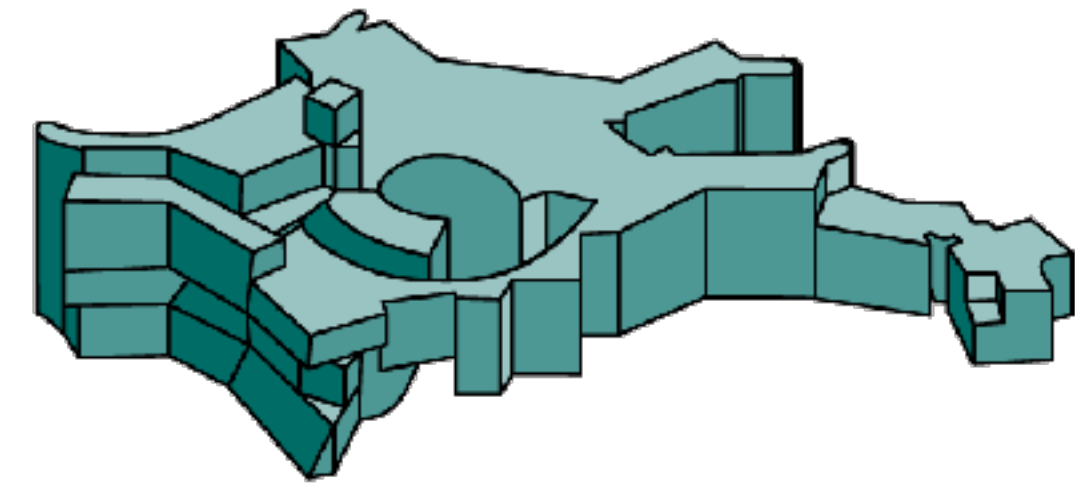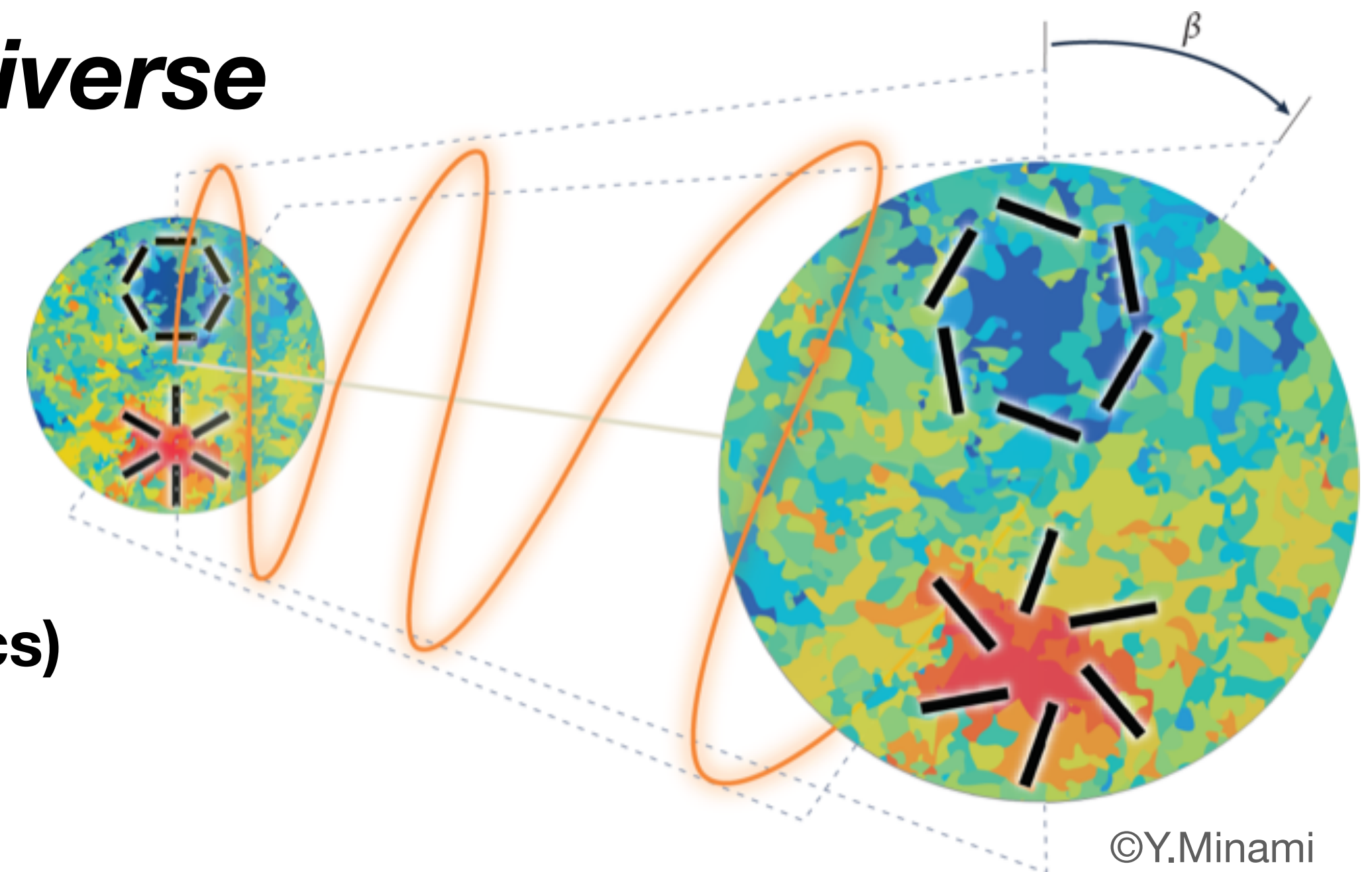$$I_{CS} = \int d^4x \sqrt{-g}\left(-\frac{\alpha}{4f}\chi F\tilde{F}\right)$$

MAX-PLANCK-INSTITUT
FÜR ASTROPHYSIK

Parity Violation in Cosmology

In search of new physics for the Universe

Eiichiro Komatsu (Max Planck Institute for Astrophysics)
DAMTP Cosmology Lunch, University of Cambridge
March 11, 2024

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Overarching Theme
Let's find new physics!

- The current cosmological model (*flat ΛCDM*) **requires** new physics beyond the standard model of elementary particles and fields.

  - What is dark matter (*CDM*)?

  - What is dark energy (*Λ*)?

  - Why is the spatial geometry of the Universe Euclidean (*flat*)?

  - What powered the Big Bang?

Overarching Theme

There are many ideas, but how can we make progress?

- The current cosmological model (*flat ΛCDM*) **requires** new physics beyond the standard model of elementary particles and fields.

  - What is dark matter (*CDM*)? => CDM, WDM, FDM, …

  - What is dark energy (*Λ*)? => Dynamical field, modified gravity, quantum gravity, …

  - Why is the spatial geometry of the Universe Euclidean (*flat*)? => Inflation, contracting universe, …

  - What powered the Big Bang? => Scalar field, gauge field, …

Ove...

New in cosmology!

Violation of parity symmetry may hold the answer to these fundamental questions.

- The current cosmological model (*flat ΛCDM*) **requires** new physics beyond the standard model of elementary particles and fields.

  - What is dark matter (*CDM*)? => CDM, WDM, FDM, …

  - What is dark energy (*Λ*)? => Dynamical field, modified gravity, quantum gravity, …

  - Why is the spatial geometry of the Universe Euclidean (*flat*)? => Inflation, contracting universe, …

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Available also at arXiv:2202.13919

Review Article | Published: 18 May 2022

New physics from the polarized light of the cosmic microwave background

Eiichiro Komatsu ✉

Key Words:
1. Cosmic Microwave Background (CMB)
2. Polarization
3. Parity Symmetry

Lectures & Reviews

2023

▷ Lecture Slides: "**Parity Violation in Cosmology**" [7 x 85 min]

  ▷ MC Specialized Course, Department of Physics, Nagoya University (June 6–30)

   ▷ The syllabus is available **here**.

   ▷ Reference: "*New Physics from the Polarized Light of the Cosmic Microwave Background*"

    ▷ **Nature Reviews Physics, 4, 452-469 (2022 May 18)**. You can have access to the full text via **this link**. Supplementary information is available **here**.

  ▷ **Lecture 1**: What is parity symmetry? (PDF 3.9 MB; last updated, June 5, 2023)

   ▷ 1.1 Parity

   ▷ 1.2 Vector and pseudovector

   ▷ 1.3 Discovery of parity violation in β-decay

   ▷ 1.4 Helicity

  ▷ **Lecture 2**: Chern-Simons interaction (PDF 1.6 MB; last updated, June 8, 2023)

   ▷ 2.1 Parity symmetry in electromagnetism (EM)

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Probing Parity Symmetry
Definition

- **Parity transformation = Inversion of all spatial coordinates**

  - (x, y, z) –> (-x, -y, -z)

- Parity symmetry in physics states:

  - *The laws of physics are invariant under inversion of all spatial coordinates.*

- Violation of parity symmetry = The laws of physics are **not** invariant under…

- Ask "*When we observe a certain phenomenon in nature, do we also observe its mirror image(*) with equal probability?*"

  - (*) "Mirror image" is an ambiguous word. A parity transformation is (x, y, z) –> (-x, -y, -z), whereas a "mirror image" often refers to, e.g., (x, y, z) –> (-x, y, z), where only one of (x,y,z) is flipped.

Do we also observe this with equal probability?

Note that this is not full parity transformation, as only one axis is flipped.

Parity and Rotation

- Parity transformation (***x*** –> -***x***) and 3d rotation (***x*** –> R***x***) are different.

  - R is a continuous transformation and the determinant of R is det(R) = +1.

 - Parity is a discrete transformation and the **determinant is –1**, as

$$
\begin{pmatrix} x \\ y \\ z \end{pmatrix} \rightarrow \begin{pmatrix} -x \\ -y \\ -z \end{pmatrix} = \begin{pmatrix} -1 & 0 & 0 \\ 0 & -1 & 0 \\ 0 & 0 & -1 \end{pmatrix} \begin{pmatrix} x \\ y \\ z \end{pmatrix}
$$

$$\begin{pmatrix} x \\ y \\ z \end{pmatrix} \rightarrow \begin{pmatrix} -x \\ -y \\ -z \end{pmatrix} = \begin{pmatrix} -1 & 0 & 0 \\ 0 & -1 & 0 \\ 0 & 0 & -1 \end{pmatrix} \begin{pmatrix} x \\ y \\ z \end{pmatrix}$$

Parity = Mirror + 2d Rotation

- One may think of parity transformation as a mirror in one of the coordinates (e.g., z –> -z) and **2d** rotation by π in the others.
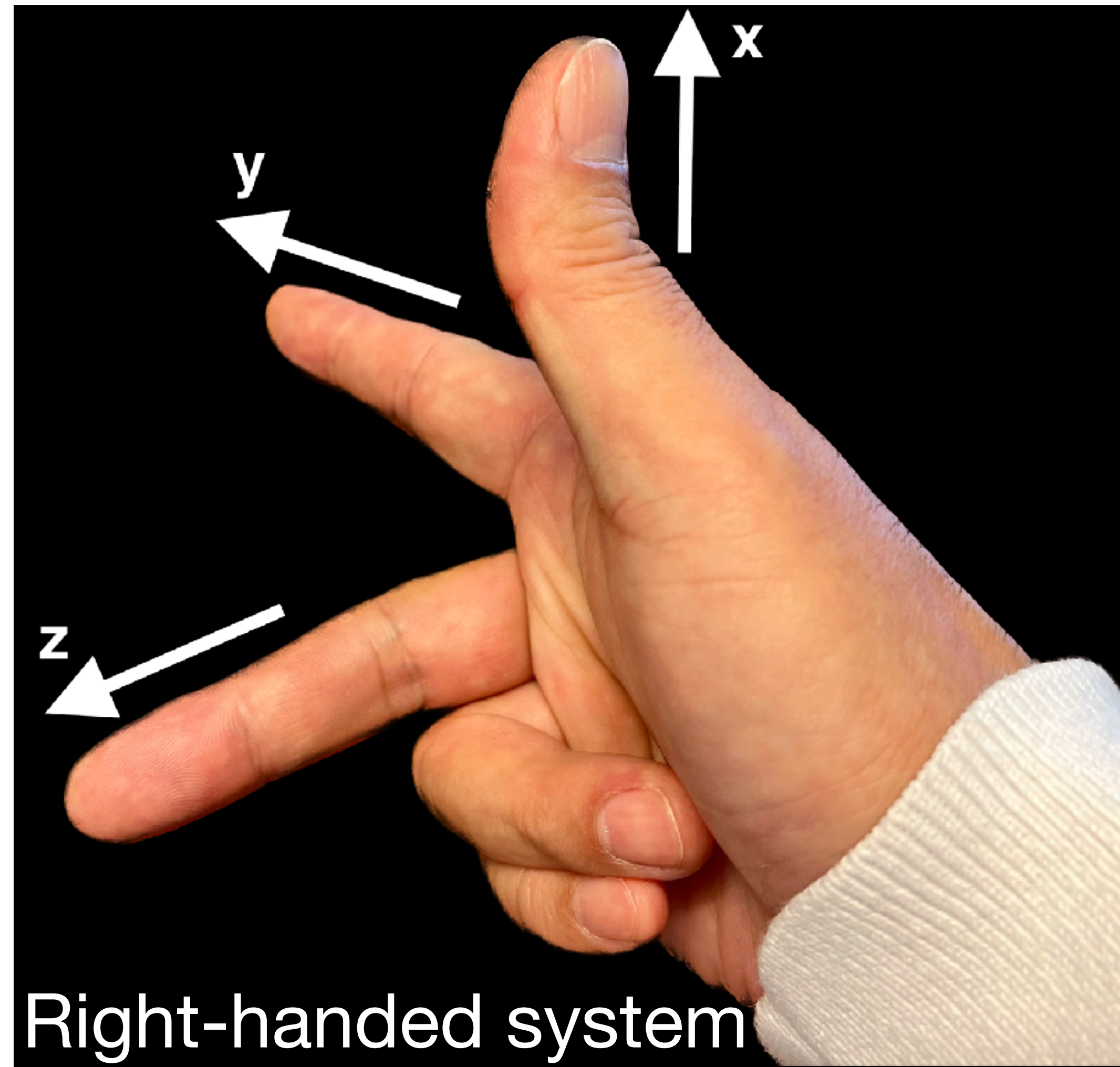
- Let's demonstrate it!
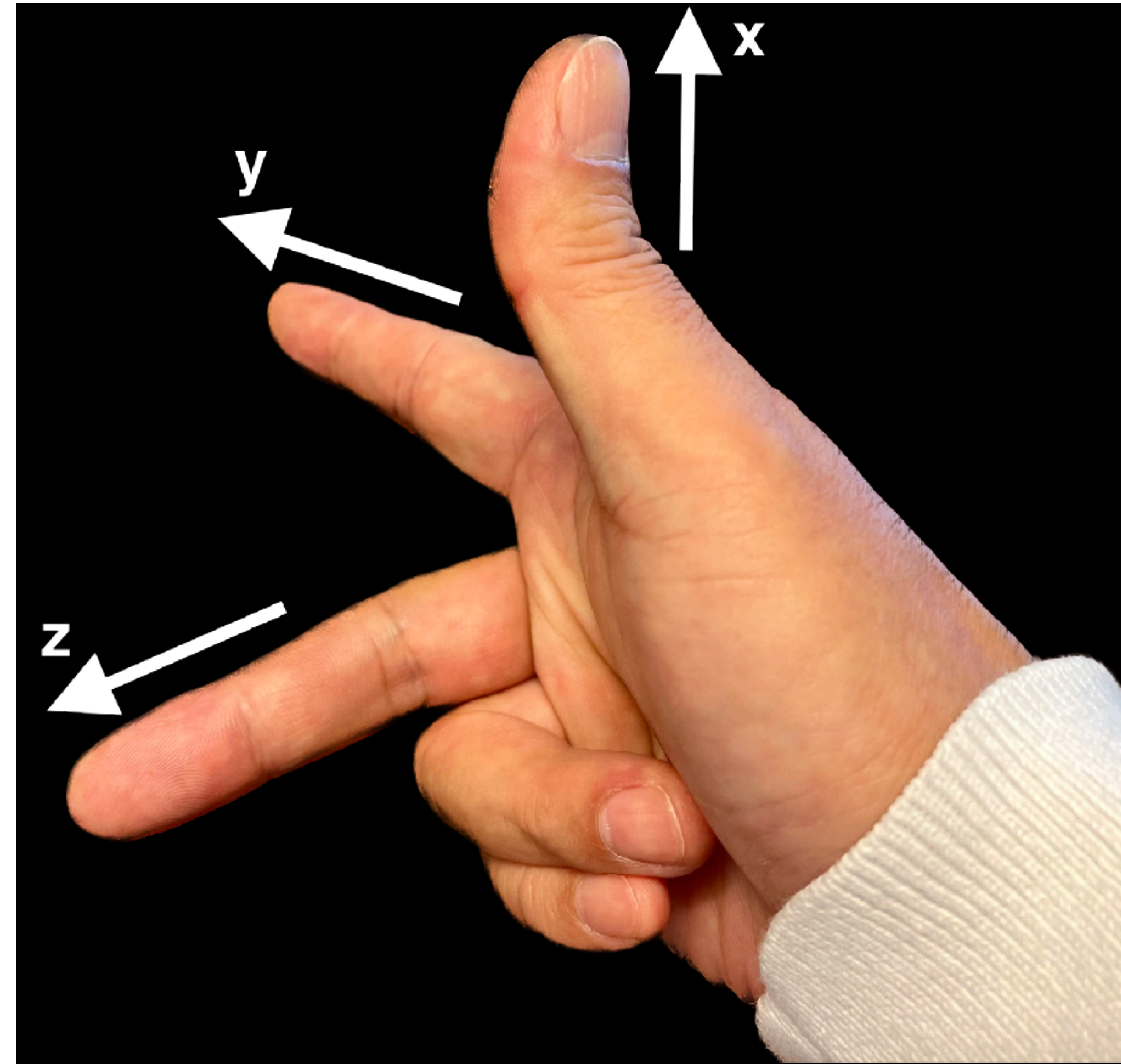
11

$$\begin{pmatrix} x \\ y \\ z \end{pmatrix} \rightarrow \begin{pmatrix} -x \\ -y \\ -z \end{pmatrix} = \begin{pmatrix} -1 & 0 & 0 \\ 0 & -1 & 0 \\ 0 & 0 & \boxed{-1} \end{pmatrix} \begin{pmatrix} x \\ y \\ z \end{pmatrix}$$

x

y

z' = -z

Left-handed system

$z \rightarrow z' = -z$

x

y

z

Right-handed system

$$\begin{pmatrix} x \\ y \\ z \end{pmatrix} \rightarrow \begin{pmatrix} -x \\ -y \\ -z \end{pmatrix} = \begin{pmatrix} -1 & 0 & 0 \\ 0 & -1 & 0 \\ 0 & 0 & -1 \end{pmatrix} \begin{pmatrix} x \\ y \\ z \end{pmatrix}$$
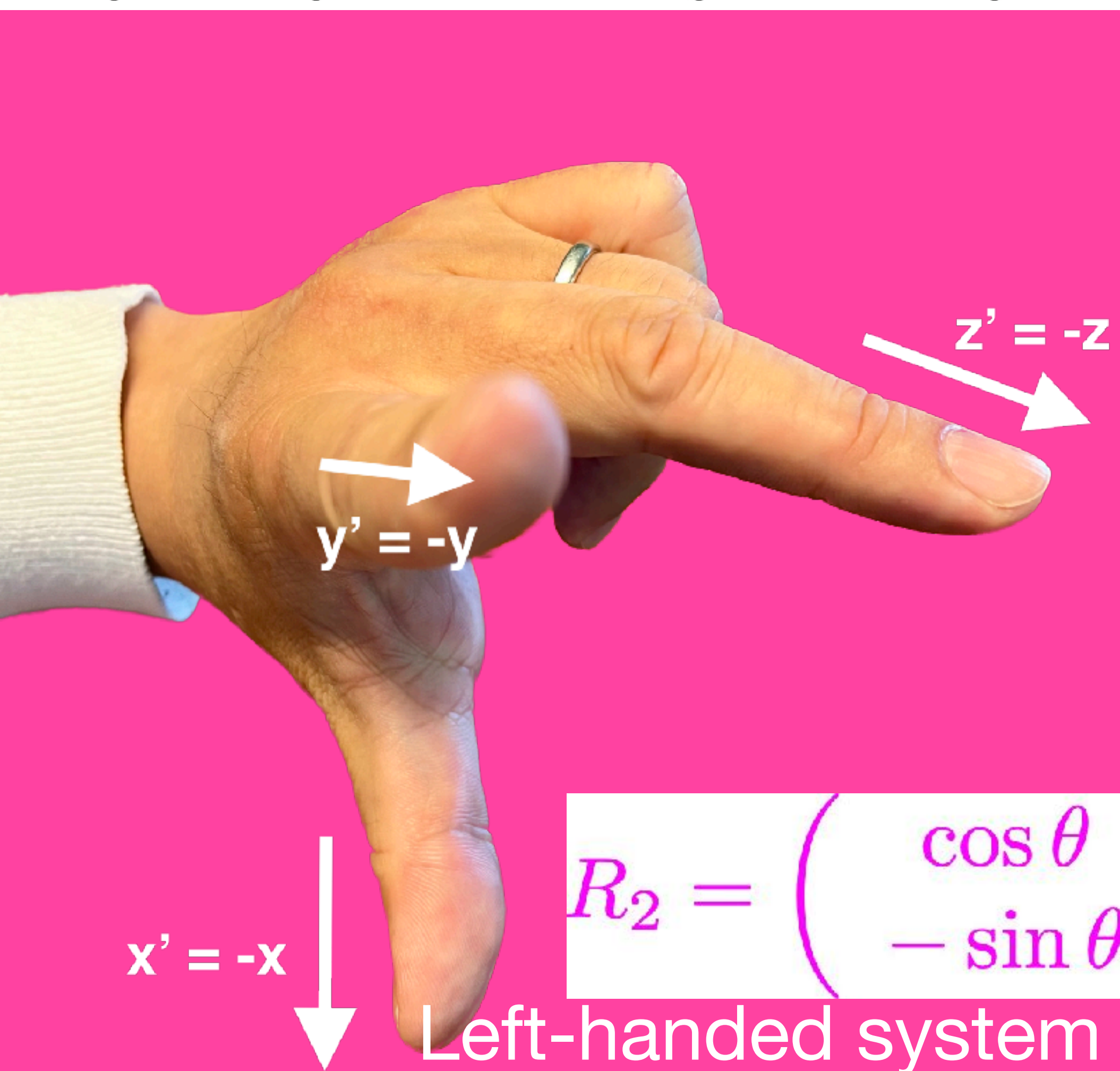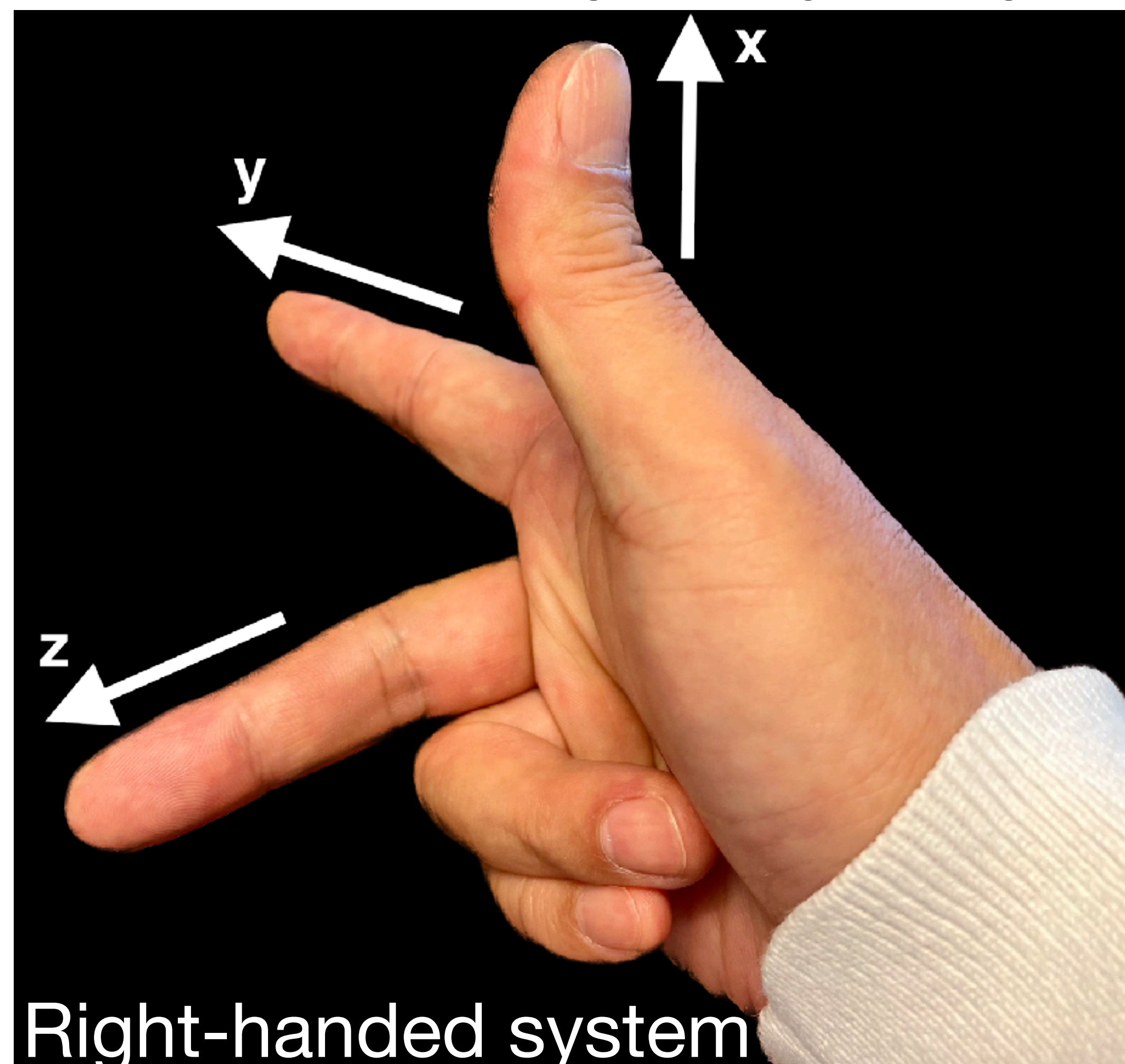

z' = -z

y' = -y

x' = -x

Rotation In x-y
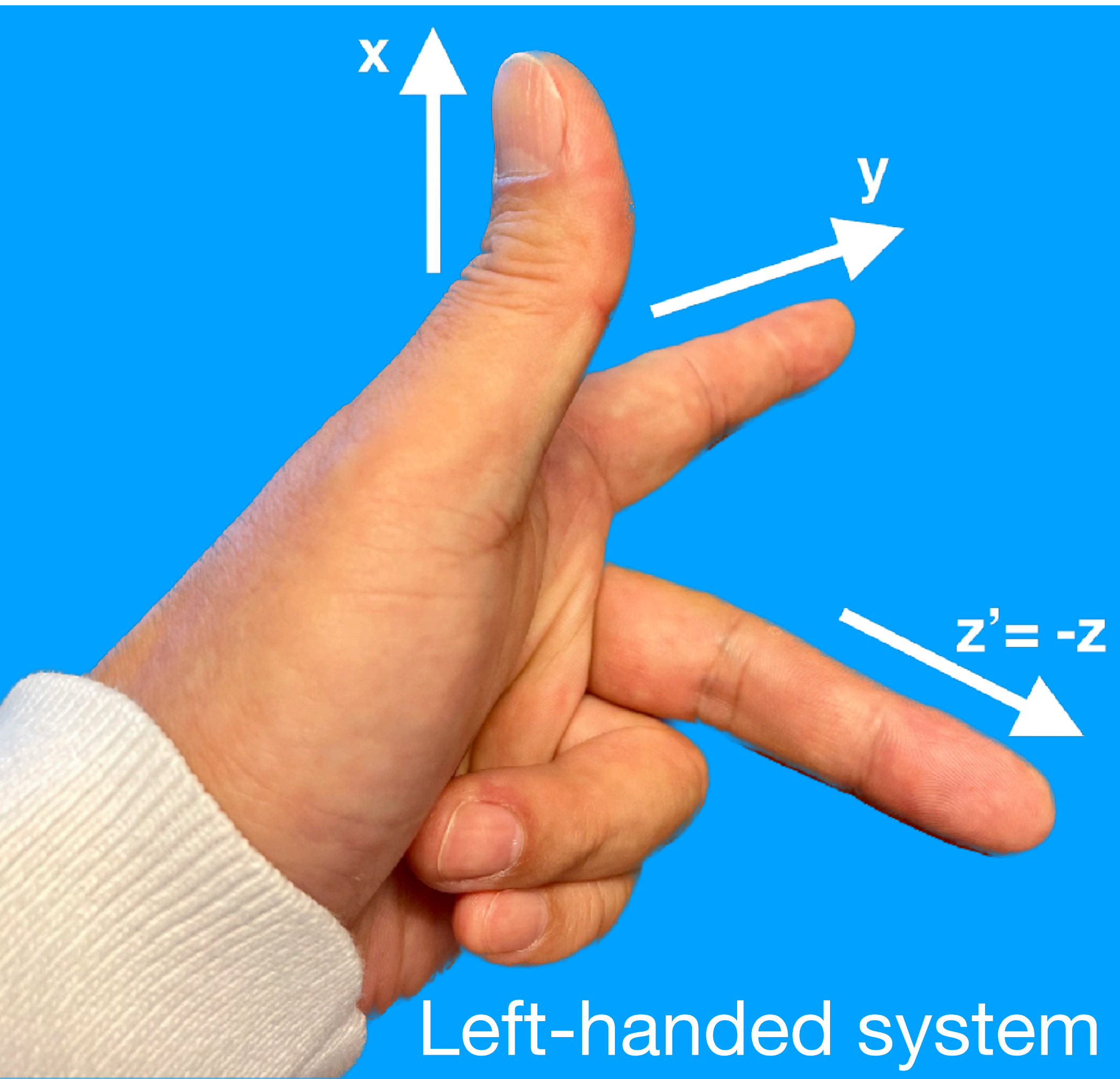
$$R_2 = \begin{pmatrix} \cos\theta & \sin\theta \\ -\sin\theta & \cos\theta \end{pmatrix}$$

Left-handed system **with θ $\overset{13}{=}$ π**

x

y

z

Right-handed system

Parity Transformation: Vector
E.g., momentum, electric field

$$\mathbf{p} = p_x \hat{e}_x + p_y \hat{e}_y + p_z \hat{e}_z$$

$\hat{e}_i$ is a unit vector.

$$\mathbf{p} = p'_x \hat{e}'_x + p'_y \hat{e}'_y + p'_z \hat{e}'_z$$
$$= -p'_x \hat{e}_x - p'_y \hat{e}_y - p'_z \hat{e}_z$$
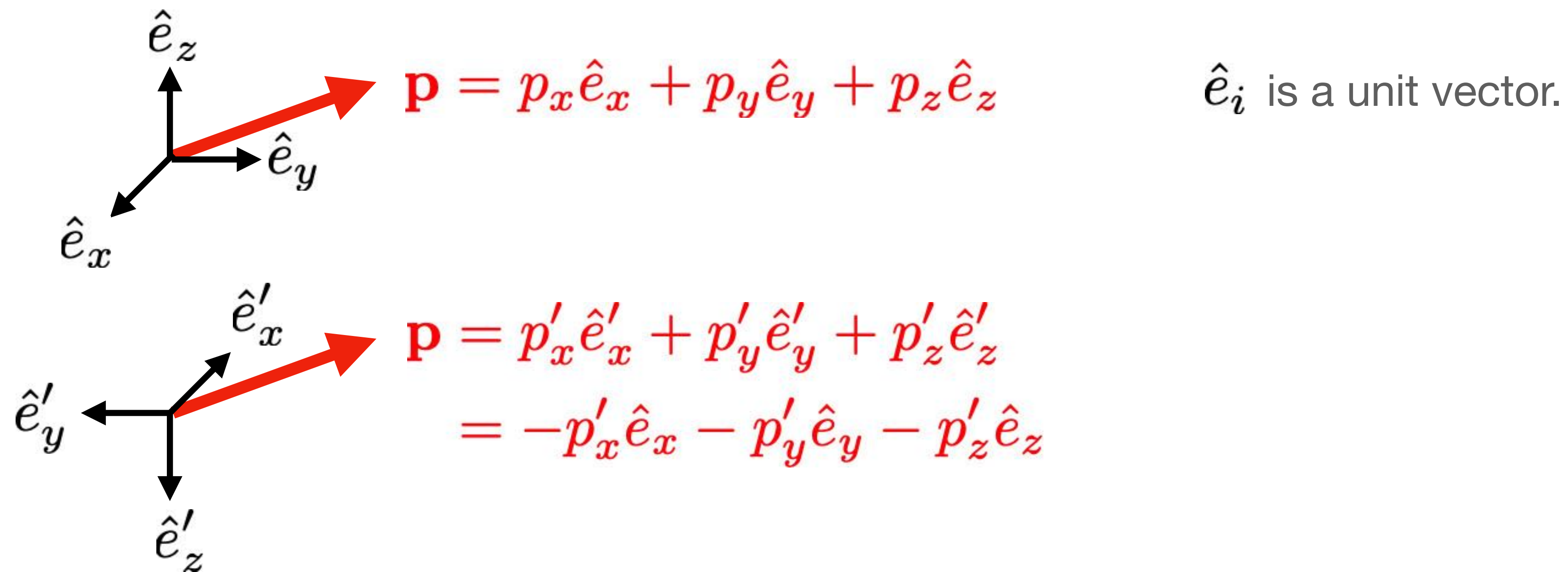
- **p** is the same vector, written using two different basis vectors.

- Therefore, **p**'s components are transformed as $(p'_x, p'_y, p'_z) = (-p_x, -p_y, -p_z)$

Parity Transformation: Pseudovector
E.g., angular momentum, magnetic field

- Orbital angular momentum, $\mathbf{L} = \mathbf{r} \times \mathbf{p}$, is a *pseudovector*. Its *components* do **not** change under parity transformation: $(L'_x, L'_y, L'_z) = (L_x, L_y, L_z)$

  - Both $\mathbf{r} = (X, Y, Z)$ and $\mathbf{p} = (p_x, p_y, p_z)$ are vectors whose components change sign. Thus, their products do not change, e.g.,

$$L'_x = Y'p'_z - Z'p'_y$$
$$= (-Y)(-p_z) - (-Z)(-p_y)$$
$$= L_x$$
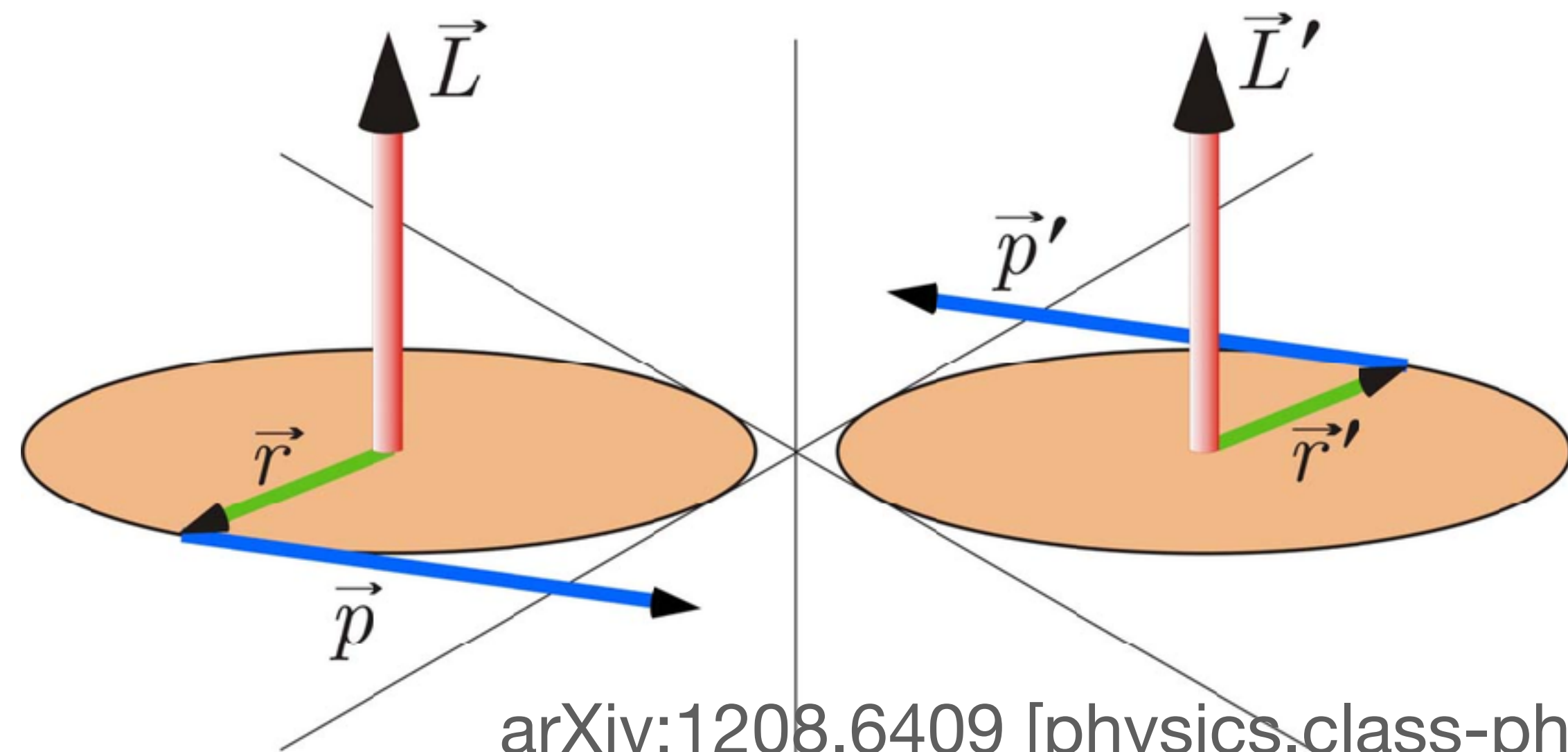
Parity Transformation: Pseudoscalar

How to test parity symmetry?

- A dot product of a vector and a pseudovector is a **pseudoscalar**.

  - Like a scalar, a pseudoscalar is invariant under rotation.

  - But, a pseudoscalar changes sign under parity transformation.

- **Experimental test of parity symmetry**: Construct a pseudoscalar and see if the average value is zero. If not, the system violates parity symmetry!

  - *Example*: a dot product of particle A's momentum and particle B's angular momentum: $\mathbf{p}_A \cdot \mathbf{L}_B$. Measure this and average over many trials. Does the average vanish, $\langle \mathbf{p}_A \cdot \mathbf{L}_B \rangle = 0$?

Experimental Test of Parity Conservation in Beta Decay*

C. S. Wu, *Columbia University, New York, New York*

AND

E. Ambler, R. W. Hayward, D. D. Hoppes, and R. P. Hudson, *National Bureau of Standards, Washington, D. C.*
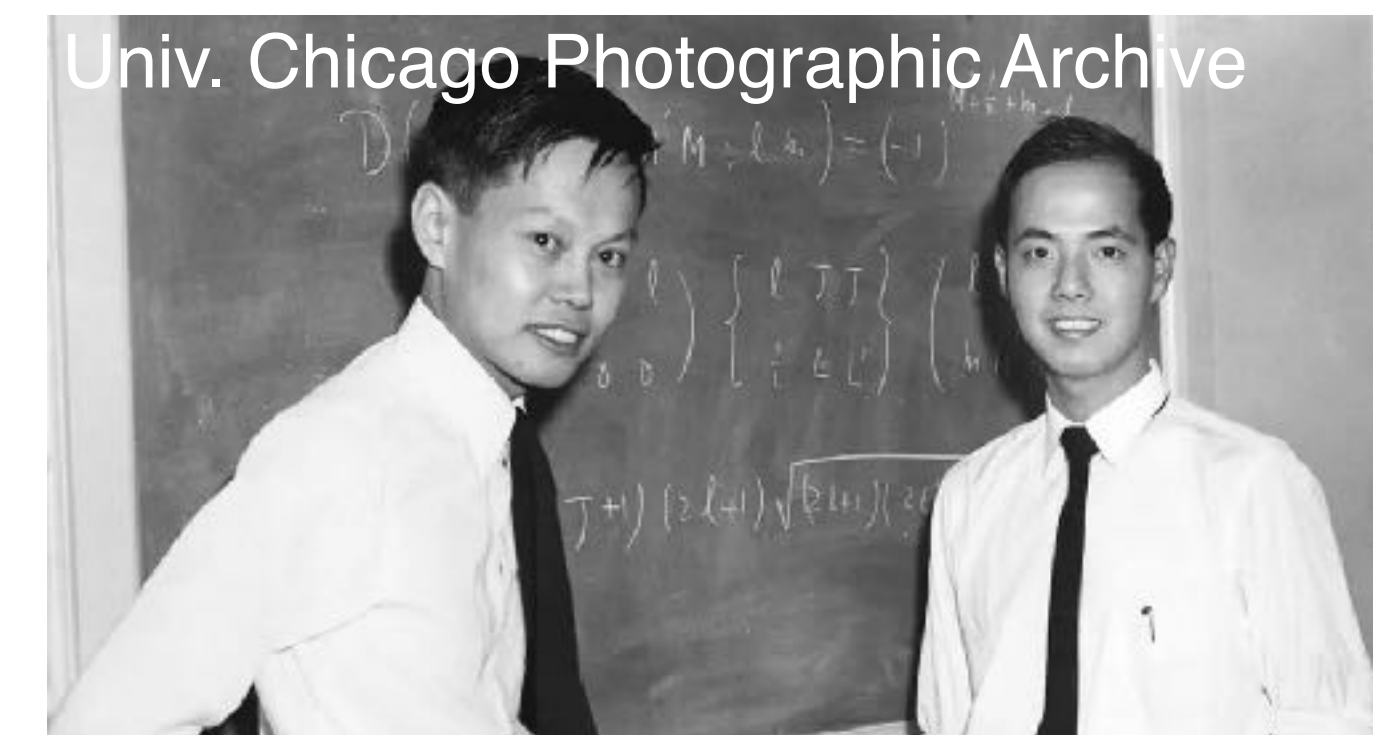
(Received January 15, 1957)

IN a recent paper[1] on the question of parity in weak interactions, Lee and Yang critically surveyed the experimental information concerning this question and reached the conclusion that there is no existing evidence either to support or to refute parity conservation in weak interactions. They proposed a number of experiments on beta decays and hyperon and meson decays which would provide the necessary evidence for parity conservation or nonconservation. In beta decay, one could measure the angular distribution of the electrons coming from beta decays of polarized nuclei. If an asymmetry in the

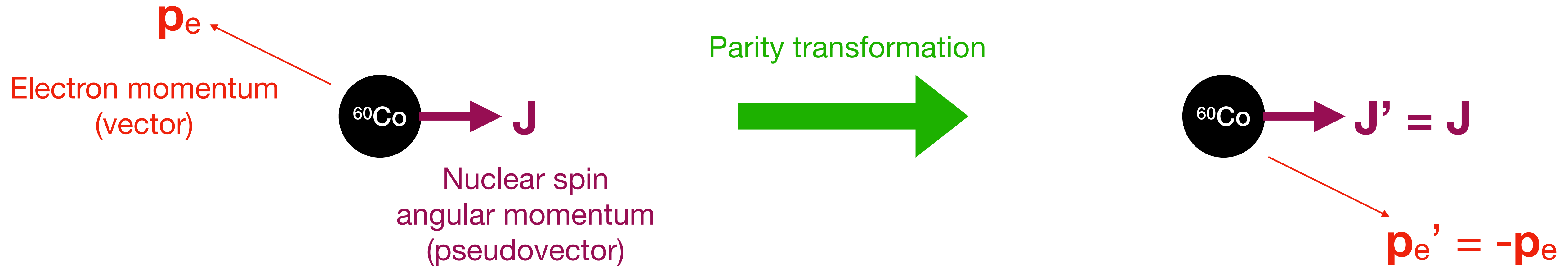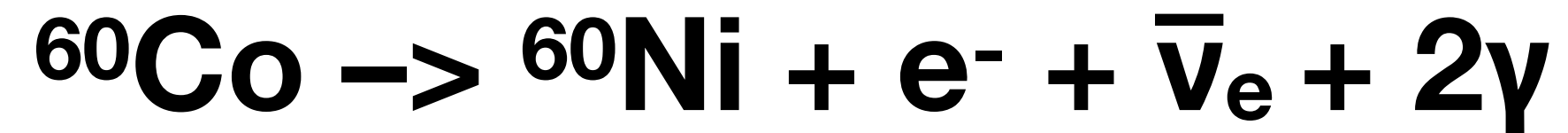Smithsonian Institution Archives

Chien-Shiung Wu

Univ. Chicago Photographic Archive

Chen-Ning Yang   Tsung-Dao Lee

The Wu Experiment of β-decay

^{60}Co –> ^{60}Ni + e$^-$ + $\overline{\nu}_e$ + 2γ

p$_e$

Electron momentum
(vector)

^{60}Co ⟶ **J**

Nuclear spin
angular momentum
(pseudovector)

Parity transformation

^{60}Co ⟶ **J' = J**

p$_e$' = -p$_e$

- Electrons must be emitted with equal probability in all directions relative to **J**, if parity symmetry is respected in β-decay.

  - This was not observed: $\langle \mathbf{p}_e \cdot \mathbf{J} \rangle \neq 0$. **Parity symmetry is violated in β-decay!**

Initial reaction

Many physicists did not believe it initially.

Bildarchiv der ETH-Bibliothek

- To Lee and Yang's theoretical paper on parity violation in β-decay:

  - Wolfgang Pauli said, "*Ich glaube aber nicht, daß der Herrgott ein schwacher Linkshänder ist*" (I do not believe that the Lord is a weak left-hander).

- To Wu's discovery paper:

  - Wolfgang Pauli said, "*Sehr aufregend. Wie sicher ist die Nachricht?*" (Very exciting. How sure is this news?)

- **This was shocking news. The weak interaction distinguishes between left and right!**

- In this talk we ask, "*Does the Universe distinguish between left and right?*" Most scientists answer, "No, of course it doesn't". **That may well be true, but one must at least have a look to be sure!**
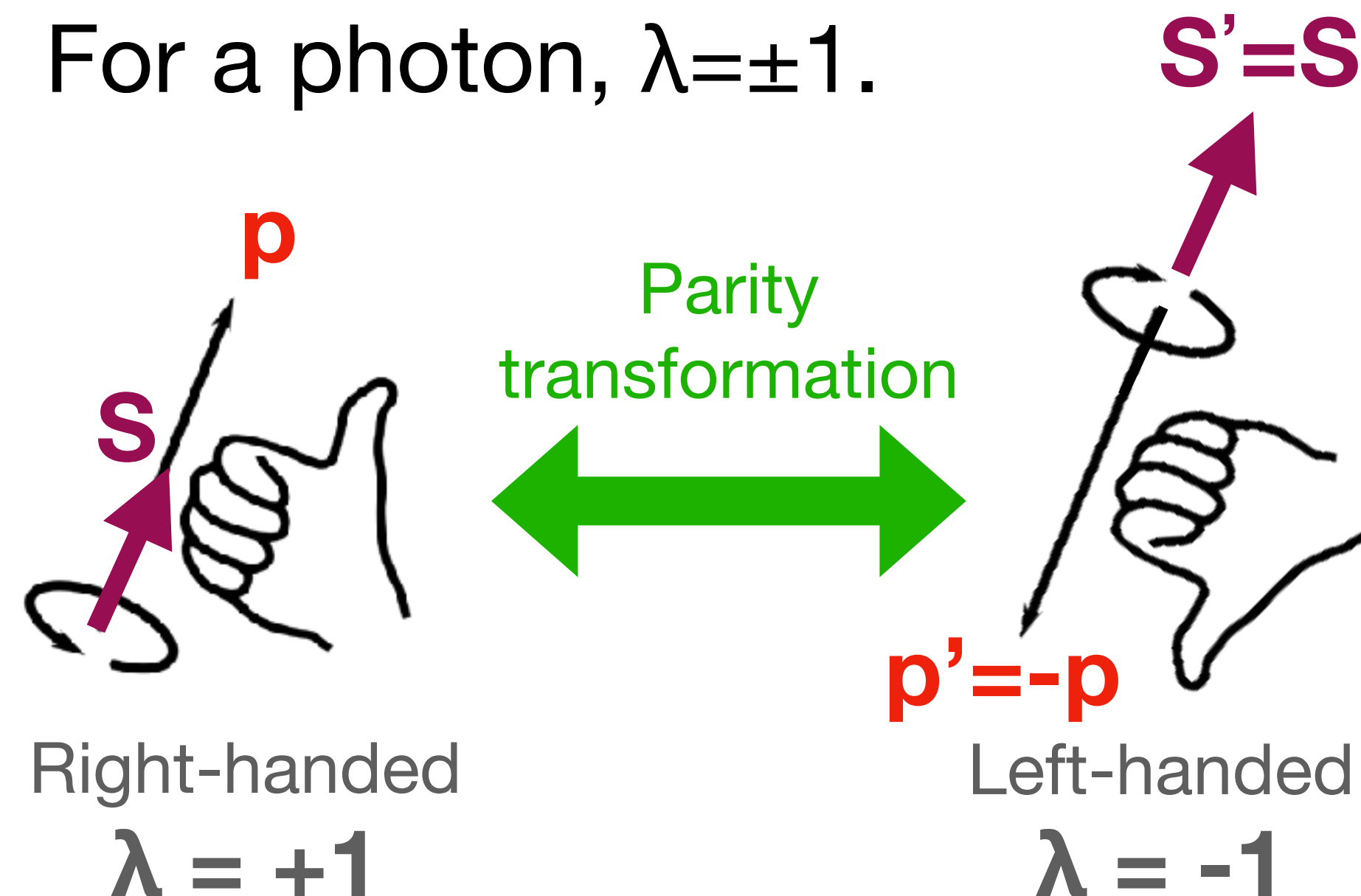
Helicity is a pseudoscalar

Party transformation changes "right-handed" to "left-handed" and vice versa

- For massless particles, we define the "helicity", λ, as

$$\mathbf{S} \cdot \frac{\mathbf{p}}{|\mathbf{p}|} = \lambda \hbar$$

- For a photon, λ=±1.

p

S

S'=S

Parity
transformation

p'=-p

Right-handed
λ = +1

Left-handed
λ = -1

- **λ is a pseudoscalar** because it is a product of a momentum vector (**p**) and a spin pseudovector (**S**).

  - On the other hand, "scalar", such as $\mathbf{p}^2$ and $\mathbf{S}^2$, does not change sign.

- For a graviton, λ=±2.

- **Asymmetry between λ=±1 and ±2 is the sign of parity violation!**

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Parity Violation in Electromagnetism with

$$I_{CS} = \int d^4 x \sqrt{-g} \left(-\frac{\alpha}{4f} \chi F \widetilde{F} \right)$$

Maxwell's Equations

In Minkowski space, Heaviside units and *c*=1

$$\nabla \cdot \mathbf{E} = \rho, \quad -\dot{\mathbf{E}} + \nabla \times \mathbf{B} = \mathbf{j}$$

$$\nabla \cdot \mathbf{B} = 0, \quad \dot{\mathbf{B}} + \nabla \times \mathbf{E} = 0$$

- These equations are invariant under Poincaré transformation (spatial translation and rotation and Lorentz boost).

Parity-flipping Maxwell's Equations
In Minkowski space, Heaviside units and *c*=1

$$(-\nabla) \cdot (-\mathbf{E}) = \rho\,, \quad -(-\dot{\mathbf{E}}) + (-\nabla) \times \mathbf{B} = (-\mathbf{j})$$

$$(-\nabla) \cdot \mathbf{B} = 0\,, \qquad \dot{\mathbf{B}} + (-\nabla) \times (-\mathbf{E}) = 0$$

- These equations are invariant under Poincaré transformation (spatial translation and rotation and Lorentz boost).

- They are also invariant under parity transformation, if **E** and **j** are vectors, ρ is a scalar, and **B** is a pseudovector.

Maxwell's Equations in a covariant form

$$\nabla \cdot \mathbf{E} = \rho, \qquad -\dot{\mathbf{E}} + \nabla \times \mathbf{B} = \mathbf{j}$$

$$\nabla \cdot \mathbf{B} = 0, \qquad \dot{\mathbf{B}} + \nabla \times \mathbf{E} = 0$$

- These equations can be written in a covariant form as

Dual tensor

$$\partial_\nu F^{\mu\nu} = j^\mu \qquad \partial_\nu \tilde{F}^{\mu\nu} = 0$$

$$\mu = 0, 1, 2, 3, \quad j^\mu = (\rho, \mathbf{j}), \quad \partial_\mu = \partial/\partial x^\mu, \quad x^\mu = (t, \mathbf{x})$$

Antisymmetric Field Strength Tensor, $F_{\mu\nu}$

$F_{\mu\nu} = -F_{\nu\mu}$

$$F_{\mu\nu} = \eta_{\mu\alpha}\eta_{\nu\beta}F^{\alpha\beta} \qquad \text{where } \eta_{\mu\alpha} = \mathrm{diag}(-1,1,1,1)$$

$$F_{\mu\nu} = \begin{pmatrix} 0 & -E_x & -E_y & -E_z \\ E_x & 0 & B_z & -B_y \\ E_y & -B_z & 0 & B_x \\ E_z & B_y & -B_x & 0 \end{pmatrix}$$

- Equivalently,

$$F^{0i} = E_i$$
$$F^{ij} = \epsilon^{ijk}B_k$$

- Therefore,

$$F^2 \equiv F_{\mu\nu}F^{\mu\nu} = 2(\mathbf{B} \cdot \mathbf{B} - \mathbf{E} \cdot \mathbf{E})$$

This is a *scalar* and is invariant under parity transformation.

Dual Field Strength Tensor, $\tilde{F}^{\mu\nu}$

$\tilde{F}^{\mu\nu} = -\tilde{F}^{\nu\mu}$

$$\tilde{F}^{\mu\nu} = \frac{1}{2}\epsilon^{\mu\nu\alpha\beta}F_{\alpha\beta}$$

where $\epsilon^{\mu\nu\alpha\beta}$ *Levi-Civita symbol* $= \begin{cases} +1 & \text{if } (\mu,\nu,\alpha,\beta) \text{ is even perm. of } (0,1,2,3) \\ -1 & \text{if } (\mu,\nu,\alpha,\beta) \text{ is odd perm. of } (0,1,2,3) \\ 0 & \text{otherwise} \end{cases}$

$$\tilde{F}^{\mu\nu} = \begin{pmatrix} 0 & B_x & B_y & B_z \\ -B_x & 0 & -E_z & E_y \\ -B_y & E_z & 0 & -E_x \\ -B_z & -E_y & E_x & 0 \end{pmatrix}$$

- Equivalently,

$$\tilde{F}^{0i} = B_i$$
$$\tilde{F}^{ij} = -\epsilon^{ijk}E_k$$

- Therefore,

$$F\tilde{F} \equiv F_{\mu\nu}\tilde{F}^{\mu\nu} = -4\mathbf{B}\cdot\mathbf{E}$$

This is a *pseudoscalar* and changes sign under parity transformation!

$F\tilde{F}$ in the action?

$$F^2 \equiv F_{\mu\nu}F^{\mu\nu} = 2(\mathbf{B} \cdot \mathbf{B} - \mathbf{E} \cdot \mathbf{E})$$

$$F\tilde{F} \equiv F_{\mu\nu}\tilde{F}^{\mu\nu} = -4\mathbf{B} \cdot \mathbf{E}$$

$$I = -\frac{1}{4} \int d^4x \ F^2 + \int d^4x \ A_\mu j^\mu$$

$$\boxed{d^4x = dt d^3\mathbf{x}}$$

- This action is sufficient to produce all of Maxwell's equations.

- Can we add $\displaystyle\int d^4x \ F\tilde{F}$ to the action?

  - The answer is yes. However, **this is only a surface term**, since $F\tilde{F}$ is a total derivative: $$F_{\mu\nu}\tilde{F}^{\mu\nu} = 2\partial_\mu(A_\nu \tilde{F}^{\mu\nu}) \text{ where}$$ $$F_{\mu\nu} = \partial_\mu A_\nu - \partial_\nu A_\mu$$

$F\tilde{F}$ in the action

Chern-Simons term

- Consider $I_{\text{CS}} = -\frac{1}{4}\alpha \int d^4x \; \theta F\tilde{F}$ with $F\tilde{F} = 2\partial_\mu(A_\nu \tilde{F}^{\mu\nu})$

  - α: a dimensionless constant

  - θ: a dimensionless pseudoscalar field

- **This is not a surface term!** Integration by parts gives

$$I_{\text{CS}} = \frac{1}{2}\alpha \int d^4x \; (\partial_\mu\theta)A_\nu \tilde{F}^{\mu\nu}$$

Jim Simons in 2023

https://einstein-chair.github.io/simons2023/

- This is a special case of the so-called *Chern-Simons term*, $p_\mu A_\nu \tilde{F}^{\mu\nu}$

  with $p_\mu = \partial_\mu\theta$

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Consistency with gauge invariance

p_μ cannot be arbitrary

$$I_{\mathrm{CS}} = \frac{1}{2}\alpha \int d^4 x \; p_\mu A_\nu \tilde{F}^{\mu\nu}$$

- This action is invariant under the gauge transformation, $A_\nu \rightarrow A_\nu + \partial_\nu f$

if $\partial_\nu p_\mu - \partial_\mu p_\nu = 0$ <u>Hint:</u> Use integration by parts and the identity

$$\partial_\nu \tilde{F}^{\mu\nu} = 0$$

- For example: This implies the presence of a preferred direction in spacetime and violation of Lorentz invariance!

  - p_μ is a constant vector and not dynamical, or

  - p_μ is a gradient of a dynamical (pseudo)scalar field, such as $p_\mu = \partial_\mu \theta$.

The main goal of this talk
Let's find new physics!

- We study the cosmological consequence of

$$I_{CS} = -\frac{1}{4}\alpha \int d^4x \; \theta F\tilde{F}$$

- Specifically, we ask if θ is —

  - responsible for dark matter and dark energy, or

  - active during cosmic inflation.

The main goal of this talk
Let's find new physics!

- We study the cosmological consequence of

$$I_{CS} = -\frac{1}{4}\alpha \int d^4x \; \theta F\tilde{F}$$

- Specifically, we ask if θ is —

  - responsible for dark matter and dark energy, or

  - active during cosmic inflation.

- More examples:

  - **Non-Abelian gauge fields** [Maleknejad, Sheikh-Jabbari, Soda, Phys. Rept. **528**, 161 (2013)]

$$F\tilde{F} = F^a_{\mu\nu}F^{\mu\nu a}$$

$$F^a_{\mu\nu} = \partial_\mu A^a_\nu - \partial_\nu A^a_\mu + g_A \epsilon^{abc} A^b_\mu A^c_\nu$$

  - **Gravitational CS** [Alexander, Yunes, Phys. Rept. **480**, 1 (2009)]

$$R\tilde{R} = R^\beta{}_\alpha{}^{\mu\nu} \tilde{R}^\alpha{}_{\beta\mu\nu}$$

You can have both!

Mirzagholi, EK, Lozanov, Watanabe (2020)

Is there a known example of this term in particle physics?

Yes, a pion. The ABJ anomaly!

Credit: HiggsTan

- A pion is a composite meson composed of a quark and an antiquark.

  - A neutral pion, π^0, is composed of either $u\bar{u}$ or $d\bar{d}$, and **is a pseudoscalar**.
    (Chinowsky & Steinberger, 1954)

  - π^0 is coupled to photons via I_{CS} where

    - $\theta = \pi^0 / f_\pi$ with $f_\pi \sim 184$ MeV (pion decay constant)

    - $a = 2\alpha_{EM}N_c / (3\pi)$ with $N_c = 3$ (the number of quark colors) and $\alpha_{EM} \sim 1/137$ (EM fine structure constant)

- **π^0 decays into 2 photons via this term, which has been observed.** So, this possibility is not completely crazy!

Correction to Maxwell's equations

In Minkowski space, Heaviside units and *c=1*

- We now derive the correction to Maxwell's equations from

$$d^4x = dt\, d^3\mathbf{x}$$

$$I = -\frac{1}{4} \int d^4x \left(F^2 + \alpha\theta F\tilde{F} \right) + \int d^4x \; A_\mu j^\mu$$

- Finding the path that gives a stationary point,

$$\partial_\nu F^{\mu\nu} + \alpha(\partial_\nu\theta)\tilde{F}^{\mu\nu} = j^\mu$$

As expected, only the space-time dependence
of the θ field affects Maxwell's equation.

Correction to the EM wave equation in vacuum

With the Chern-Simons term

$$\partial_\nu F^{\mu\nu} + \alpha(\partial_\nu\theta)\tilde{F}^{\mu\nu} = 0$$
where $F_{\mu\nu} = \partial_\mu A_\nu - \partial_\nu A_\mu$

- With $A^0 = \phi = 0$ in the Lorenz gauge, we find

$$-\Box A^i + \alpha(\partial_\nu\theta)\tilde{F}^{i\nu} = 0$$

$$\Box = \eta^{\alpha\beta}\partial_\alpha\partial_\beta = -\frac{\partial^2}{\partial t^2} + \nabla^2$$

$$A^\mu = \eta^{\mu\alpha}A_\alpha = (\phi, \mathbf{A})$$

$$\Rightarrow \quad \ddot{\mathbf{A}} - \nabla^2\mathbf{A} + \alpha\left[-\dot{\theta}(\nabla\times\mathbf{A}) + (\nabla\theta)\times\dot{\mathbf{A}}\right] = 0$$

Correction to the EM wave equation!

Note: **A** is a vector and θ is a pseudoscalar.

Helicity basis to probe parity symmetry
Going to Fourier space

- Fourier transform of **A**(t,**x**) is $\mathbf{A}(t, \mathbf{x}) = (2\pi)^{-3/2} \int d^3\mathbf{k} \, \mathbf{A_k}(t) e^{i\mathbf{k}\cdot\mathbf{x}}$

  - The EM wave propagates in the direction of **k**. The change in **A**_{**k**} is perpendicular to **k**.

"Coulomb gauge" $\nabla \cdot \mathbf{A}(t, \mathbf{x}) = 0 \rightarrow \mathbf{k} \cdot \mathbf{A_k}(t) = 0$

- Choose **k** to be on the z(=x³) axis. The helicity states, λ=±1, are given for each Fourier mode by

$$A_\pm = \frac{A_\mathbf{k}^1 \mp i A_\mathbf{k}^2}{\sqrt{2}}$$

35
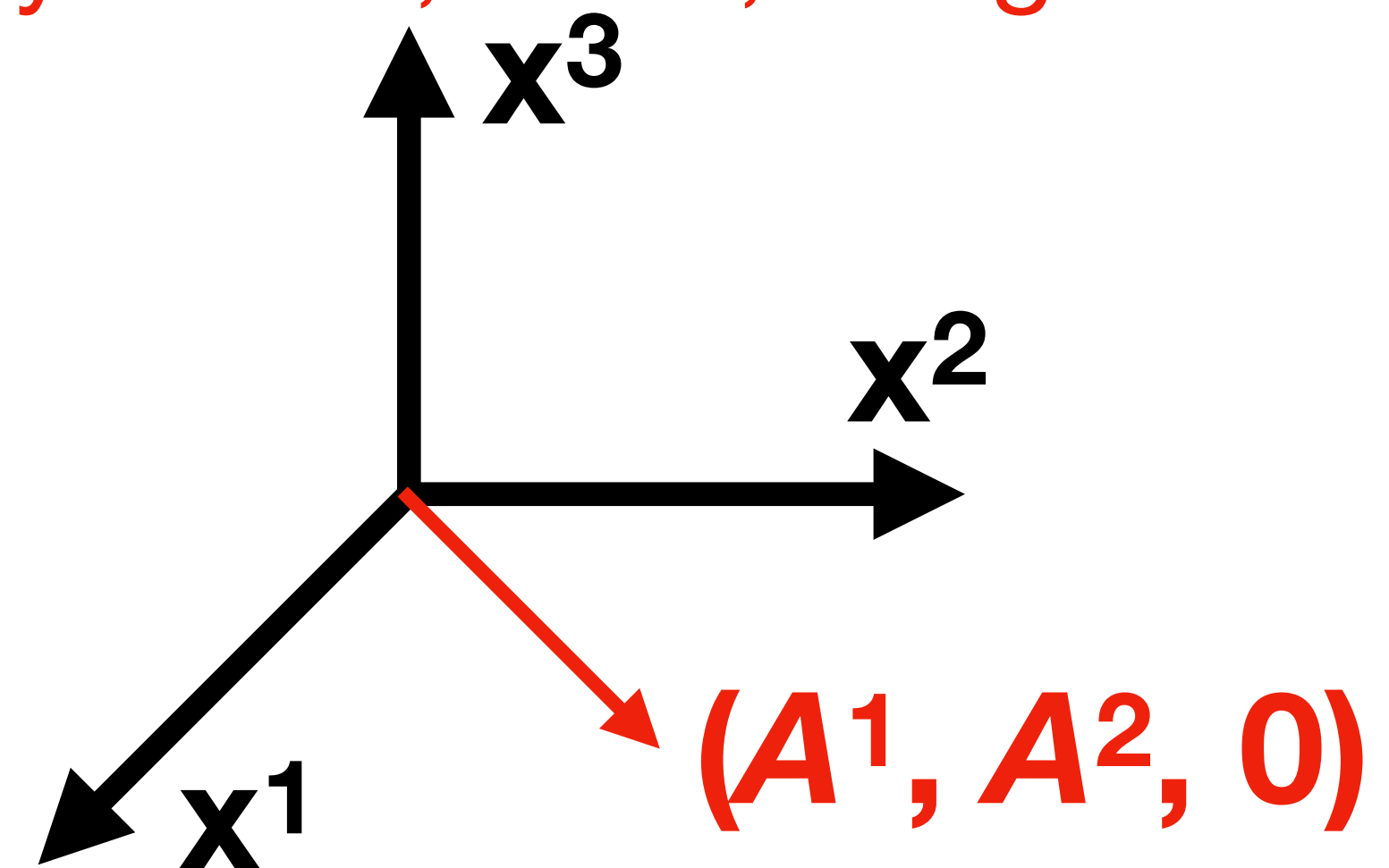
Correction to the EM wave equation

In the helicity basis

$$\ddot{\mathbf{A}} - \nabla^2 \mathbf{A} + \alpha \left[-\dot{\theta}(\nabla \times \mathbf{A}) + (\nabla\theta) \times \dot{\mathbf{A}} \right] = 0$$

Correction to the EM wave equation!

- If θ has a time-dependent vacuum expectation value, $\theta(t,\mathbf{x}) \rightarrow \bar{\theta}(t)$, we find in Fourier space

$$\ddot{\mathbf{A}}_{\mathbf{k}} + k^2 \mathbf{A}_{\mathbf{k}} - i\alpha\dot{\bar{\theta}}(\mathbf{k} \times \mathbf{A}) = 0$$

$$\Rightarrow \quad \ddot{A}_\pm + \left(k^2 \mp k\alpha\dot{\bar{\theta}} \right) A_\pm = 0$$

Parity violation
The equation of motion depends on handedness!

$$I_{CS} = \int d^4x \sqrt{-g} \left(-\frac{\alpha}{4f} \chi F\widetilde{F} \right)$$
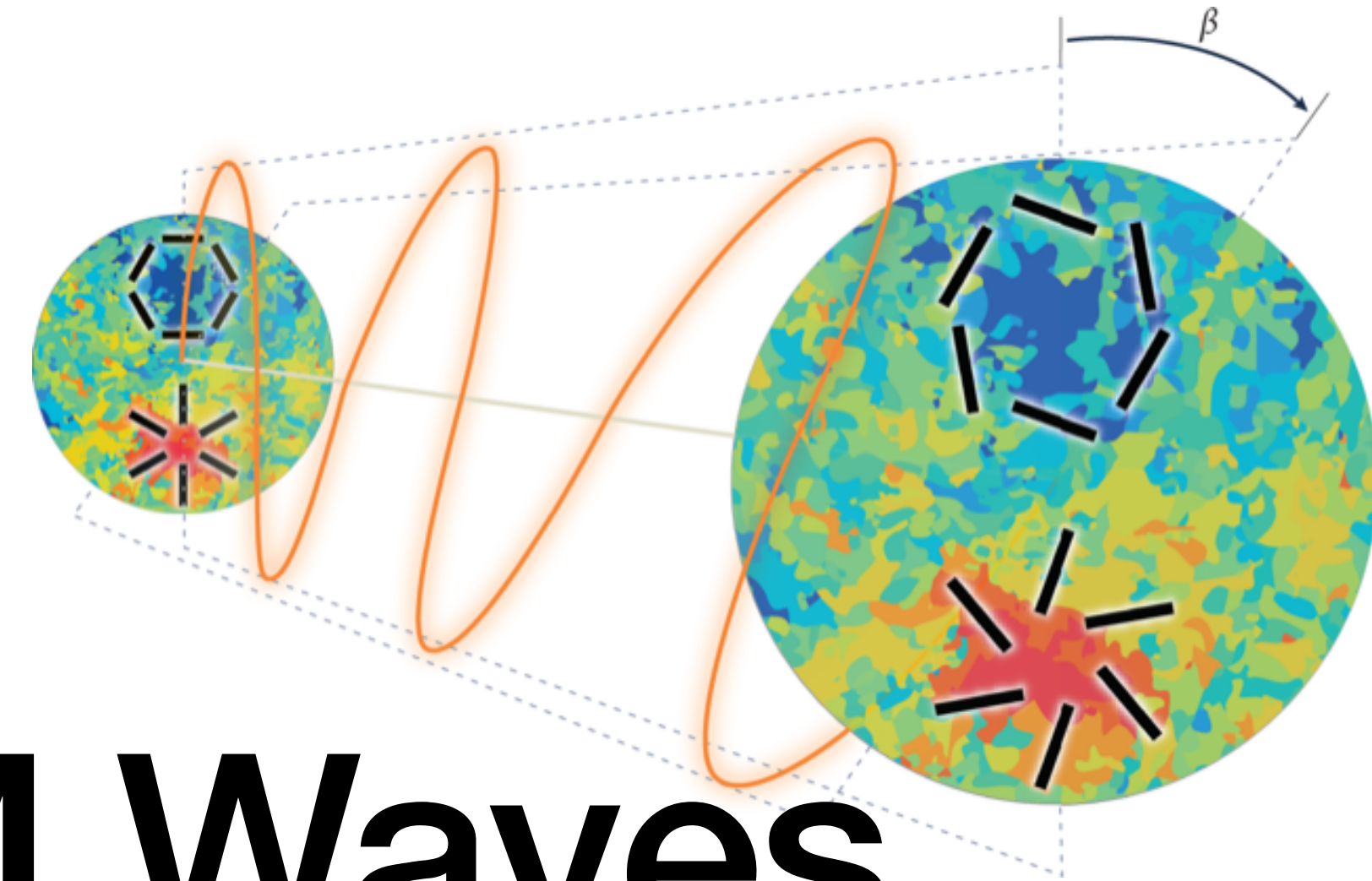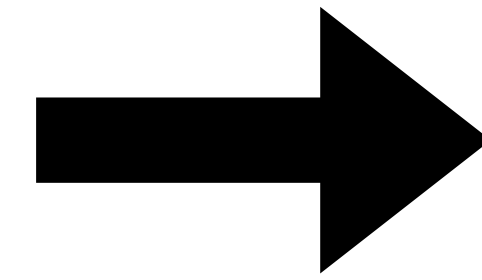
Parity Violation in EM Waves due to Dark Matter and Dark Energy

Scalar field DM/DE coupled to the CS term

DM = Dark Matter; DE = Dark Energy

$$I = \int d^4x \sqrt{-g} \left[-\frac{1}{2}(\partial\chi)^2 - V(\chi) - \frac{1}{4}F^2 - \frac{\alpha}{4f}\chi F\tilde{F} \right]$$

- χ is a neutral pseudoscalar field (spin 0).

- Why consider χ as a good DM/DE candidate?

  - *Why not*? We have an example in the Standard Model: a neutral pion.

  - We expect $\alpha \simeq \alpha_{\mathsf{EM}} \simeq 10^{-2}$ and $f < M_{\mathsf{Pl}} \simeq 2.4 \times 10^{18}$ GeV.

- χ can be composed of fermions like a pion, or a fundamental pseudoscalar like an "axion" field.

We wrote

$$\theta = \frac{\chi}{f}$$

Distinction between DE and DM

How small is its mass? Example of $V(\chi) = m^2\chi^2/2$

(a) DE

(b) DM

- The useful criterion is the equation of state parameter, *w*.

$$w = \frac{P}{\rho} = \frac{\langle\dot{\chi}^2\rangle - m^2\langle\chi^2\rangle}{\langle\dot{\chi}^2\rangle + m^2\langle\chi^2\rangle}$$
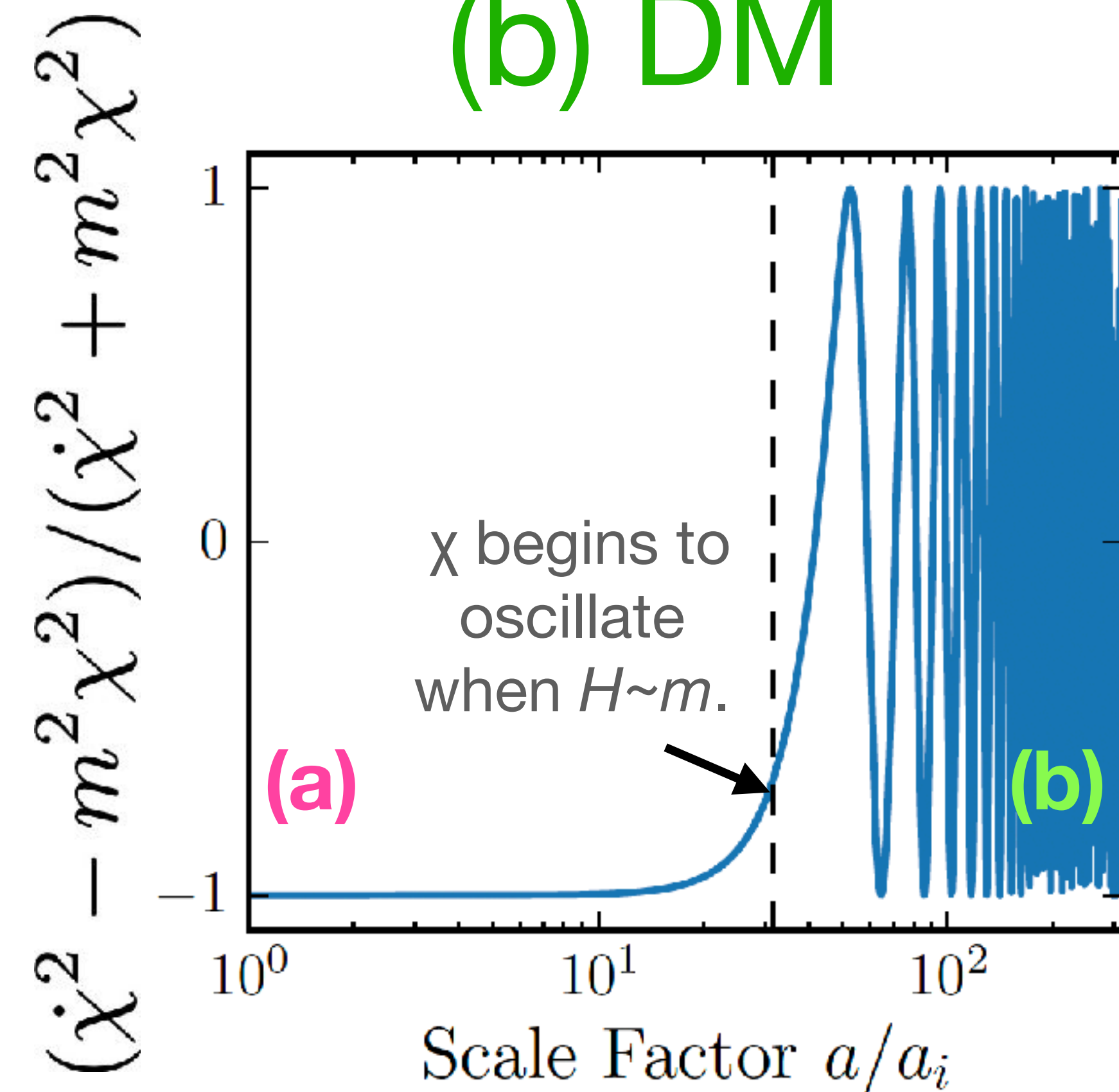
- $w \simeq -1$: Dark Energy (DE)

  - $m \lesssim H_0 \simeq 10^{-33}$ eV

- $w \simeq 0$: Dark Matter (DM)

  - $m \gtrsim H_0$
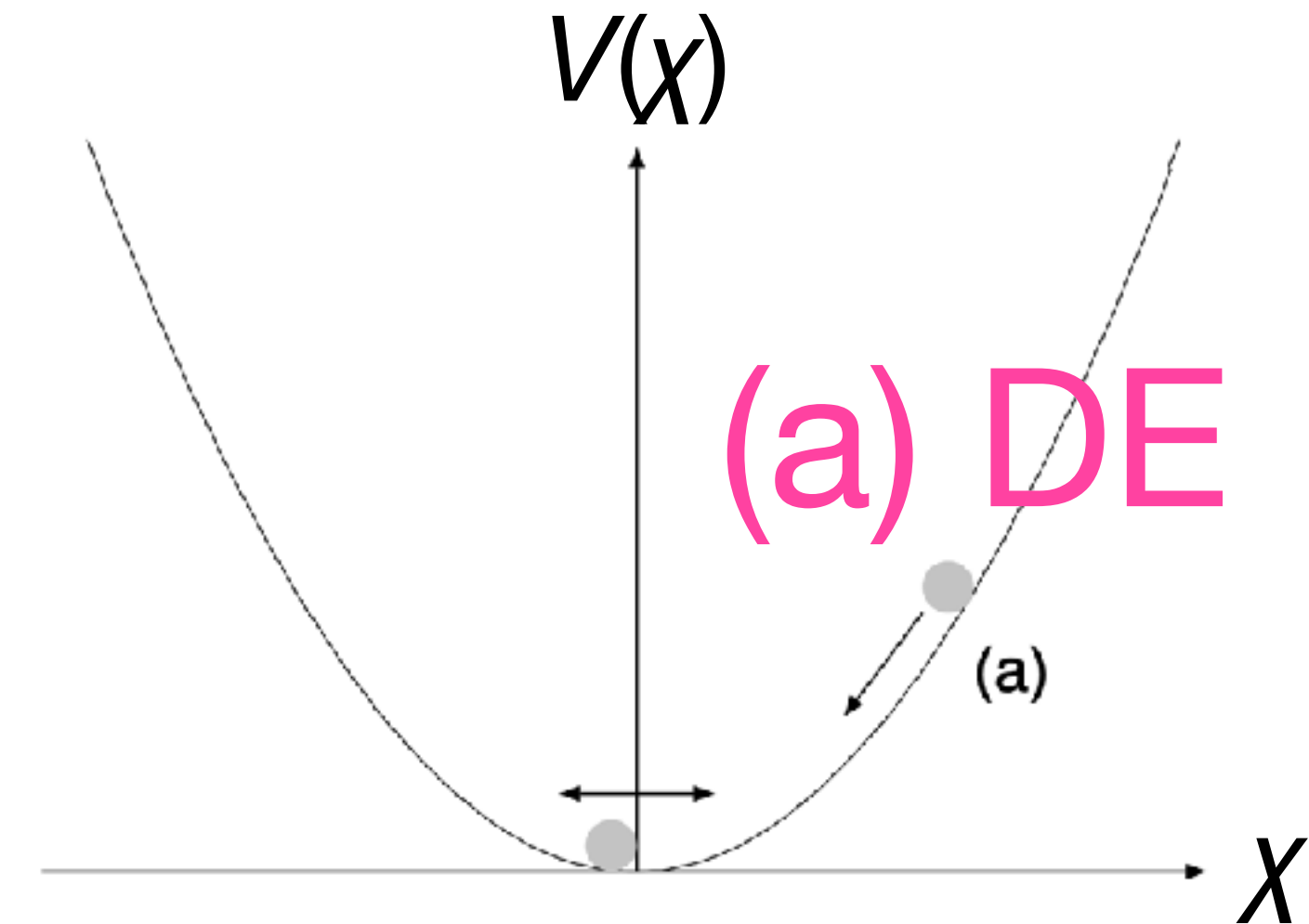
Phase velocity of circular polarization states

Expanding space, _c_=1

where $\quad ' = \dfrac{\partial}{\partial \tau} = a \dfrac{\partial}{\partial t}$

- We write

τ : conformal time

$$A''_\pm + \omega^2_\pm A_\pm = 0, \quad \omega^2_\pm = k^2 \mp \frac{k\alpha\chi'}{f}$$

- We work in the limit of $k^2 \gg k\alpha\chi'/f$. This approximation is accurate for the photons we observe today. (However, $\omega^2_\pm$ can become negative during inflation!)

- The phase velocity of circular polarization states, $\omega_\pm/k$, is

$$\frac{\omega_\pm}{k} \simeq 1 \mp \frac{\alpha\chi'}{2kf}$$

+: Right-handed state
−: Left-handed state
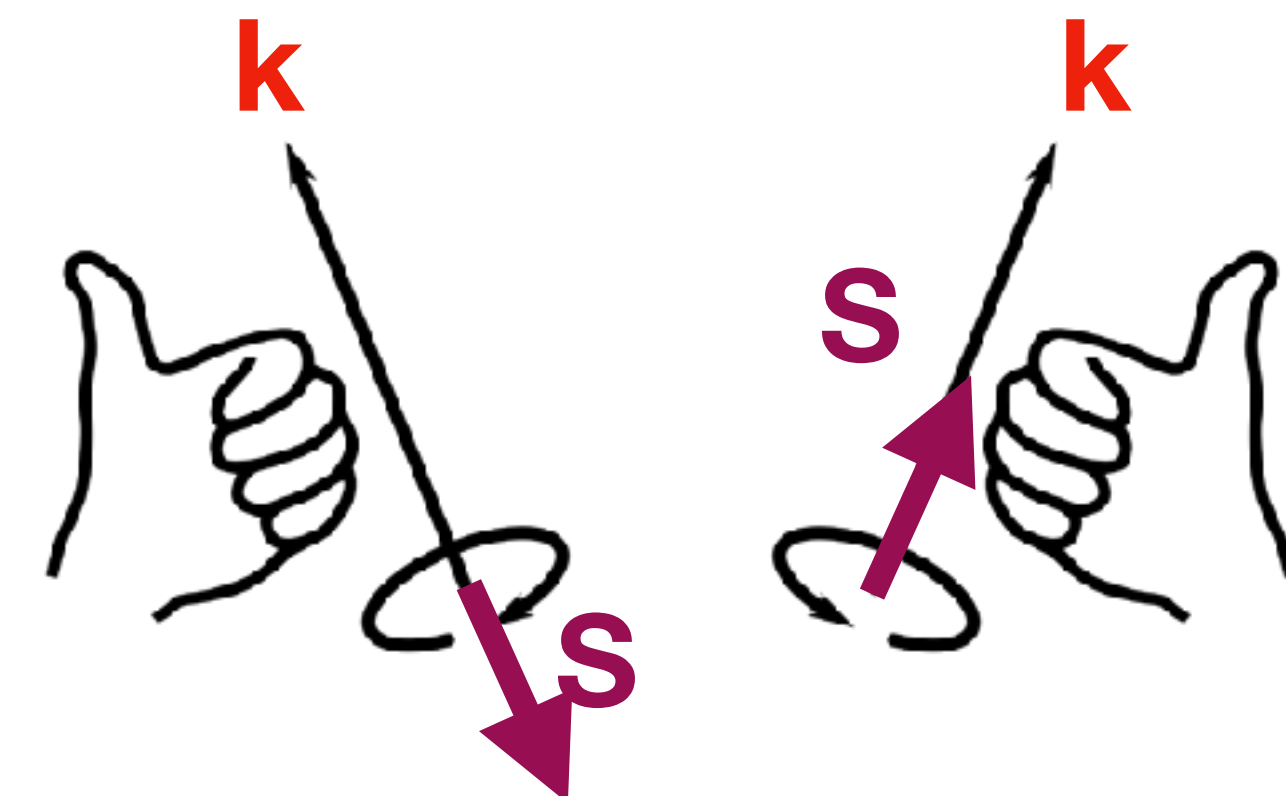
Left-handed   Right-handed

40

Plane-wave (WKB) Solution
Expanding space, *c*=1

$$A''_\pm + \omega_\pm^2 A_\pm = 0, \quad \omega_\pm \simeq k \mp \frac{\alpha \chi'}{2f}$$

- For $|\omega'_\pm| \ll \omega_\pm^2$, which is satisfied here, an accurate solution is given by

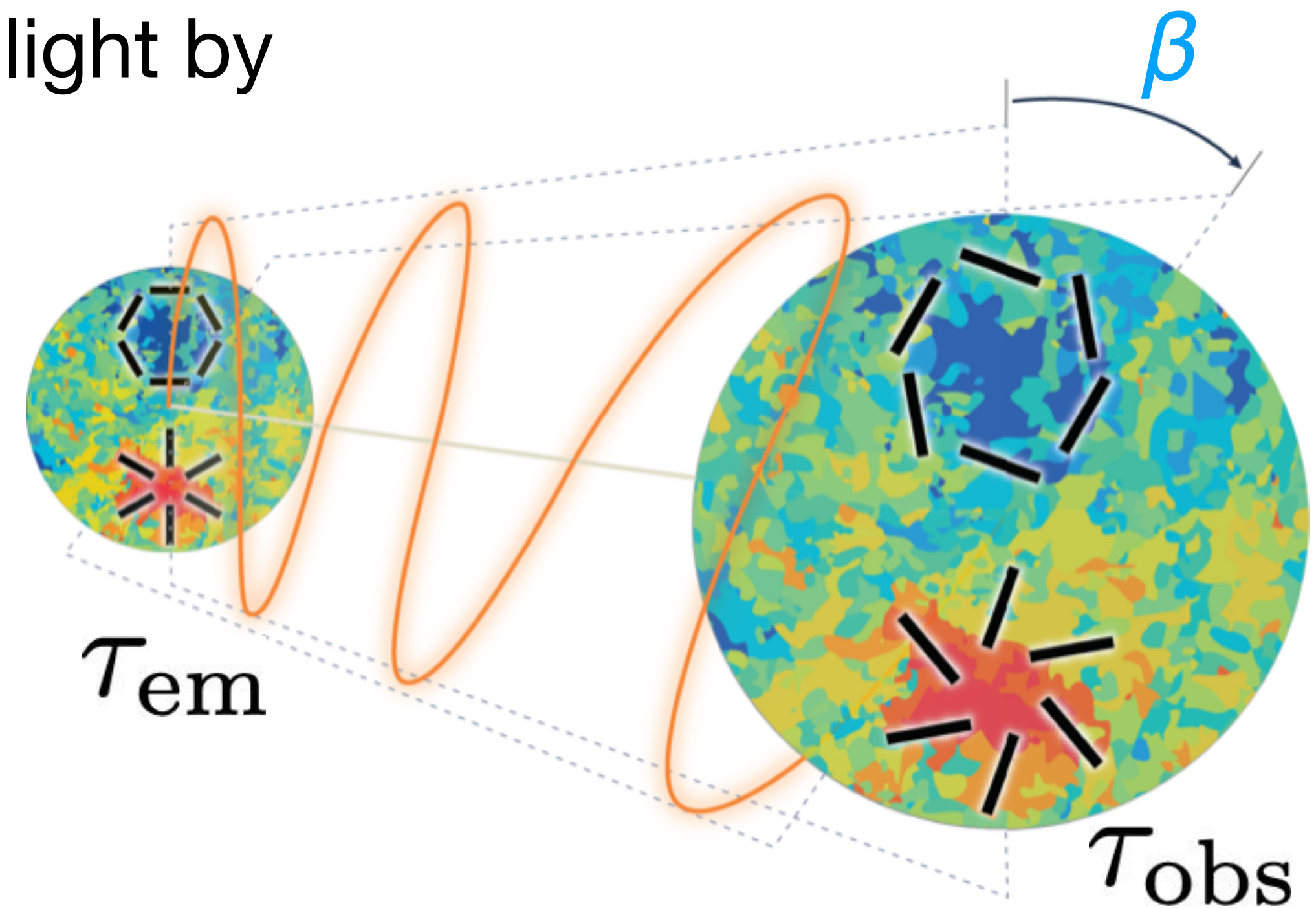$$A_\pm \simeq C_\pm \frac{\exp\left(-i \int d\tau \, \omega_\pm + i\delta_\pm\right)}{\boxed{\sqrt{2\omega_\pm}} \simeq \sqrt{2k}}$$

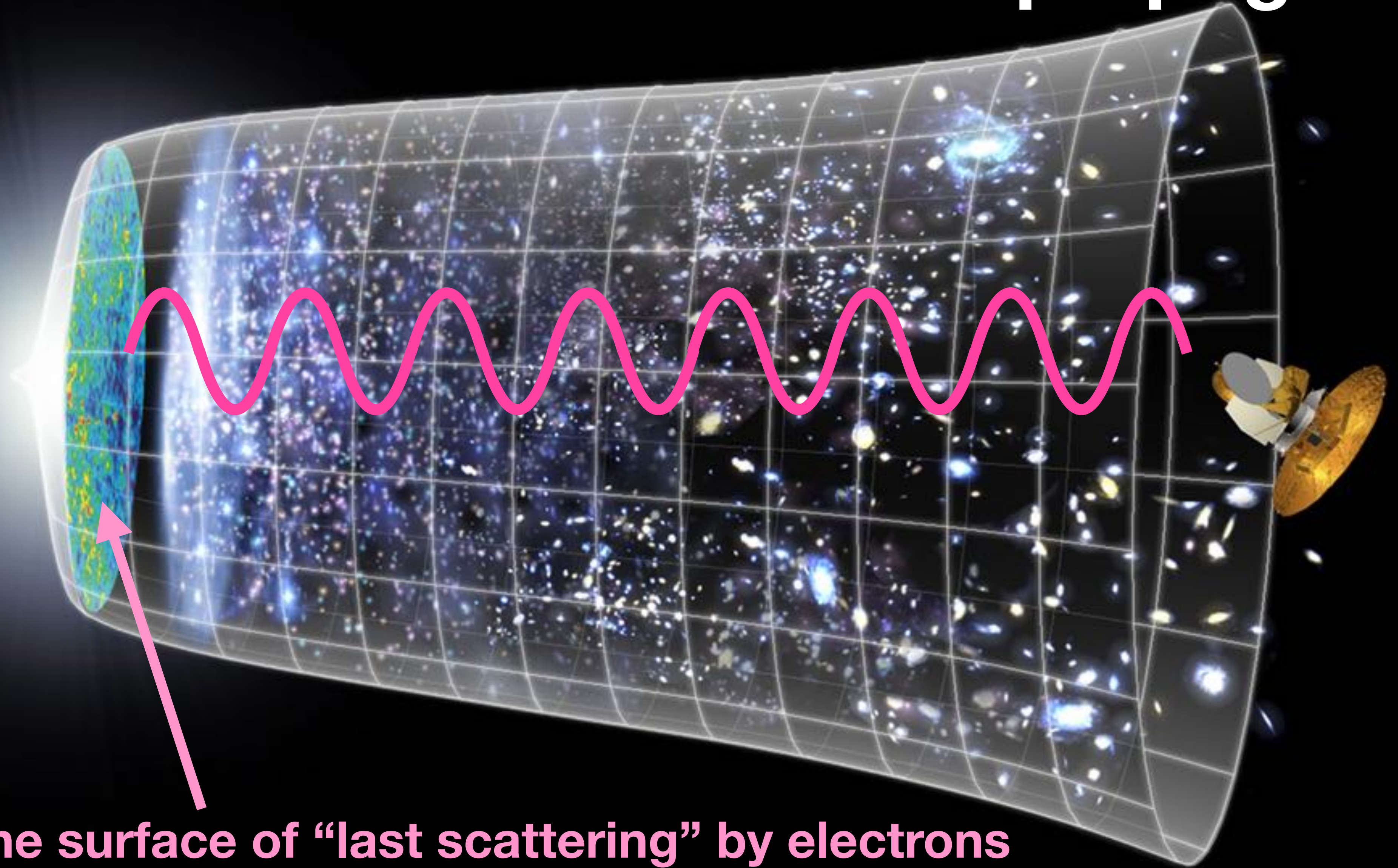We can replace $\omega_\pm$ in amplitude (but not in phase) with k.

where $C_\pm$ is the initial amplitude and $\delta_\pm$ is the initial phase.

Cosmic Birefringence

Rotation of the plane of linear polarization

with

$$A_\pm \simeq C_\pm \frac{\exp\left(-i \int d\tau \, \omega_\pm + i\delta_\pm\right)}{\boxed{\sqrt{2\omega_\pm}} \simeq \sqrt{2k}} \qquad \frac{\omega_\pm}{k} \simeq 1 \mp \frac{\alpha \chi'}{2kf}$$

- This **rotates** the plane of linear polarization of light by

$$\beta = -\int_{\tau_{\rm em}}^{\tau_{\rm obs}} d\tau \, (\omega_+ - \omega_-)$$

$$= \frac{\alpha}{2f} \left[\chi(\tau_{\rm obs}) - \chi(\tau_{\rm em})\right]$$
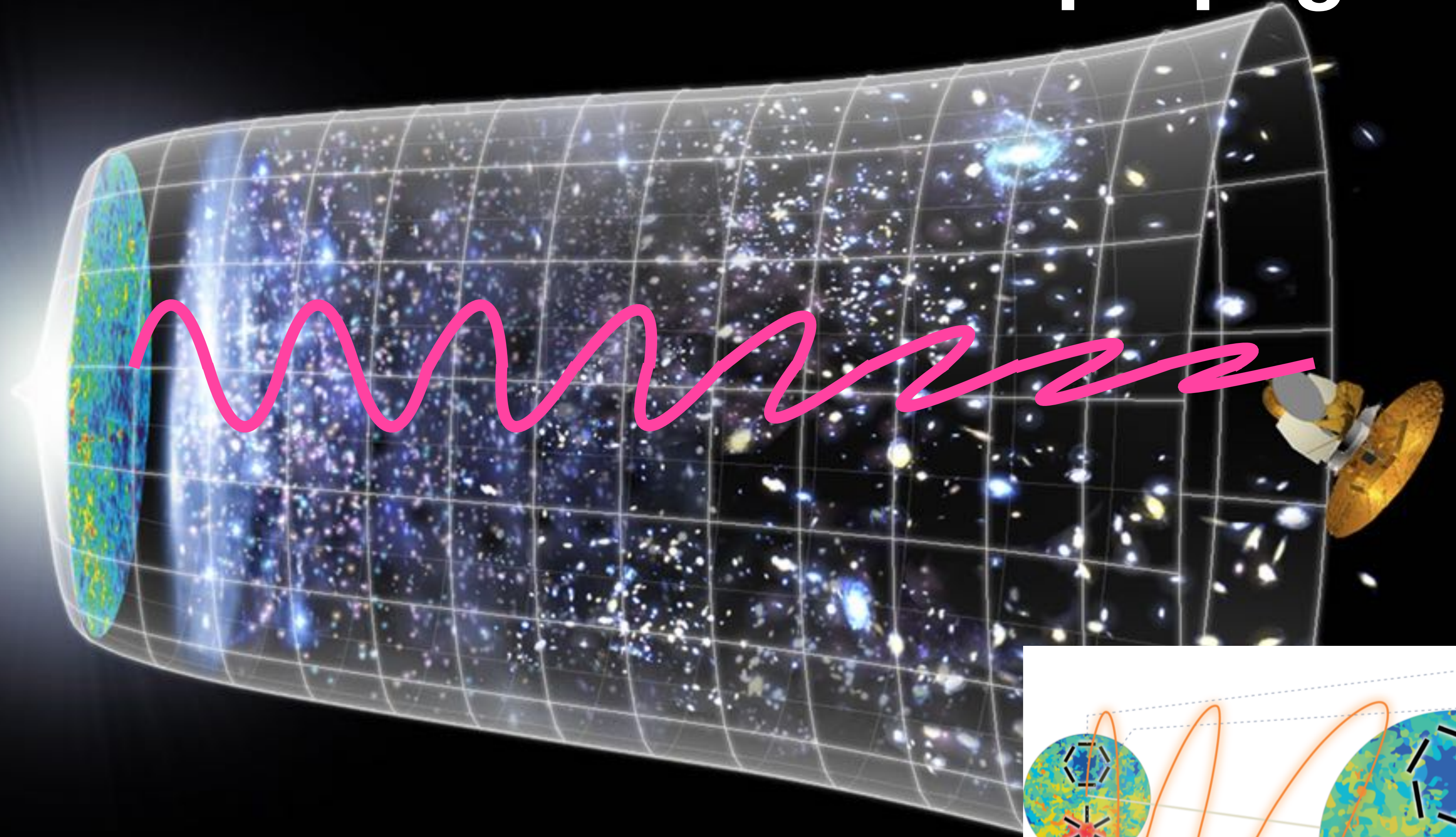
$\tau_{\rm em}$

$\tau_{\rm obs}$

β

How does the EM wave of the CMB propagate?

The surface of "last scattering" by electrons
(Scattering generates *polarization*!)
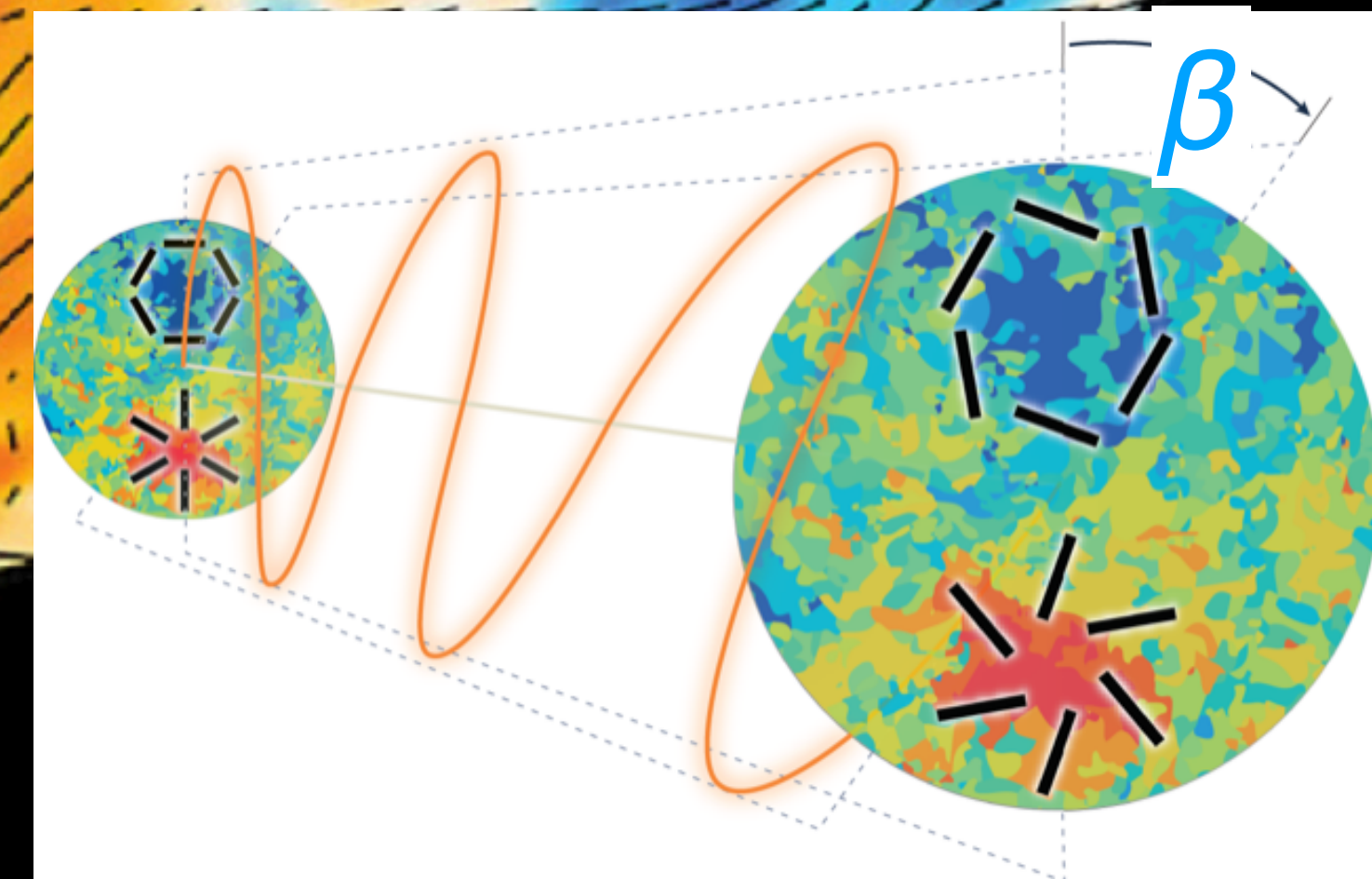
Credit: WMAP Science Team

How does the EM wave of the CMB propagate?

Credit: ESA
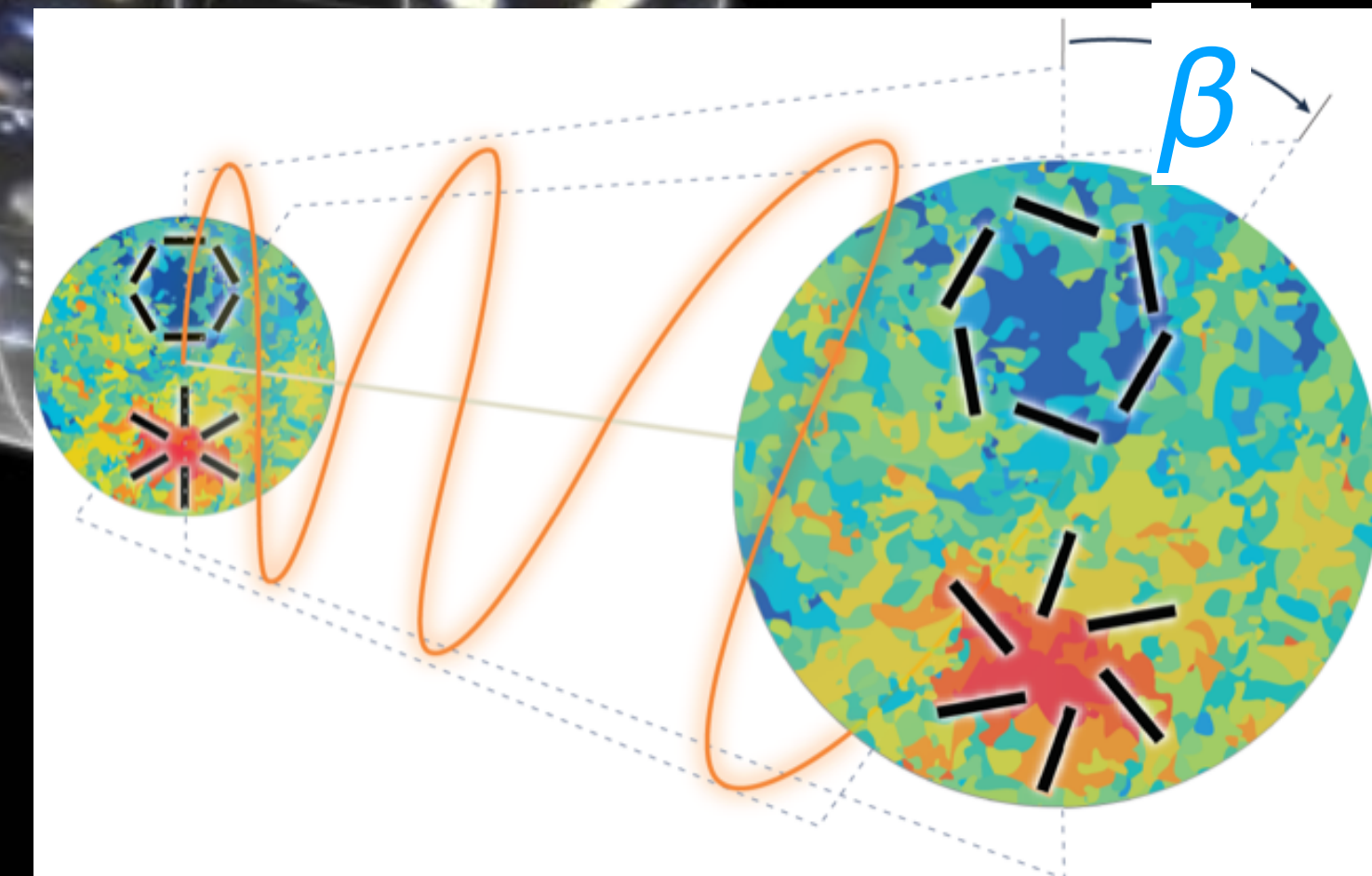
"*Cosmic Birefringence*"

If the plane of linear polarization of the CMB is rotated uniformly by β, it is the sign of parity violation!

Temperature (smoothed) + Polarisation

β

Pseudoscalar: EB correlation

- The observed pattern of the CMB polarization can be decomposed into eigenstates of parity, called "E modes" and "B modes".

- E and B modes are transformed differently under the parity transformation. Therefore, the product of the two, **the "EB correlation", is a pseudoscalar**.

- **The full-sky average of the EB correlation must vanish (to within the measurement uncertainty), if there is no parity violation!**
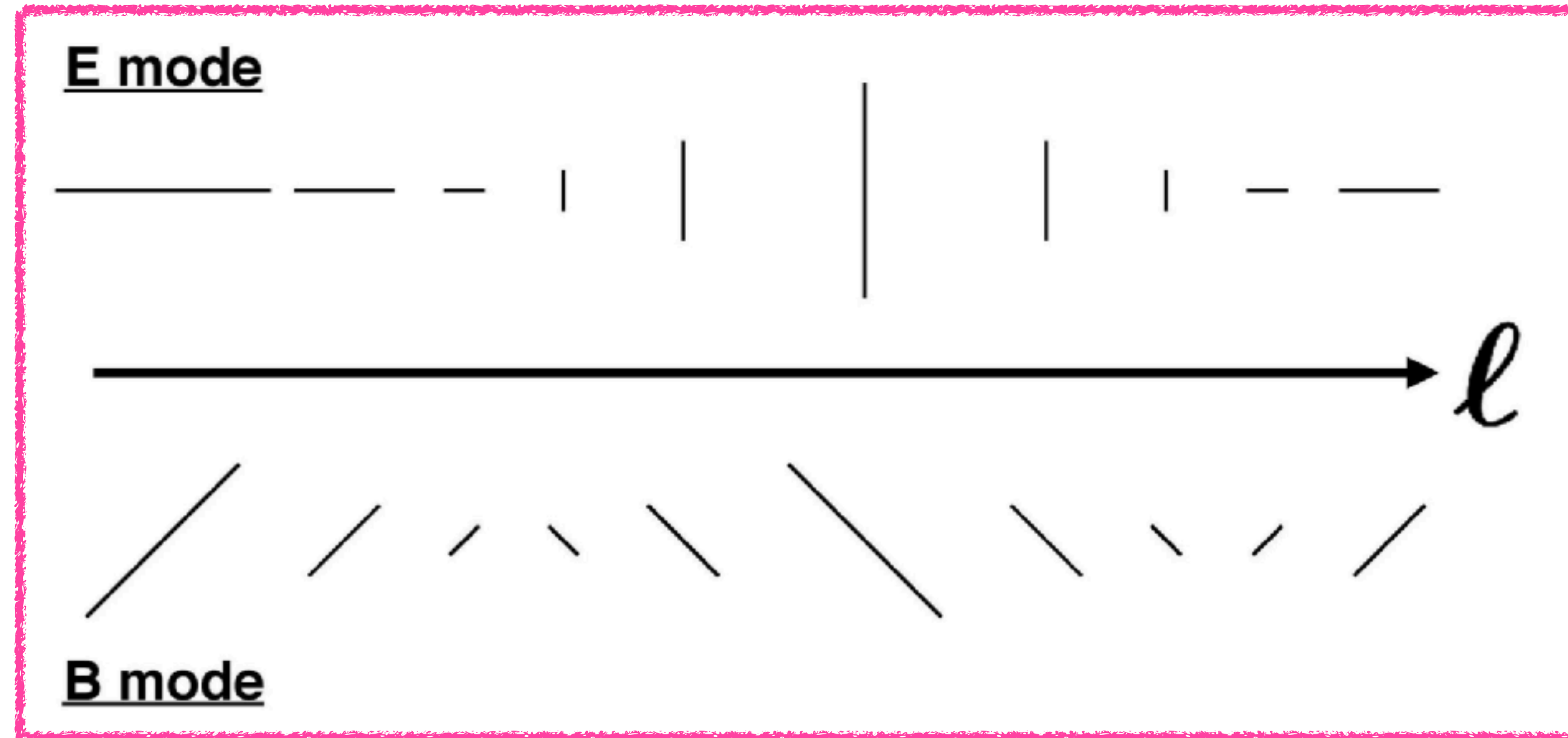
Parity eigenstates: E and B modes

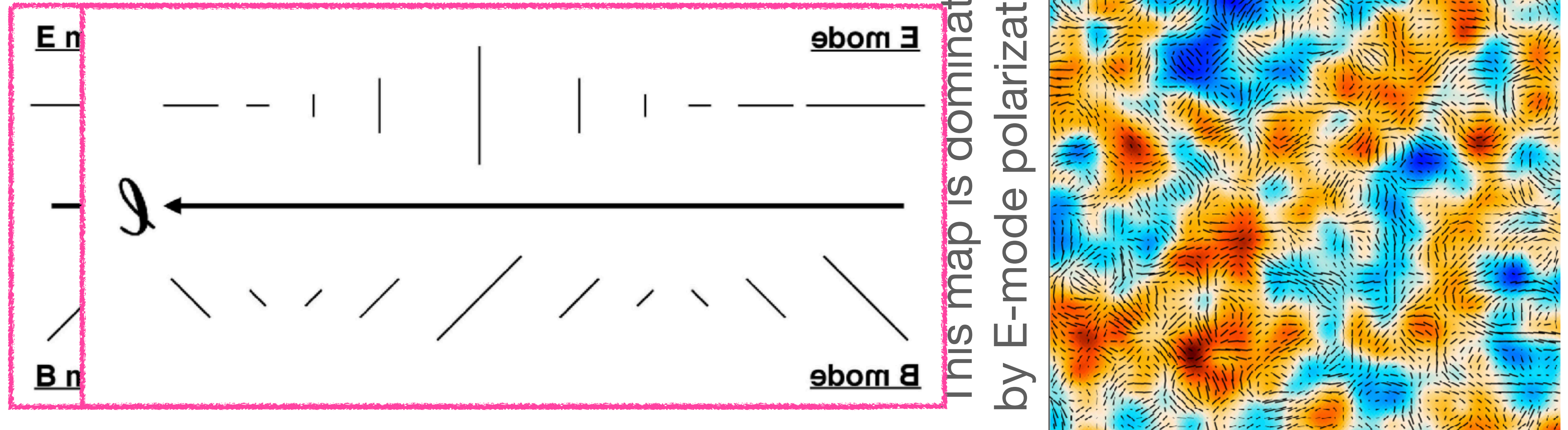**Concept defined in Fourier space**

E mode

ℓ

B mode

This map is dominated by E-mode polarization

- **E-mode**：Polarization directions are **parallel or perpendicular** to the wavenumber direction

- **B-mode**：Polarization directions are **45 degrees tilted** w.r.t the wavenumber direction

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Parity eigenstates: E and B modes

Concept defined in Fourier space

This map is dominated by E-mode polarization
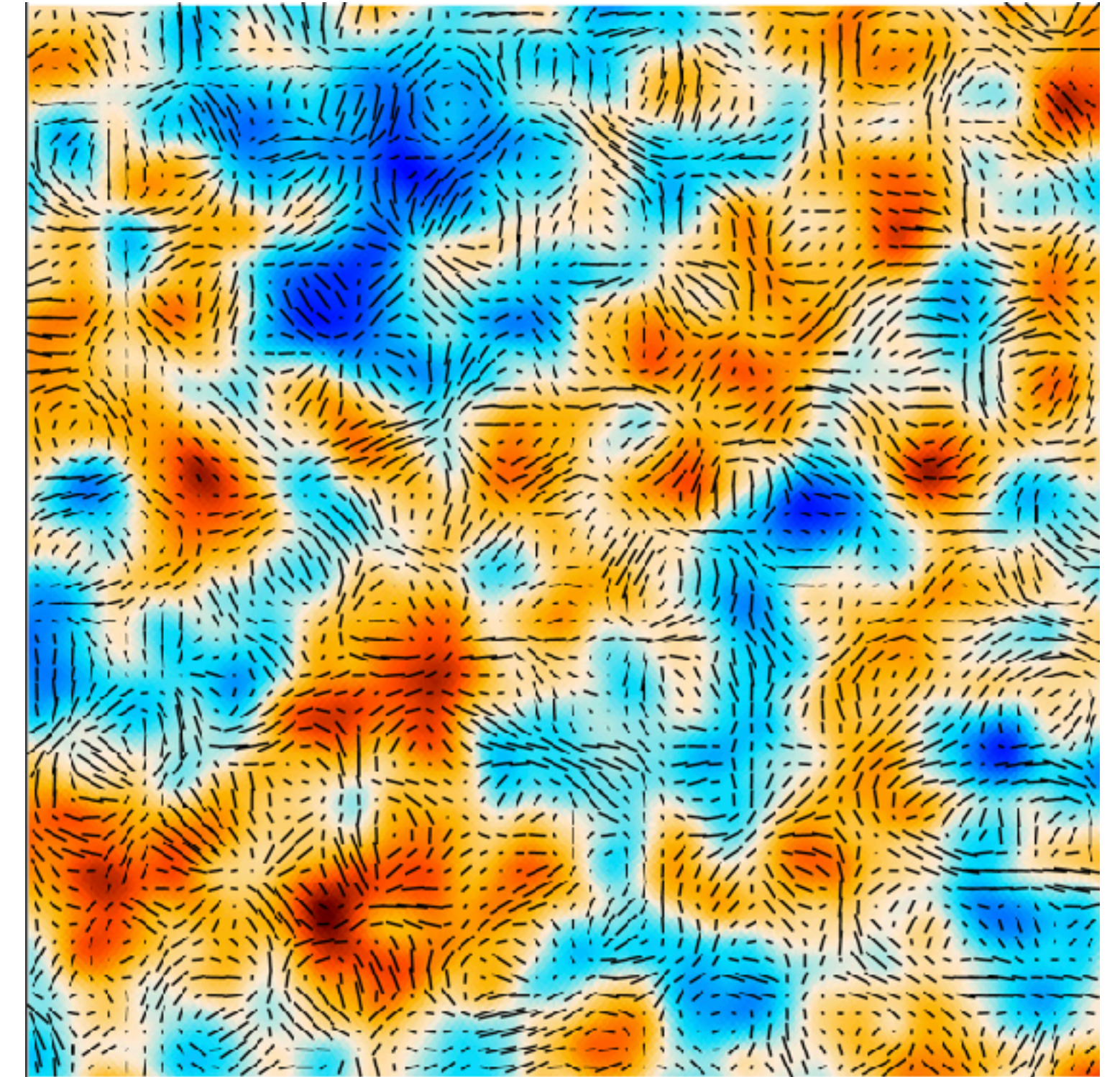
- **E-mode**：Polarization directions are **parallel or perpendicular** to the wavenumber direction

- **B-mode**：Polarization directions are **45 degrees tilted** w.r.t the wavenumber direction
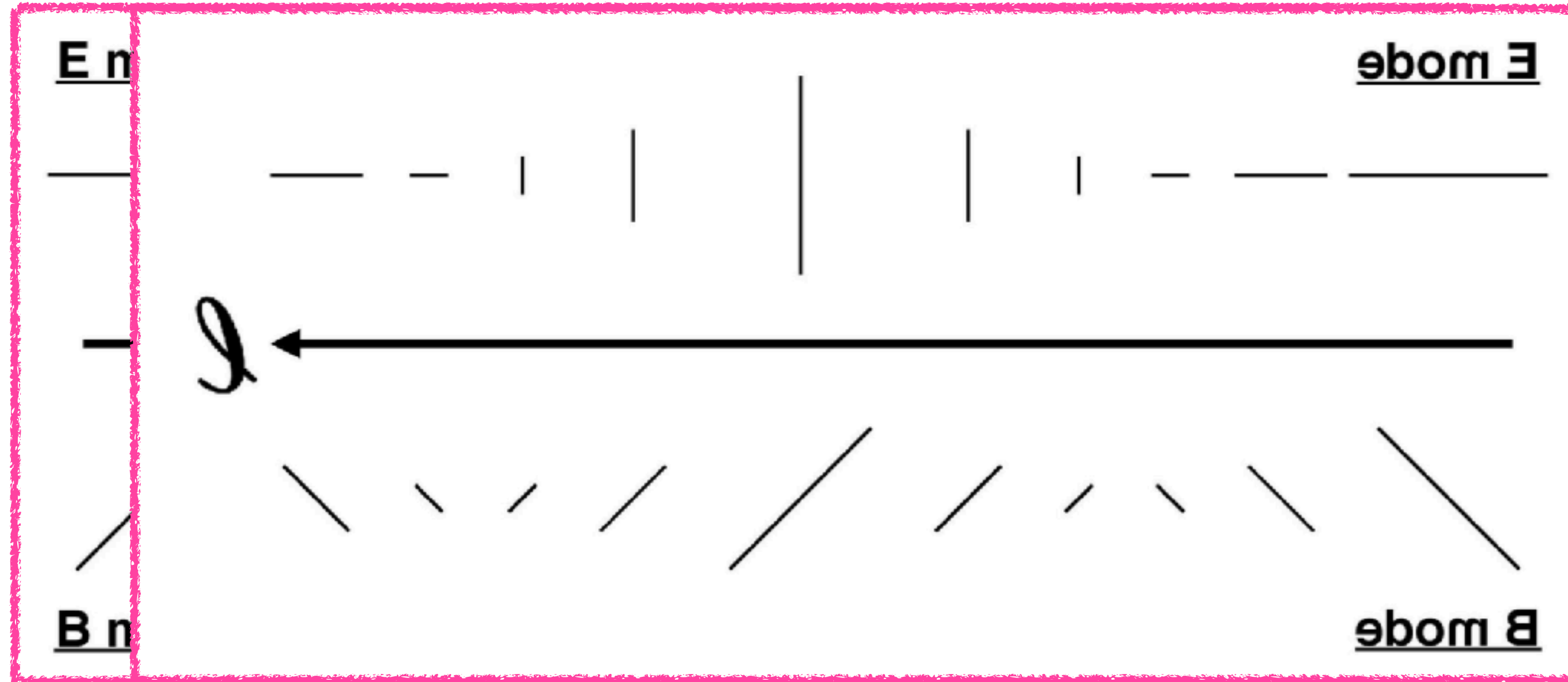
Parity eigenstates: E and B modes
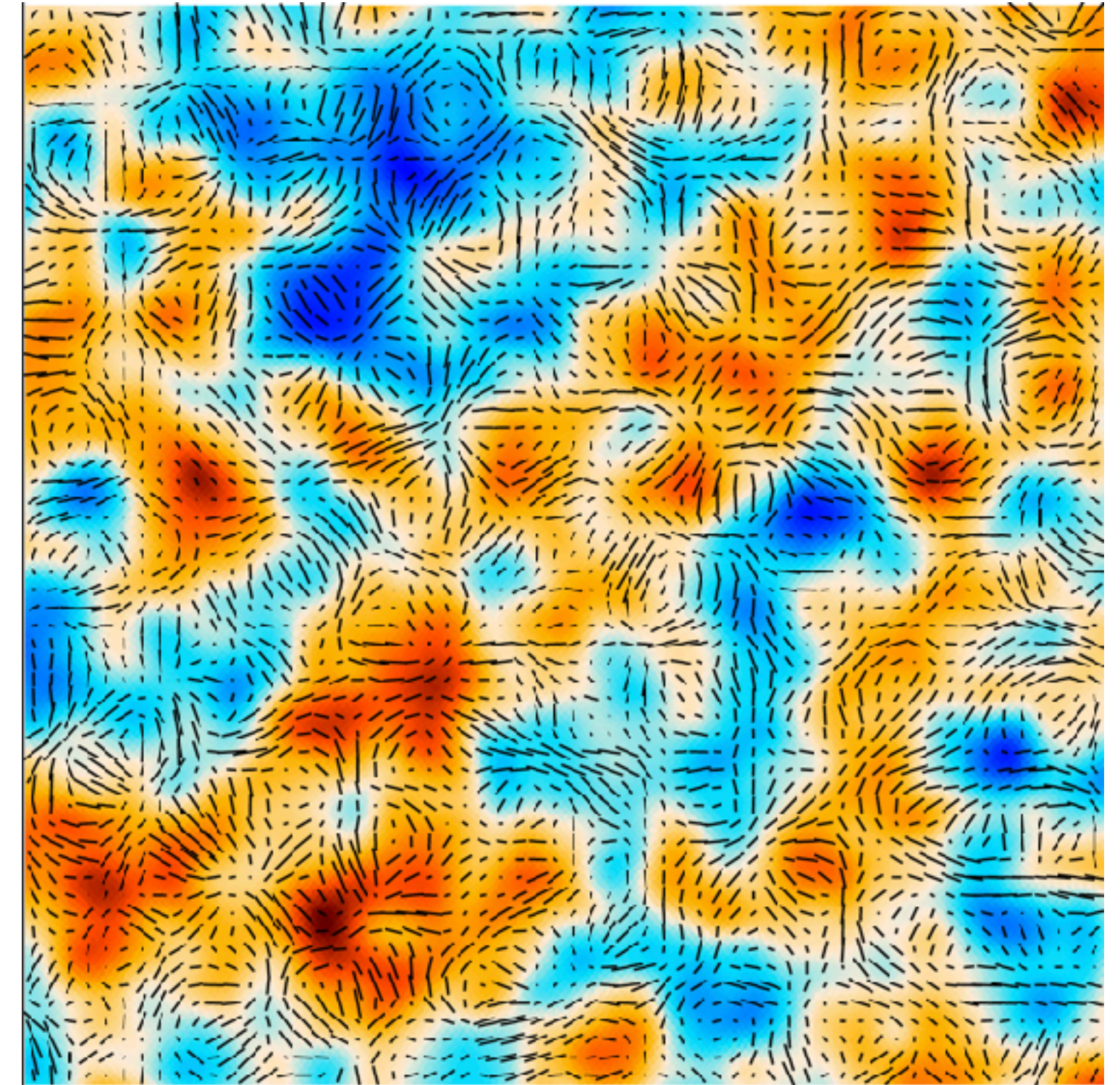
Concept defined in Fourier space

This map is dominated by E-mode polarization

$$\langle E_{\boldsymbol{\ell}} E_{\boldsymbol{\ell'}}^* \rangle = (2\pi)^2 \delta_D^{(2)}(\boldsymbol{\ell} - \boldsymbol{\ell'}) C_{\ell}^{EE}$$

$$\langle B_{\boldsymbol{\ell}} B_{\boldsymbol{\ell'}}^* \rangle = (2\pi)^2 \delta_D^{(2)}(\boldsymbol{\ell} - \boldsymbol{\ell'}) C_{\ell}^{BB}$$

$$\langle T_{\boldsymbol{\ell}} E_{\boldsymbol{\ell'}}^* \rangle = \langle T_{\boldsymbol{\ell}}^* E_{\boldsymbol{\ell'}} \rangle = (2\pi)^2 \delta_D^{(2)}(\boldsymbol{\ell} - \boldsymbol{\ell'}) C_{\ell}^{TE}$$

These are scalars and insensitive to parity violation.

Parity eigenstates: E and B modes

Concept defined in Fourier space

E mode

ℓ

B mode

This map is dominated by E-mode polarization

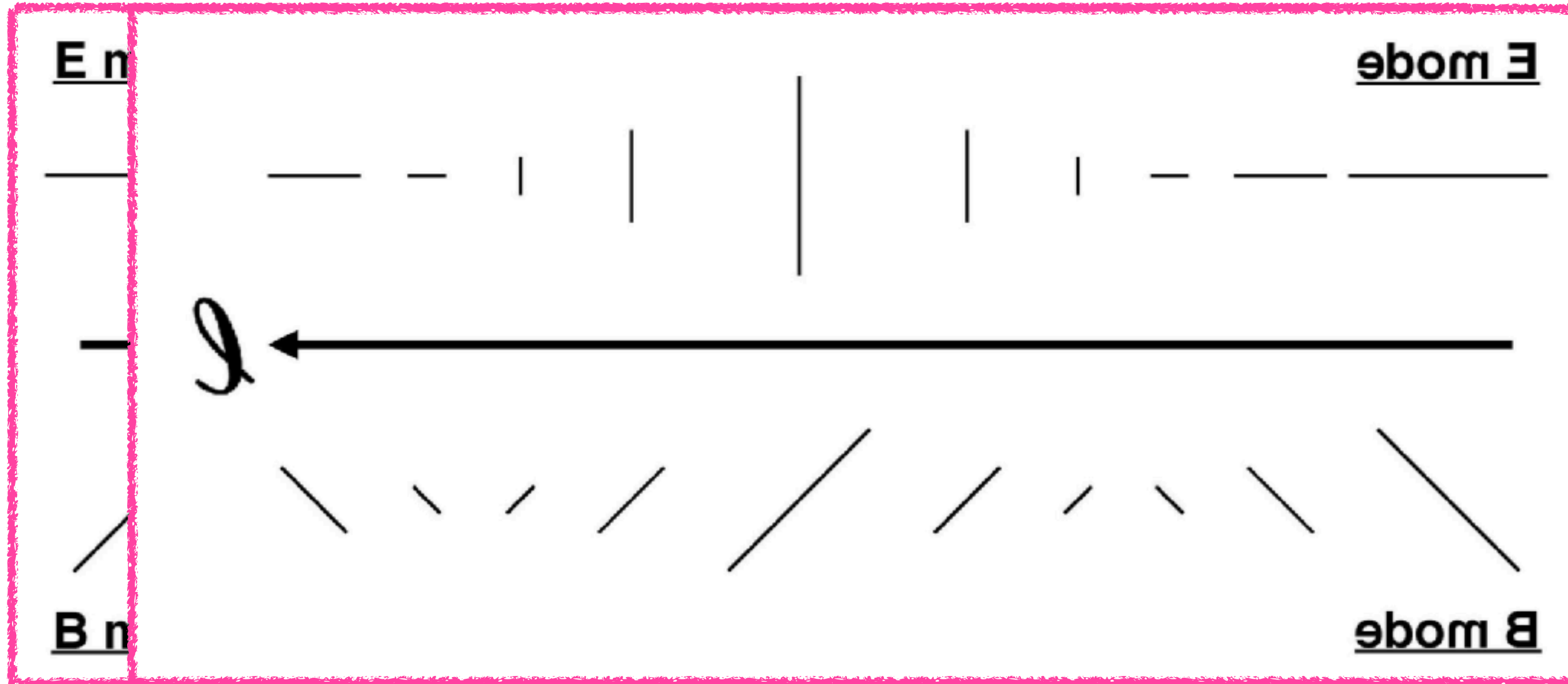$$\langle E_\ell E_{\ell'}^* \rangle = (2\pi)^2 \delta_D^{(2)}(\ell - \ell') C_\ell^{EE}$$

$$\langle B_\ell B_{\ell'}^* \rangle = (2\pi)^2 \delta_D^{(2)}(\ell - \ell')$$

$$\langle T_\ell E_{\ell'}^* \rangle = \langle T_\ell^* E_{\ell'} \rangle = (2\pi)^2 \delta_D^{(2)}(\ell - \ell') C_\ell^{TE}$$
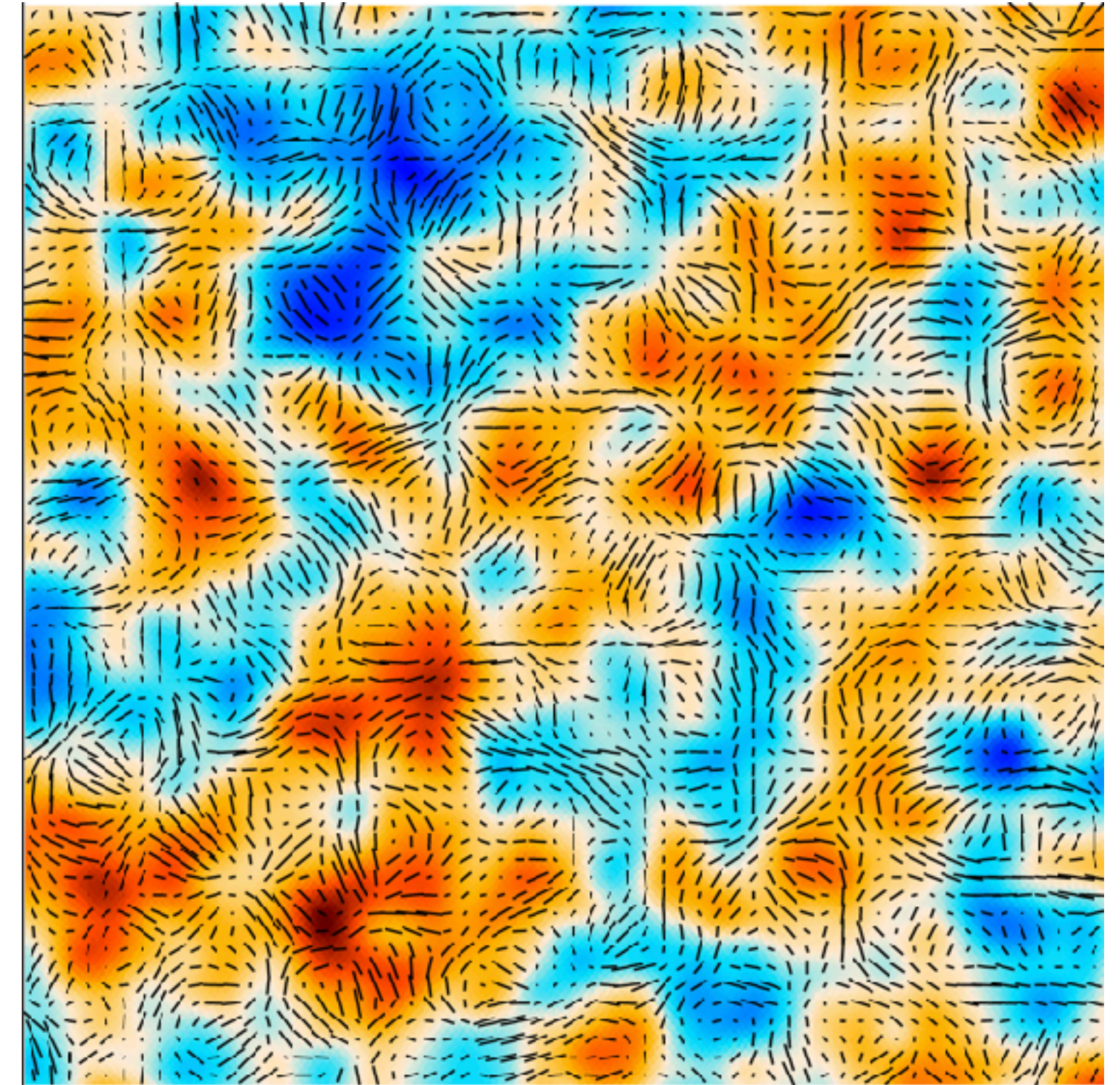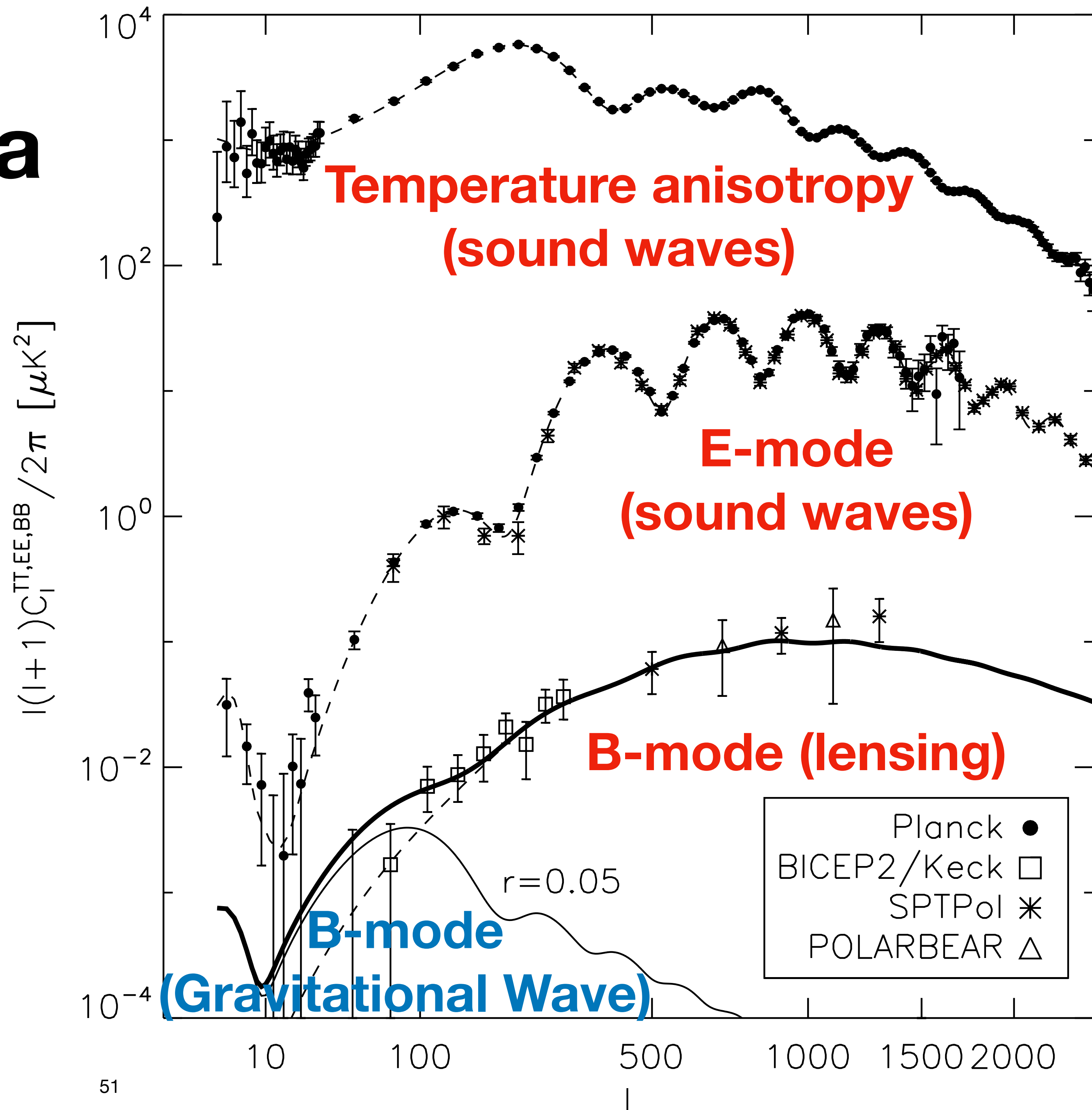
The other combinations, <TB> and <EB>, are pseudoscalars and sensitive to parity violation!
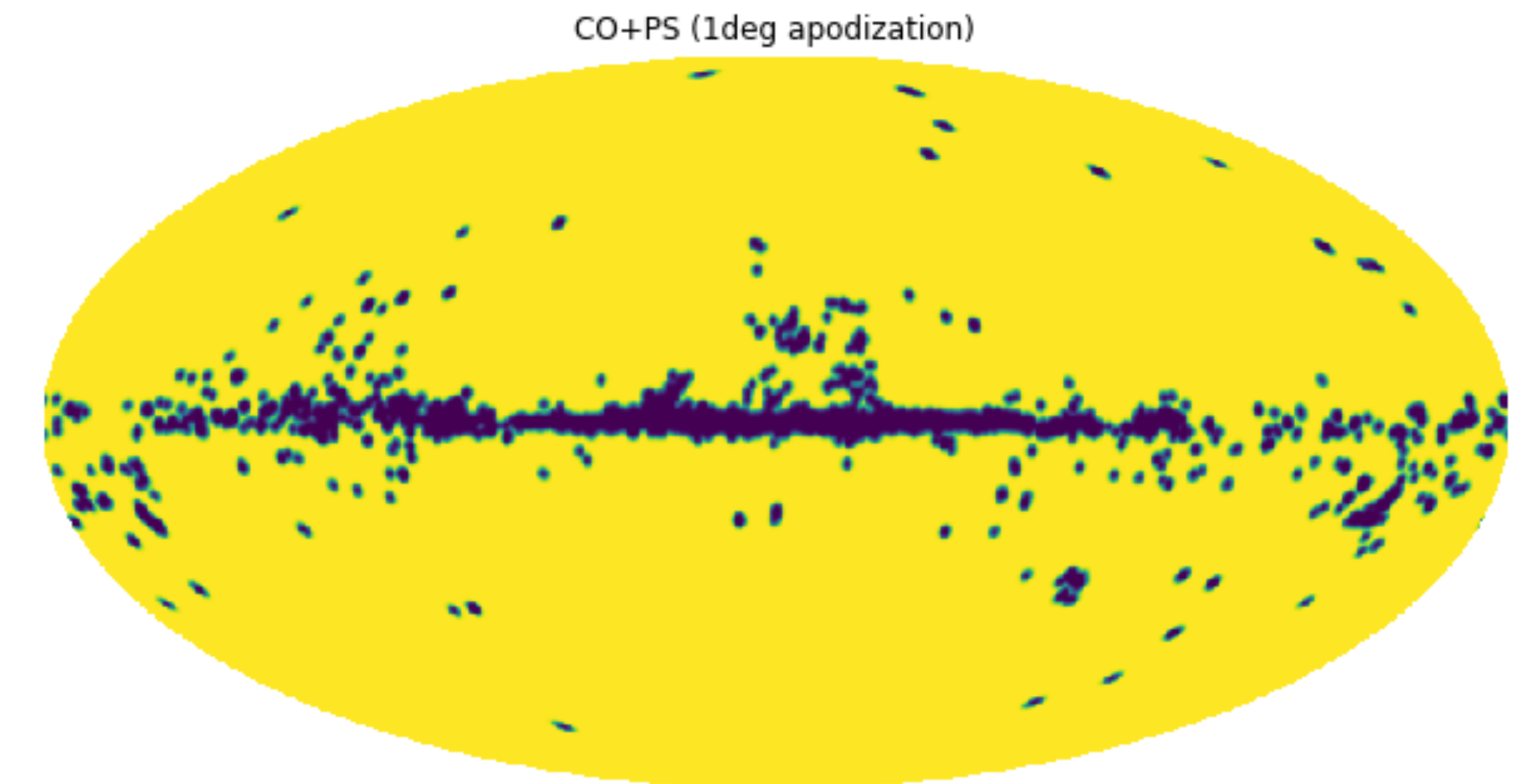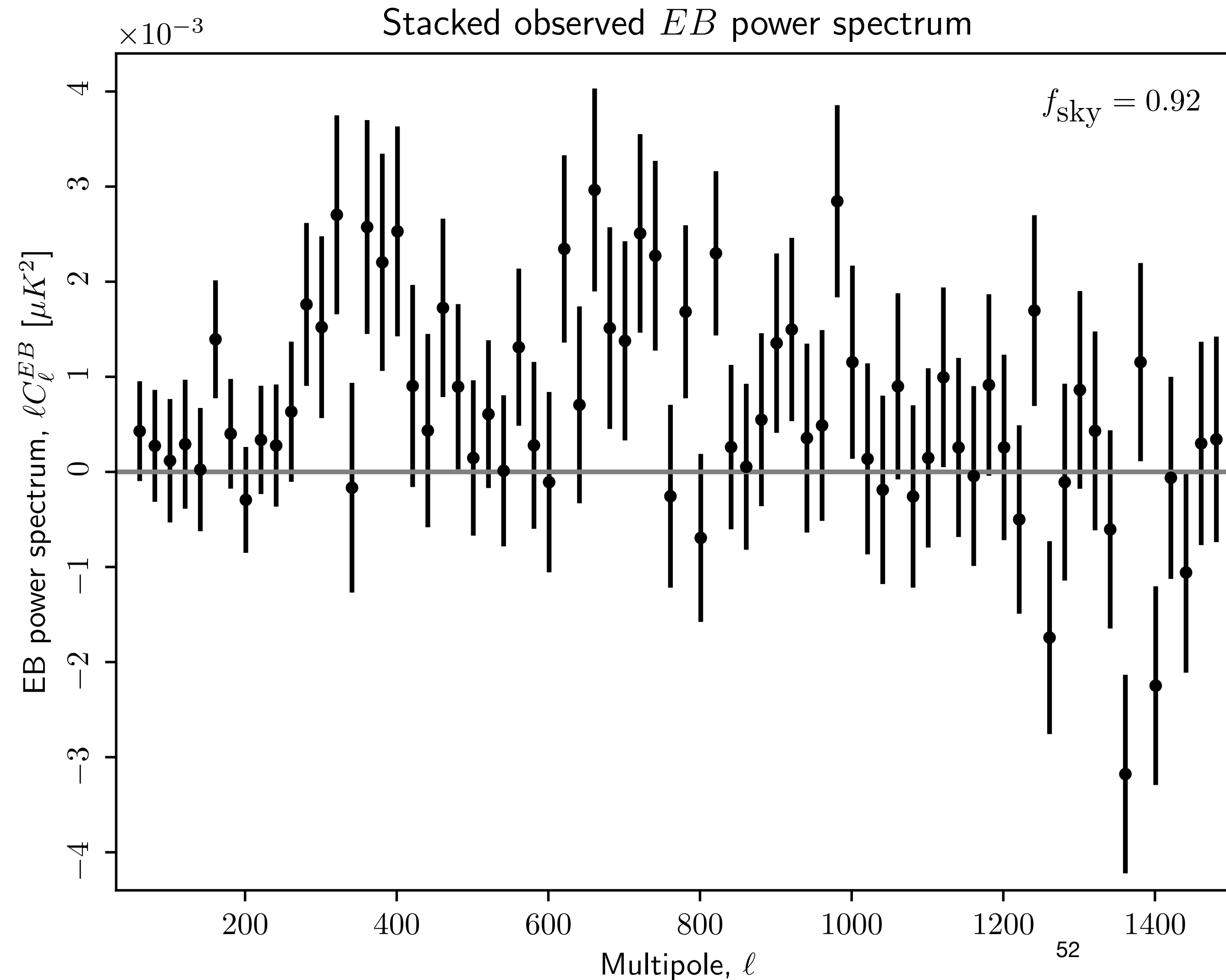
CMB Power Spectra
Progress over 30 years

- This is the typical figure seen in talks and lectures on the CMB.

  - The temperature and the E- and B-mode polarization power spectra are well measured.

- **Parity violation appears in the TB and EB power spectra, not shown here.**

Temperature anisotropy (sound waves)

E-mode (sound waves)

B-mode (lensing)

B-mode (Gravitational Wave)

r=0.05

Planck ●
BICEP2/Keck ☐
SPTPol ✳
POLARBEAR △

$l(l+1)C_l^{TT,EE,BB}/2\pi\ [\mu K^2]$

51

This is the EB power spectrum (WMAP+Planck)

Nearly full-sky data (92% of the sky)

Stacked observed EB power spectrum

$f_{\mathrm{sky}} = 0.92$

EB power spectrum, $\ell C_\ell^{EB} \ [\mu K^2]$

Multipole, ℓ

CO+PS (1deg apodization)

- $\chi^2 = 125.5$ for DOF=72

  - Unambiguous signal of something!

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This is the EB power spectrum (WMAP+Planck)

Galactic plane removed (62% of the sky)

Stacked observed EB power spectrum

$f_{\rm sky} = 0.62$
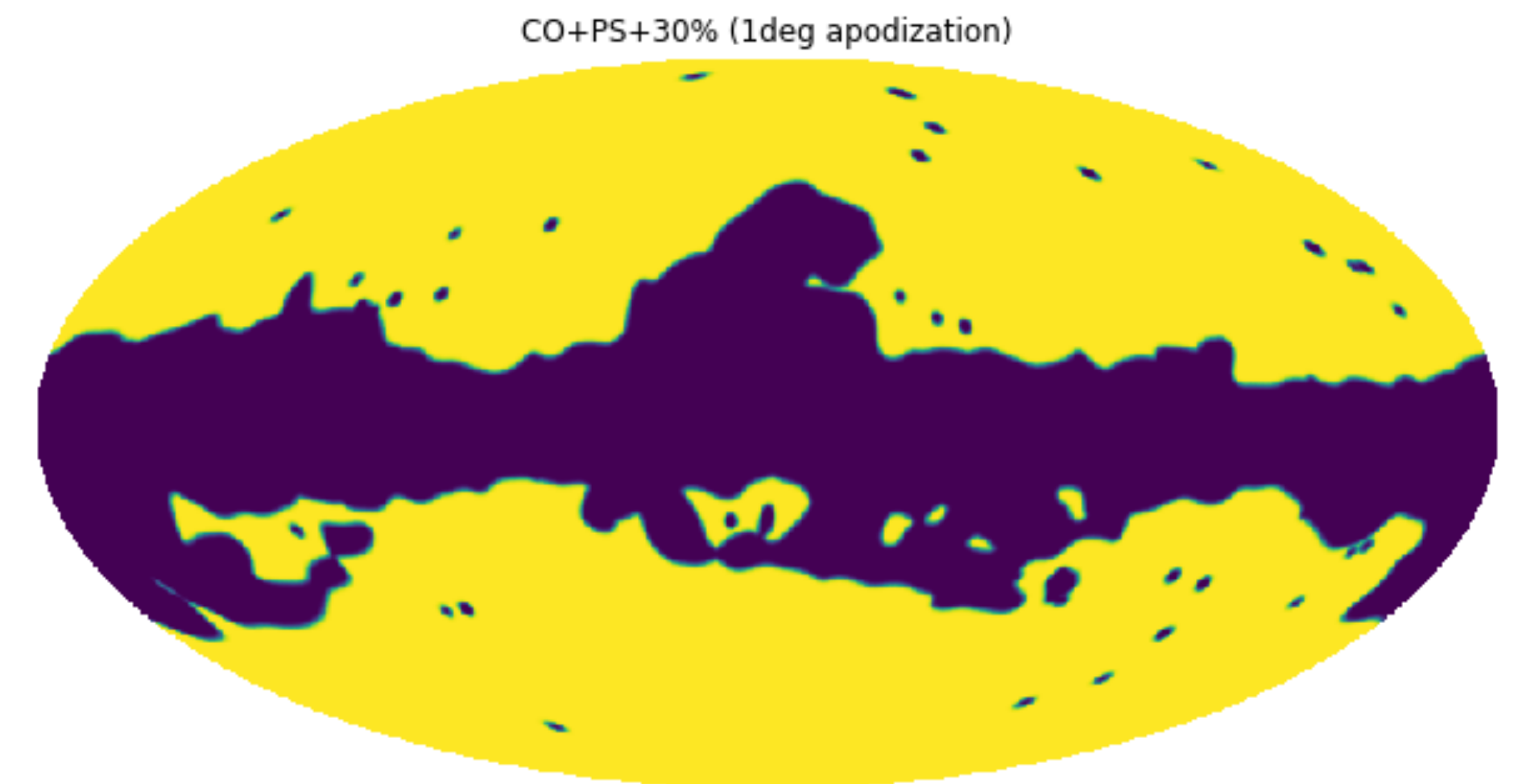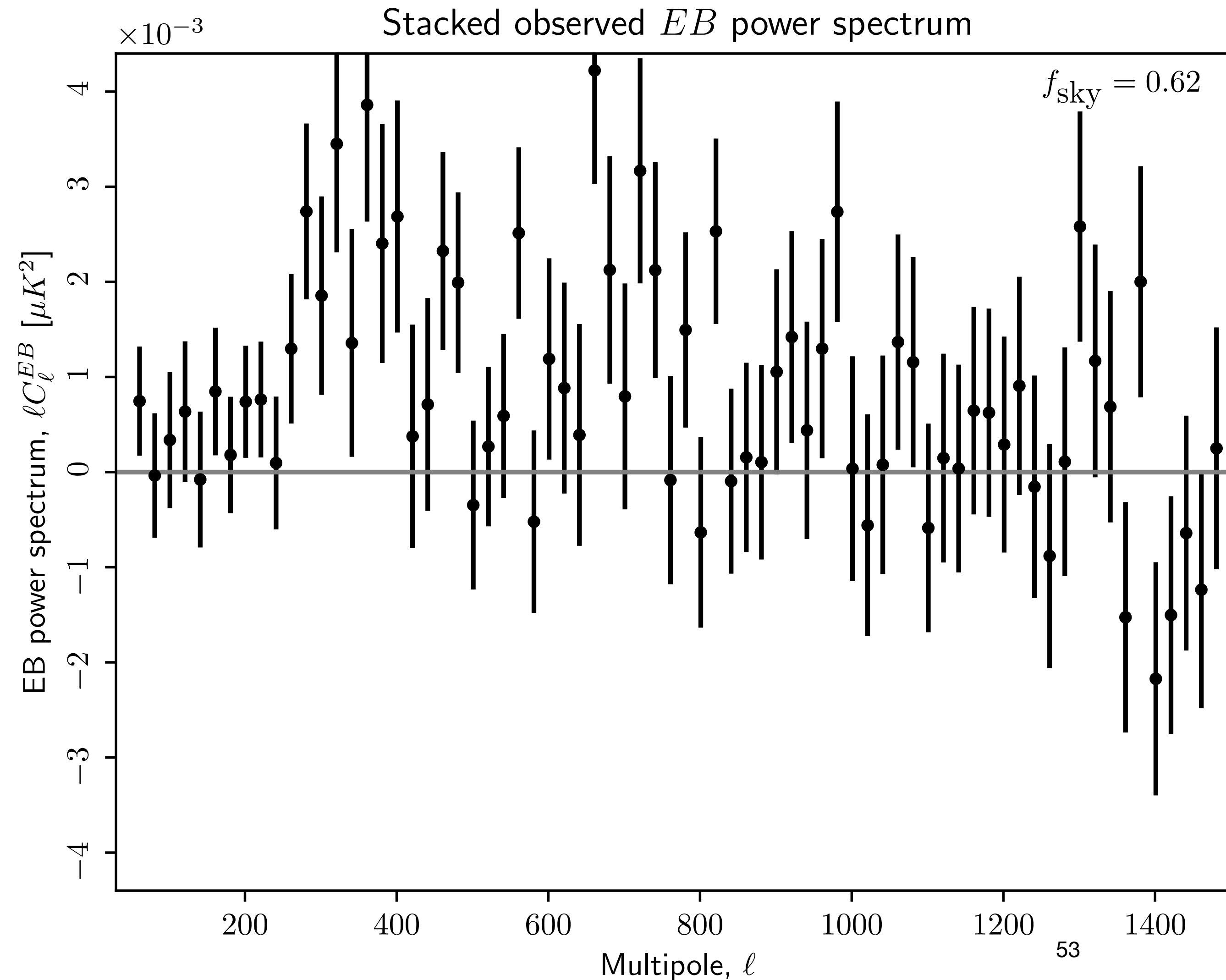
- χ² = 138.4

  - The signal exists regardless of the Galactic mask. This rules out the Galactic foreground.

E-B mixing by rotation of the plane of linear polarization

- Observed E- and B-mode polarization, E_ℓ^o and B_ℓ^o, are related to those before rotation as

$$E_\ell^o \pm iB_\ell^o = (E_\ell \pm iB_\ell)e^{\pm 2i\beta}$$

- which gives

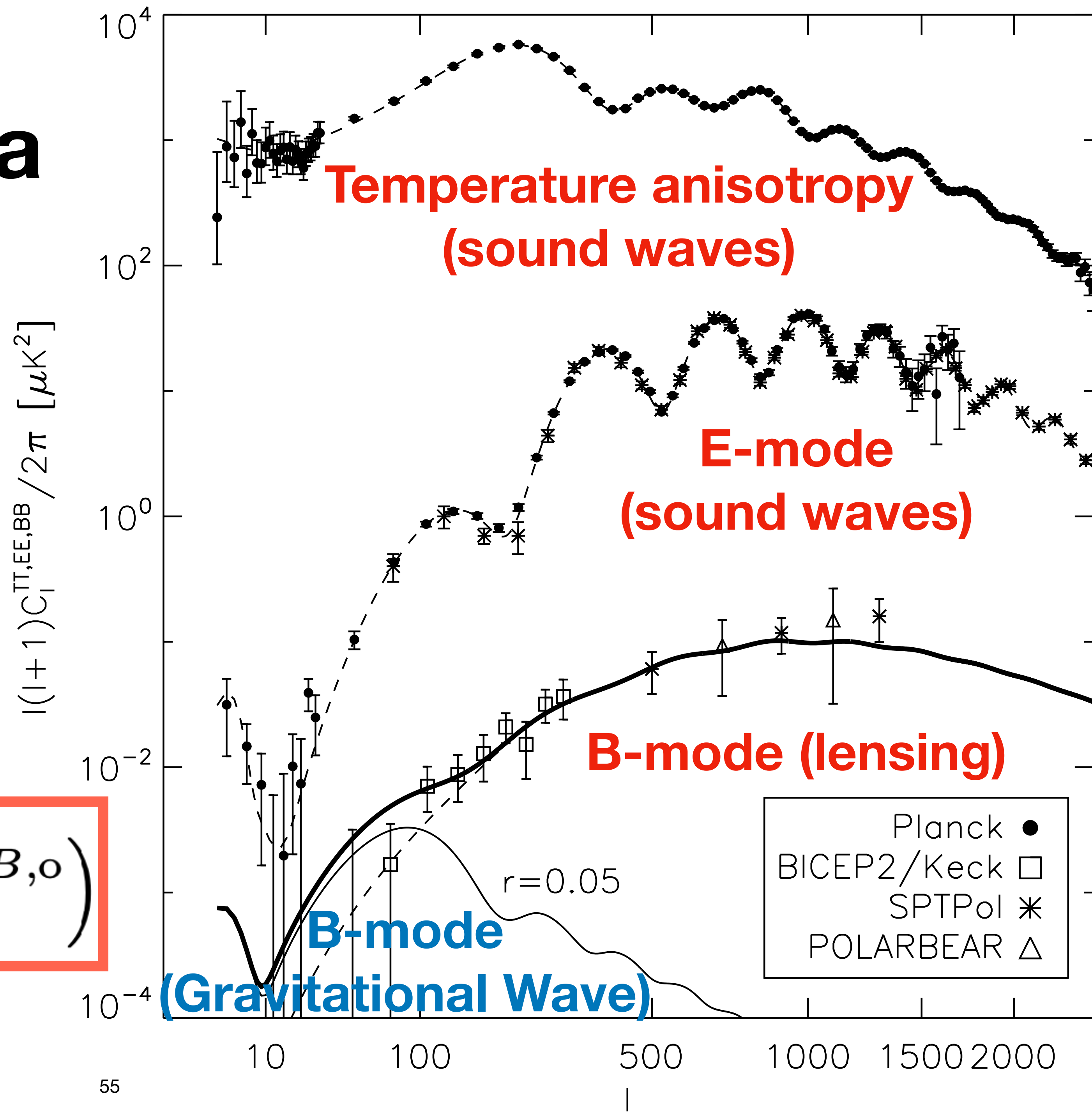$$E_\ell^o = E_\ell \cos(2\beta) - B_\ell \sin(2\beta)$$

$$B_\ell^o = E_\ell \sin(2\beta) + B_\ell \cos(2\beta)$$
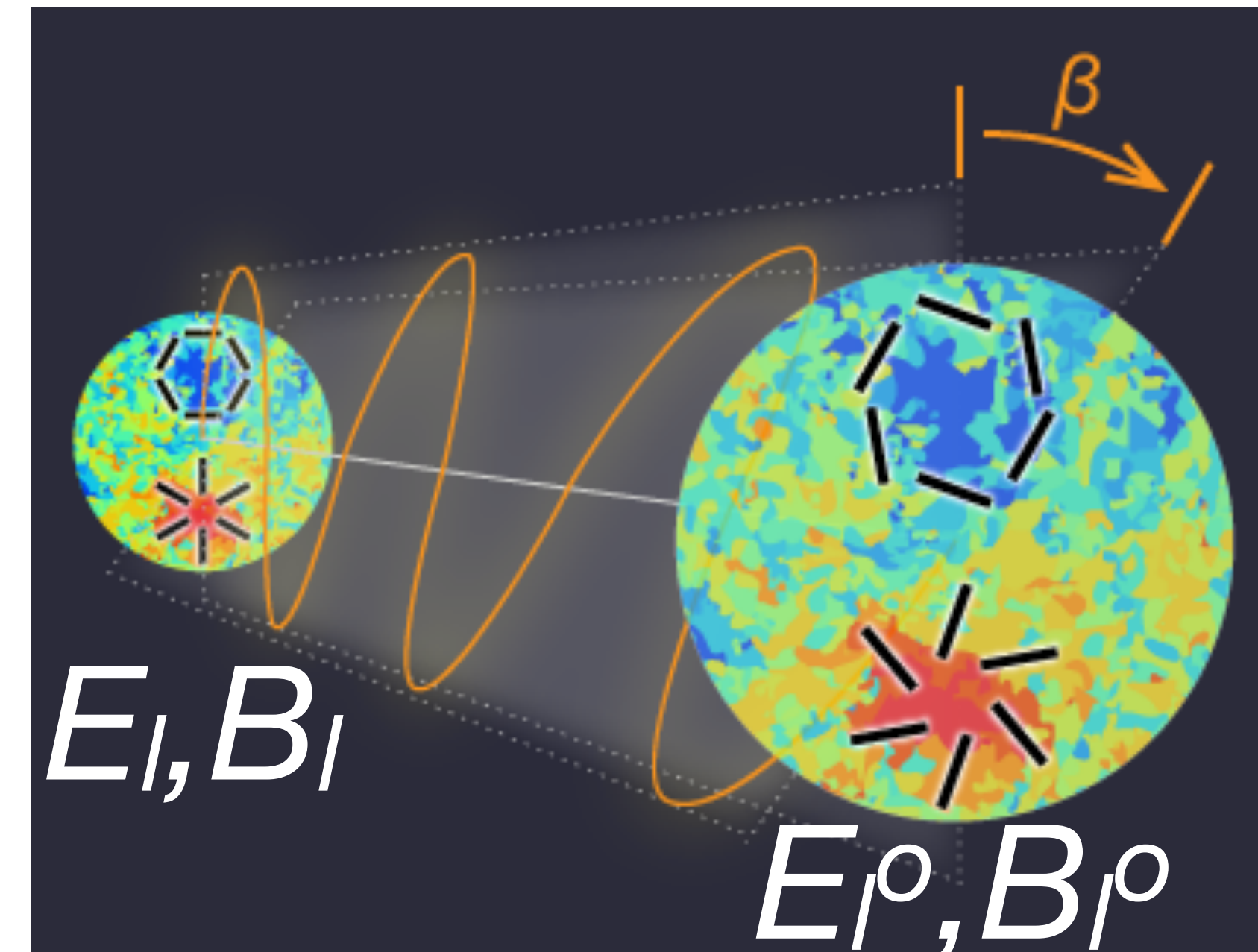
CMB Power Spectra

- Rotation of the plane of linear polarization **mixes** E and B modes.

- Therefore, the EB correlation will be given by the difference between the EE and BB correlations.

- Observed EE is much greater than BB. We expect EB to look like EE!

$$C_\ell^{EB,o} = \frac{\tan(4\beta)}{2}\left(C_\ell^{EE,o} - C_\ell^{BB,o}\right)$$

Temperature anisotropy (sound waves)

E-mode (sound waves)

B-mode (lensing)

B-mode (Gravitational Wave)

r=0.05

Planck ●
BICEP2/Keck □
SPTPol ✳
POLARBEAR △

$l(l+1)C_l^{TT,EE,BB}/2\pi$ $[\mu K^2]$

10   100   500   1000 1500 2000

l

55

Cosmic Birefringence fits well(?)

$$C_\ell^{EB,o} = \frac{\tan(4\beta)}{2}\left(C_\ell^{EE,o} - C_\ell^{BB,o}\right)$$

Nearly full-sky data (92% of the sky)

Stacked observed EB power spectrum

$f_{\rm sky} = 0.92$

Cosmic birefringence ($\alpha_i = 0$)

Residual with respect to the model

Multipole, ℓ

CO+PS (1deg apodization)
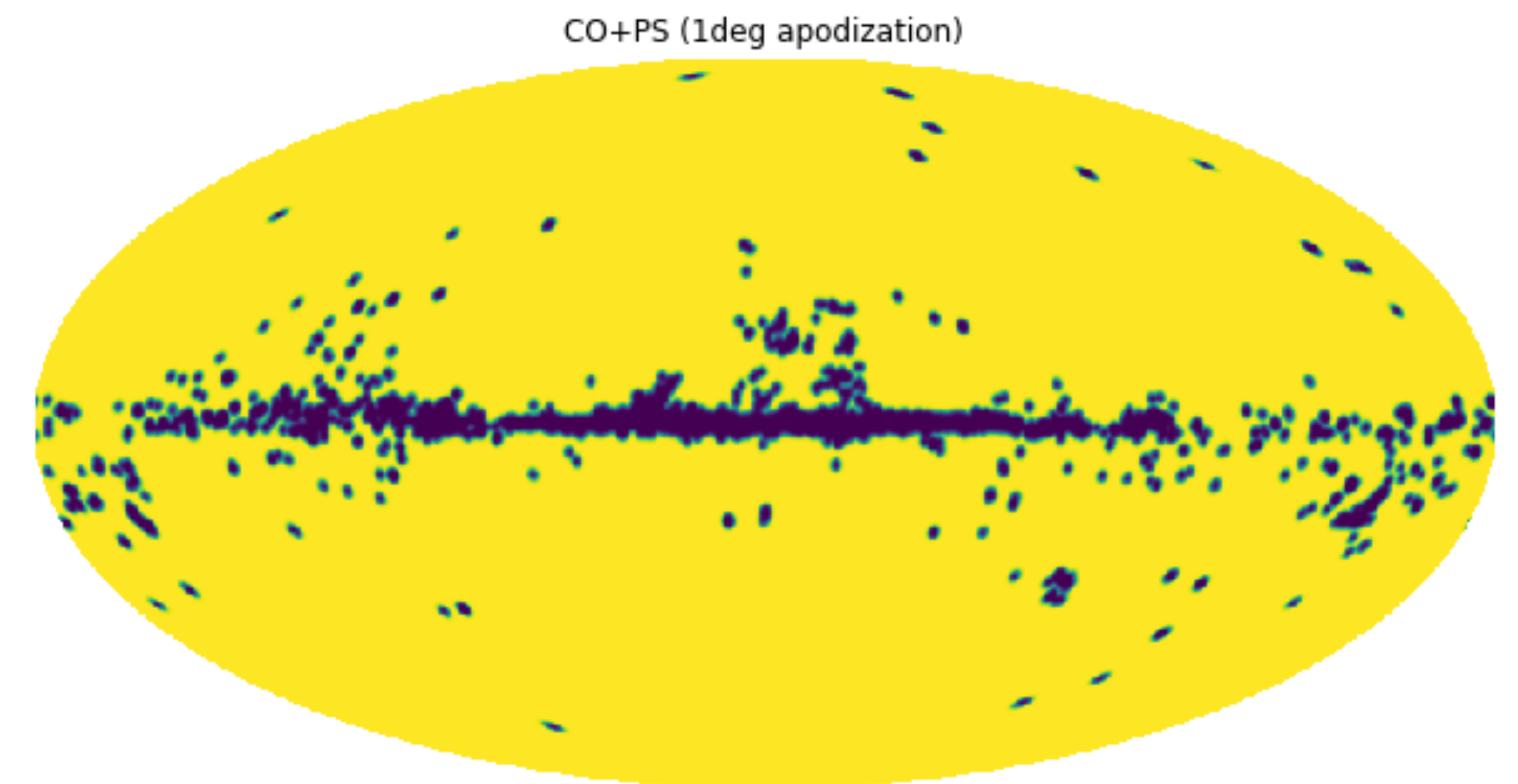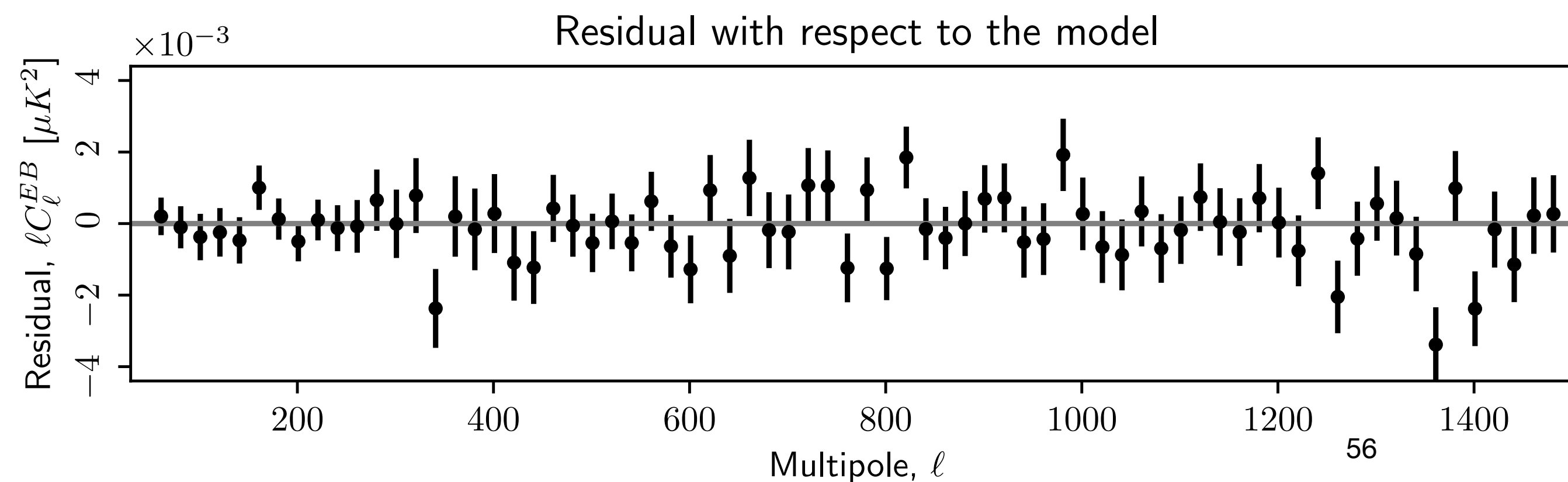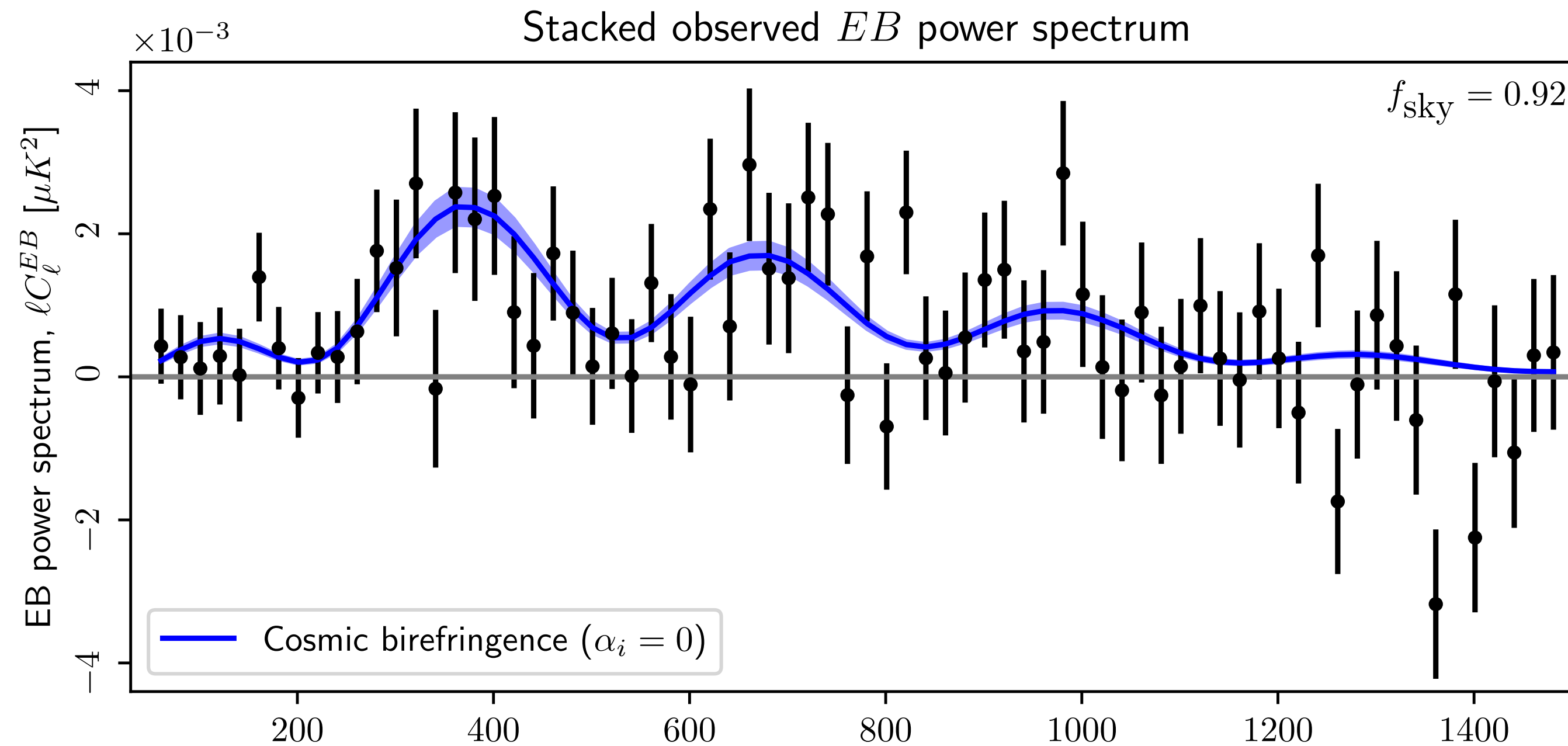
- β = 0.288 ± 0.032 deg

- χ² = 66.1 for DOF=71

  - Good fit! 9σ detection?

Cosmic Birefringence fits well(?)
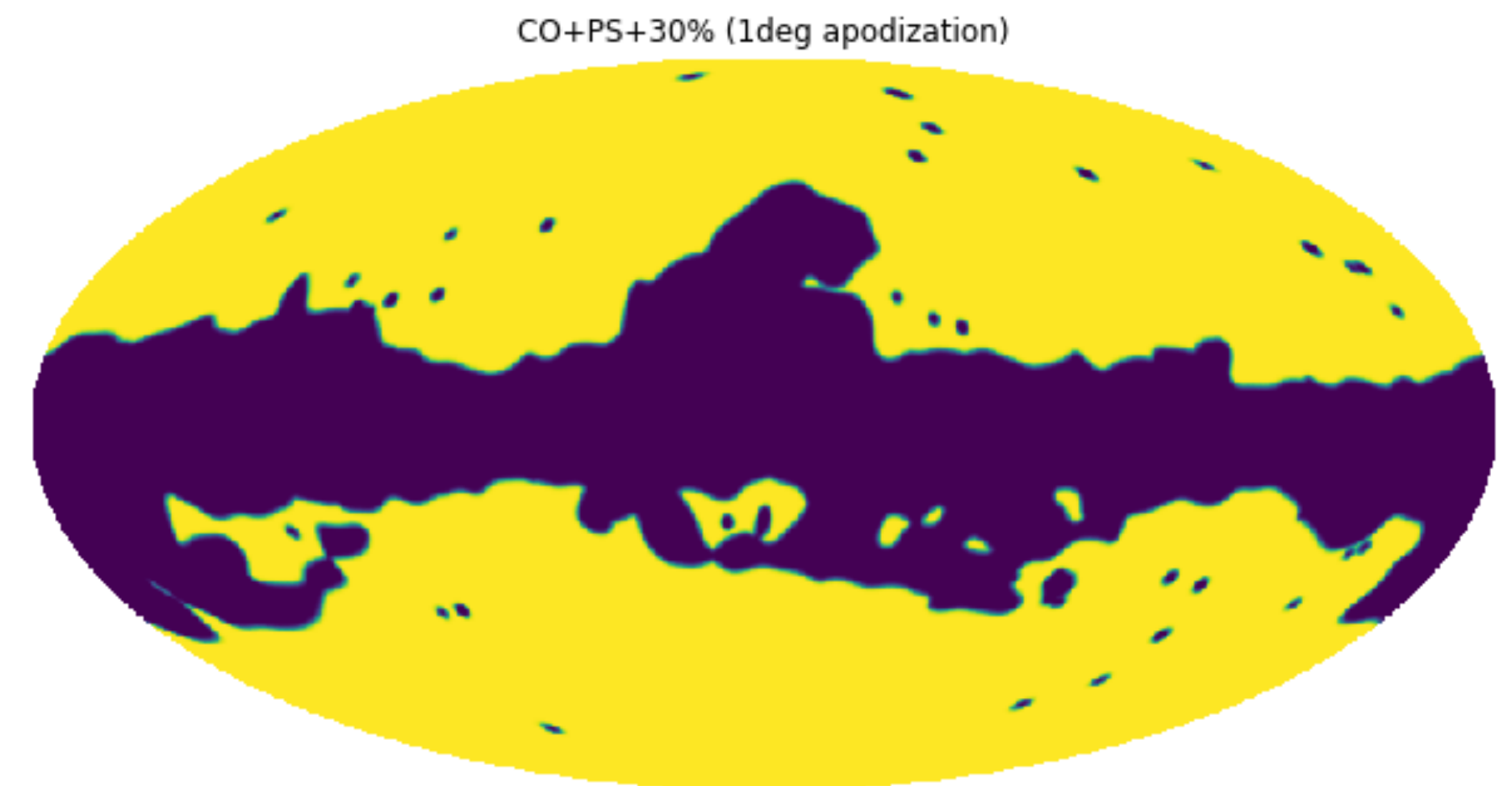
$$C_\ell^{EB,o} = \frac{\tan(4\beta)}{2}\left(C_\ell^{EE,o} - C_\ell^{BB,o}\right)$$

Galactic plane removed (62% of the sky)

Stacked observed EB power spectrum

$f_{\rm sky} = 0.62$

Cosmic birefringence ($\alpha_i = 0$)

Residual with respect to the model

Multipole, ℓ

CO+PS+30% (1deg apodization)
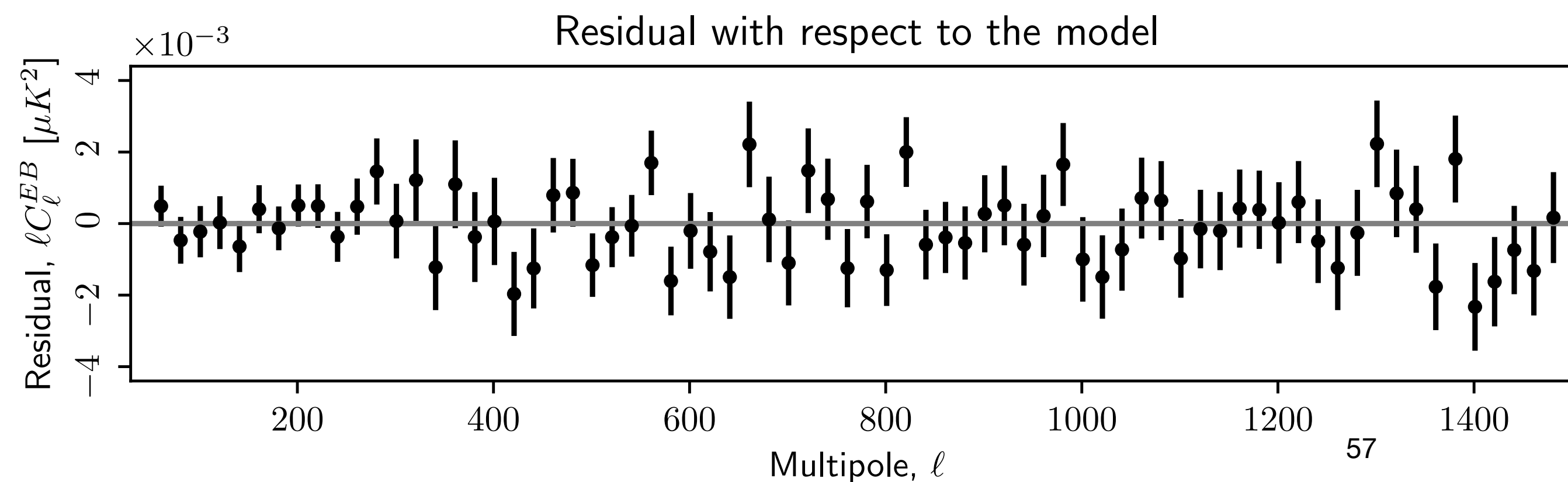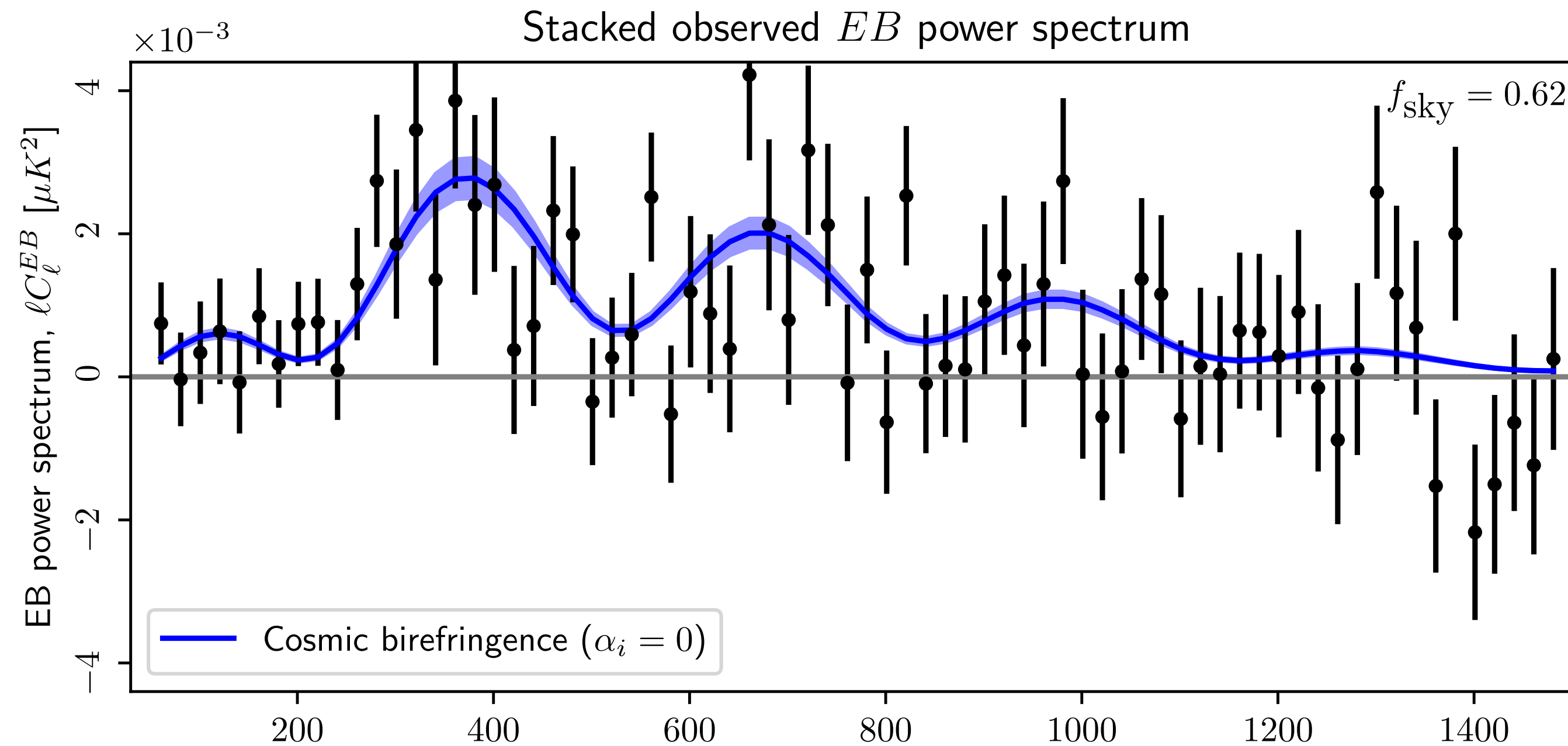
- β = 0.330 ± 0.035 deg

- χ² = 64.5

- Signal is robust with respect to the Galactic mask.

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CO+PS (1deg apodization)

$f_{sky} = 0.90$

CO+PS+5% (1deg apodization)

$f_{sky} = 0.85$

CO+PS+10% (1deg apodization)
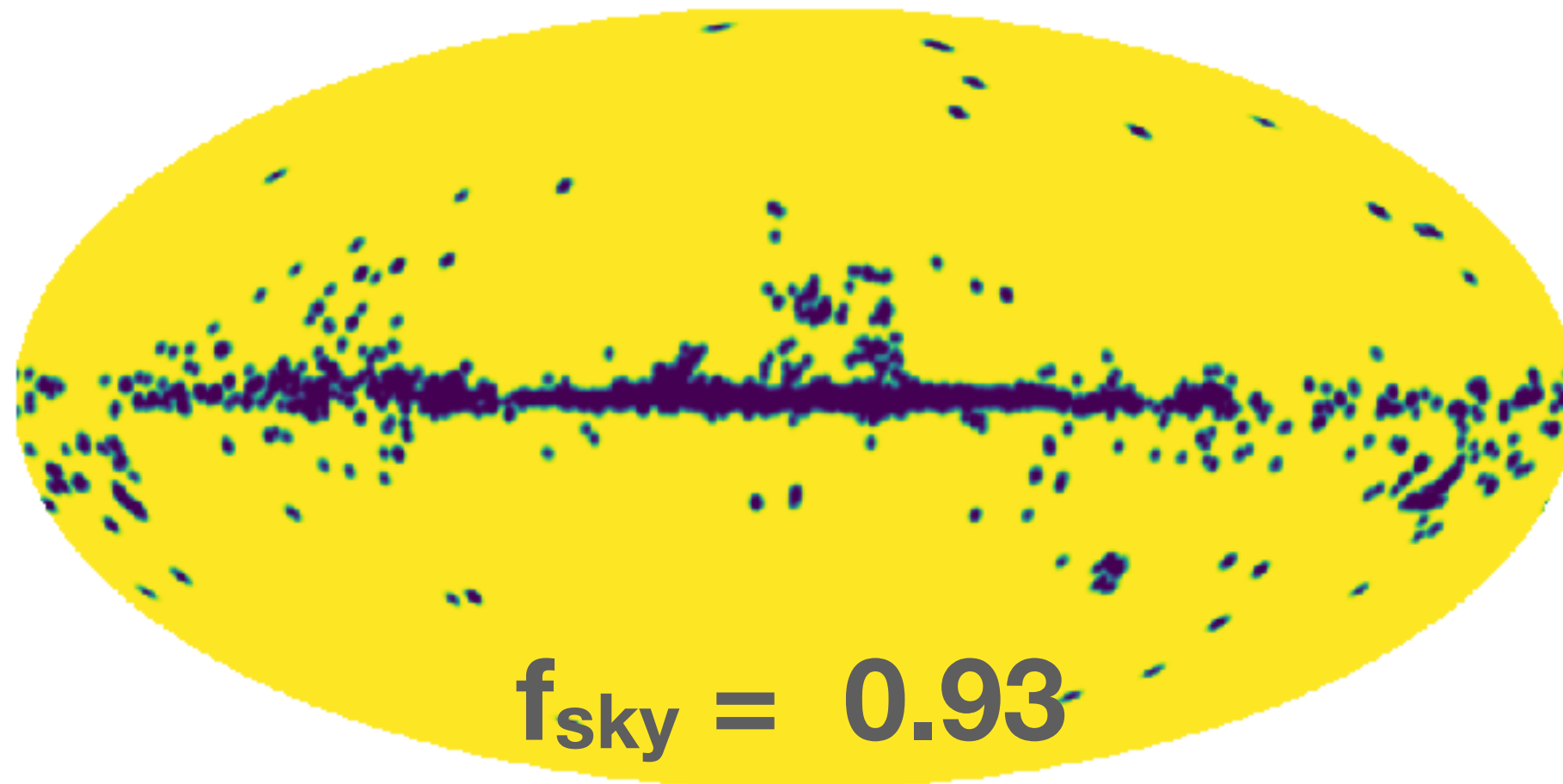
$f_{sky} = 0.93$
= nearly full sky
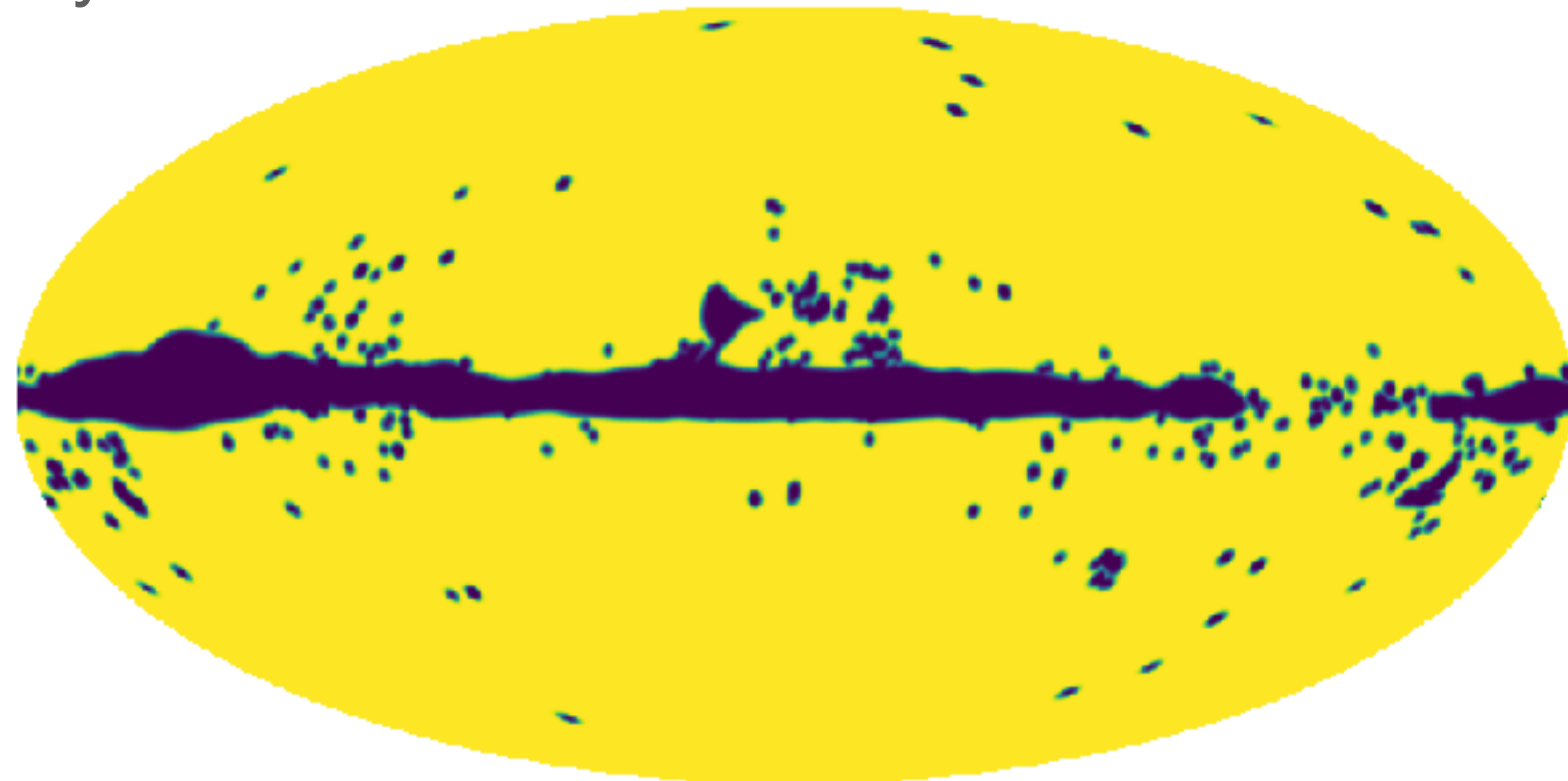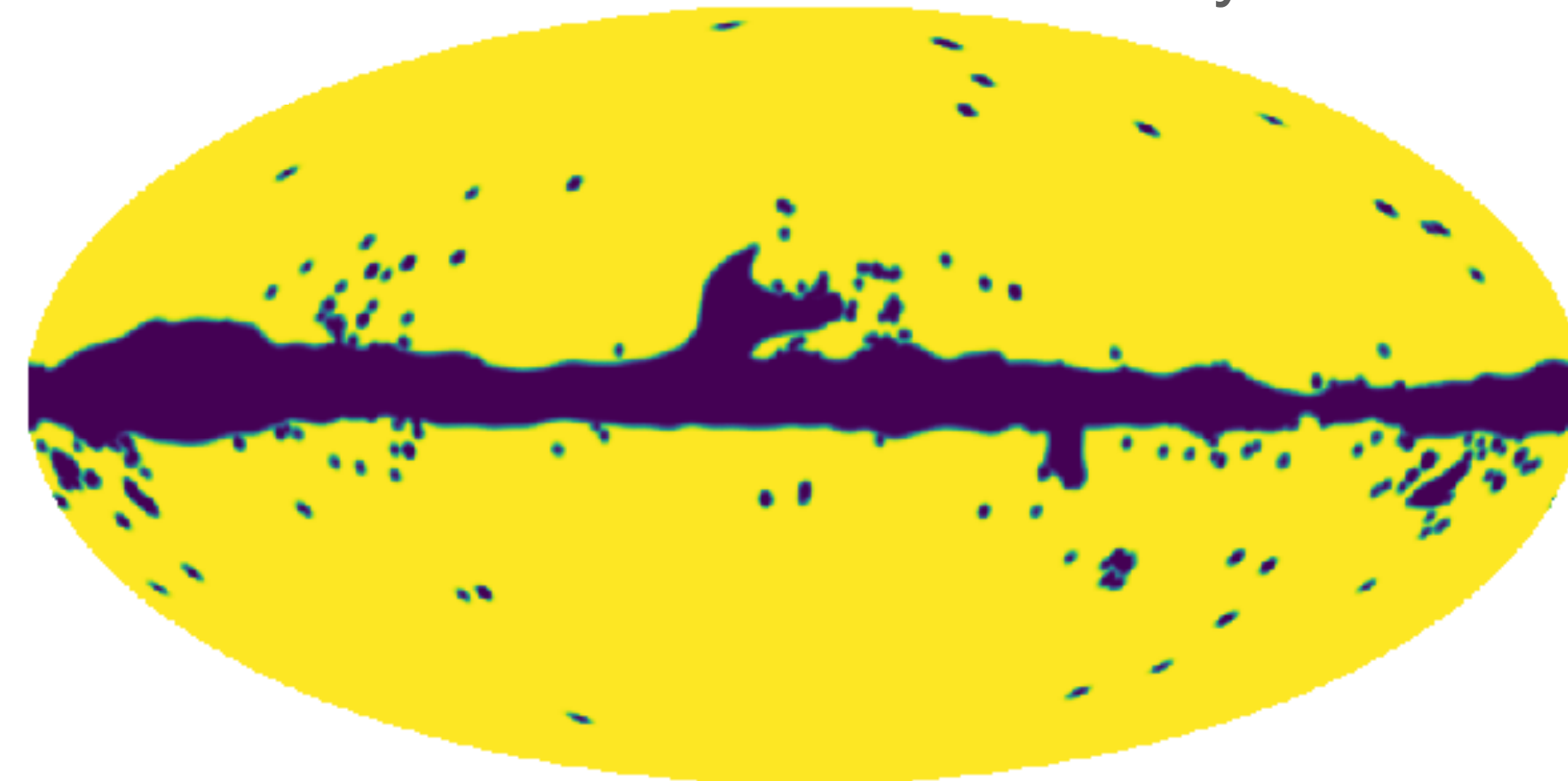
CO+PS+20% (1deg apodization)

CO+PS+30% (1deg apodization)

$f_{sky} = 0.75$

$f_{sky} = 0.63$

58
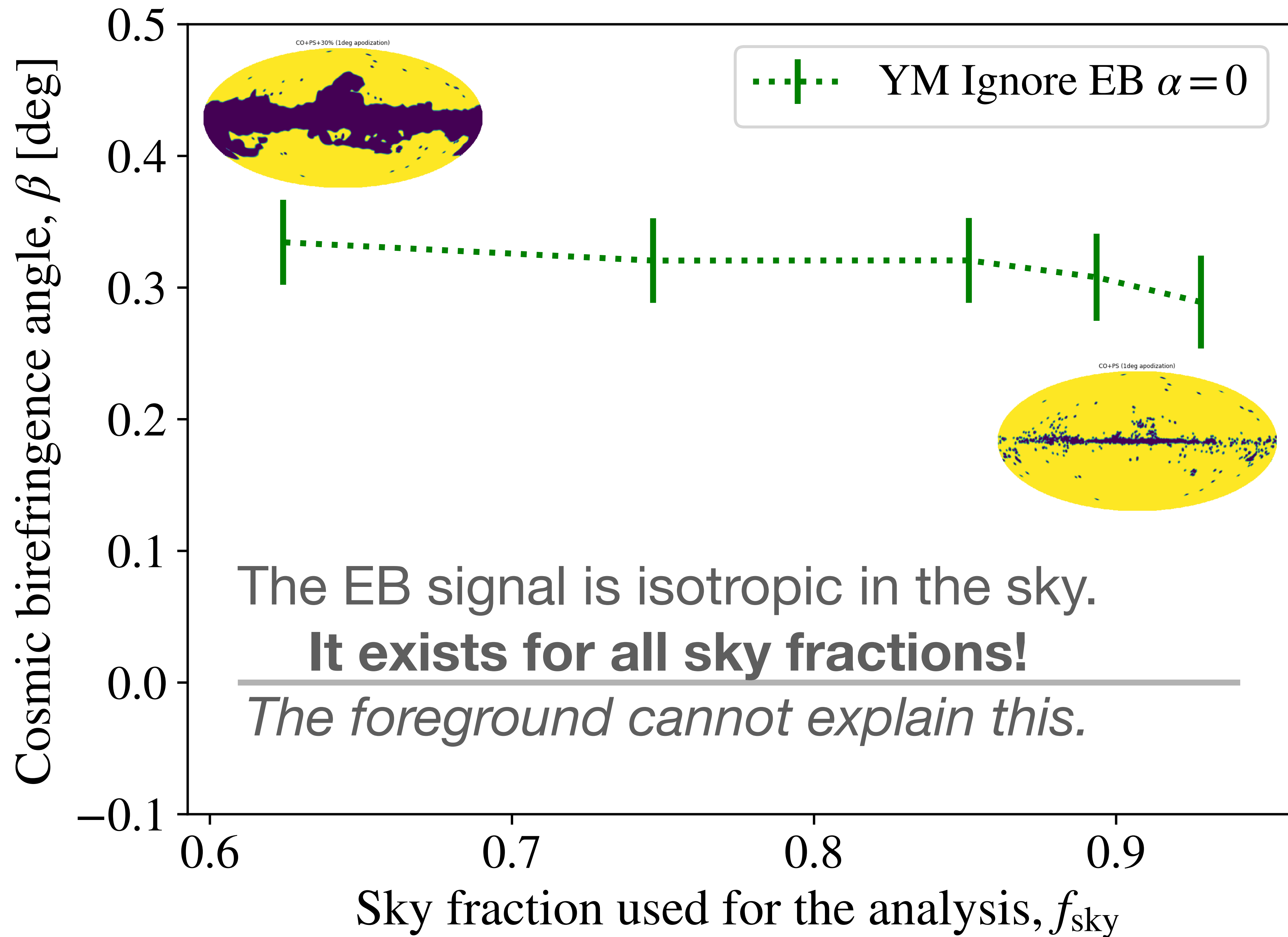
The Biggest Problem: Miscalibration of detectors

Impact of miscalibration of polarization angles

Cosmic or Instrumental?

Polarization-sensitive
detectors on the focal plane

rotated by an angle "α"
(but we do not know it)

OR

- Is the plane of linear polarization rotated by the genuine cosmic birefringence effect, or simply because the polarization-sensitive directions of the detectors are rotated with respect to the sky coordinates (and we did not know it)?

- If the detectors are rotated by α, it seems that we can measure only the **sum α+β**.

The past measurements
The quoted uncertainties are all statistical only (68%CL)

- $\alpha+\beta = -6.0 \pm 4.0$ deg (Feng et al. 2006) **first measurement**

- $\alpha+\beta = -1.1 \pm 1.4$ deg (WMAP Collaboration, Komatsu et al. 2009; 2011)

- $\alpha+\beta = 0.55 \pm 0.82$ deg (QUaD Collaboration, Wu et al. 2009)

- …

- $\alpha+\beta = 0.31 \pm 0.05$ deg (Planck Collaboration 2016)

- $\alpha+\beta = -0.61 \pm 0.22$ deg (POLARBEAR Collaboration 2020)

- $\alpha+\beta = 0.63 \pm 0.04$ deg (SPT Collaboration, Bianchini et al. 2020)

- $\alpha+\beta = 0.12 \pm 0.06$ deg (ACT Collaboration, Namikawa et al. 2020)

- $\alpha+\beta = 0.07 \pm 0.09$ deg (ACT Collaboration, Choi et al. 2020)

} Why not yet discovered?

The past measurements
Now including the estimated systematic errors on α

- β = –6.0 ± 4.0 ± **??** deg (Feng et al. 2006)

- β = –1.1 ± 1.4 ± **1.5** deg (WMAP Collaboration, Komatsu et al. 2009; 2011)

- β = 0.55 ± 0.82 ± **0.5** deg (QUaD Collaboration, Wu et al. 2009)

- …

- β = 0.31 ± 0.05 ± **0.28** deg (Planck Collaboration 2016)

- β = –0.61 ± 0.22 ± **??** deg (POLARBEAR Collaboration 2020)

- β = 0.63 ± 0.04 ± **??** deg (SPT Collaboration, Bianchini et al. 2020)

- β = 0.12 ± 0.06 ± **??** deg (ACT Collaboration, Namikawa et al. 2020)

- β = 0.07 ± 0.09 ± **??** deg (ACT Collaboration, Choi et al. 2020)

Uncertainty in the calibration of α has been the major limitation

The Key Idea: The polarized Galactic foreground emission as a calibrator
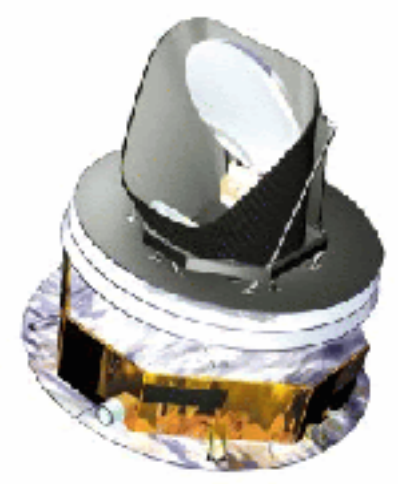
ESA's Planck

Polarized dust emission within our Milky Way!

Emitted "right there" - it would not be affected by the cosmic birefringence.

Directions of the magnetic field inferred from polarization of the thermal dust emission in the Milky Way

Miscalibration angles (WMAP and Planck)
Nearly full-sky data (92% of the sky)
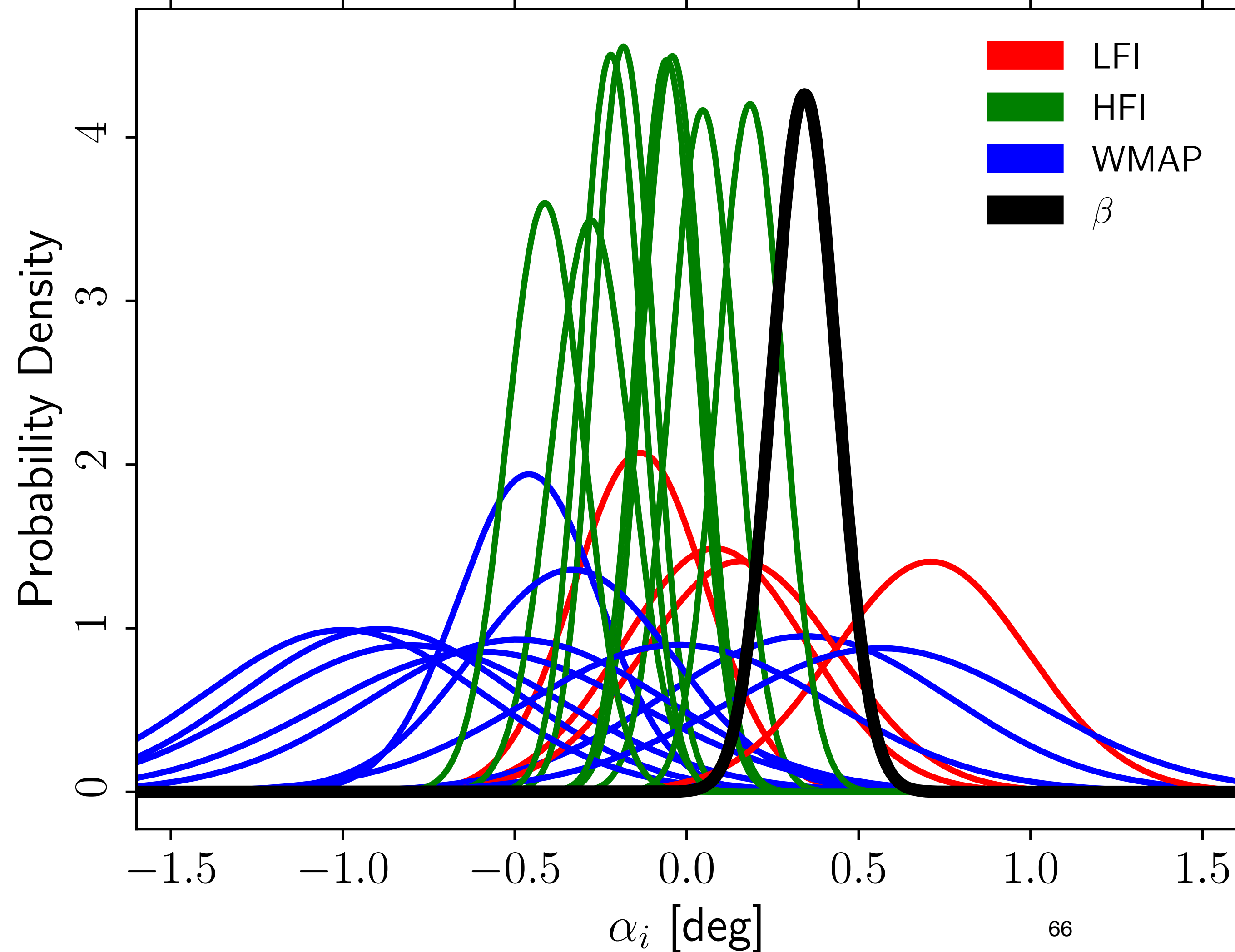
- The angles are all over the place, and are well within the quoted calibration uncertainty of instruments.

  - 1.5 deg for WMAP

  - 1 deg for Planck

- They cancel!

  - The power of adding independent datasets.

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Cosmic Birefringence fits well (WMAP+Planck)

Nearly full-sky data (92% of the sky)
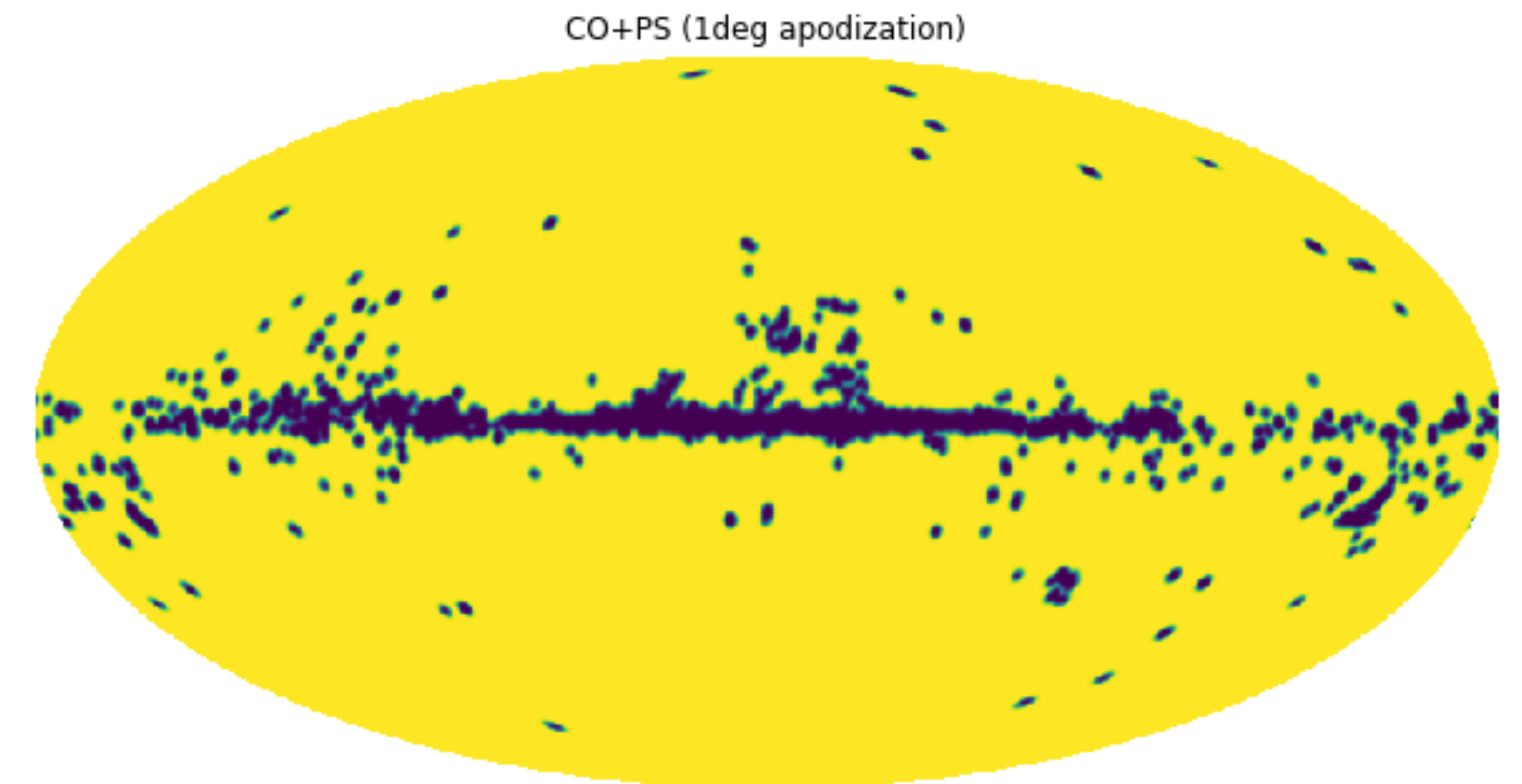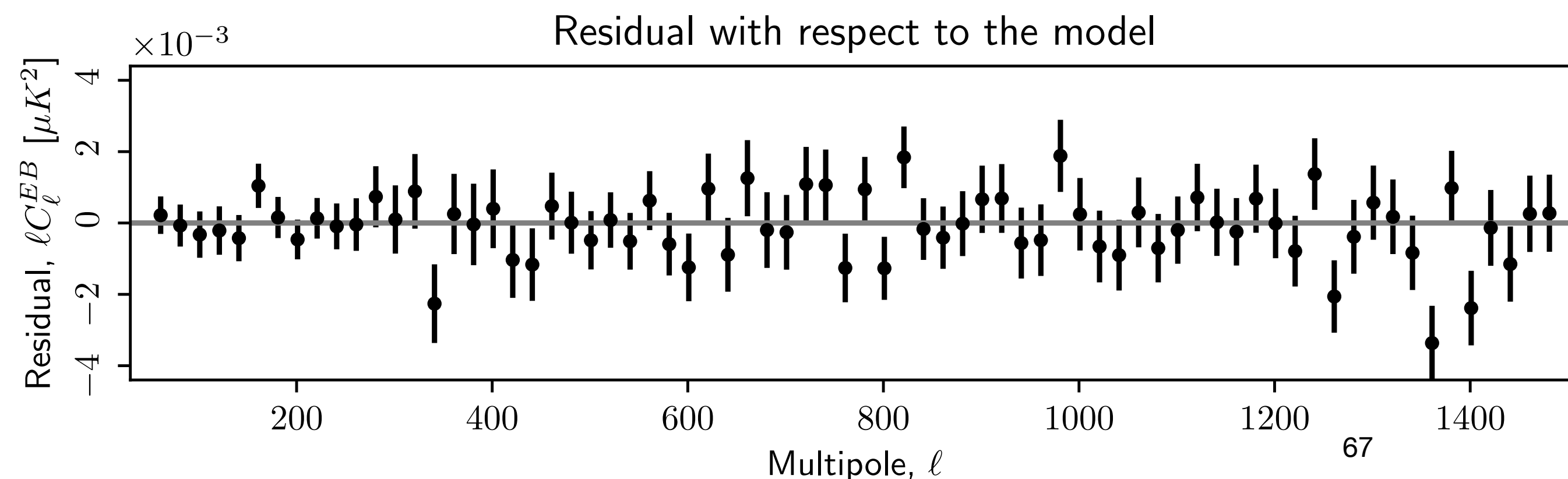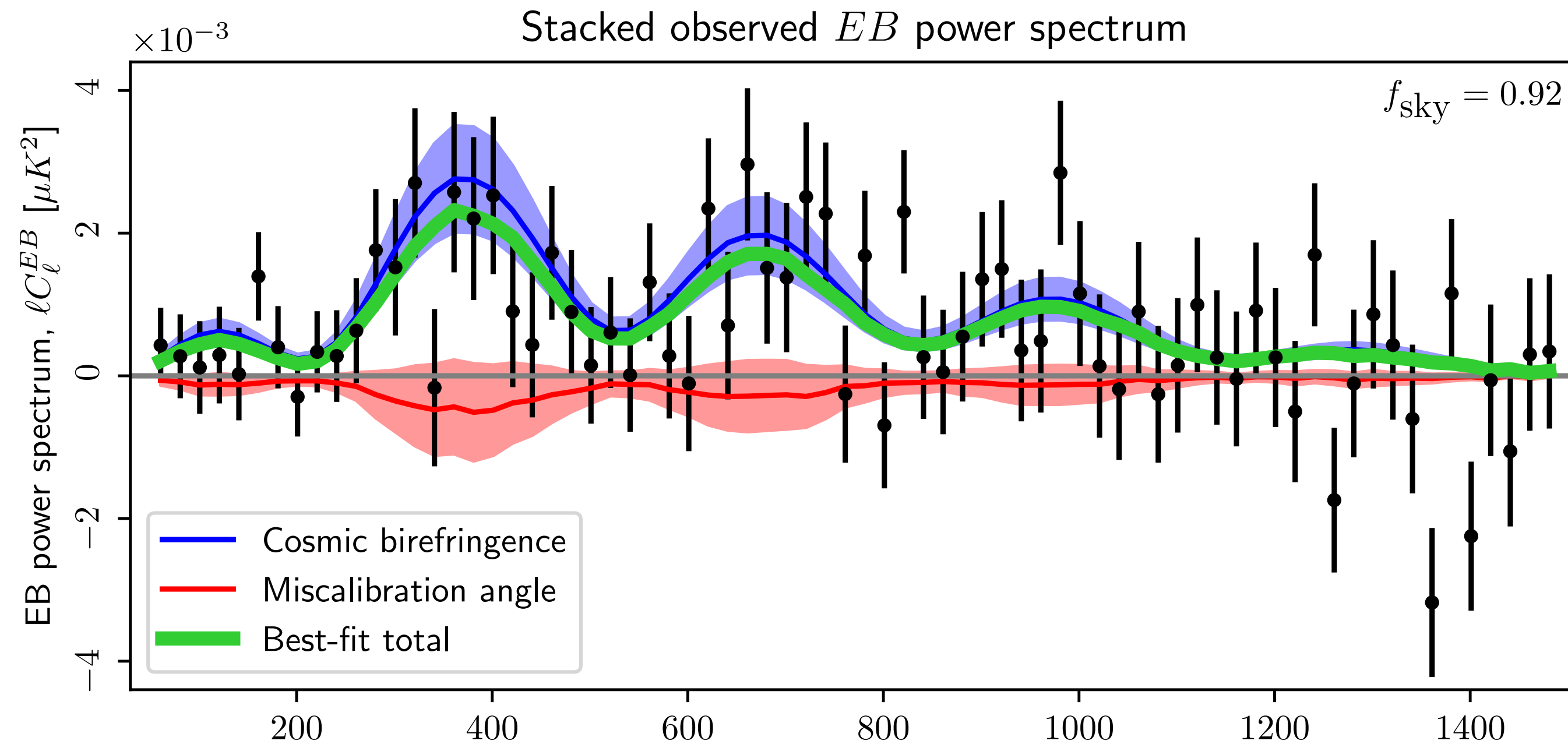
Stacked observed EB power spectrum

$f_{\rm sky} = 0.92$

Cosmic birefringence
Miscalibration angle
Best-fit total

Residual with respect to the model

Multipole, ℓ

CO+PS (1deg apodization)

- **Miscalibration angles** make only small contributions thanks to the cancellation.

- **β = 0.34 ± 0.09 deg**

- $\chi^2 = 65.3$

Cosmic Birefringence fits well (WMAP+Planck)

Robust against the Galactic mask (62% of the sky)
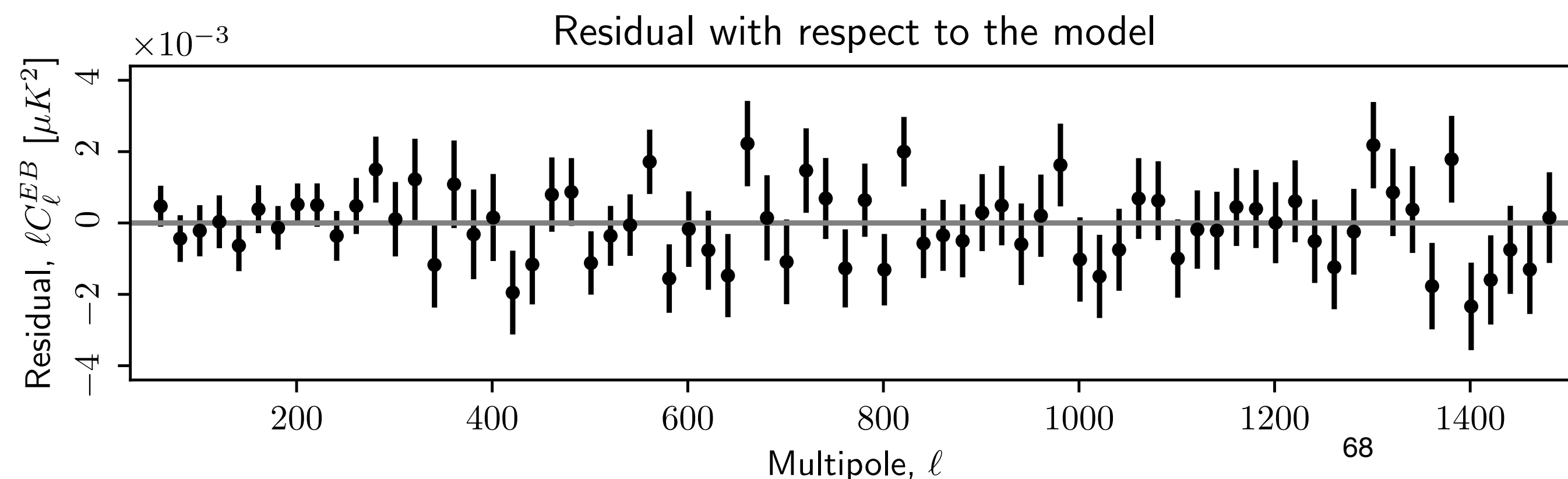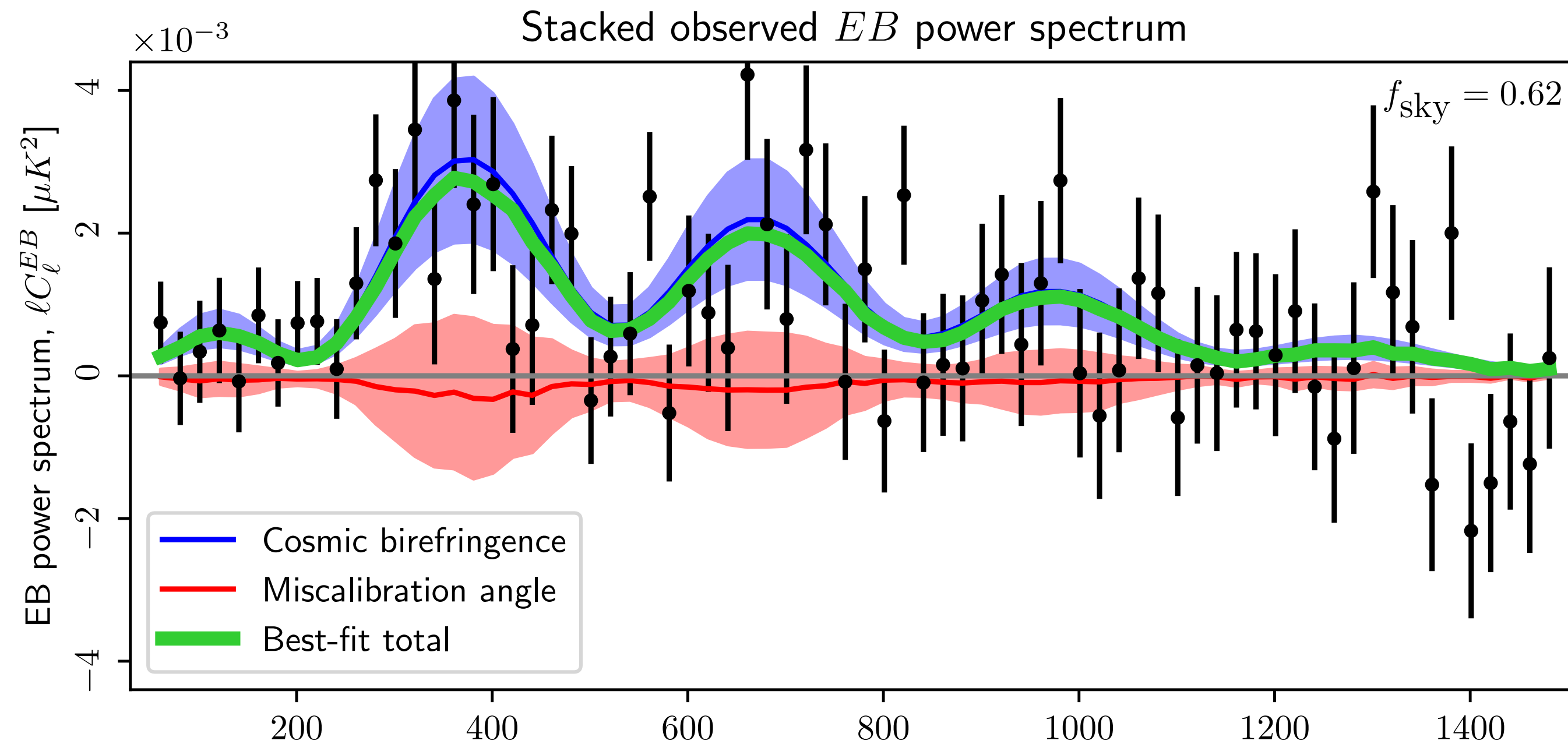
Stacked observed EB power spectrum

$f_{\rm sky} = 0.62$

EB power spectrum, ℓC_ℓ^{EB} [μK^2]

— Cosmic birefringence
— Miscalibration angle
— Best-fit total

Residual with respect to the model

Residual, ℓC_ℓ^{EB} [μK^2]

Multipole, ℓ

CO+PS+30% (1deg apodization)

- **Miscalibration angles** make only small contributions thanks to the cancellation.

- **β = 0.37 ± 0.14 deg**

- $\chi^2 = 65.8$

No frequency dependence is found
Consistent with the expectation from cosmic birefringence

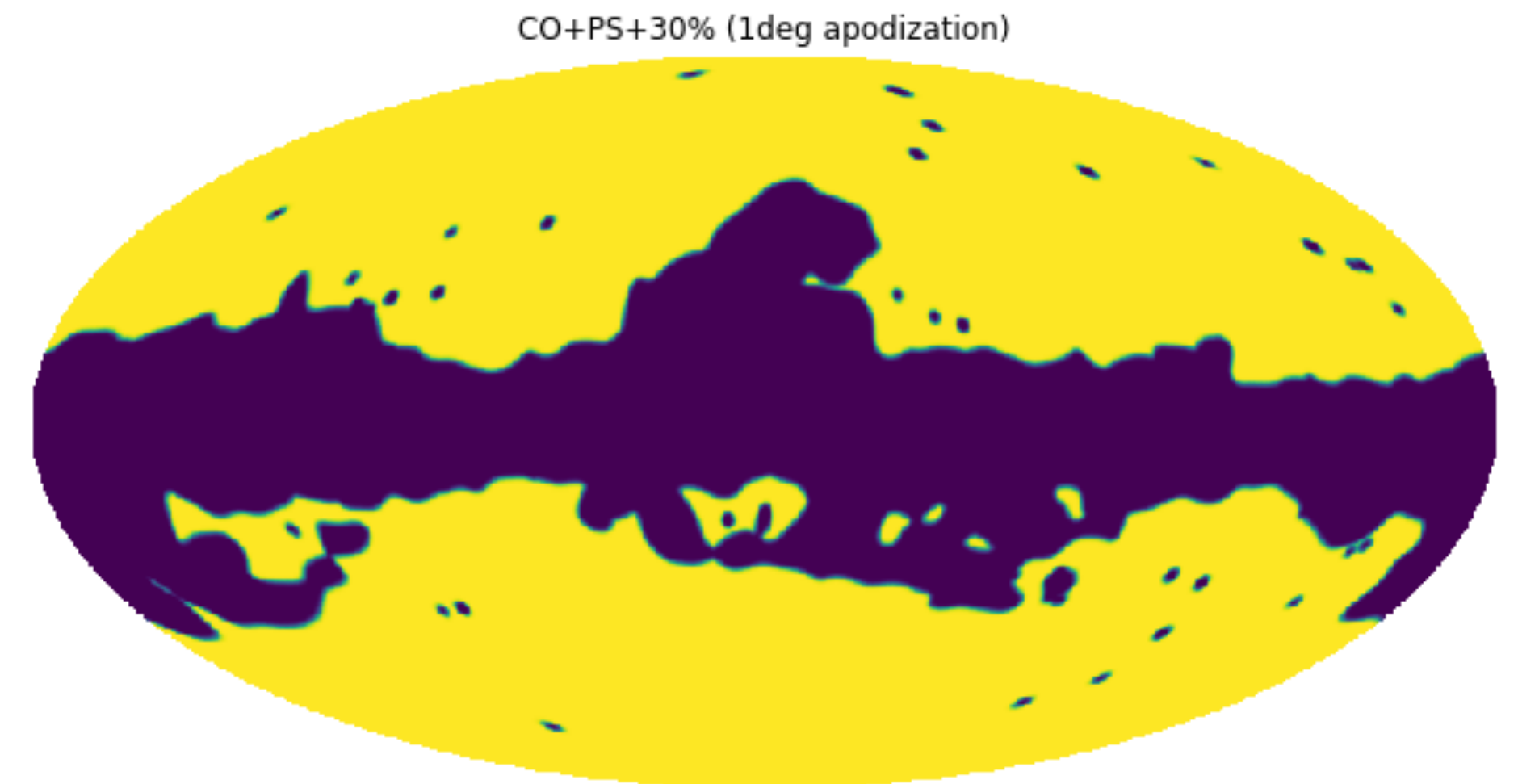Plot: Cosmic birefringence angle, β [deg] vs Frequency, ν [GHz]. Dashed green line at $0.33° \pm 0.10°$. Frequency axis: 30 44 70 100 143 217 353.
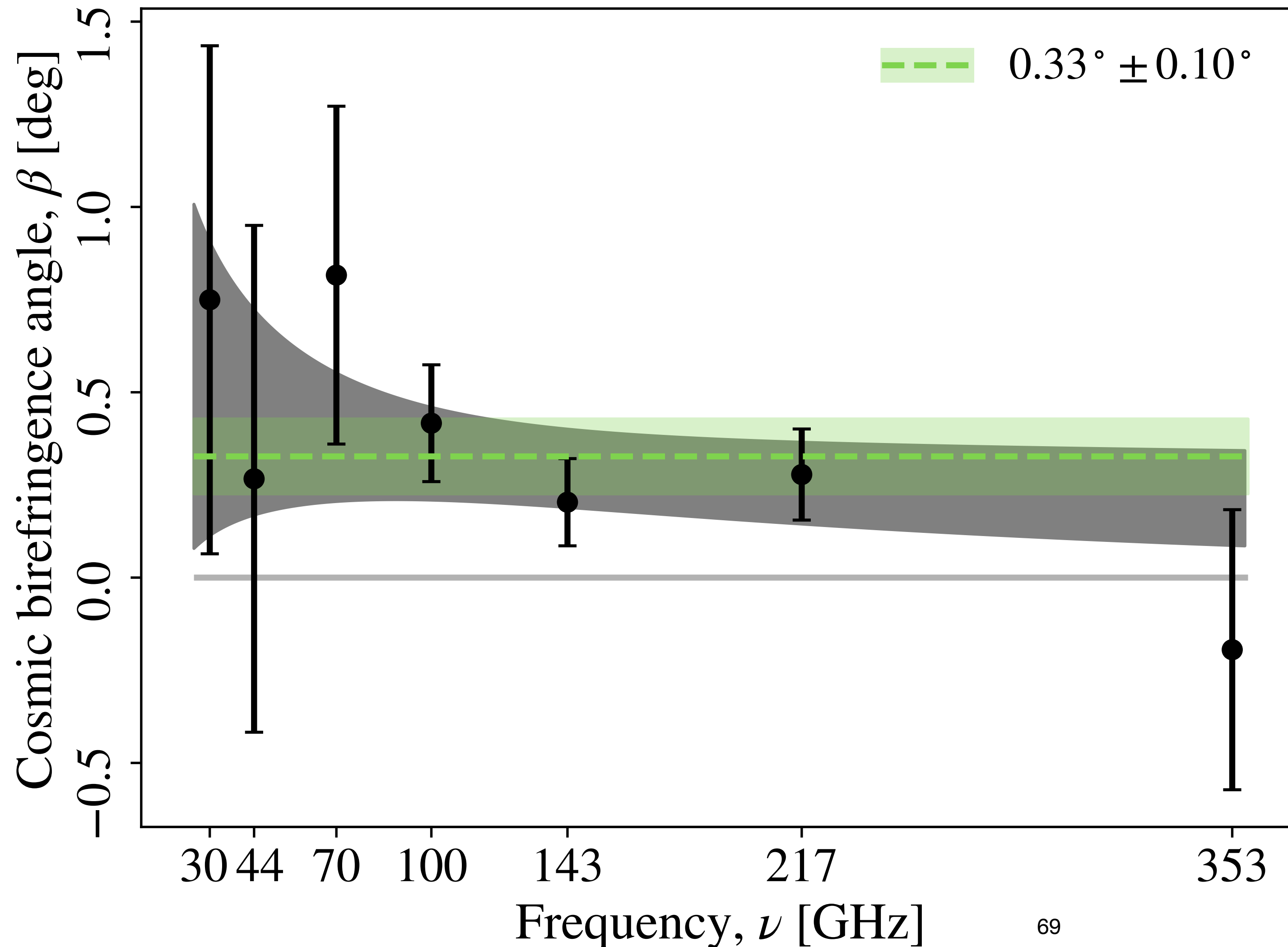
- Light traveling in a uniform magnetic field also experiences a rotation of the plane of linear polarization, called "**Faraday rotation**". However, the rotation angle depends on the frequency, as $\beta(\nu) \propto \nu^{-2}$.

- No evidence for frequency dependence is found!

  - For $\beta \propto \nu^n$, $n = -0.20^{+0.41}_{-0.39}$ (68% CL)

- **Faraday rotation ($n = -2$) is disfavoured.**

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Is β caused by non-cosmological effects?

We need to measure it in independent experiments.

- The **known** instrumental effects of the WMAP and Planck missions are shown to have negligible effects on β.

  - However, we can never rule out **unknown** instrumental effects… We need to measure β in independent experiments.

- The polarized Galactic foreground emission was used to calibrate the instrumental polarization angles, α. The intrinsic EB correlations of the Galactic foreground emission (**polarized dust and synchrotron emission**) could affect the results.

  - We need to measure β without relying on the foreground by calibrating α well, e.g., Cornelison et al. (BICEP3 Collab.), arXiv:2207.14796; Murphy et al. (ACT Collab.), arXiv:2403.00763.

Implications

This term exists for a pion.
What if DM/DE is "pion-like particle"

DM = Dark Matter; DE = Dark Energy

$$I = \int d^4x \sqrt{-g} \left[-\frac{1}{2}(\partial\chi)^2 - V(\chi) - \frac{1}{4}F^2 - \frac{\alpha}{4f}\chi F\tilde{F} \right]$$

- The measured angle, β, implies that the field has evolved by

$$\Delta\chi = \chi(\tau_{\mathrm{obs}}) - \chi(\tau_{\mathrm{em}}) \simeq \frac{10^{-2}}{\alpha}f$$

- If it is due to DE: this measurement rules out DE being a cosmological constant.

- If it is due to DM: at least a fraction of DM violates parity symmetry.

Parity Violation during Cosmic Inflation

$$I_{\text{CS}} = \int \mathrm{d}^4 x \sqrt{-g} \left(-\frac{\alpha}{4f} \chi F\tilde{F} \right) \blacktriangleright$$

Scalar fluctuations

$$\Box\chi - \frac{\partial V}{\partial \chi} = -\frac{\alpha}{f} \mathbf{E} \cdot \mathbf{B}$$

Gravitational waves

$$\Box h_{ij} = 16\pi G (E_i E_j + B_i B_j)^{\text{TT}}$$

Afterglow Light Pattern 375,000 yrs.

Dark Ages

Development of Galaxies, Planets, etc.

Dark Energy Accelerated Expansion

Inflation

Quantum Fluctuations

WMAP

1st Stars about 400 million yrs.

Big Bang Expansion

13.77 billion years

NASA/WMAP Science Team
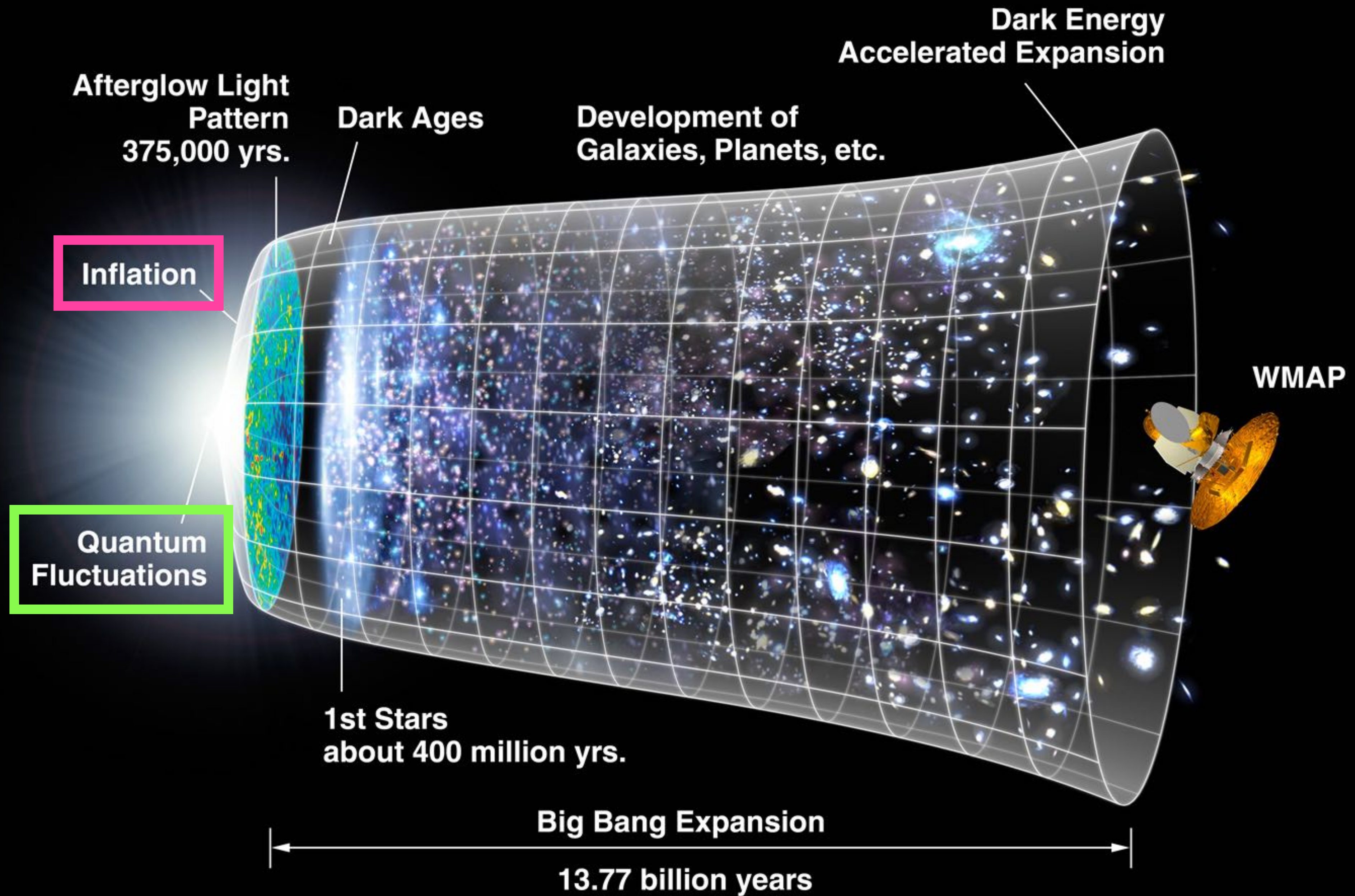
Cosmic Inflation: Key Features
More than 40 years of research in a single slide

- Inflation is the period of **accelerated** expansion in the very early Universe.

  - If the distance between two points increases as $a(t)$, **$d^2a/dt^2 > 0$**.

    This is the definition of inflation.

- *Primordial fluctuations* are generated **quantum mechanically**.

  - <u>Scalar modes</u>: Density fluctuations –> The origin of all cosmic structure.

  - <u>Tensor modes</u>: Gravitational waves –> Yet to be discovered.

  - <u>Vector modes</u>: ?

- **A New Paradigm**: Sourced contributions (this talk)

Anber, Sorbo (2010); Barnaby, Peloso (2011); Sorbo (2011); Barnaby, Namba, Peloso (2011)

The full action
Observational consequences

Similar phenomenology for non-Abelian gauge fields (Maleknejad et al.)

$$F\tilde{F} = F^a_{\mu\nu}F^{\mu\nu a}$$

$$I = I_{\text{inflation}}$$ [no one understands this]

$$+ \int d\tau d^3\mathbf{x}\sqrt{-g}\left[\frac{R}{16\pi G}\right.$$

Gravitational waves

$$\Box h_{ij} = 16\pi G(E_i E_j + B_i B_j)^{\text{TT}}$$

$$-\frac{1}{2}(\partial\chi)^2 - V(\chi)$$

Scalar fluctuations

$$\Box\chi - \frac{\partial V}{\partial\chi} = -\frac{\alpha}{f}\mathbf{E}\cdot\mathbf{B}$$

$$\left.-\frac{1}{4}F^2 - \frac{\alpha}{4f}\chi F\tilde{F}\right]$$

Parity violation in A_μ

$$A''_\pm + \omega^2_\pm A_\pm = 0, \quad \omega^2_\pm = k^2 \mp \frac{k\alpha\chi'}{f}$$

A note on terminology
"Photons" = Massless spin-1 particles

- Since inflation occurred long before the electroweak symmetry breaking, "photons" as we know them did not exist during inflation.

- We should think of them more generally as "**massless spin-1 particles**".

Gravitational waves

$$\Box h_{ij} = 16\pi G (E_i E_j + B_i B_j)^{\mathrm{TT}}$$

Scalar fluctuations

$$\Box \chi - \frac{\partial V}{\partial \chi} = -\frac{\alpha}{f} \mathbf{E} \cdot \mathbf{B}$$

Spin-1 sources, which violate parity symmetry due to the Chern-Simons term.
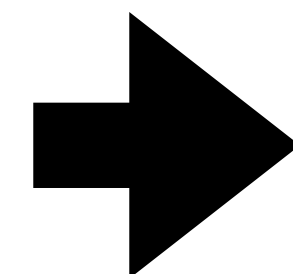
➤ Non-Gaussian and parity-violating gravitational waves and scalar fluctuations!

Particle production due to χ$F\tilde{F}$ during inflation

Kinetic energy of χ is used to produce massless spin-1 particles

$$A''_\pm + \omega^2_\pm A_\pm = 0 \quad \text{where} \quad \begin{cases} \omega^2_\pm = k^2 \mp \dfrac{2k\xi}{-\tau} \\ \xi = \dfrac{\alpha\dot{\chi}}{2fH} \end{cases} \quad (-\infty < \tau < 0)$$

- Instability occurs when $\omega^2_+ < 0$ or $\omega^2_- < 0$. In other words, $-k\tau < 2|\xi|$.

  - The mode function for *one of the helicity states* is **amplified** on large scales (small -kτ) **relative to the vacuum solution, $e^{-ik\tau}/\sqrt{2k}$.**

  - The right-handed (+ helicity) state is amplified for ξ>0, whereas the left-handed (- helicity) state remains close to the vacuum solution.

  - **Parity violation!**

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Truly *ab initio* simulation!
World's first lattice simulation of inflation

Drew Jamieson

$$\Box \chi - \frac{\partial V}{\partial \chi} = -\frac{\alpha}{f} \mathbf{E} \cdot \mathbf{B}$$

Angelo Caravano

$\frac{\Delta}{\sigma}$
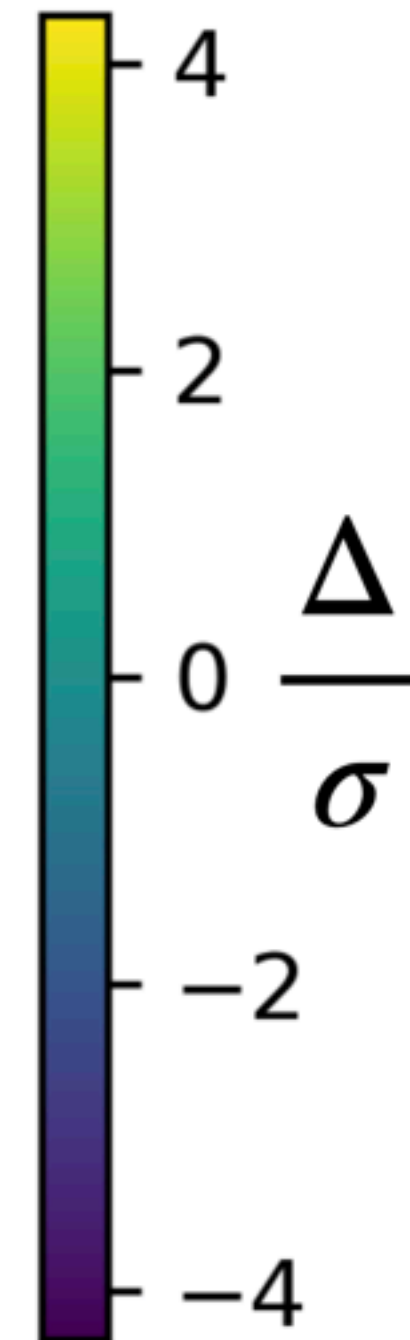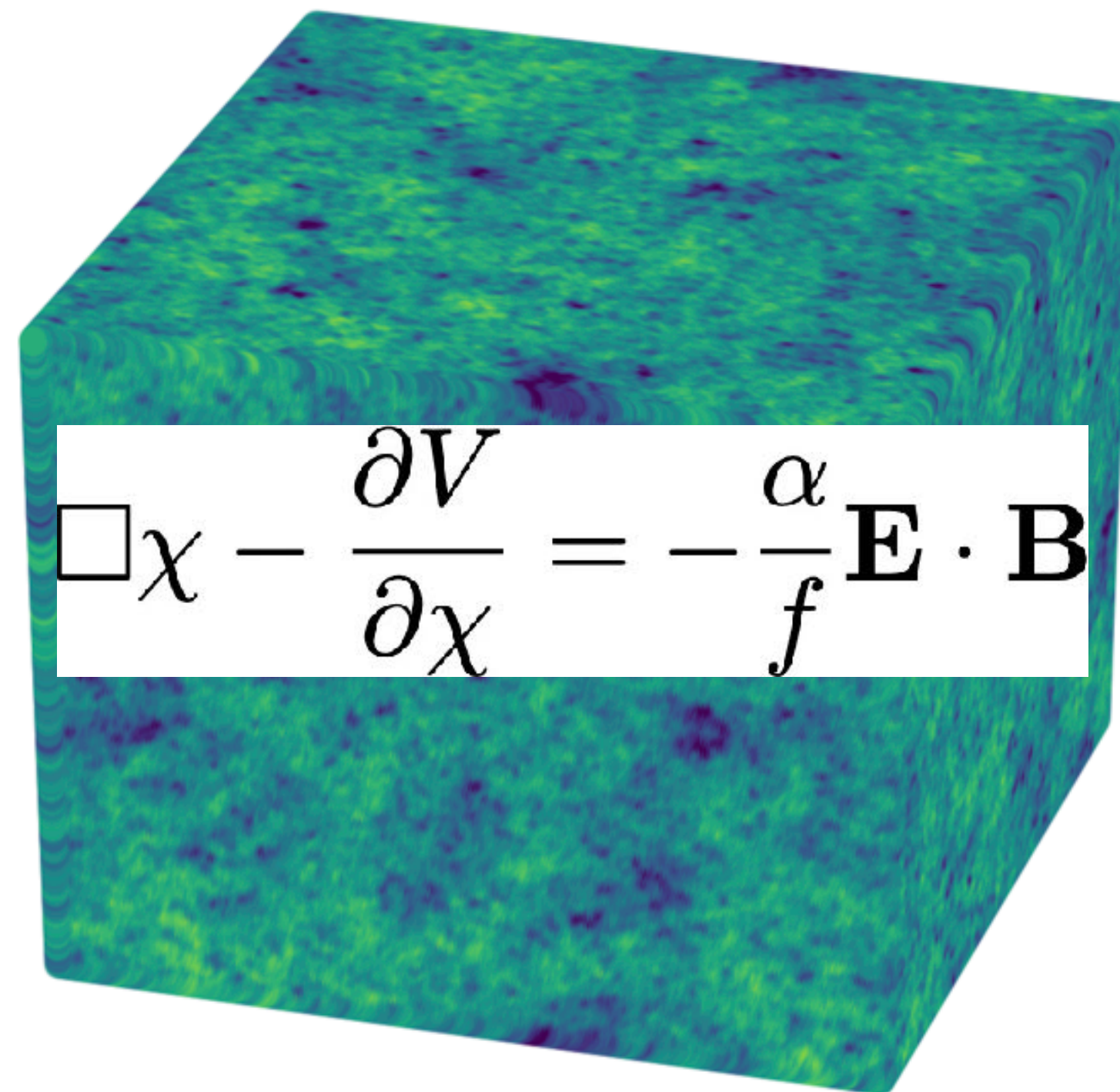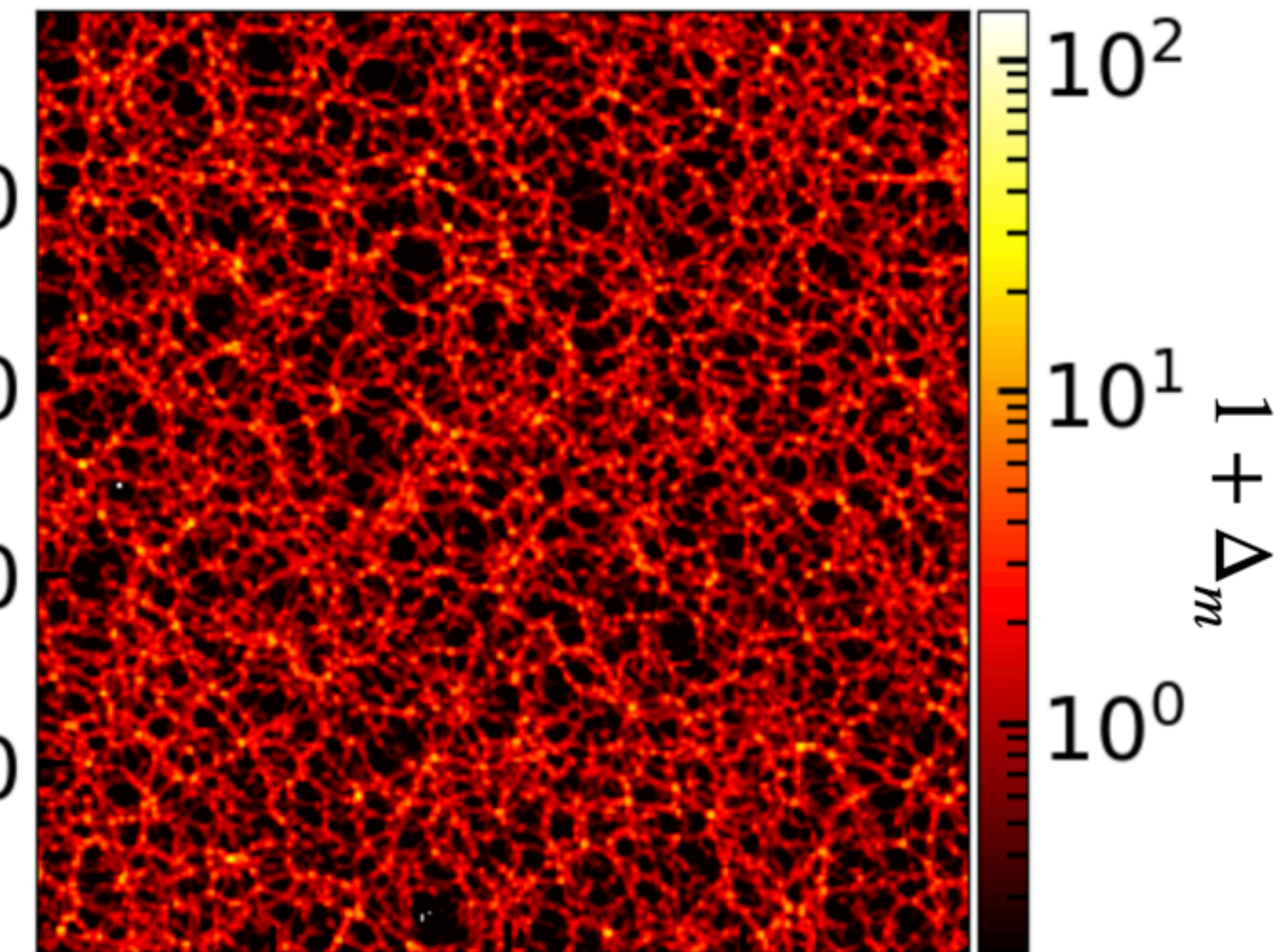
- (Left) Parity-violating and non-Gaussian density fluctuation during inflation.

- (Right) Outcome of N-body simulation at $z=0$, using the left panel as the initial condition.

$1 + \Delta_m$

y [Mpc h^{-1}]

x [Mpc h^{-1}]

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GR + Maxwell (+ Chern-Simons)

$$\Box = \frac{1}{\sqrt{-g}}\partial_\mu(\sqrt{-g}g^{\mu\nu}\partial_\nu)$$

$$= \frac{1}{a^2}\left(-\frac{\partial^2}{\partial\tau^2} - 2\frac{a'}{a}\frac{\partial}{\partial\tau} + \nabla^2\right)$$

where $g^{\mu\nu} = a^{-2}\text{diag}(-1, \mathbf{1})$

$$I = \int d\tau d^3\mathbf{x}\sqrt{-g}\left(\frac{R}{16\pi G} - \frac{1}{4}F^2 - \frac{\alpha}{4f}\chi F\tilde{F}\right)^{\sqrt{-g} = a^4}$$

- The F^2 term contributes to the equation of motion for the GW via the stress-energy tensor (this is the second-order fluctuation).

$$\Box h_{ij} = 16\pi G(E_i E_j + B_i B_j)^{\text{TT}}$$ "Transverse and Traceless"

- The $F\tilde{F}$ term does **not** contribute directly to the equation of motion for the GW.

  - But, it creates a parity violation in **E** and **B**, which also creates a parity violation in the GW.

Helicity basis to probe parity symmetry

Circular polarization states of GW. GW's helicity is λ = ±2.

- Just like for EM waves,

$$A_\pm = \frac{A_\mathbf{k}^1 \mp iA_\mathbf{k}^2}{\sqrt{2}}$$
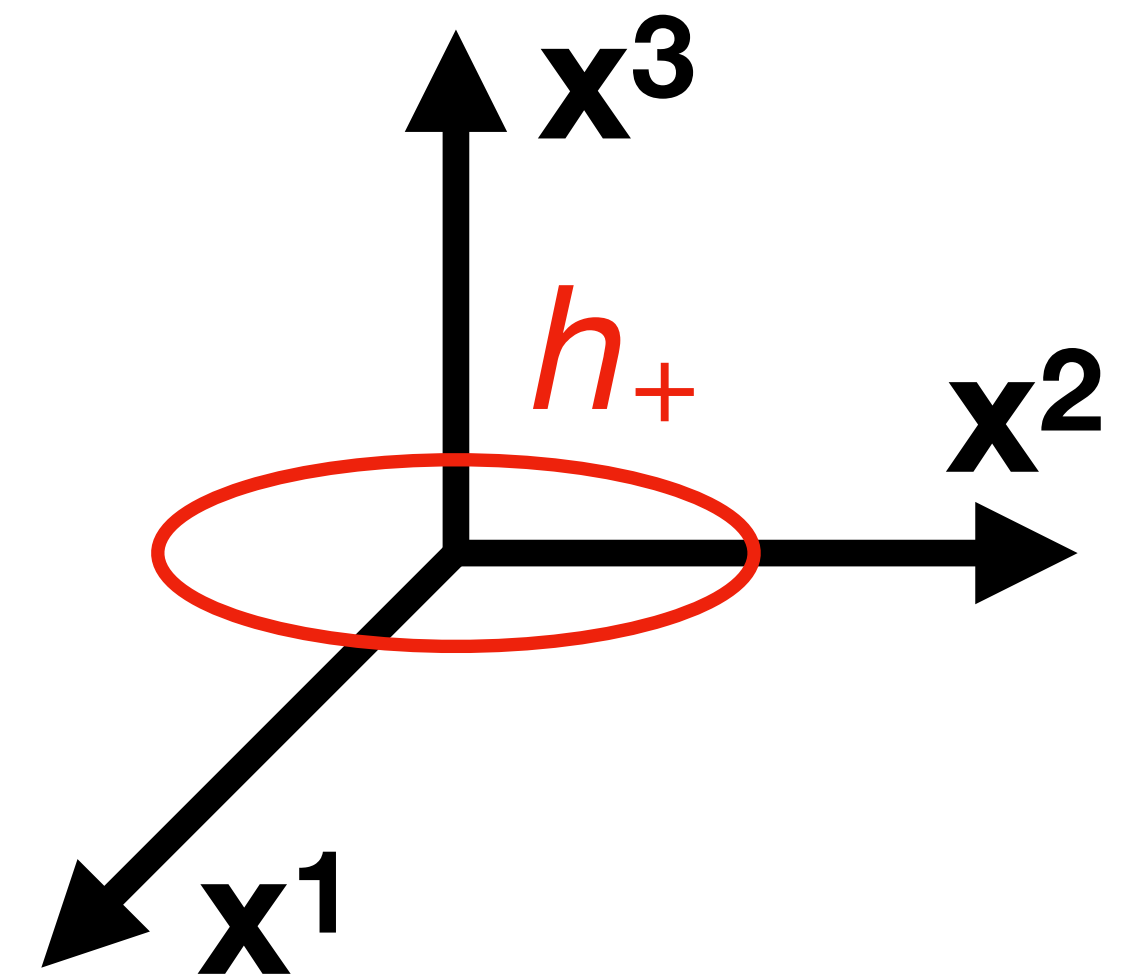
A_+: Right-handed state

A_-: Left-handed state

$$h_{ij} = \begin{pmatrix} h_+ & h_\times & 0 \\ h_\times & -h_+ & 0 \\ 0 & 0 & 0 \end{pmatrix}$$

we write the helicity states of GW in Fourier space as

$$h_{\pm 2} = \frac{h_{+,\mathbf{k}} \mp ih_{\times,\mathbf{k}}}{\sqrt{2}}$$

h_{+2}: Right-handed state

h_{-2}: Left-handed state

Parity Violation in GW
For a slowly varying ξ>0

$$\xi = \frac{\alpha \dot{\bar{\theta}}}{2H} = \frac{\alpha \dot{\chi}}{2Hf}$$

$$\frac{k^3 P_{+2}(k)}{2\pi^2} \simeq \frac{2}{M_{\rm Pl}^2}\left(\frac{H}{2\pi}\right)^2\left[1 + 8.6\times 10^{-7}\frac{H^2}{M_{\rm Pl}^2}\frac{e^{4\pi\xi}}{\xi^6}\right]$$

$$\frac{k^3 P_{-2}(k)}{2\pi^2} \simeq \frac{2}{M_{\rm Pl}^2}\left(\frac{H}{2\pi}\right)^2\left[1 + 1.8\times 10^{-9}\frac{H^2}{M_{\rm Pl}^2}\frac{e^{4\pi\xi}}{\xi^6}\right]$$
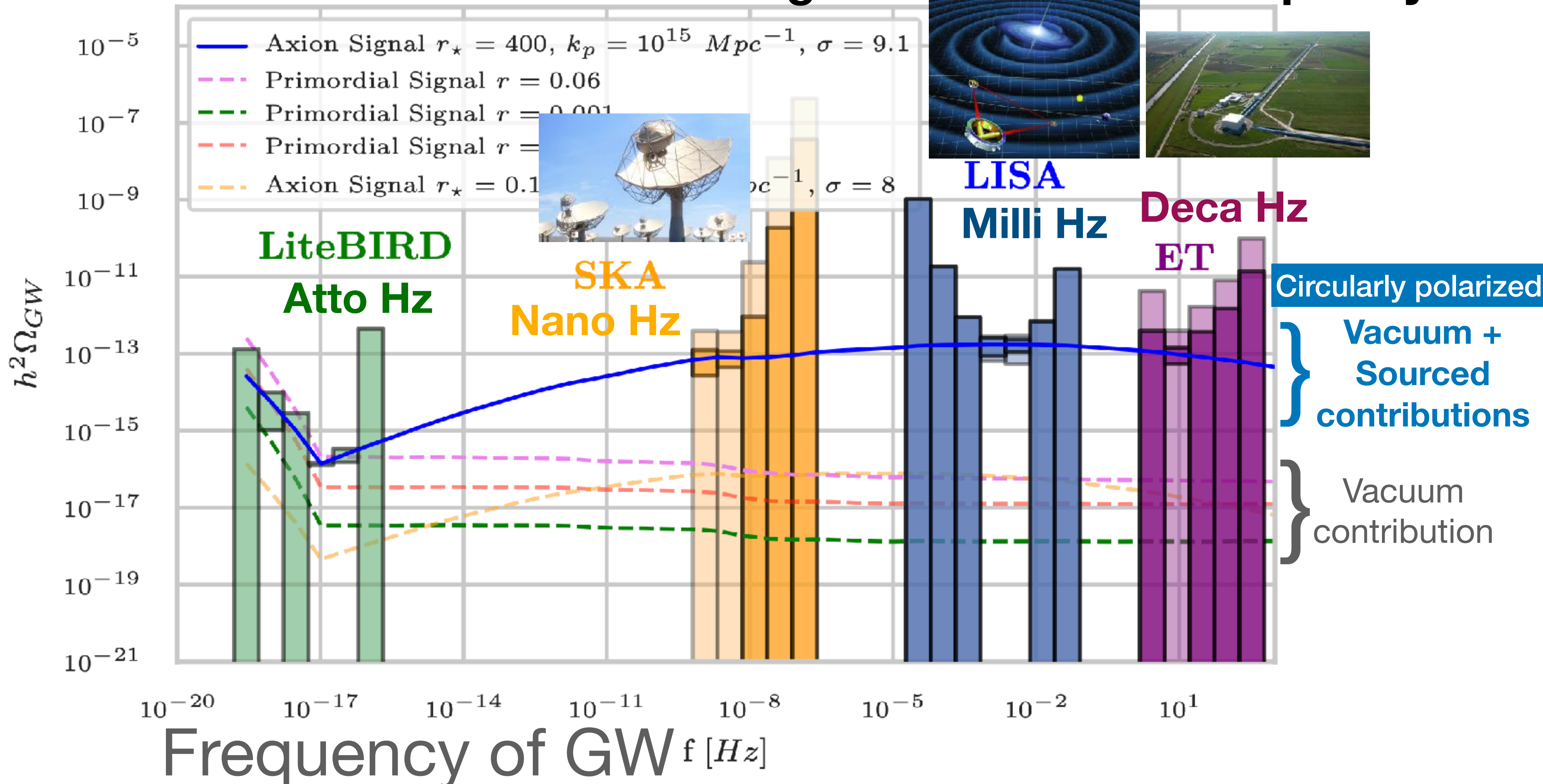
Vacuum contribution

Parity Violation!

- The sourced contributions are almost perfectly circularly polarized.

- The sum of the vacuum and sourced contributions is partially circularly polarized. **This can be observationally tested!** (Seto 2006; Seto, Taruya 2007)

Campeti, EK, Poletti, Baccigalupi (2021)

GWs from the early Universe are everywhere!
We can measure it across 21 orders of magnitude in the GW frequency

Energy Density of GW today

$h^2\Omega_{GW}$

Axion Signal $r_\star = 400$, $k_p = 10^{15}\ Mpc^{-1}$, $\sigma = 9.1$
Primordial Signal $r = 0.06$
Primordial Signal $r = 0.001$
Primordial Signal $r = $
Axion Signal $r_\star = 0.1$

LiteBIRD
Atto Hz

SKA
Nano Hz

LISA
Milli Hz

Deca Hz
ET

Circularly polarized

Vacuum +
Sourced
contributions

Vacuum
contribution

Frequency of GW $f\ [Hz]$

Experimental Strategy Commonly Assumed So Far

1. Detect CMB polarization in multiple frequencies, to make sure that it is from the CMB (i.e., Planck spectrum)

2. Check for scale invariance: Consistent with a scale invariant spectrum?

   - Yes => Announce discovery of the vacuum fluctuation in spacetime

   - No => WTF?

New Experimental Strategy: New Standard!

1. Detect CMB polarization in multiple frequencies, to make sure that it is from the CMB (i.e., Planck spectrum)

2. Check for scale invariance: Consistent with a scale invariant spectrum?

3. Parity violating correlations consistent with zero?

4. Consistent with Gaussianity?

- If, and **ONLY IF** Yes to **all** => Announce discovery of the vacuum fluctuation in spacetime

If not, you may have just discovered new physics during inflation!

1. De... ma...rum)

2. Check for scale invariance: Consistent with a scale invariant spectrum?

3. Parity violating correlations consistent with zero?

4. Consistent with Gaussianity?

• If, and **ONLY IF** Yes to **all** => Announce discovery of the vacuum fluctuation in spacetime

Summary
Let's find new physics!

- Violation of parity symmetry is a new topic in cosmology.

- It may hold the answers to fundamental questions, such as

  - *What is Dark Matter and Dark Energy?*

  - *What is the fundamental physics behind cosmic inflation?*

- Rich phenomenology of Chern-Simons term: $I_{CS} = \int d^4 x \sqrt{-g} \left(-\frac{\alpha}{4f} \chi F \tilde{F} \right)$

  - Cosmic birefringence <mark>3.6σ hint of the signal</mark>

    Abelian and non-Abelian gauge fields; Gravitational CS; …

  - Parity-violating and non-Gaussian gravitational waves and scalar fluctuations

- **What else should we look at? New and great topics of research.**