



# Cosmic Microwave Background as a Probe of the Very Early Universe

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Colloquium, STScl, October 1, 2008

# WMAP 5-Year Papers

- **Hinshaw et al.**, “*Data Processing, Sky Maps, and Basic Results*” [0803.0732](#)
- **Hill et al.**, “*Beam Maps and Window Functions*” [0803.0570](#)
- **Gold et al.**, “*Galactic Foreground Emission*” [0803.0715](#)
- **Wright et al.**, “*Source Catalogue*” [0803.0577](#)
- **Nolta et al.**, “*Angular Power Spectra*” [0803.0593](#)
- **Dunkley et al.**, “*Likelihoods and Parameters from the WMAP data*” [0803.0586](#)
- **Komatsu et al.**, “*Cosmological Interpretation*” [0803.0547](#)

# WMAP 5-Year Science Team

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Special  
Thanks to  
**WMAP**  
**Graduates!**

- C. Barnes
- R. Bean
- O. Dore
- H.V. Peiris
- L. Verde

# Night Sky in Optical ( $\sim 0.5\text{nm}$ )



# Night Sky in Microwave ( $\sim 1\text{mm}$ )



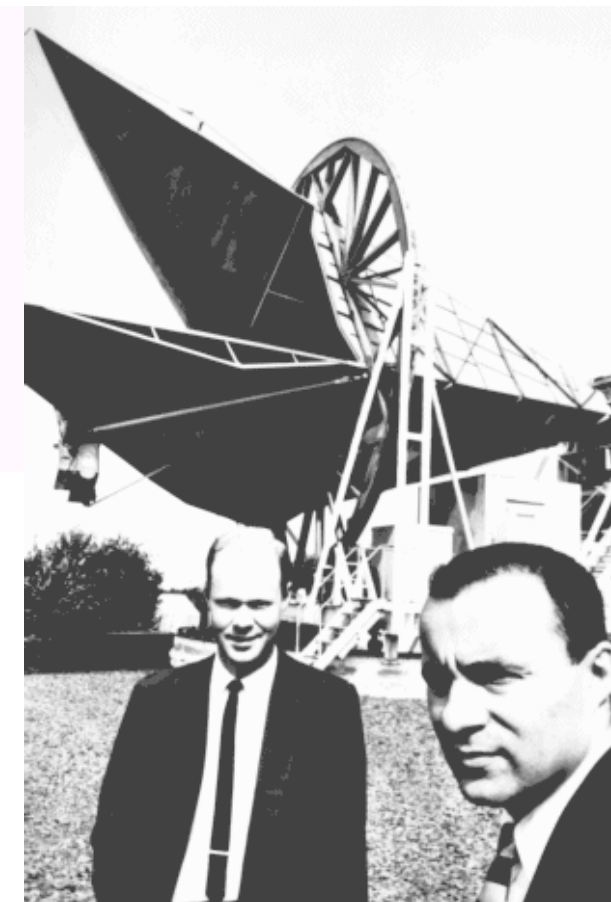
# A. Penzias & R. Wilson, 1965

## A MEASUREMENT OF EXCESS ANTENNA TEMPERATURE AT 4080 Mc/s

Measurements of the effective zenith noise temperature of the 20-foot horn-reflector antenna (Crawford, Hogg, and Hunt 1961) at the Crawford Hill Laboratory, Holmdel, New Jersey, at 4080 Mc/s have yielded a value about 3.5° K higher than expected. This excess temperature is, within the limits of our observations, isotropic, unpolarized, and free from seasonal variations (July, 1964–April, 1965). A possible explanation for the observed excess noise temperature is the one given by Dicke, Peebles, Roll, and Wilkinson (1965) in a companion letter in this issue.

- **Isotropic**
- **Unpolarized**

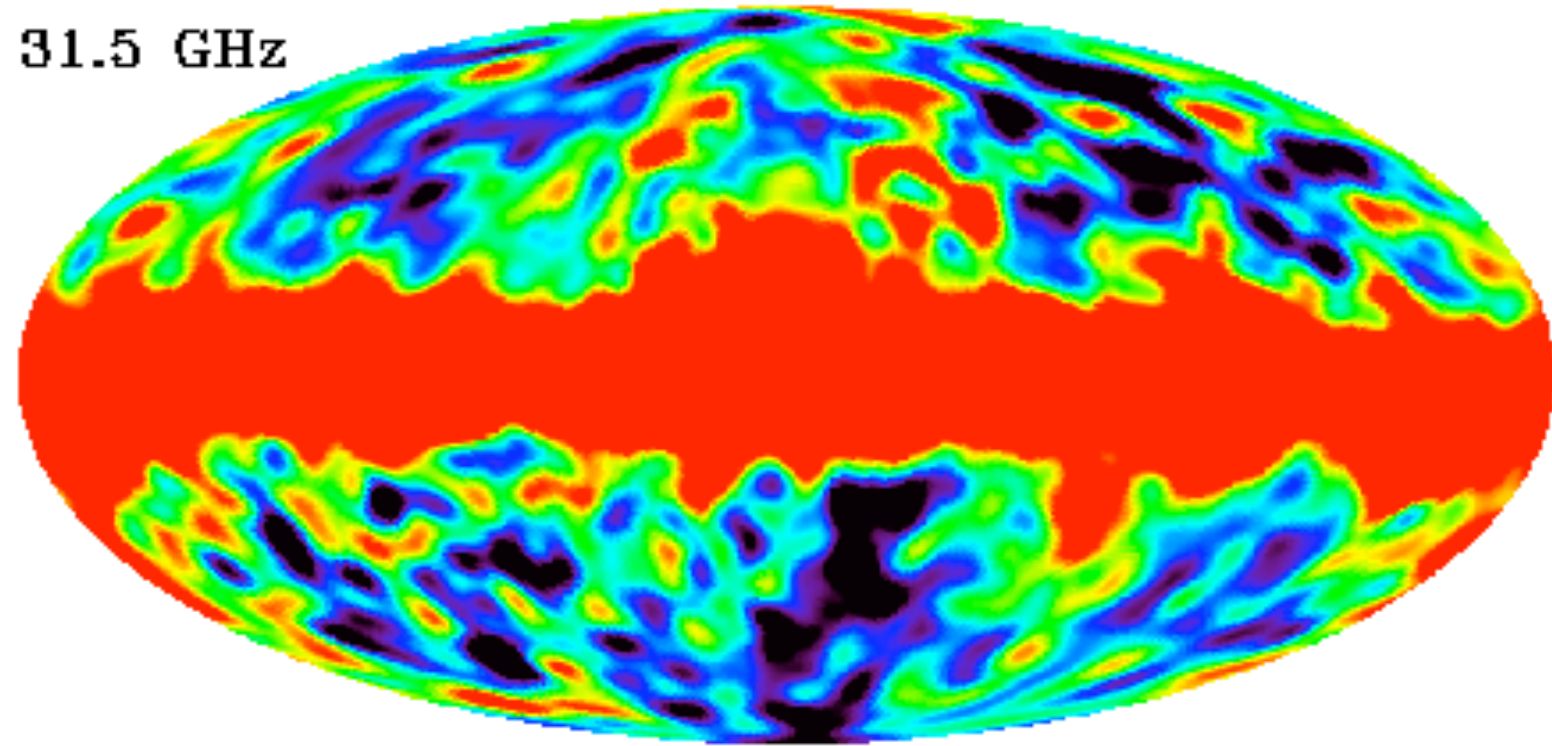
May 13, 1965  
BELL TELEPHONE LABORATORIES, INC  
CRAWFORD HILL, HOLMDEL, NEW JERSEY



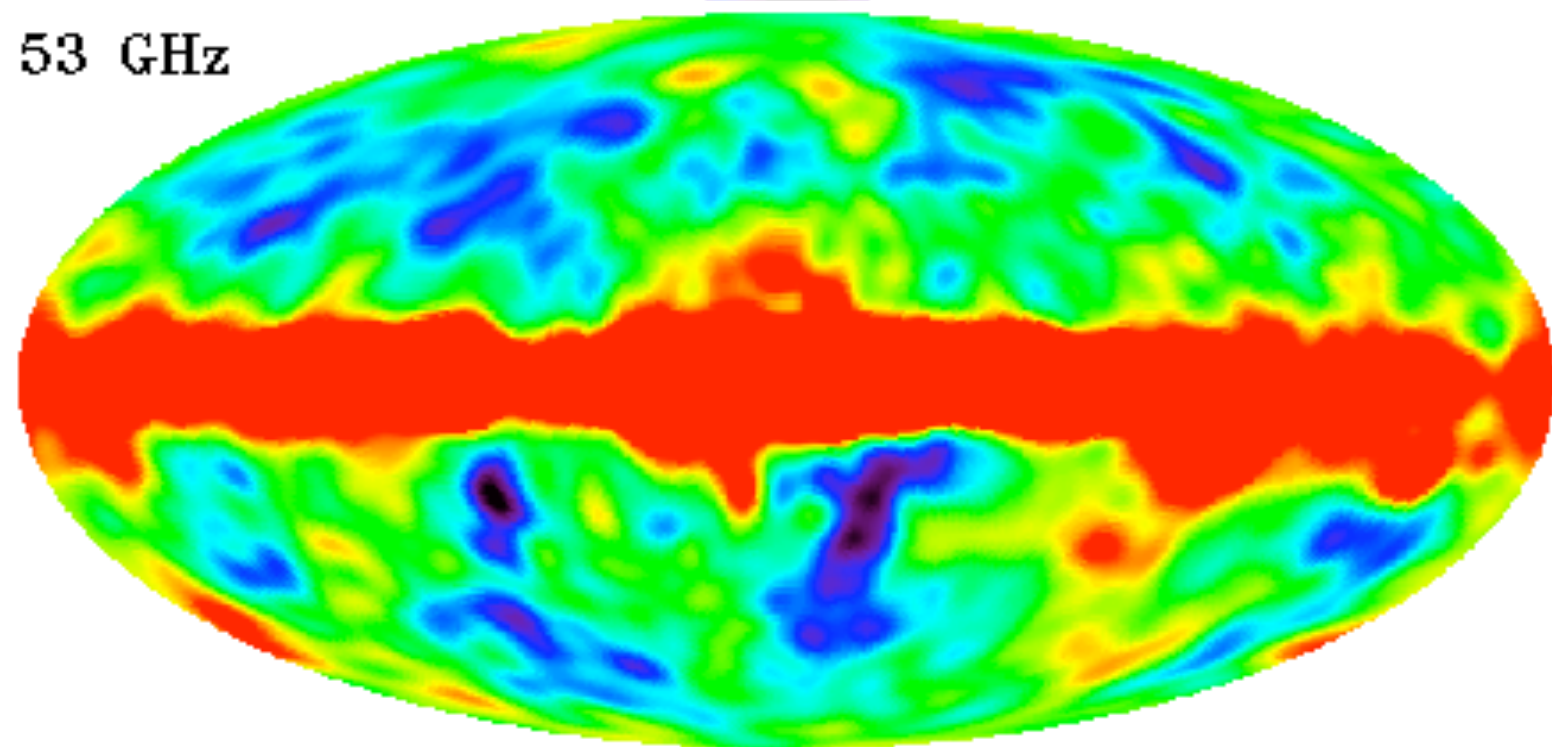
A. A. PENZIAS  
R. W. WILSON

# COBE/DMR, 1992

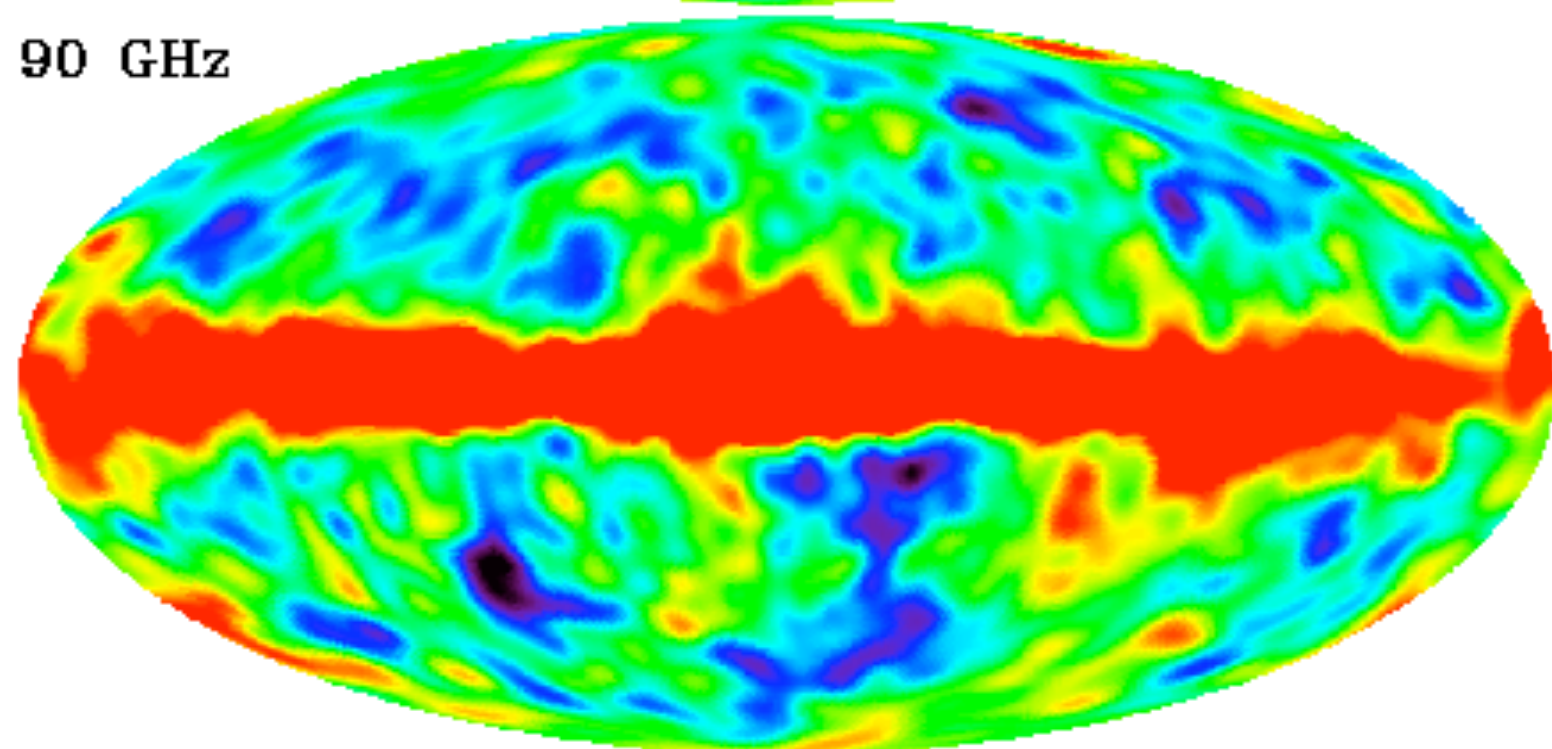
31.5 GHz



53 GHz



90 GHz



-100  $\mu\text{K}$   +100  $\mu\text{K}$



• **Isotropic?**

• **CMB is *anisotropic*! (at the 1/100,000 level)**

# COBE to WMAP (x35 better resolution)

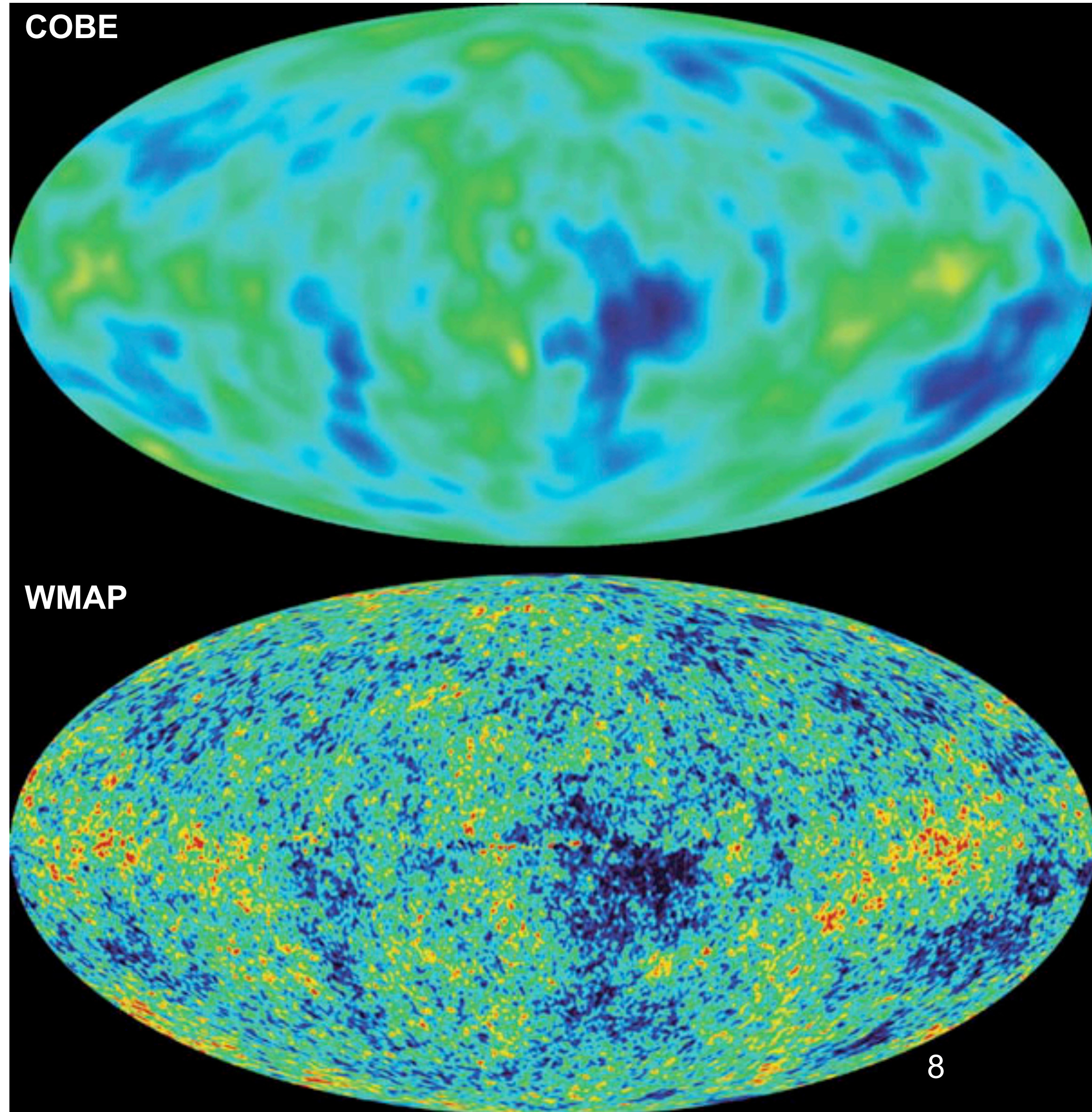
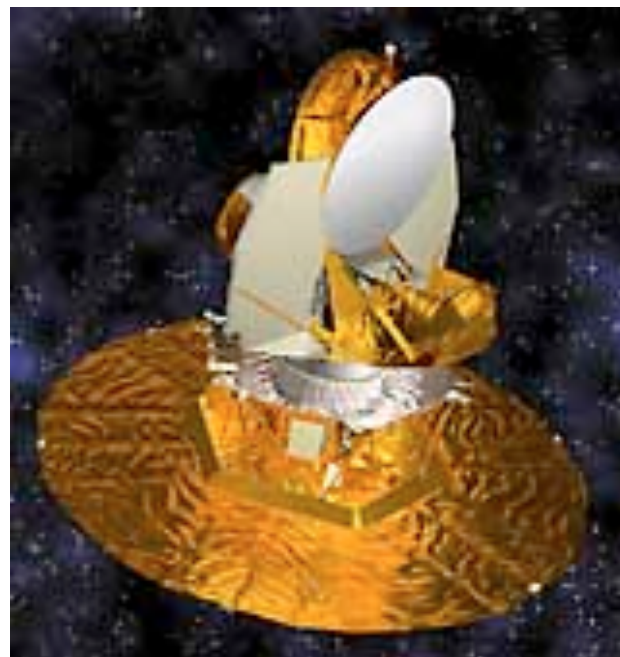


COBE  
1989

## Press Release from the Nobel Foundation

[COBE's] measurements also marked the inception of cosmology as a precise science. It was not long before **it was followed up**, for instance **by the WMAP satellite**, which yielded even clearer images of the background radiation.

WMAP  
2001





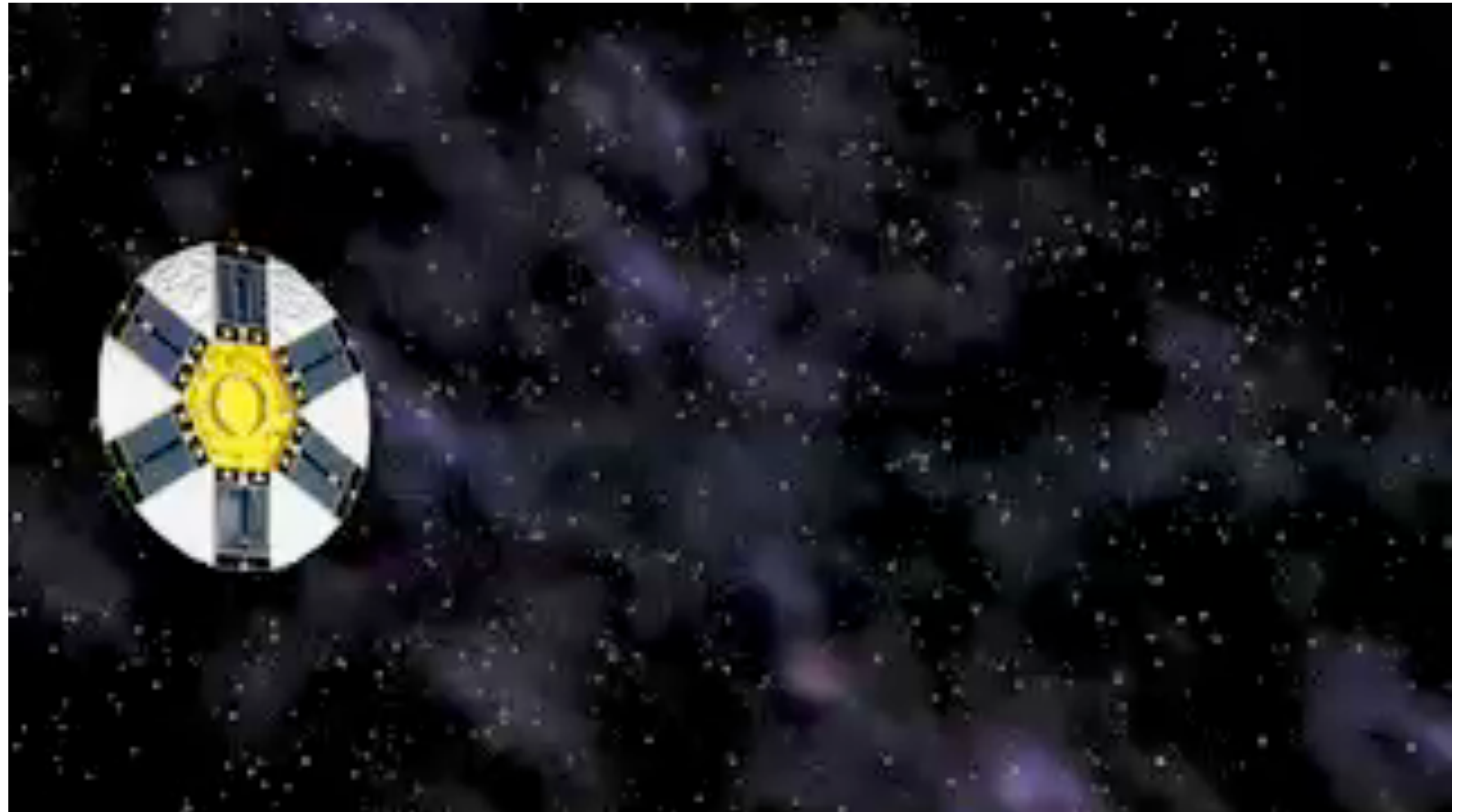
# WMAP at Lagrange 2 (L2) Point

June 2001:  
WMAP launched!

February 2003:  
The first-year data  
release

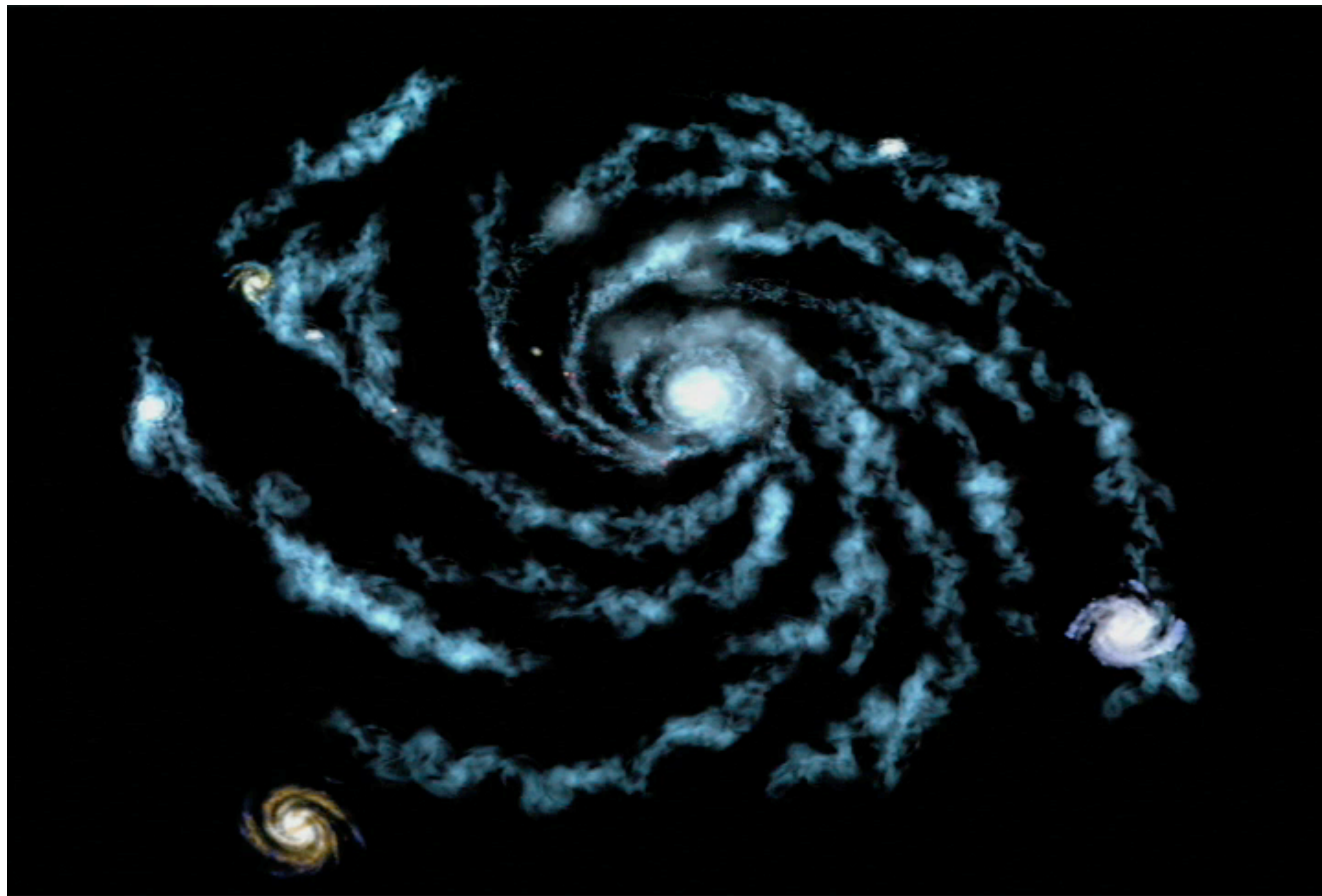
March 2006:  
The three-year data  
release

**March 2008:**  
**The five-year**  
**data release**  
9-year survey funded  
recently



- L2 is a million miles from Earth
- WMAP leaves Earth, Moon, and Sun behind it to avoid radiation from them

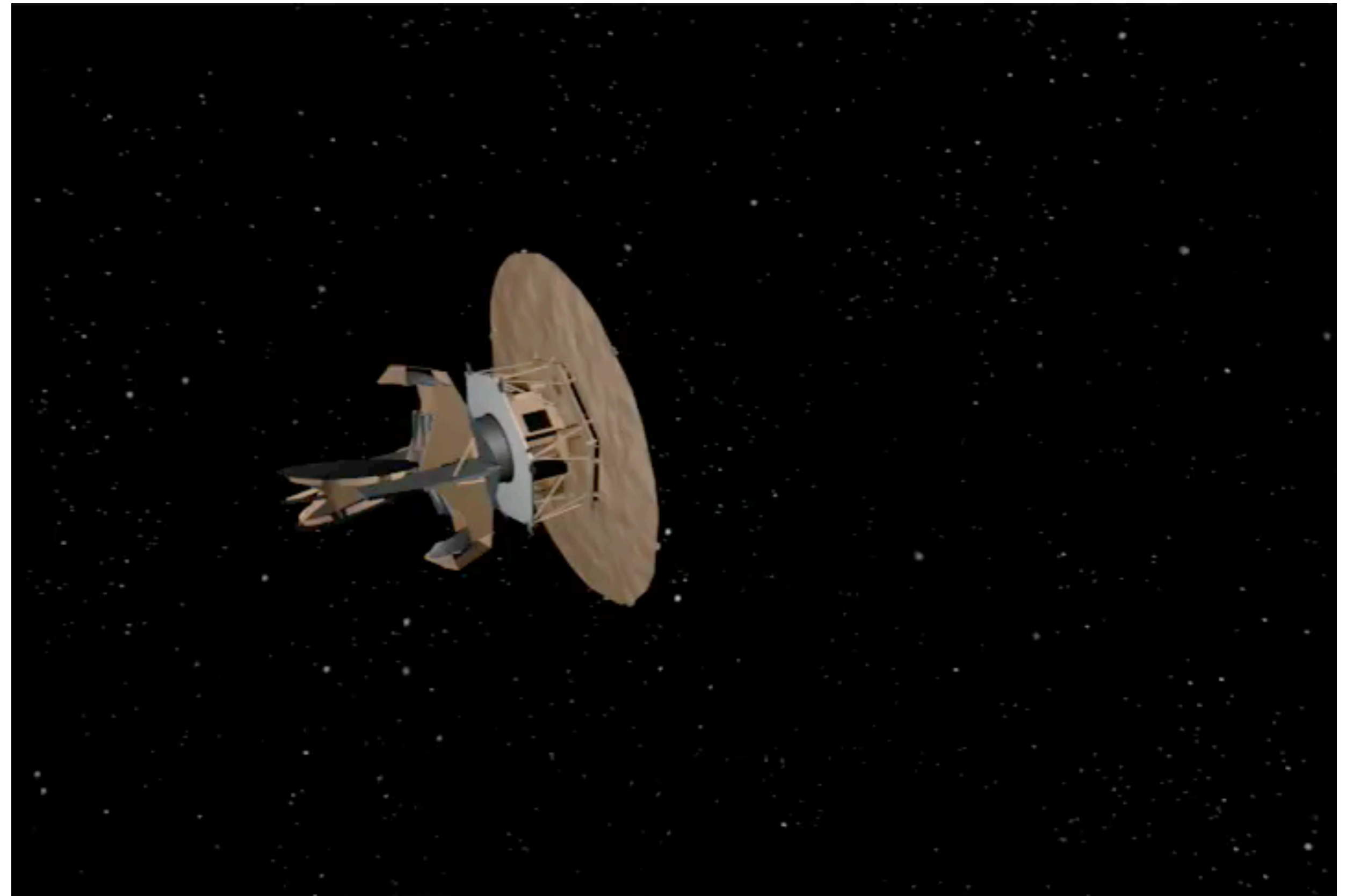
# WMAP Measures Microwaves From the Universe



- The mean temperature of photons in the Universe today is 2.725 K
- WMAP is capable of measuring the temperature *contrast* down to better than **one part in millionth**

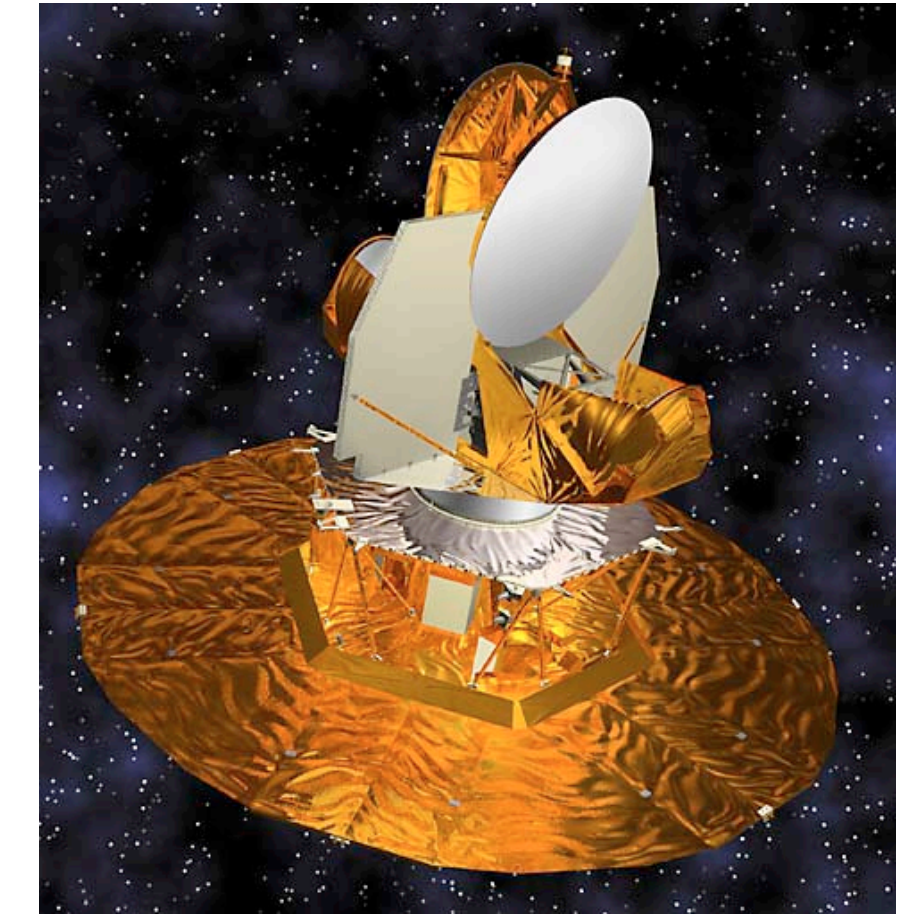
# Journey Backwards in Time

- The Cosmic Microwave Background (**CMB**) is *the fossil light from the Big Bang*
- This is the oldest light that one can ever hope to measure
- CMB is a direct image of the Universe when the Universe was only 380,000 years old



- CMB photons, after released from the cosmic plasma “soup,” traveled for **13.7 billion years** to reach us.
- CMB collects information about the Universe as it travels through it.

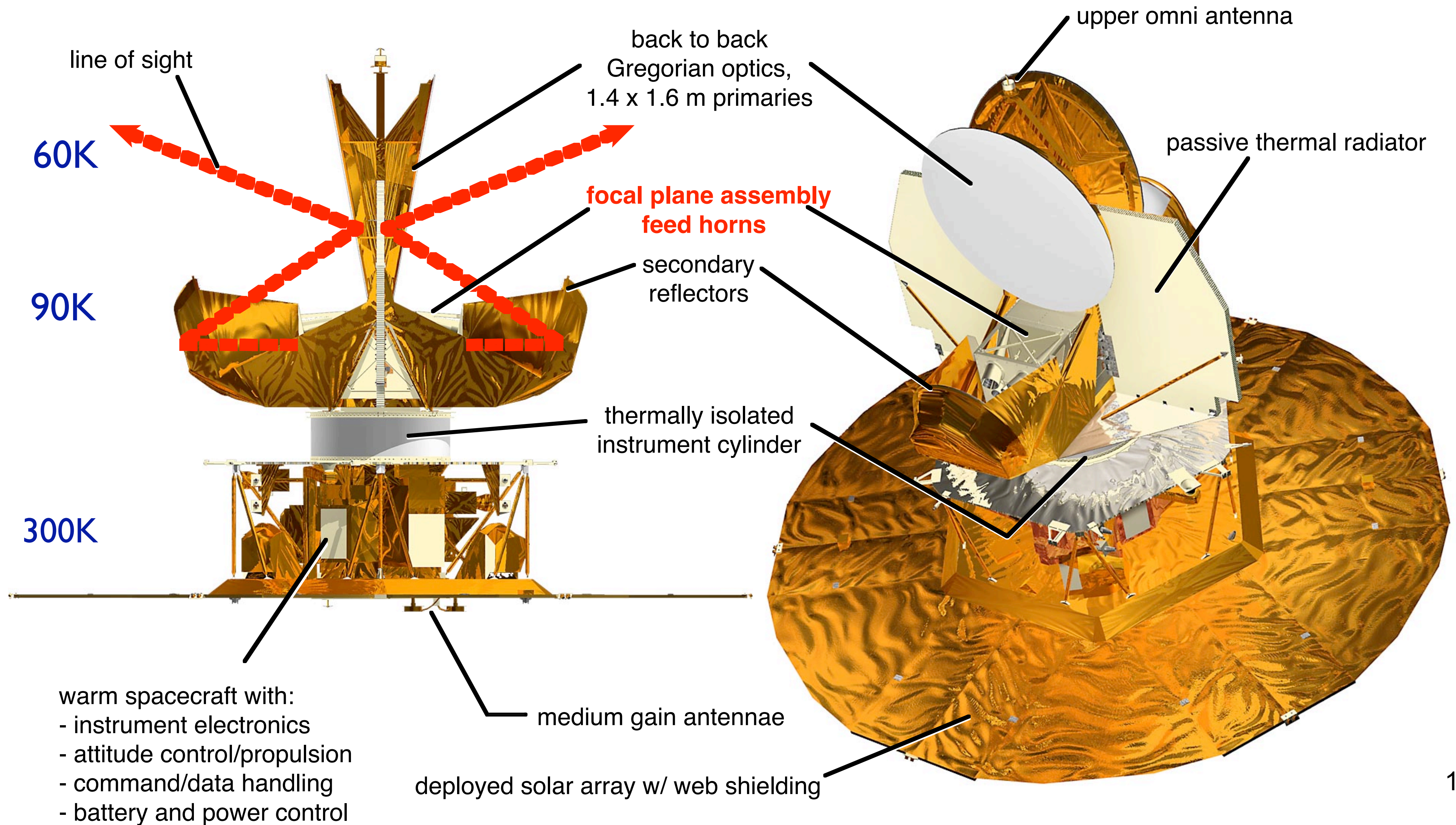
# The Wilkinson Microwave Anisotropy Probe (*WMAP*)

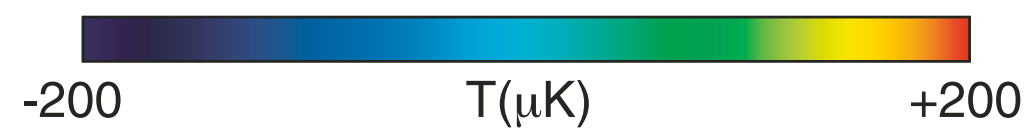
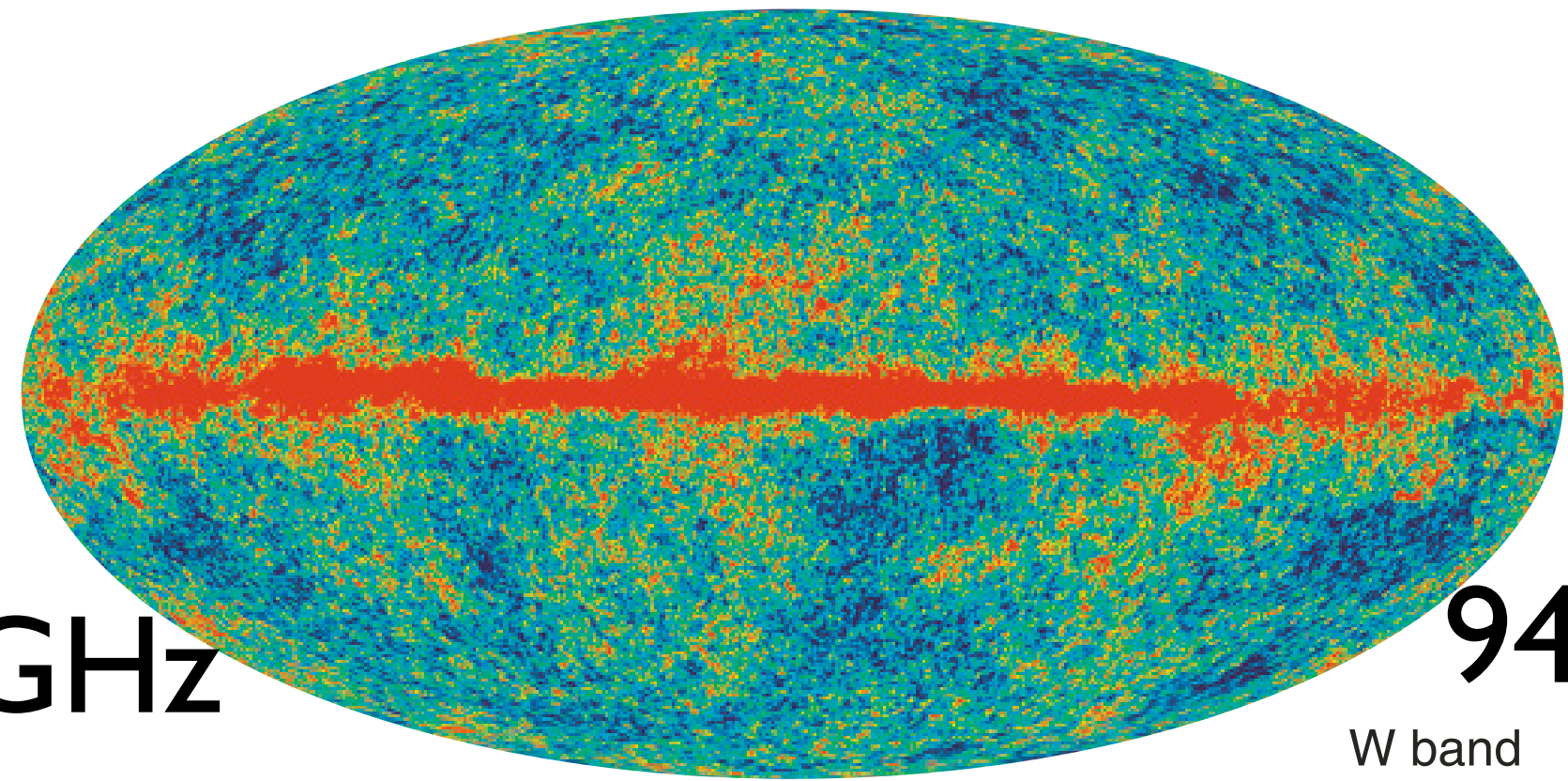
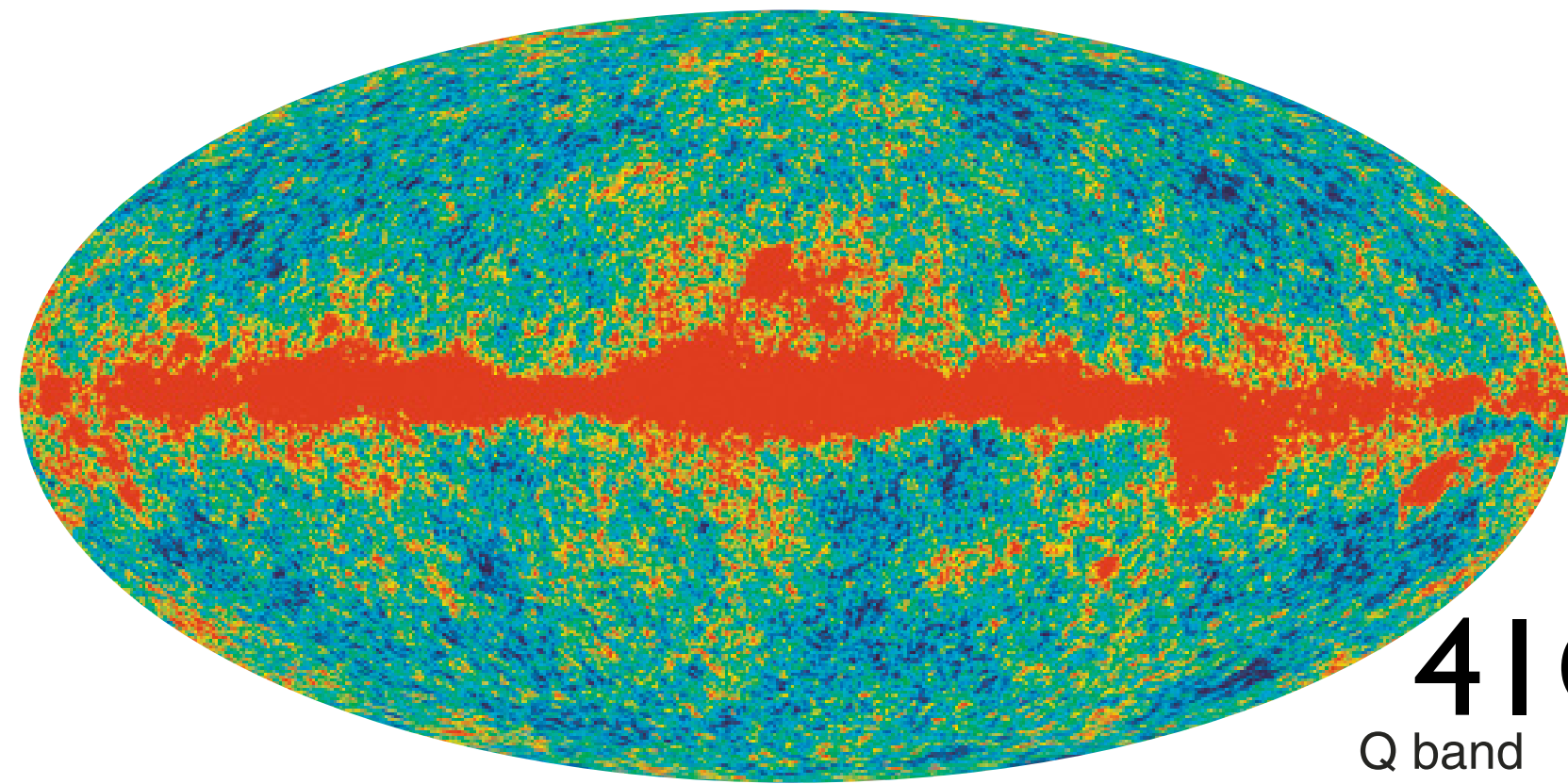
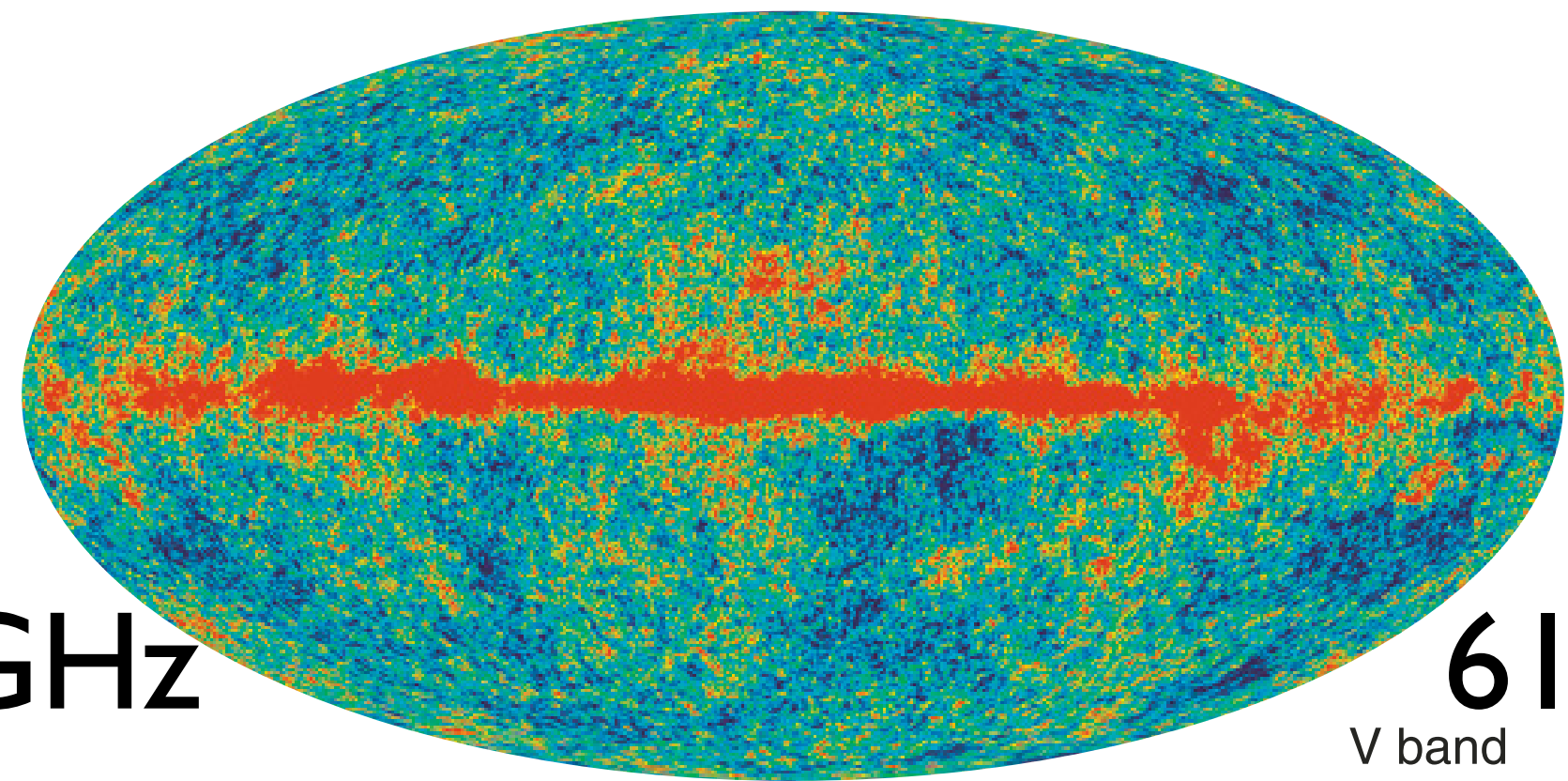
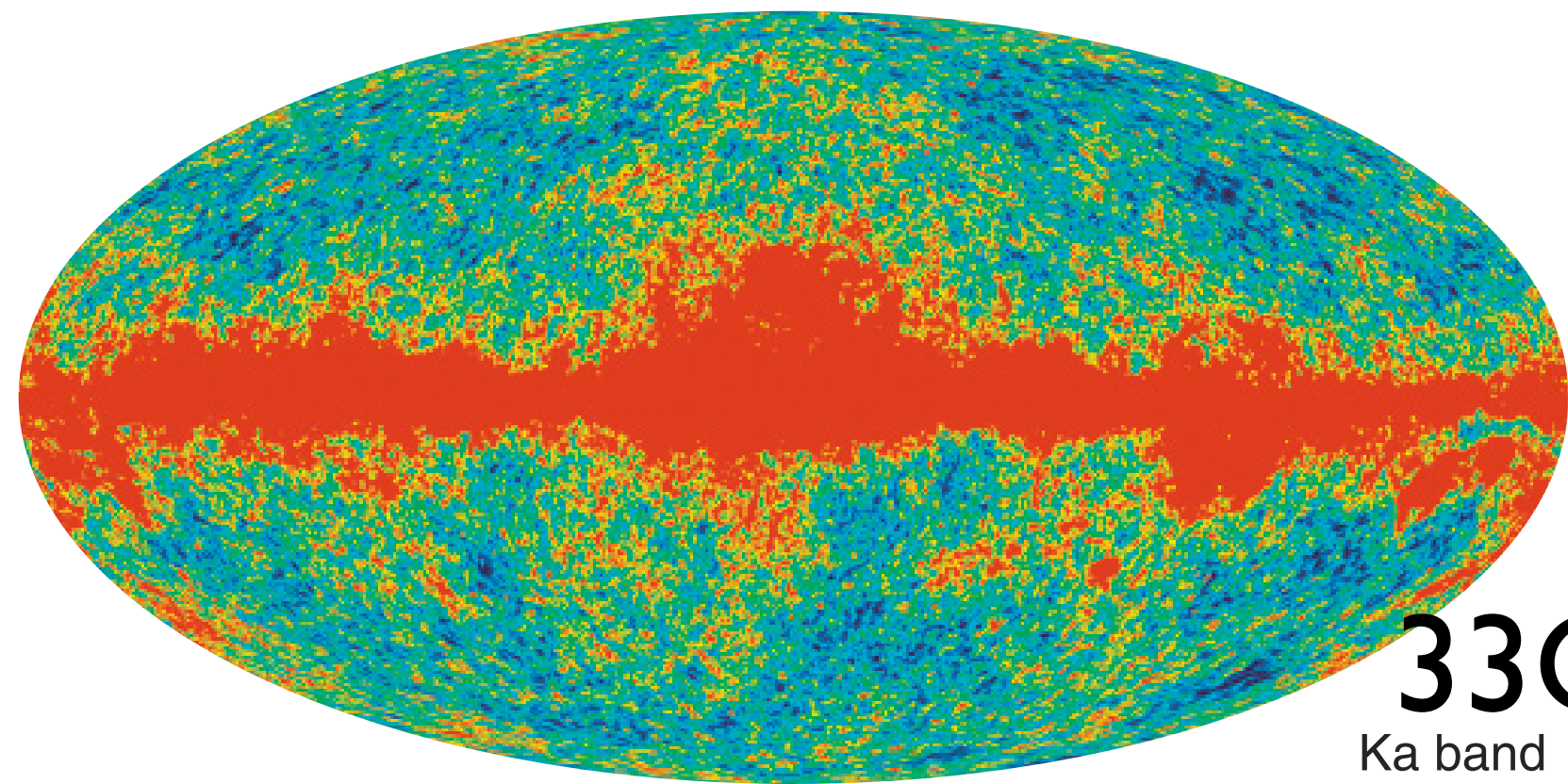
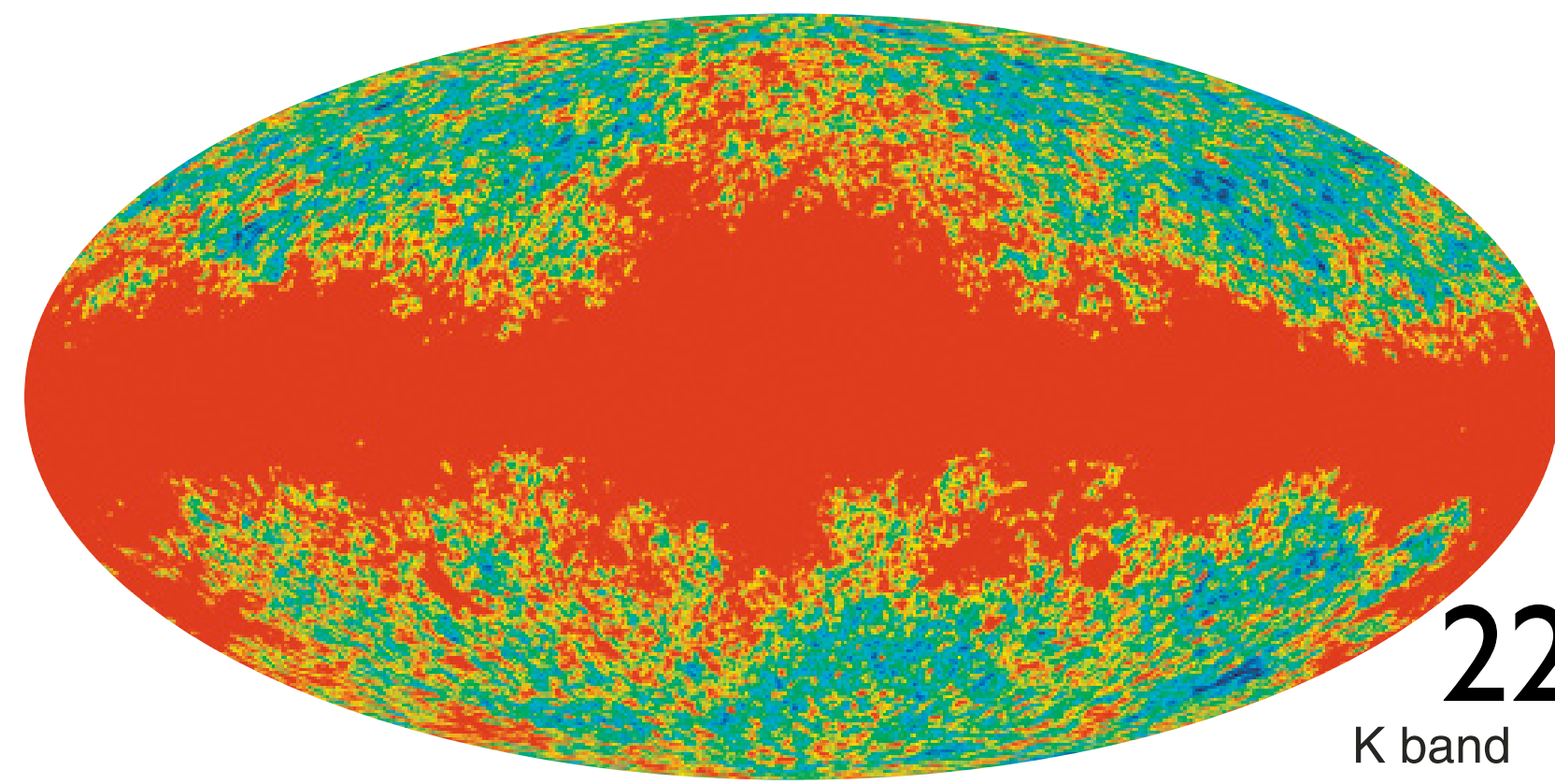


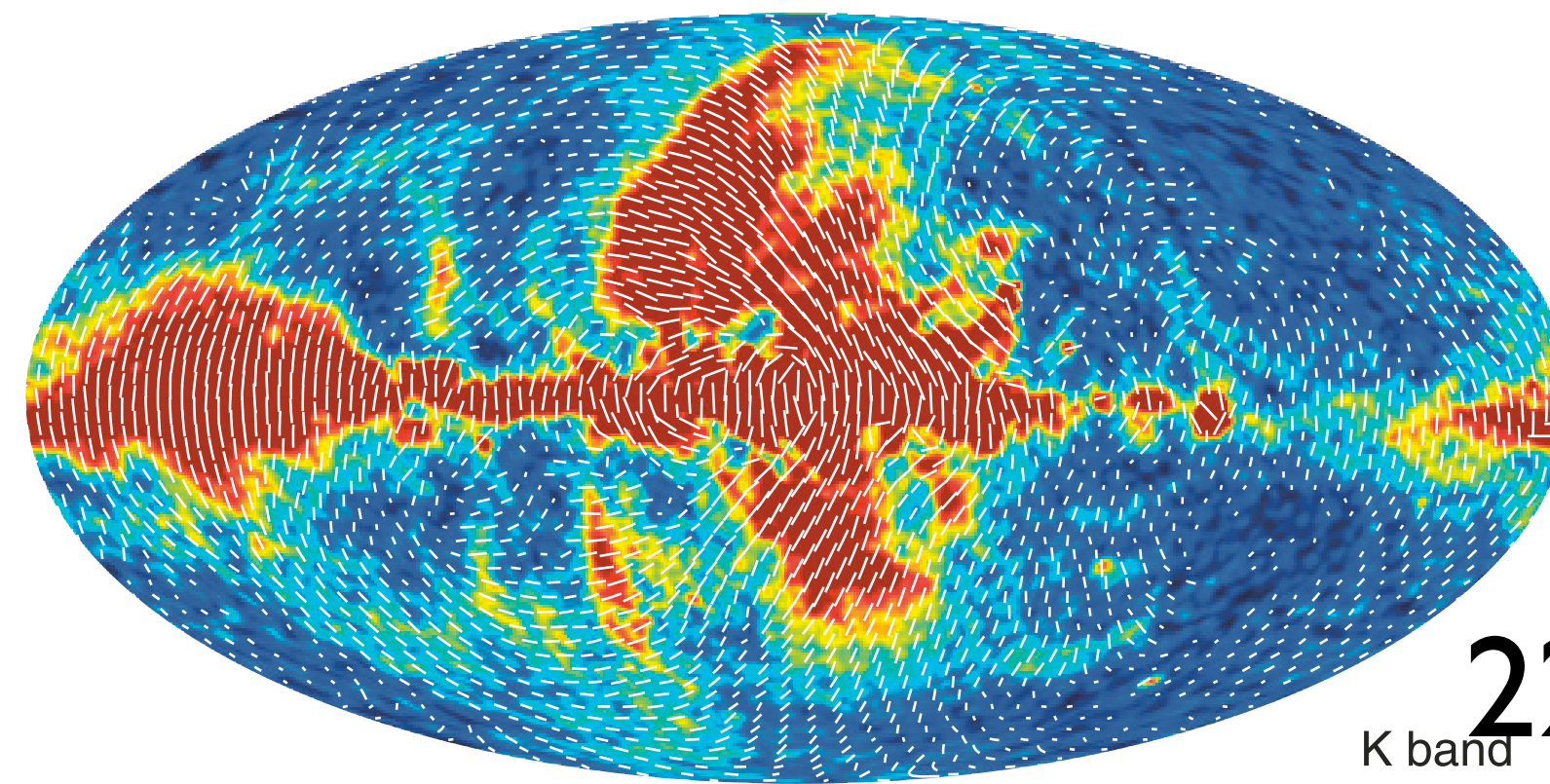
- A microwave satellite working at L2
  - Five frequency bands
    - K (22GHz), Ka (33GHz), Q (41GHz), V (61GHz), W (94GHz)
    - Multi-frequency is crucial for cleaning the Galactic emission
  - **The Key Feature: Differential Measurement**
    - The technique inherited from COBE
    - 10 “Differencing Assemblies” (DAs)
    - K1, Ka1, Q1, Q2, V1, V2, W1, W2, W3, & W4, each consisting of two radiometers that are sensitive to orthogonal linear polarization modes.
  - Temperature anisotropy is measured by **single difference**.
  - Polarization anisotropy is measured by **double difference**.
- WMAP can measure polarization as well!**

# WMAP Spacecraft

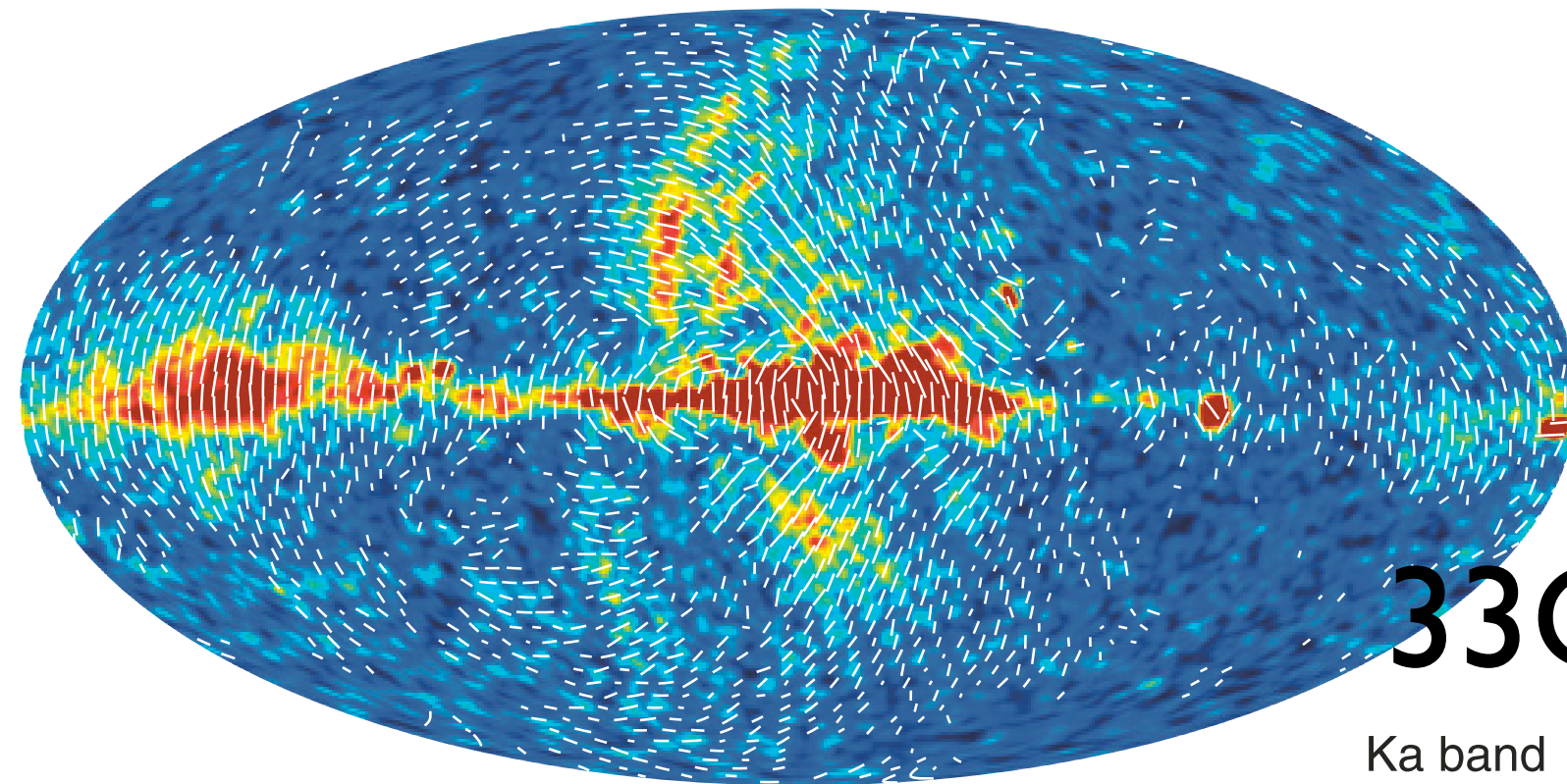
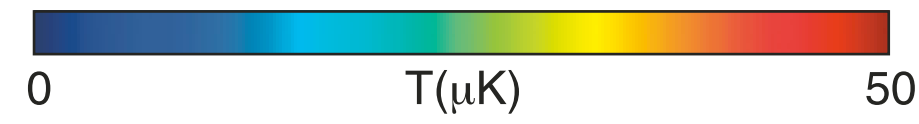
## Radiative Cooling: No Cryogenic System



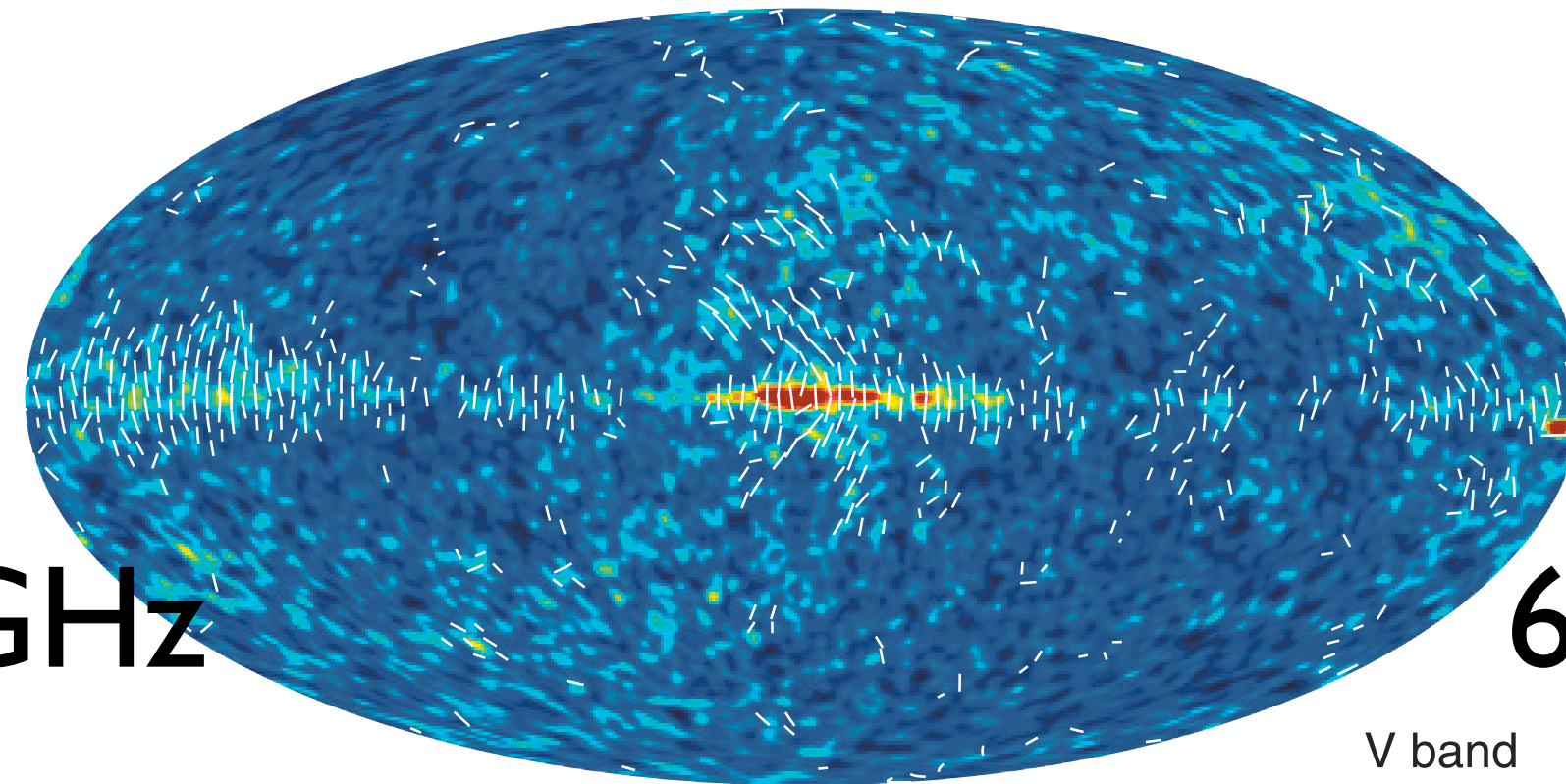




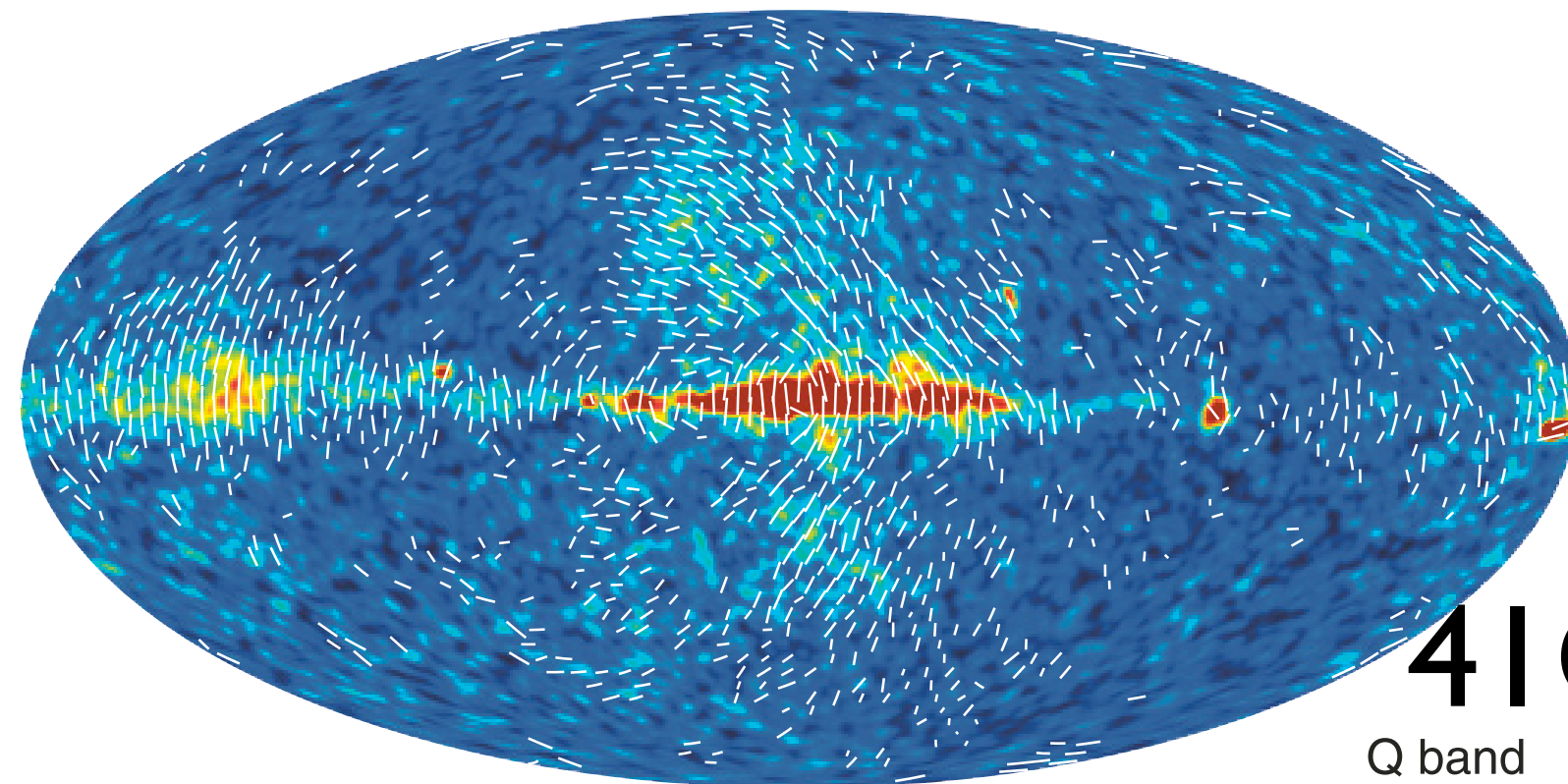
**22GHz**  
K band



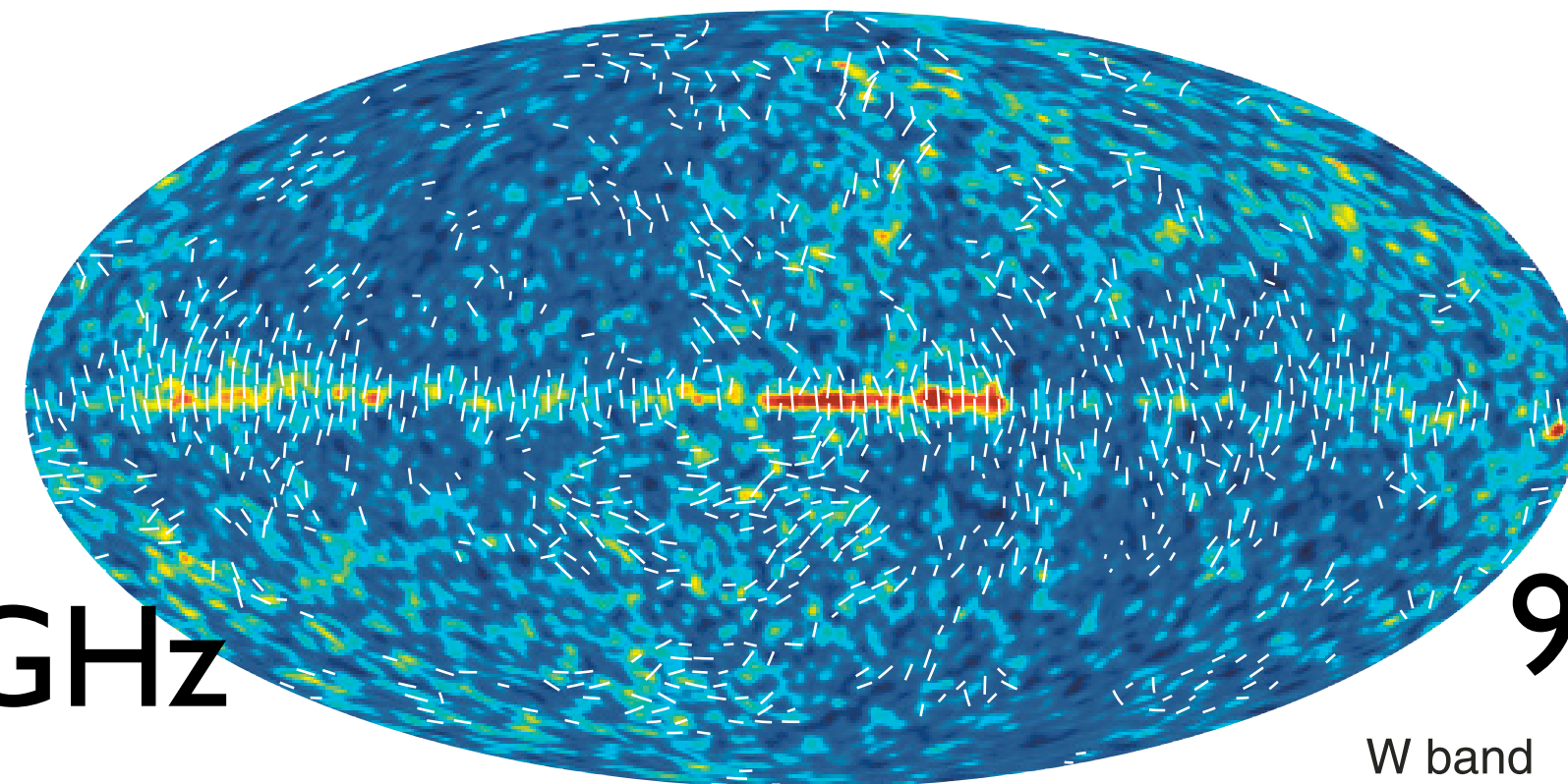
**33GHz**  
Ka band



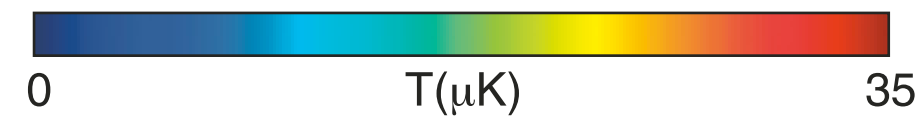
**61GHz**  
V band



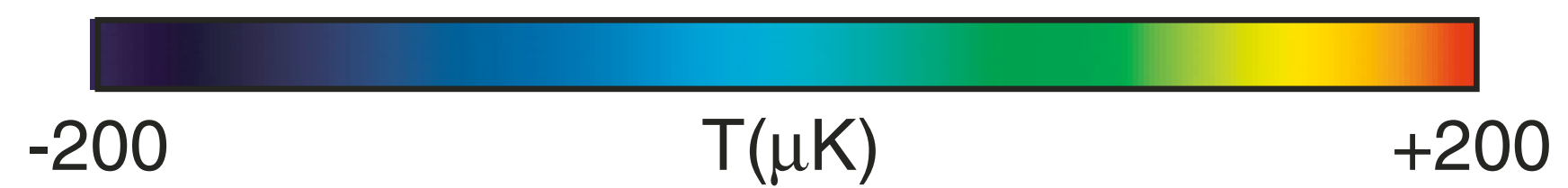
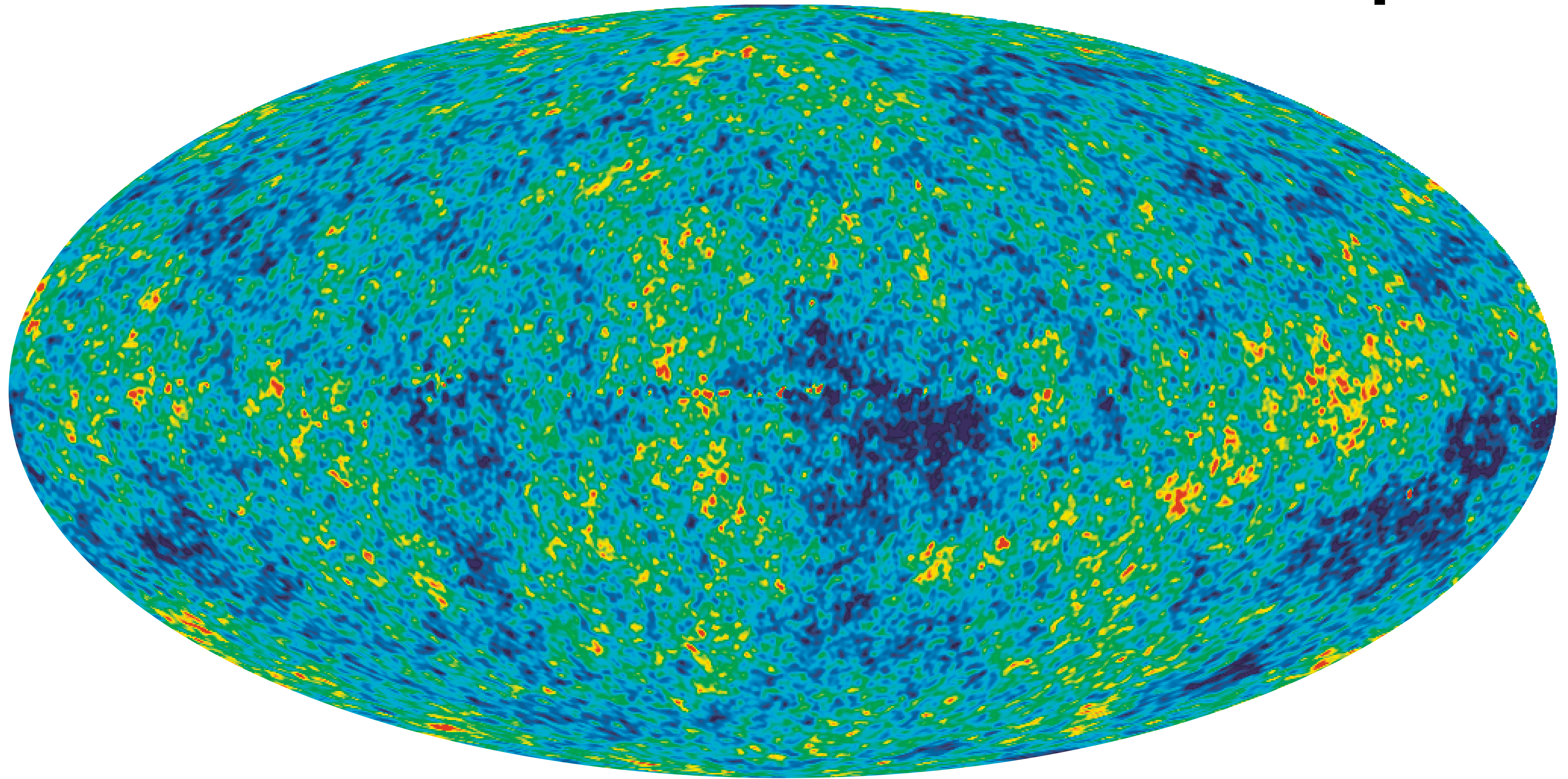
**41GHz**  
Q band



**94GHz**  
W band



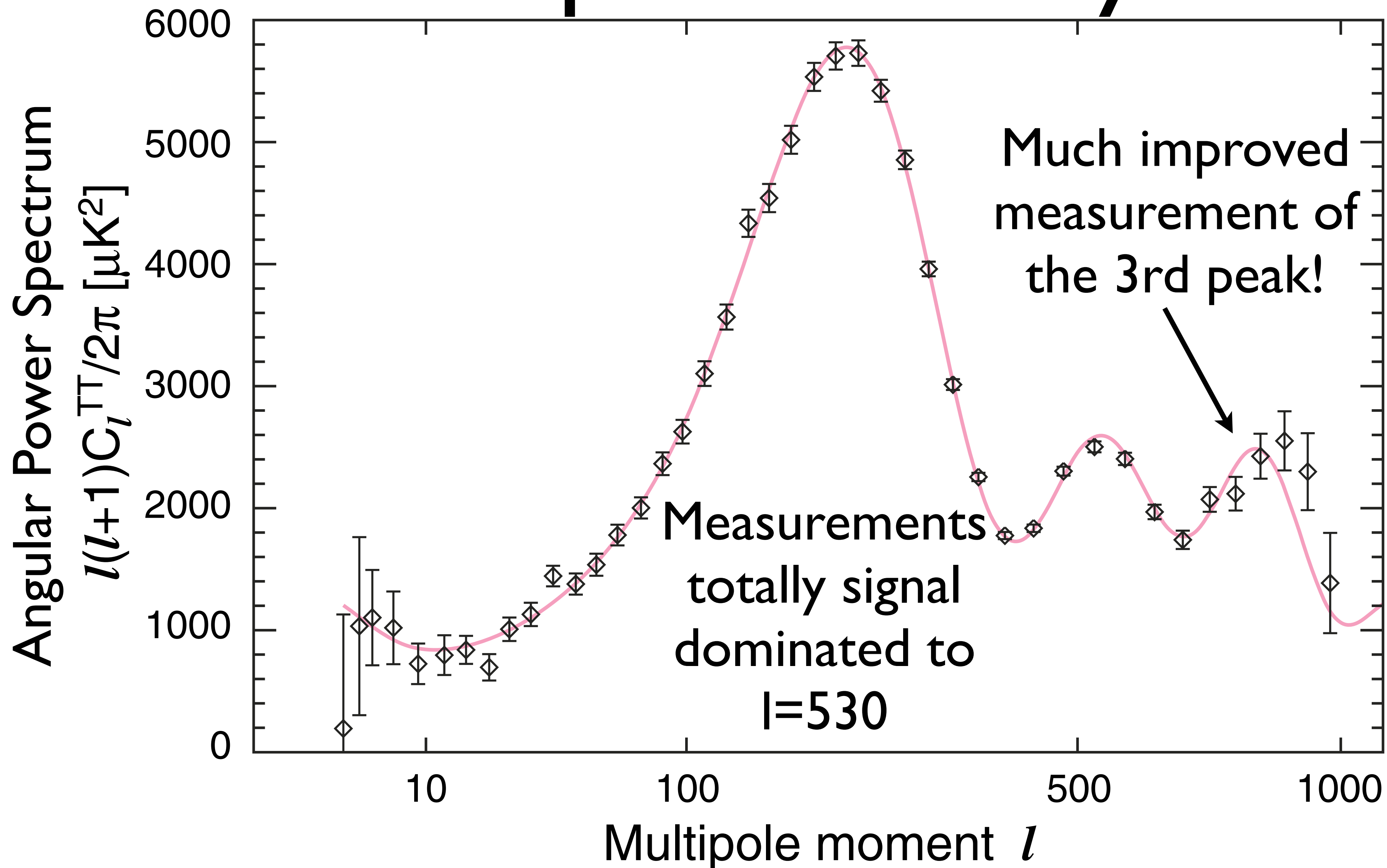
# How Did We Use This Map?



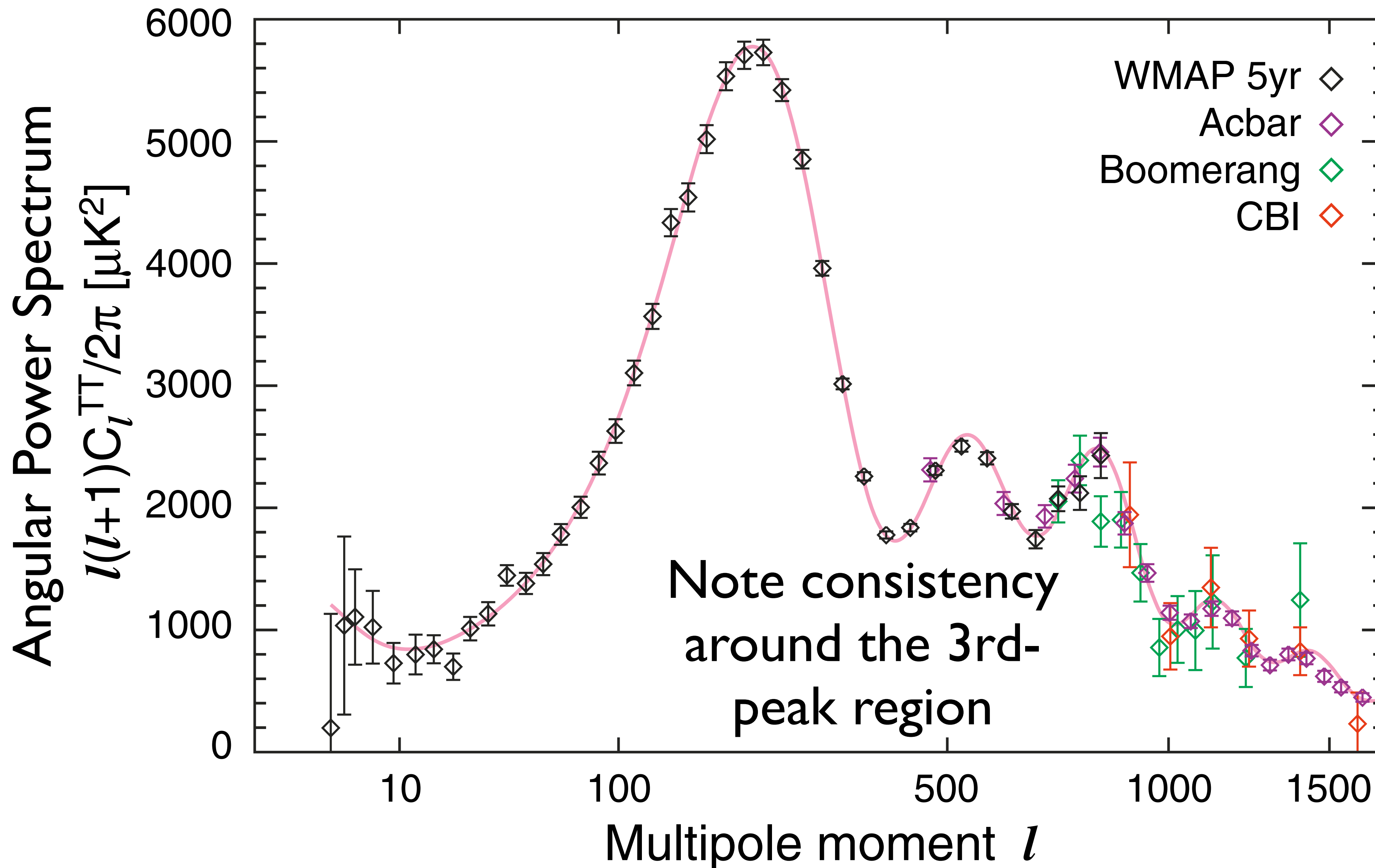
WMAP 5-year



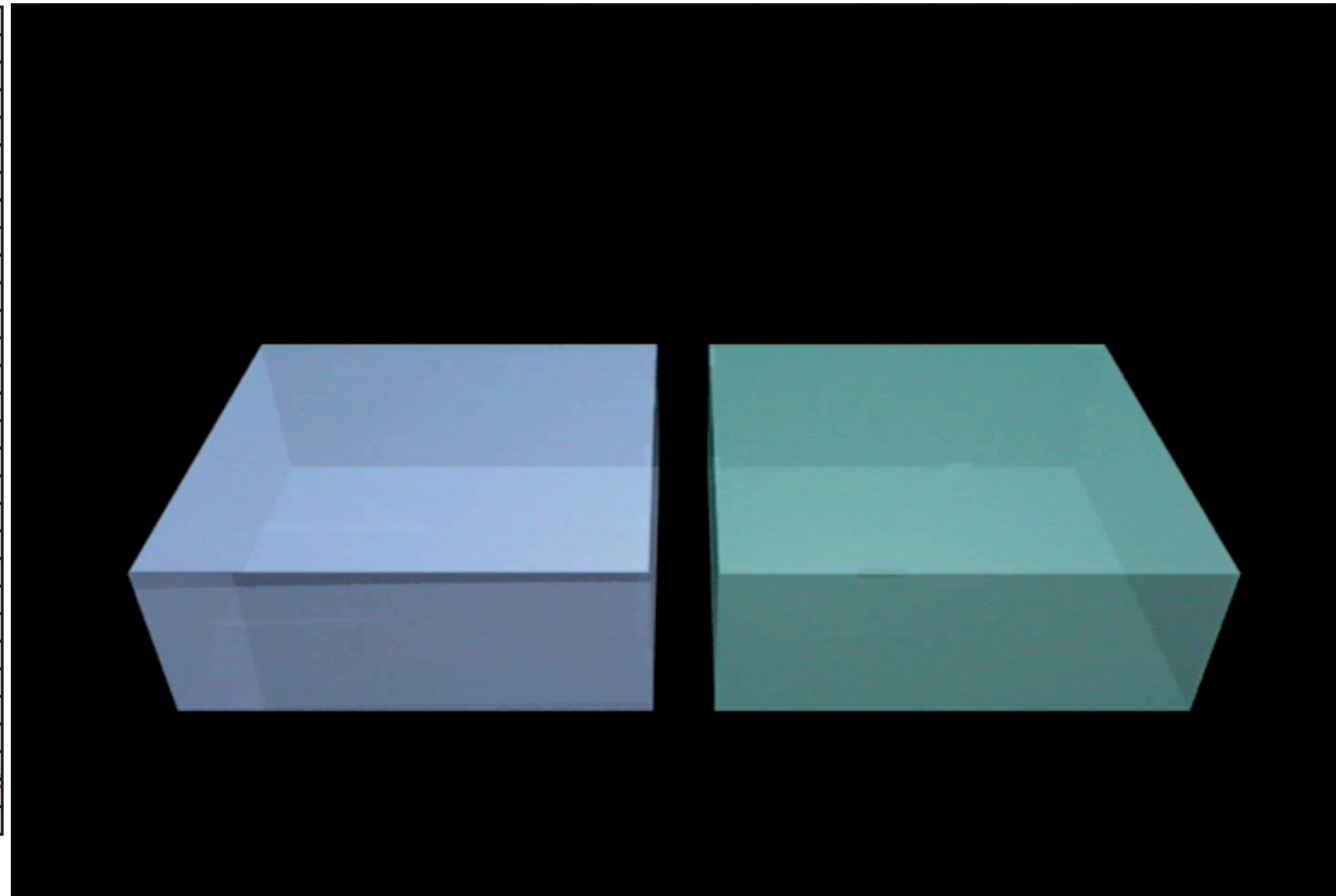
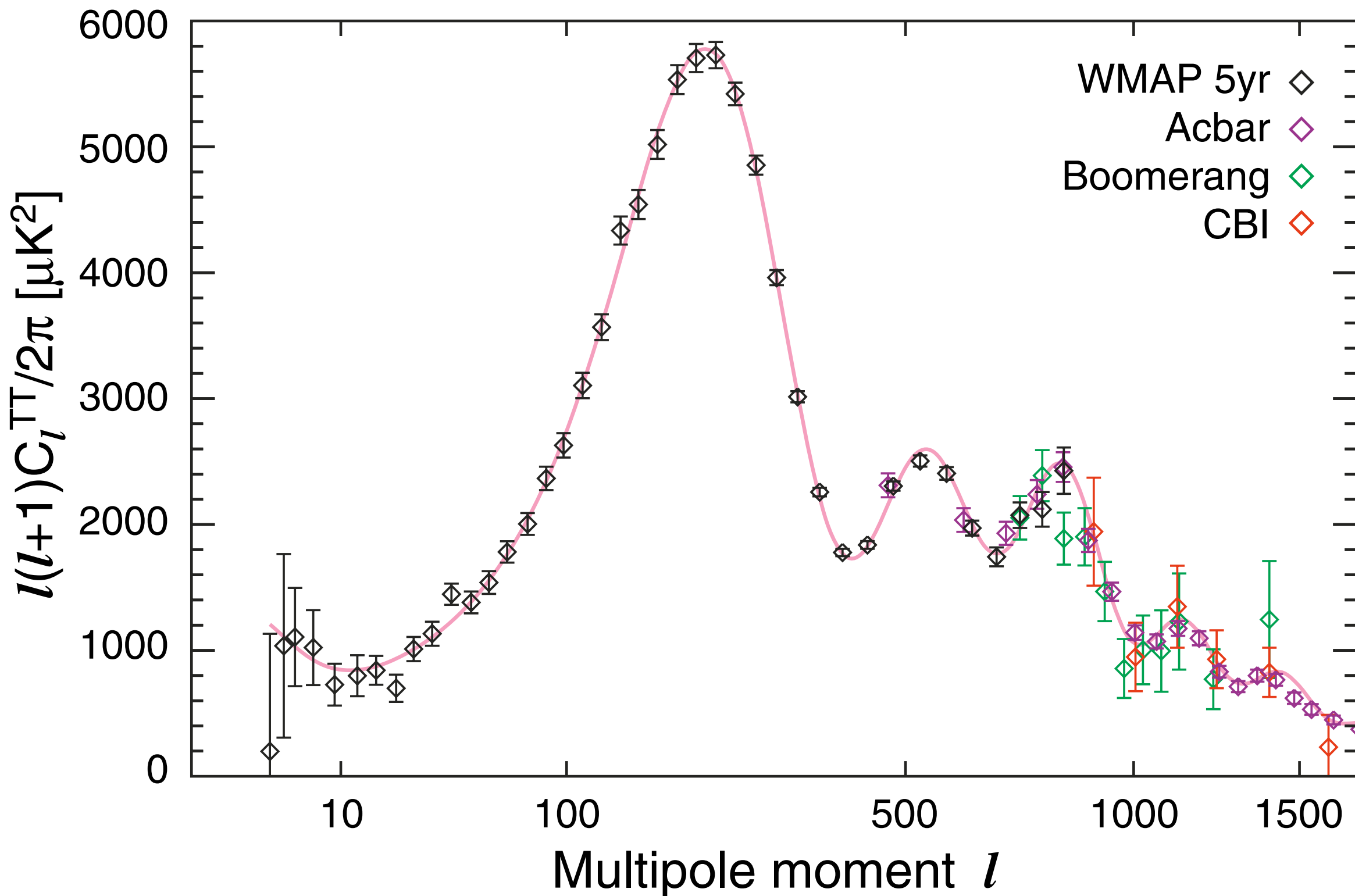
# The Spectral Analysis



# The Cosmic Sound Wave

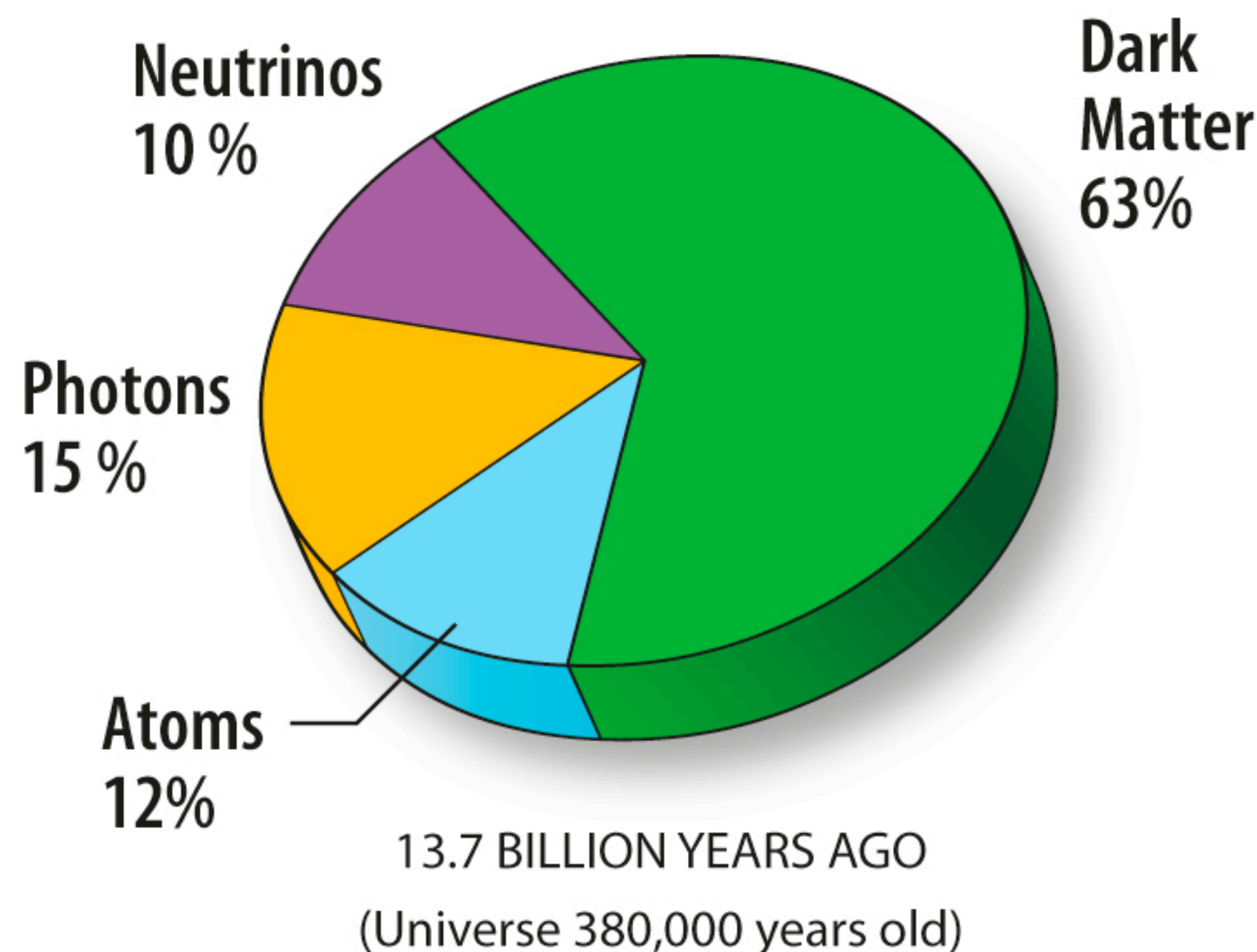
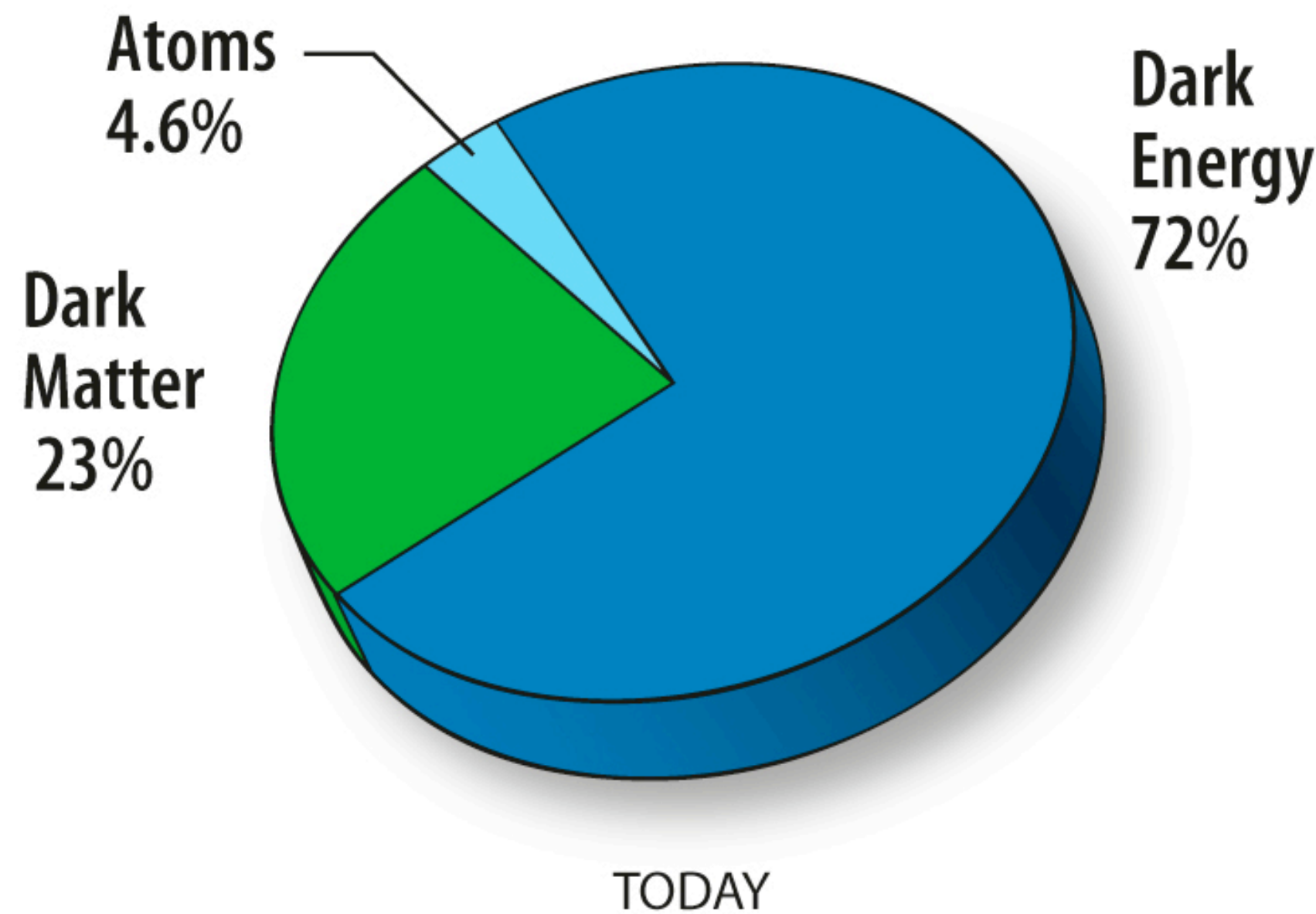


# The Cosmic Sound Wave



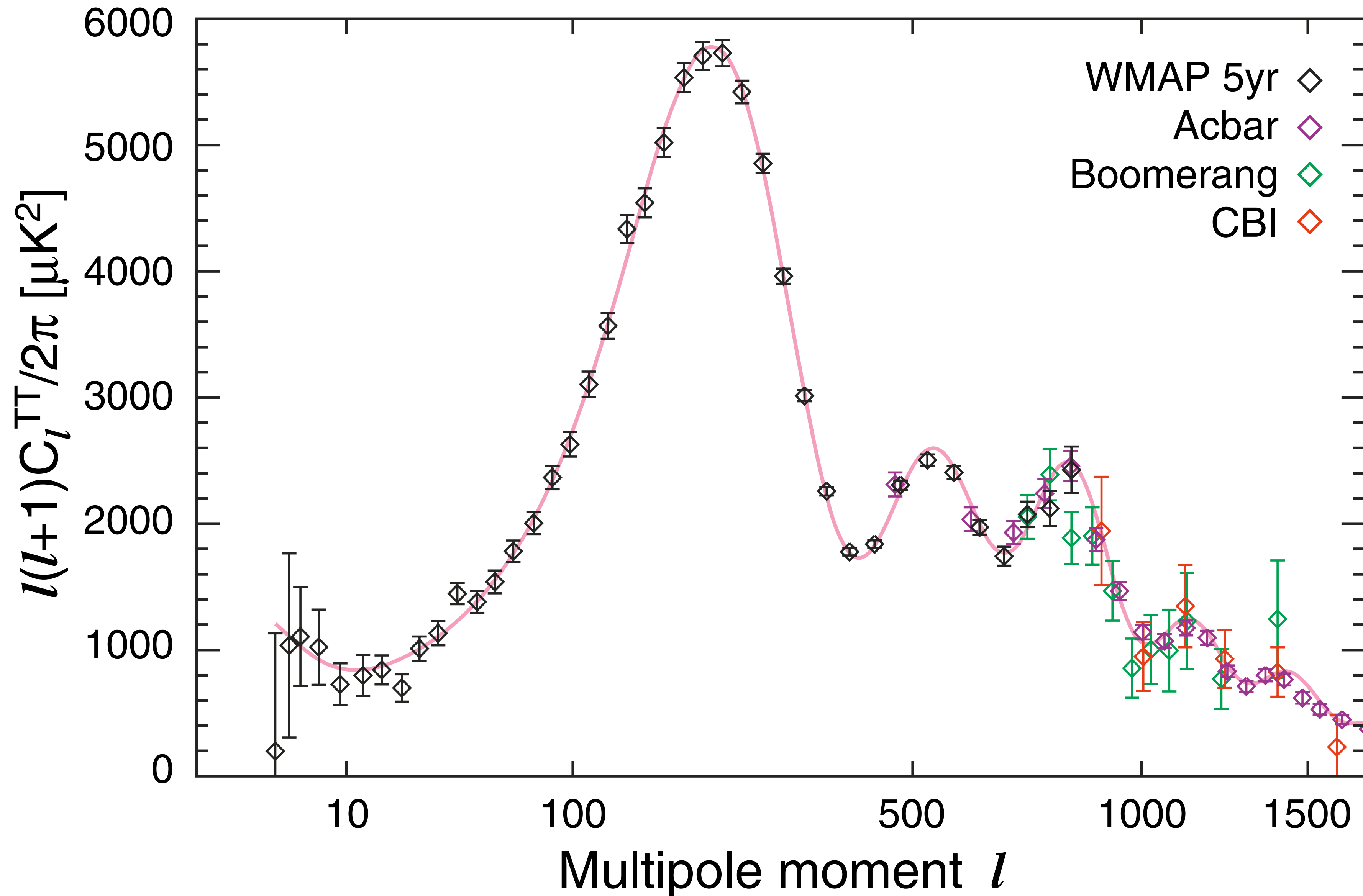
- We measure the composition of the Universe by analyzing the wave form of the cosmic sound waves. E.g.,
  - **1st-to-2nd-peak** ratio: baryon-to-photon ratio
  - **1st-to-3rd-peak** ratio: total matter-to-total radiation ratio

# ~WMAP 5-Year~ Pie Chart Update!

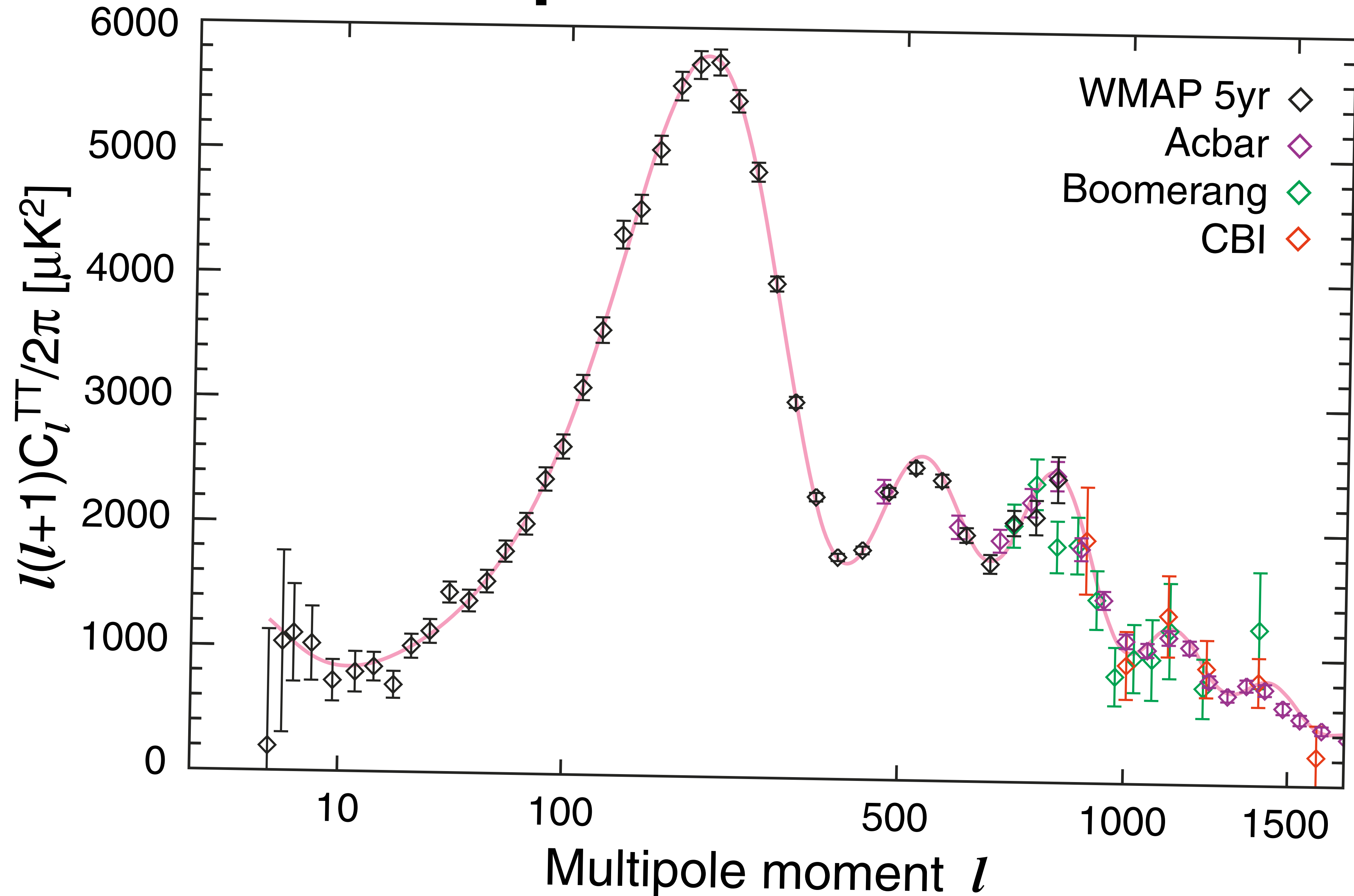


- Universe today
  - Age: **13.72 +/- 0.12 Gyr**
  - Atoms: **4.56 +/- 0.15 %**
  - Dark Matter: **22.8 +/- 1.3%**
  - Vacuum Energy: **72.6 +/- 1.5%**
- When CMB was released 13.7 B yrs ago
  - A significant contribution from the *cosmic neutrino background*

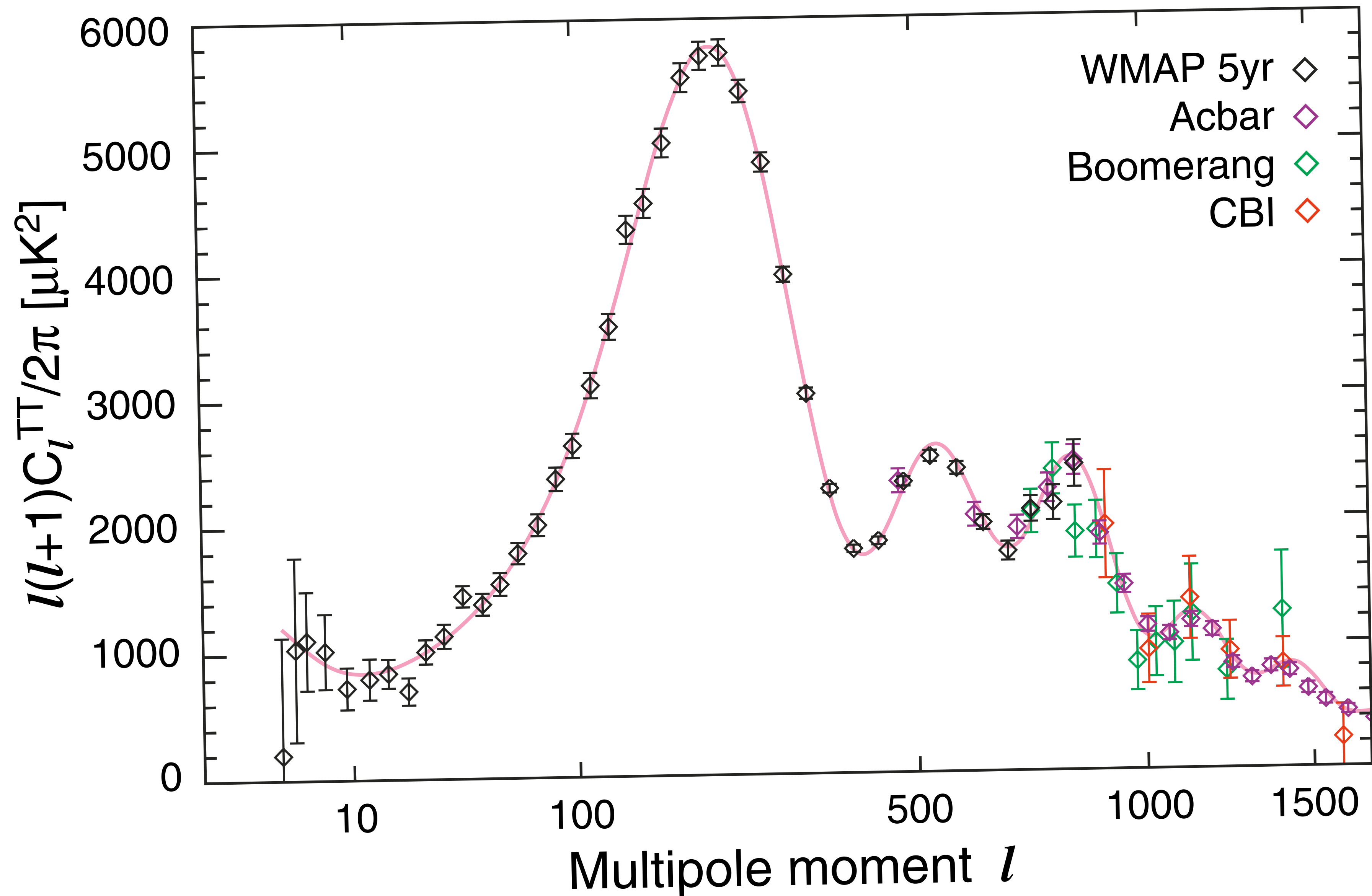
# *Tilting*=Primordial Shape->Inflation



# “Red” Spectrum: $n_s < 1$



# “Blue” Spectrum: $n_s > 1$

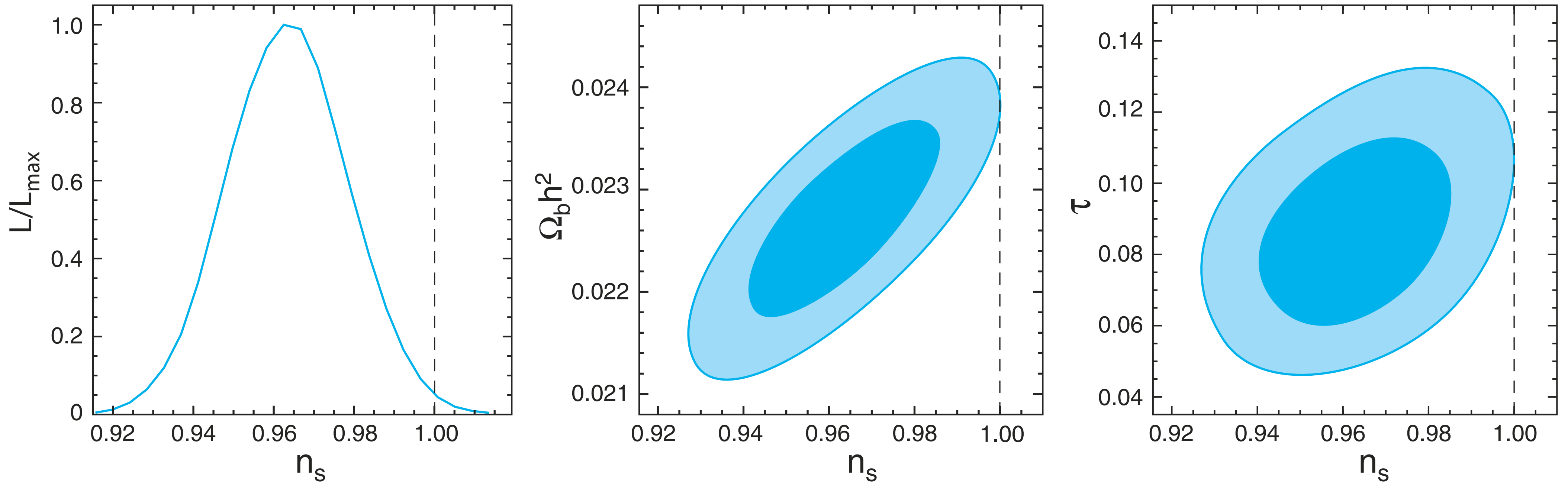


# Expectations From 1970's: $n_s=1$

- Metric perturbations in  $g_{ij}$  (let's call that “curvature perturbations”  $\Phi$ ) is related to  $\delta$  via
  - $k^2\Phi(k)=4\pi G\rho a^2\delta(k)$
- Variance of  $\Phi(x)$  in position space is given by
  - $\langle\Phi^2(x)\rangle=\int\ln k \mathbf{k}^3|\Phi(\mathbf{k})|^2$
  - In order to avoid the situation in which curvature (geometry) diverges on small or large scales, a “scale-invariant spectrum” was proposed:  $\mathbf{k}^3|\Phi(\mathbf{k})|^2 = \text{const.}$
  - This leads to the expectation:  $\mathbf{P}(\mathbf{k})=|\delta(k)|^2=\mathbf{k} \ (n_s=1)$ 
    - *Harrison 1970; Zel'dovich 1972; Peebles&Yu 1970*<sup>24</sup>



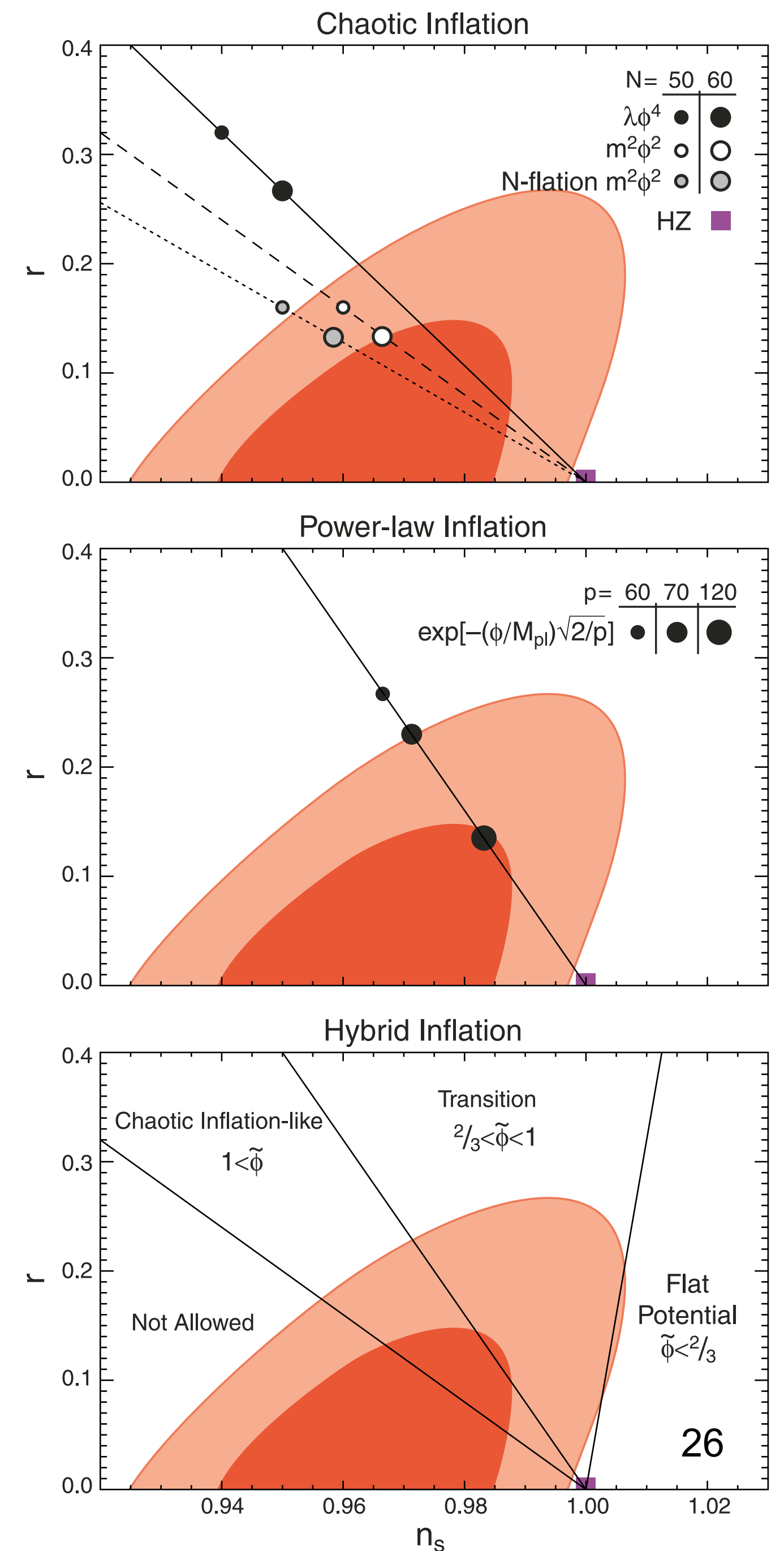
# Is $n_s$ different from ONE?



- WMAP-alone:  $n_s = \mathbf{0.963}$  (+0.014) (-0.015) (Dunkley et al.)
  - 2.5-sigma away from  $n_s = 1$ , “scale invariant spectrum”
- $n_s$  is degenerate with  $\Omega_b h^2$ ; thus, we can't really improve upon  $n_s$  further unless we improve upon  $\Omega_b h^2$

# Deviation from $n_s=1$

- This was expected by many inflationary models
- In  $n_s$ - $r$  plane (where  $r$  is called the “tensor-to-scalar ratio,” which is  $P(k)$  of gravitational waves divided by  $P(k)$  of density fluctuations) **many inflationary models are compatible with the current data**
- Many models have been excluded also



# Searching for Primordial Gravitational Waves in CMB

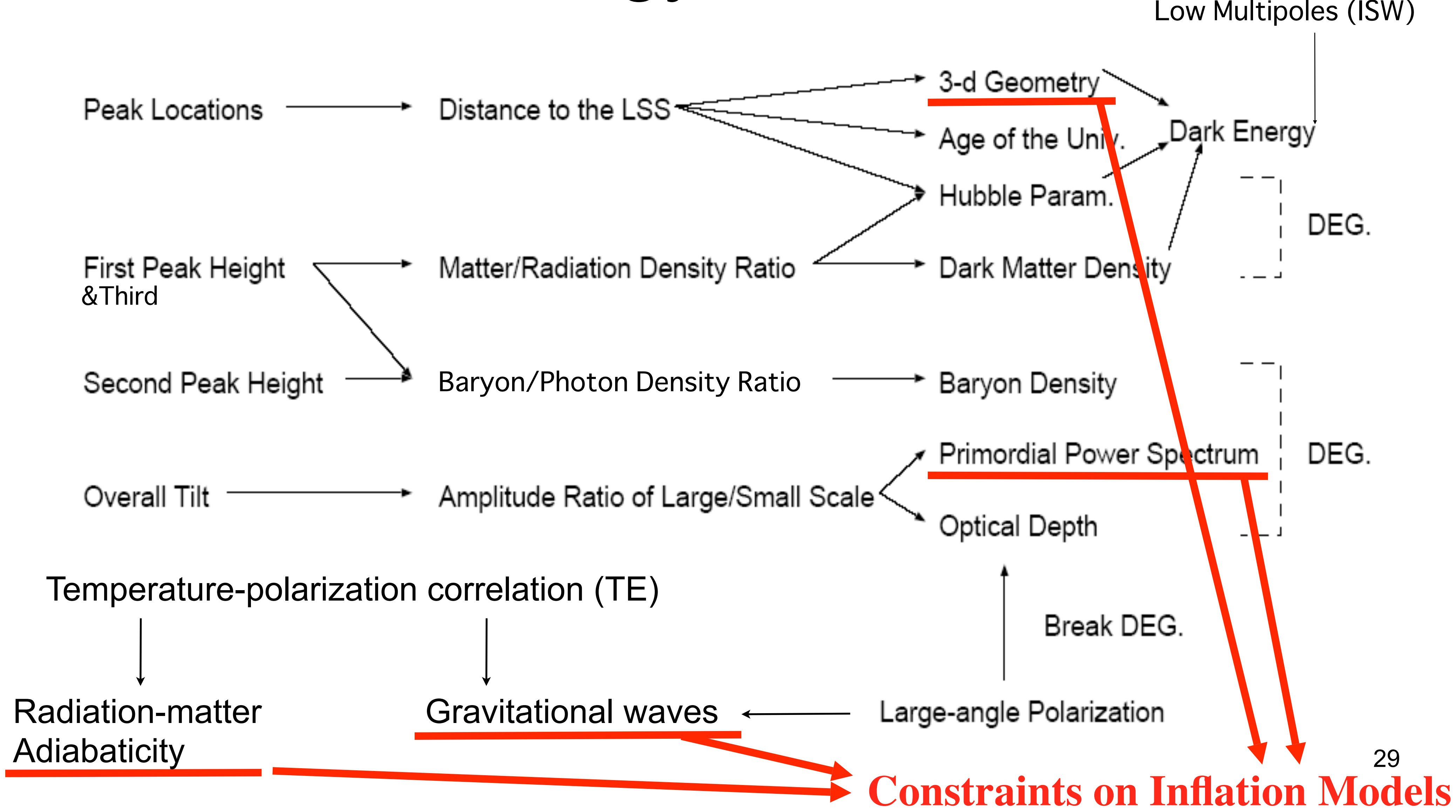
- Not only do inflation models produce density fluctuations, but also primordial gravitational waves
- Some predict the observable amount ( $r > 0.01$ ), some don't
- Current limit:  **$r < 0.22$**  (95%CL) (WMAP5+BAO+SN)
- Alternative scenarios (e.g., New Ekpyrotic) don't
- A powerful probe for testing inflation and testing specific models: next "Holy Grail" for CMBist

# Testing Cosmic Inflation

~5 Tests~

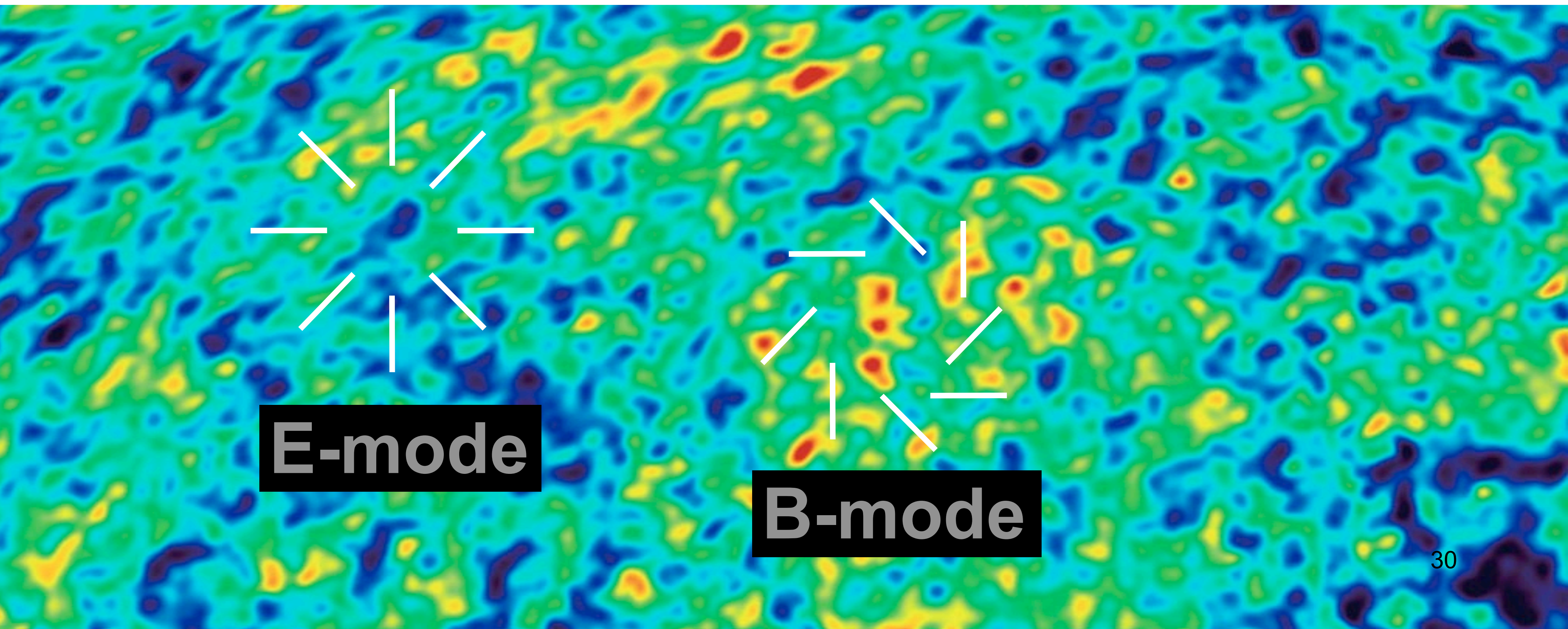
- Is the observable universe flat?
- Are the primordial fluctuations adiabatic?
- Are the primordial fluctuations nearly Gaussian?
- Is the power spectrum nearly scale invariant?
- Is the amplitude of gravitational waves reasonable?

# CMB to Cosmology to Inflation



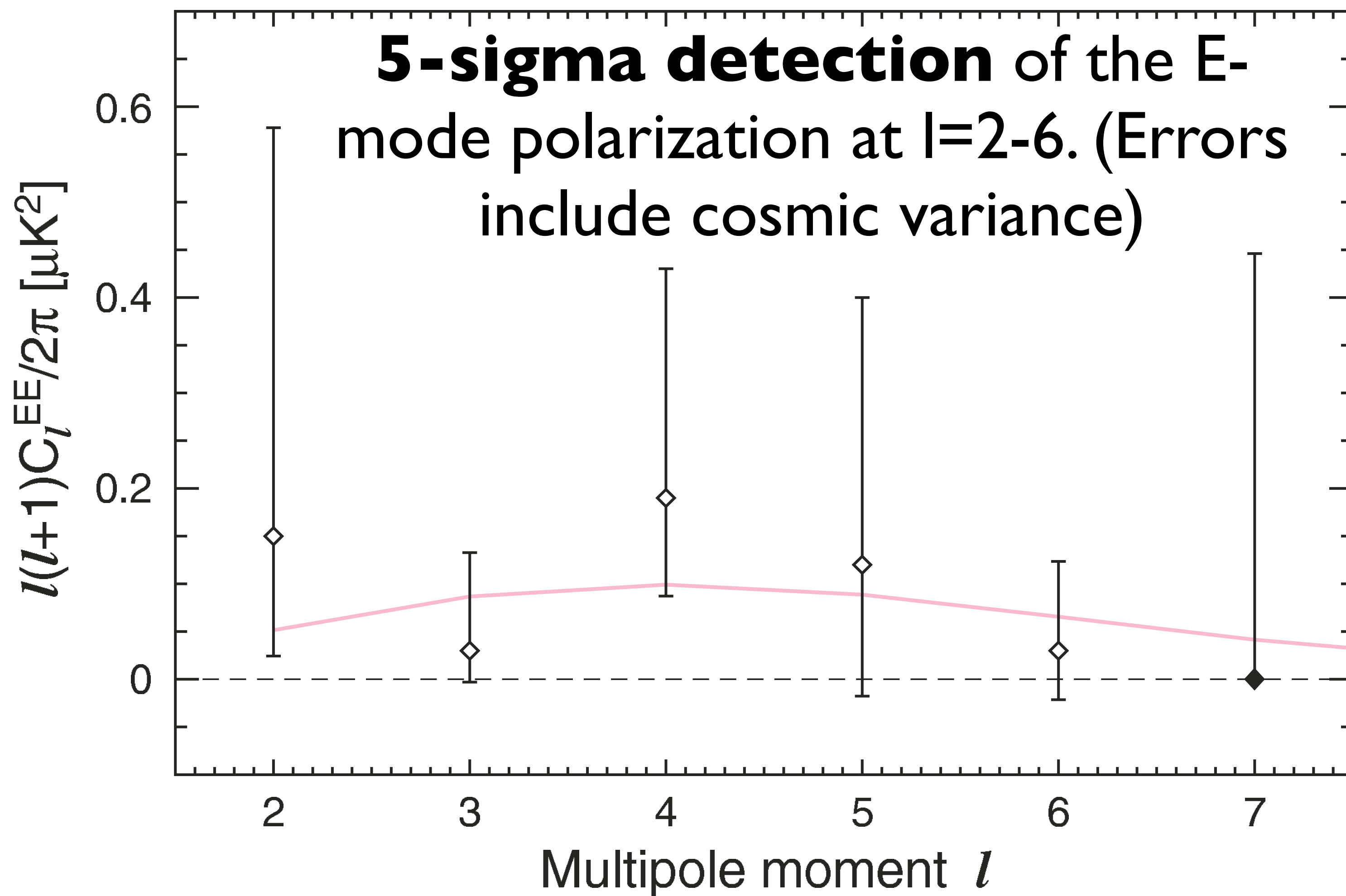
# *What About Polarization?*

- Polarization is a rank-2 tensor field.
- One can decompose it into a divergence-like “E-mode” and a vorticity-like “B-mode”.



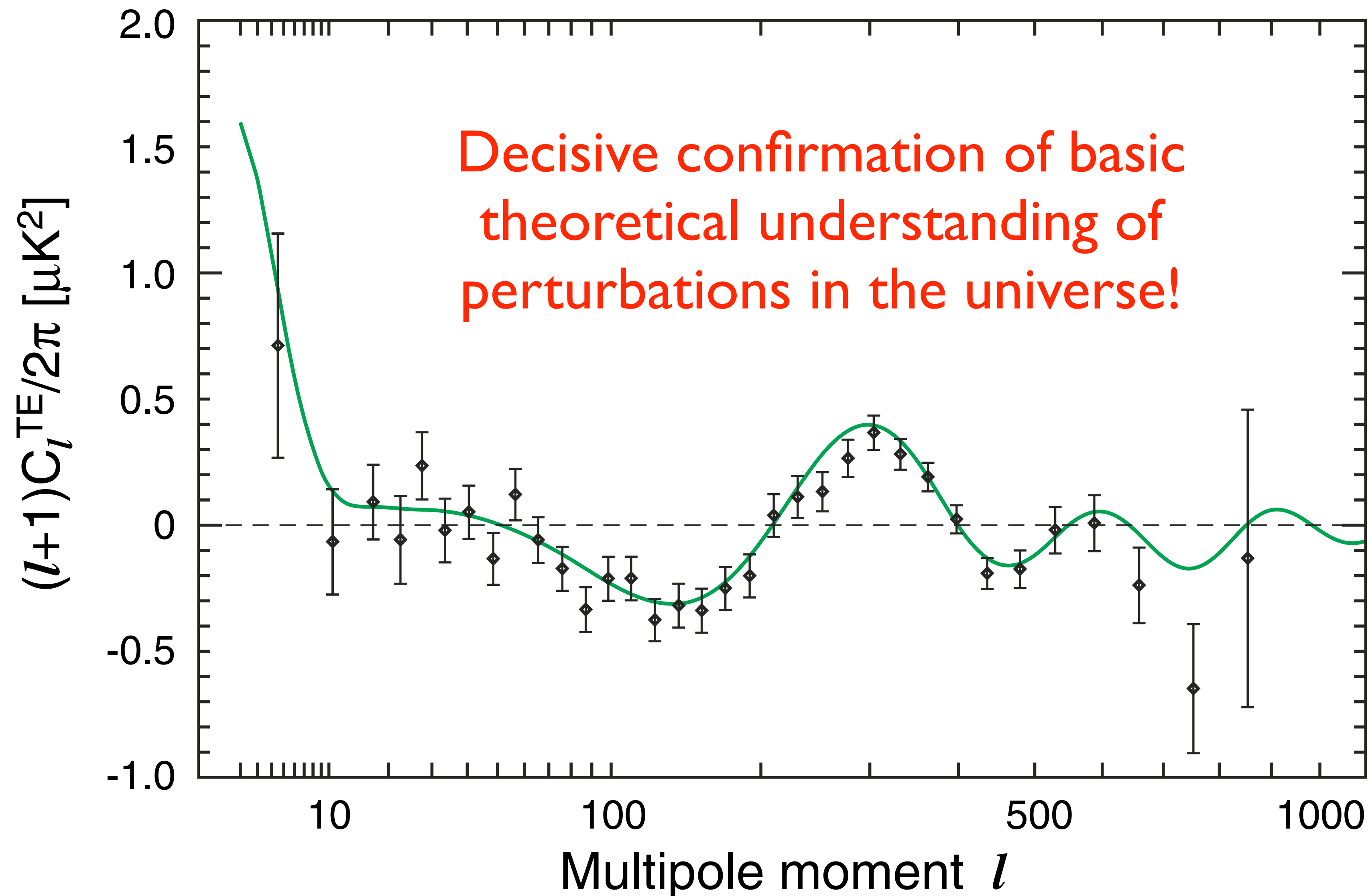
# 5-Year E-Mode Polarization Power Spectrum at Low $l$

E-Mode Angular Power Spectrum



Black Symbols are upper limits

# 5-Year TxE Power Spectrum





# B-modes

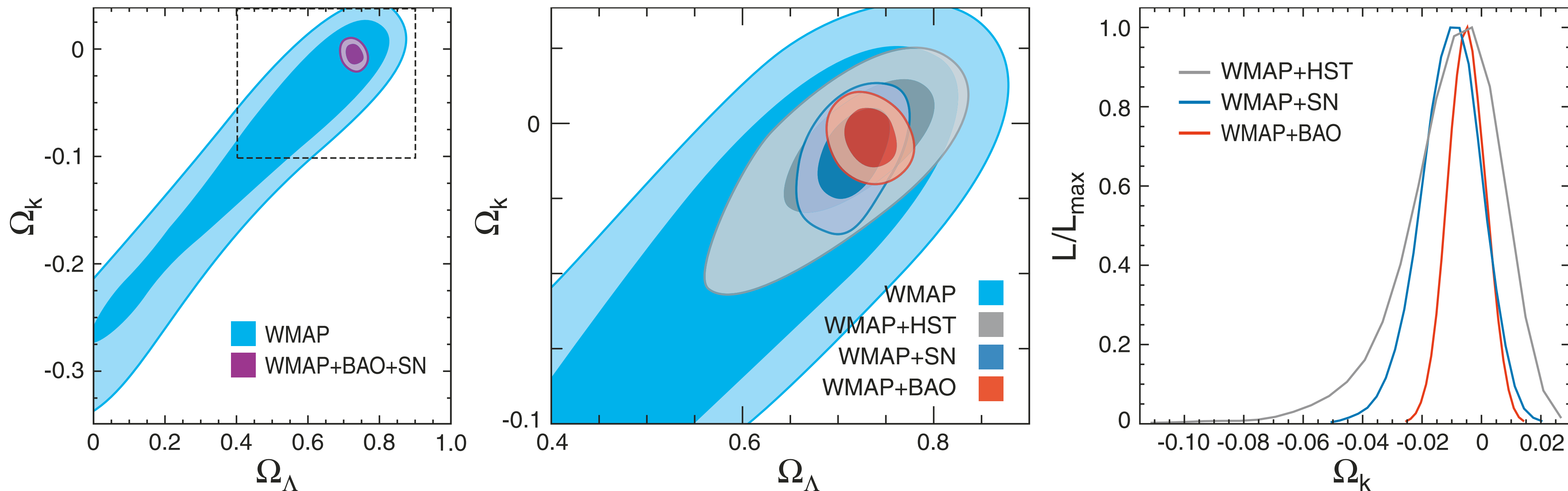
- No detection of B-mode polarization yet.
- I will come back to this later.

# How Do We Test Inflation?

- The WMAP data alone can put tight limits on most of the items in the check list. (For the WMAP-only limits, see Dunkley et al.)
- However, we can improve the limits on many of these items by adding the extra information from the **cosmological distance measurements**:
  - *Luminosity Distances* from Type Ia Supernovae (SN)
  - *Angular Diameter Distances* from the Baryon Acoustic Oscillations (BAO) in the distribution of galaxies

# Example: Flatness

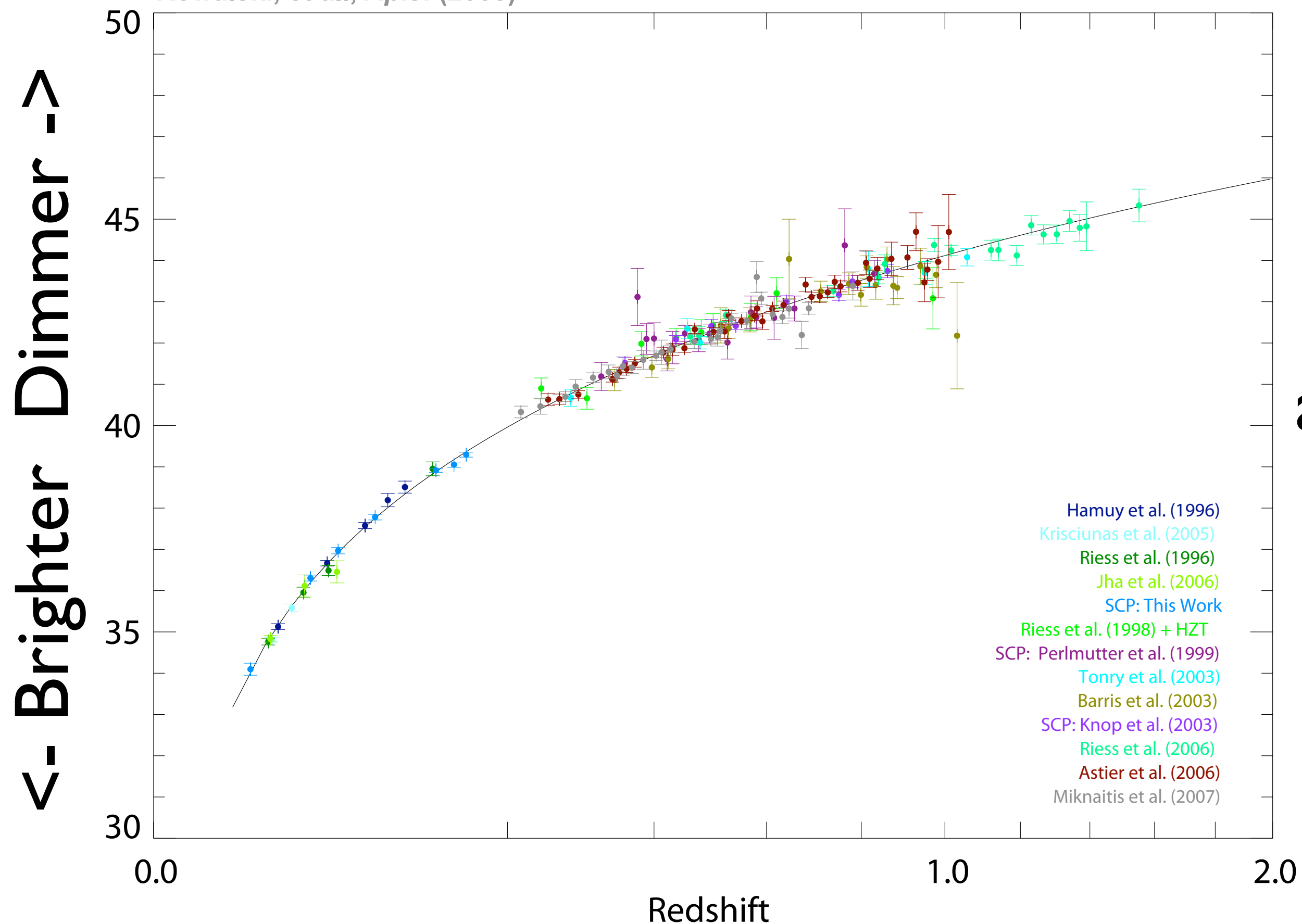
*Komatsu et al.*



- WMAP measures the angular diameter distance to the decoupling epoch at  $z=1090$ .
- The distance depends on curvature AND other things, like the energy content; thus, we need more than one distance indicators, in order to constrain, e.g.,  $\Omega_m$  and  $H_0$

# Type Ia Supernova (SN) Data

Supernova Cosmology Project  
Kowalski, et al., *Ap.J.* (2008)

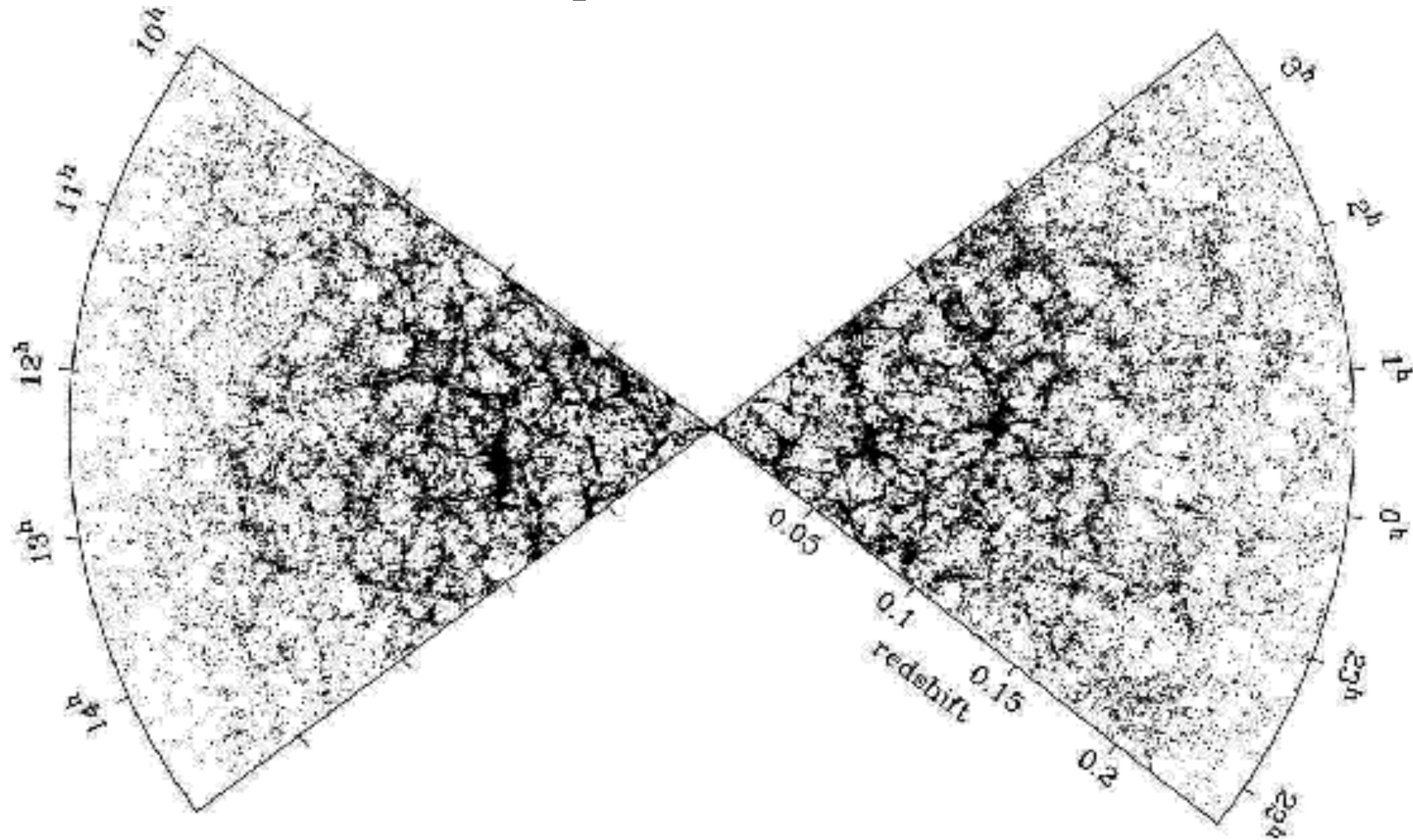


From these measurements, we get the **relative** luminosity distances between Type Ia SNe. Since we marginalize over the absolute magnitude, the current SN data are **not** sensitive to the absolute distances.

- Latest “Union” supernova compilation (Kowalski et al.)

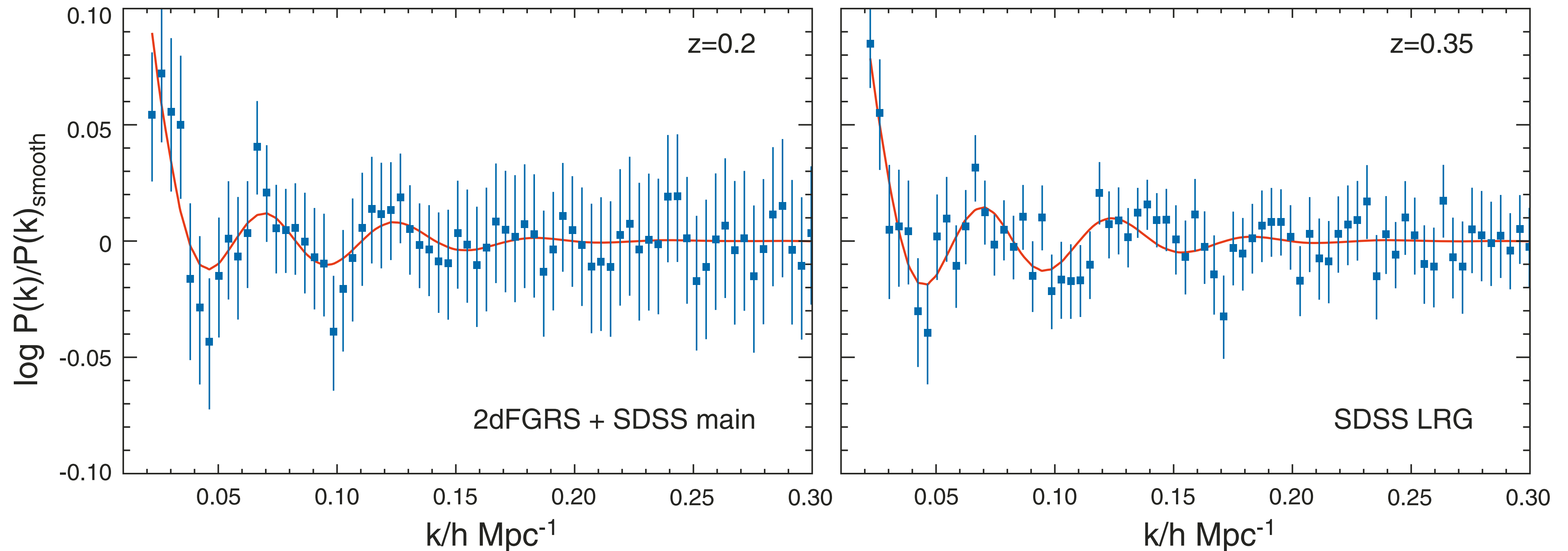
# BAO in Galaxy Distribution

2dFGRS



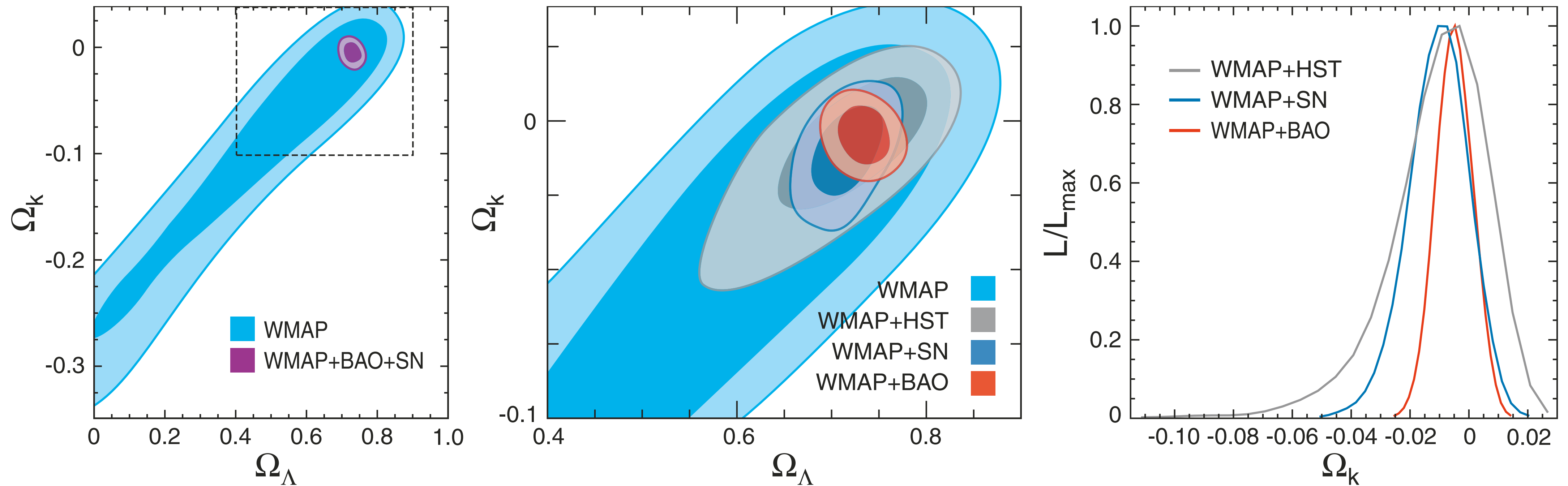
- The same acoustic oscillations should be hidden in this galaxy distribution...

# BAO in Galaxy Distribution *Dunkley et al.*



- BAO measured from SDSS (main samples and LRGs) and 2dFGRS (Percival et al. 2007)
- Just like the acoustic oscillations in CMB, the galaxy BAOs can be used to measure the **absolute** distances <sup>38</sup>

# As a result..



- **$-0.0181 < \Omega_k < 0.0071$**  (95% CL) for  $w=-1$  (i.e., dark energy being a cosmological constant)
- The constraint driven mostly by WMAP+BAO

# How Big Is Our Universe?

- By definition, the curvature radius of the universe is given by
  - $R_{\text{curv}} = 3h^{-1}\text{Gpc} / \text{sqrt}(\Omega_k)$
  - For negatively curved space ( $\Omega_k > 0$ ):  $R > 33h^{-1}\text{Gpc}$
  - For positively curved space ( $\Omega_k < 0$ ):  $R > 22h^{-1}\text{Gpc}$
- The particle horizon today is  $9.7h^{-1}\text{Gpc}$ 
  - The curvature radius of the universe is at least 3 times as large as the observable universe.



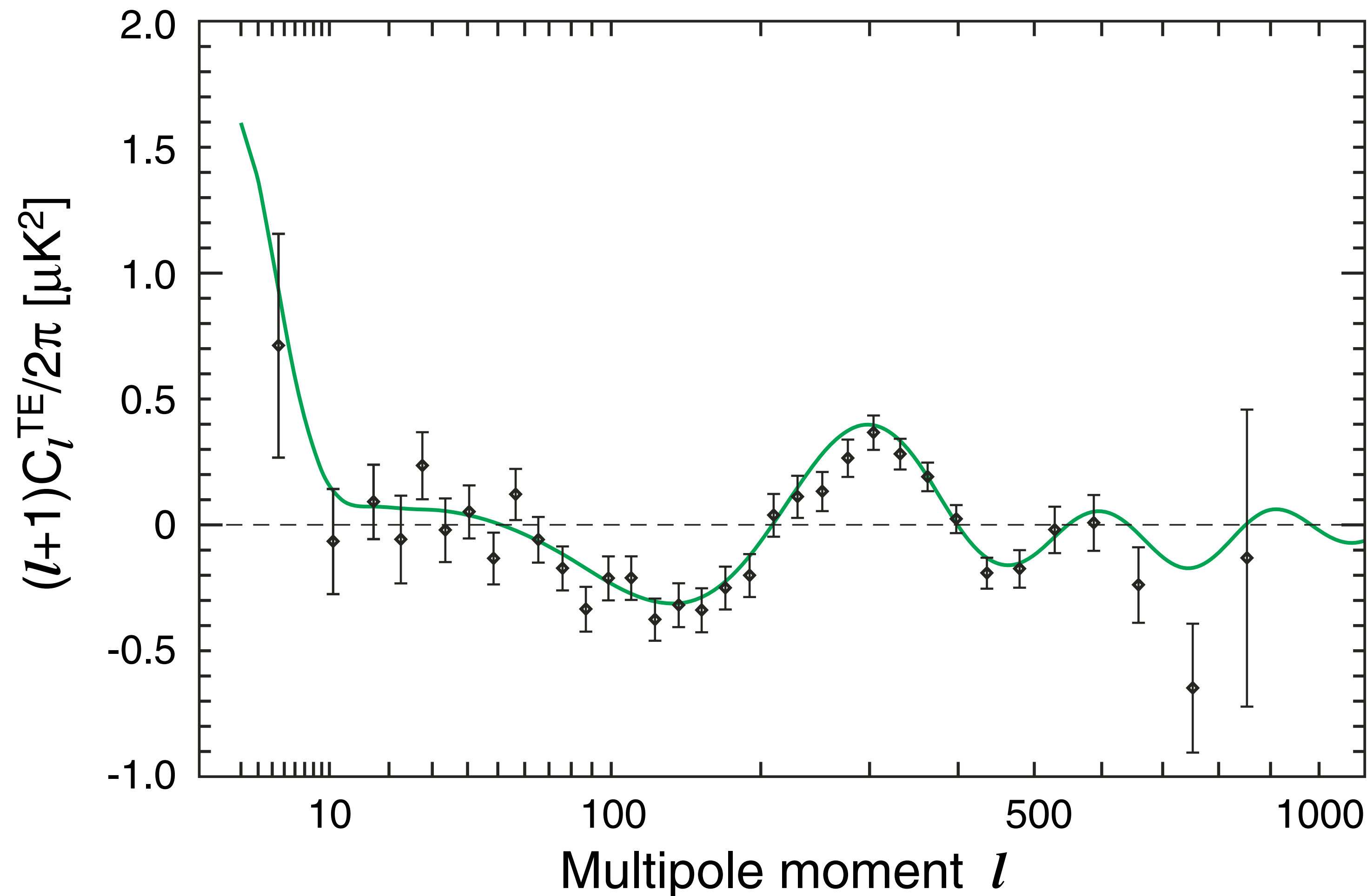
# How Long Did Inflation Last?

- The universe had expanded by  $e^{N_{\text{tot}}}$  during inflation.
  - Q. How long should inflation have lasted to explain the observed flatness of the universe?
  - A.  $N_{\text{total}} > 36 + \ln(T_{\text{reheating}}/1 \text{ TeV})$
  - A factor of 10 improvement in  $\Omega_k$  will raise this lower limit by 1.2.
  - Lower if the reheating temperature was  $< 1 \text{ TeV}$
- This is the check list #1

# Check List #2: Adiabaticity

- The **adiabatic relation** between radiation and matter:
  - $3\delta\rho_{\text{radiation}}/(4\rho_{\text{radiation}}) = \delta\rho_{\text{matter}}/\rho_{\text{matter}}$
- *Deviation from adiabaticity*: A simple-minded quantification
  - Fractional deviation of A from B =  $(A-B) / [(A+B)/2]$ 
    - $\delta_{\text{adi}} = [3\delta\rho_{\text{radiation}}/(4\rho_{\text{radiation}}) - \delta\rho_{\text{matter}}/\rho_{\text{matter}}] / \{ [3\delta\rho_{\text{radiation}}/(4\rho_{\text{radiation}}) + \delta\rho_{\text{matter}}/\rho_{\text{matter}}] / 2 \}$
  - Call this the “**adiabaticity deviation parameter**”
    - “Radiation and matter obey the adiabatic relation to  $(100\delta_{\text{adi}})\%$  level.”

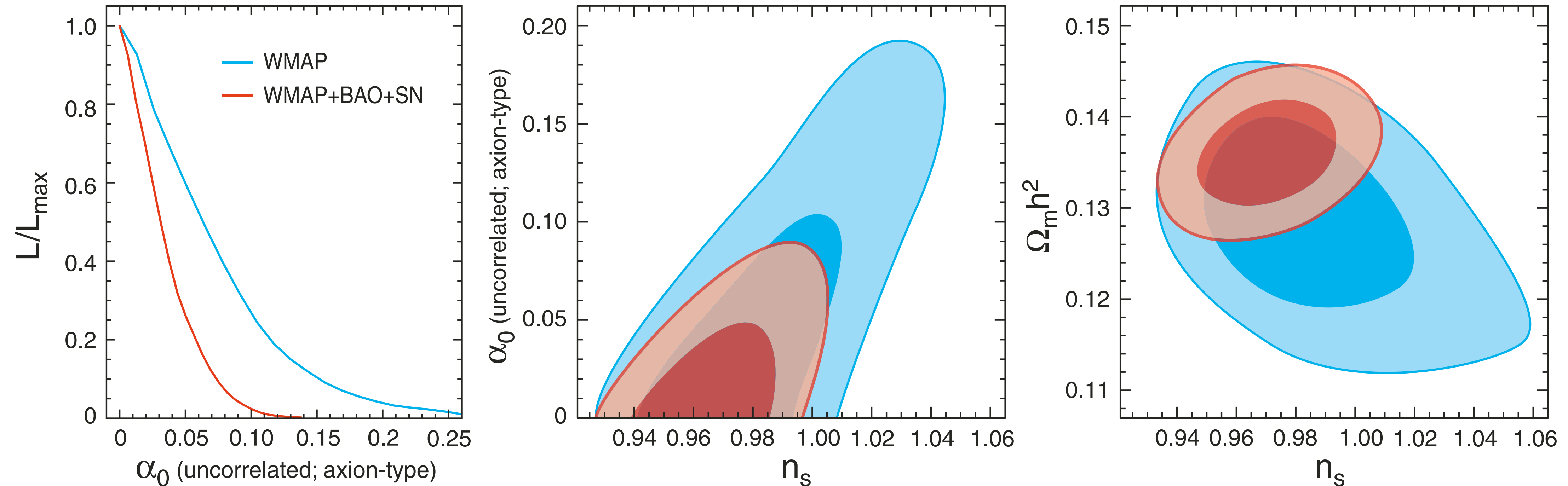
# WMAP 5-Year TE Power Spectrum



- The negative TE at  $l \sim 100$  is the distinctive signature of super-horizon adiabatic perturbations (Spergel & Zaldarriaga 1997)
- Non-adiabatic perturbations would fill in the trough, and shift the zeros.

# Axion Dark Matter

*Komatsu et al.*



- $\alpha_{\text{axion}} < 0.16$  [WMAP-only; 95% CL]
- $\alpha_{\text{axion}} < 0.072$  [WMAP+BAO+SN; 95% CL]
- CMB and axion-type dark matter are adiabatic to **8.9%**

# Axion Dark Matter?

- CMB and axion-type dark matter are adiabatic to **8.6%**
- **This puts a severe limit on axions being the dominant dark matter candidate.**

$$\frac{\Omega_a}{\Omega_c} < \frac{3.0 \times 10^{-39}}{\theta_a^5 \gamma^6} \left( \frac{0.01}{r} \right)^{7/2}$$

The non-adiabatic perturbations, combined with the expression for  $\Omega_a$ , constrain  $\Omega_a^{1/7}$ .

# Check list #3: Gaussianity

- In the simplest model of inflation, the distribution of primordial fluctuations is close to a Gaussian with random phases.
- The level of non-Gaussianity predicted by the simplest model is well below the current detection limit.
- A convincing detection of primordial non-Gaussianity will rule out most of inflation models in the literature.
  - **Detection of non-Gaussianity would be a breakthrough in cosmology**

# Getting the Most Out of Fluctuations, $\delta(\mathbf{x})$

- In Fourier space,  $\delta(\mathbf{k}) = A(\mathbf{k})\exp(i\varphi_{\mathbf{k}})$ 
  - **Power:**  $P(\mathbf{k}) = \langle |\delta(\mathbf{k})|^2 \rangle = A^2(\mathbf{k})$
  - **Phase:**  $\varphi_{\mathbf{k}}$
- We can use the observed distribution of...
  - matter (e.g., galaxies, gas)
  - radiation (e.g., Cosmic Microwave Background)
- to learn about both  $P(\mathbf{k})$  and  $\varphi_{\mathbf{k}}$ .

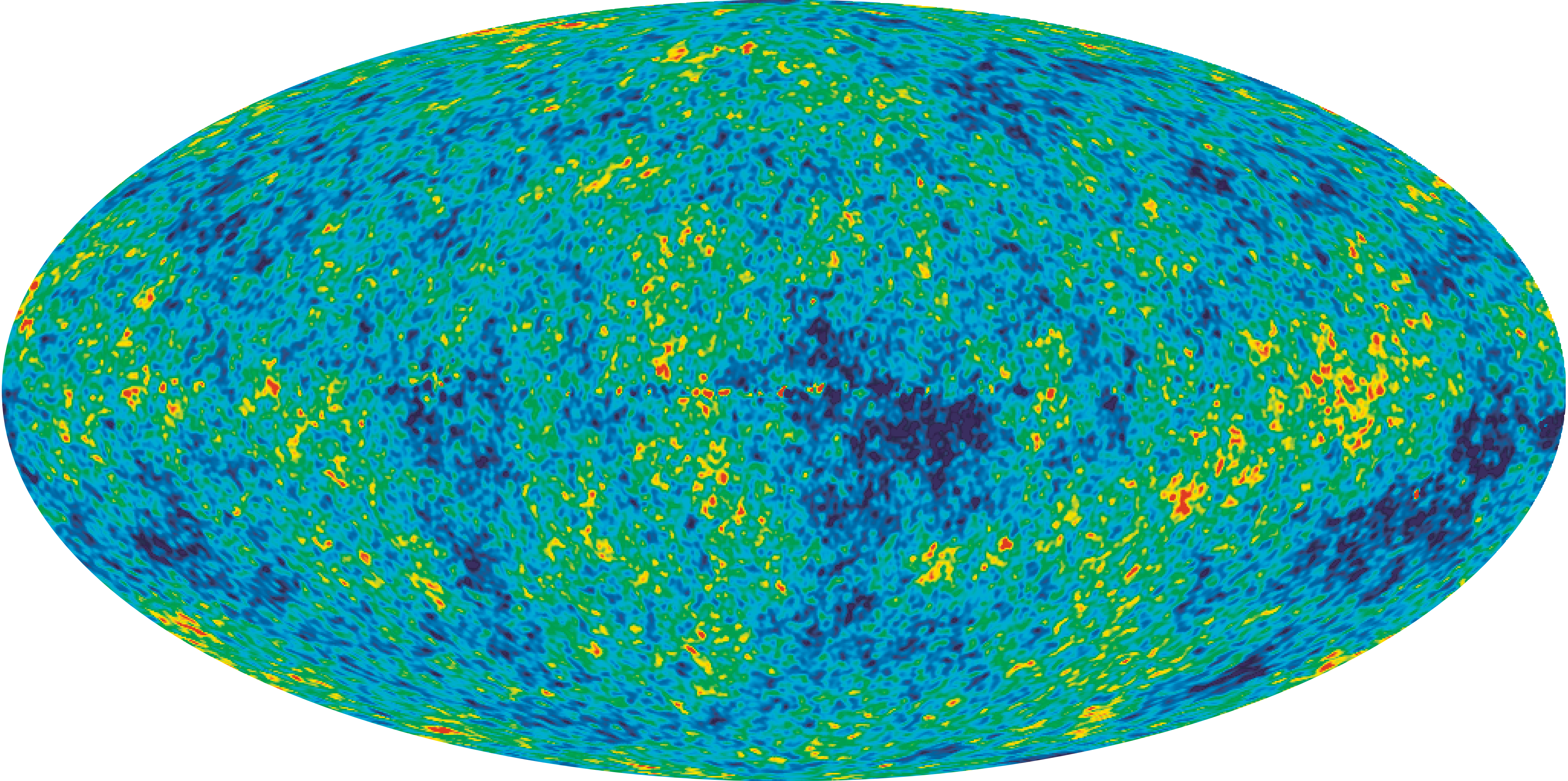
# What About Phase, $\varphi_k$

- There were expectations also:
  - Random phases! (Peebles, ...)
- Collection of random, uncorrelated phases leads to the most famous probability distribution of  $\delta$ :

# **Gaussian Distribution**

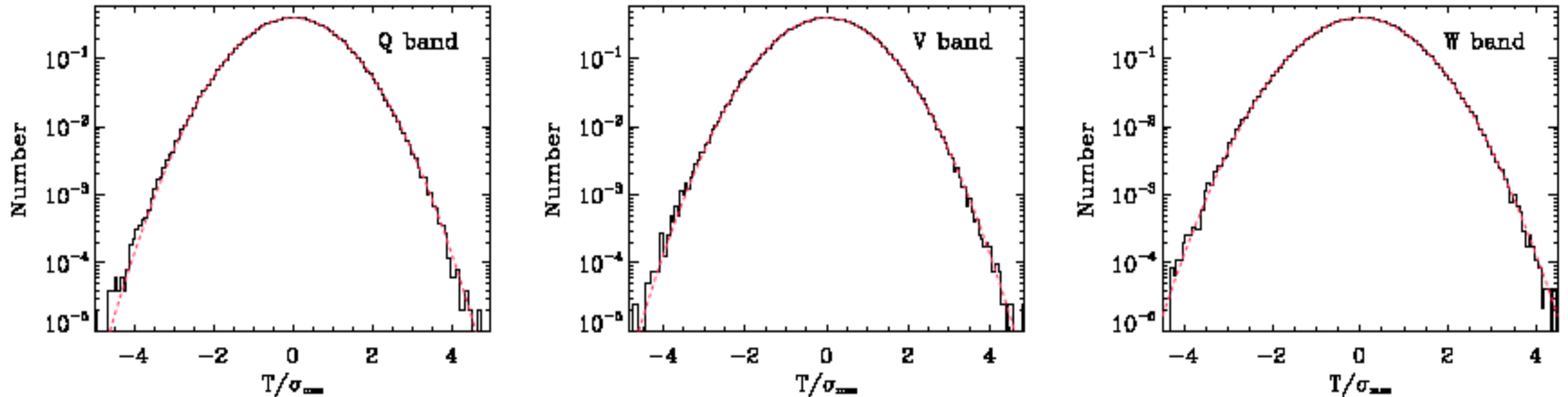


# Gaussian?



WMAP 5-year

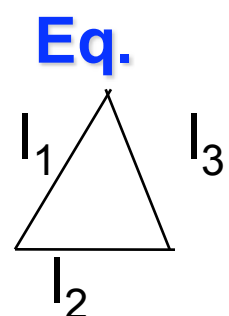
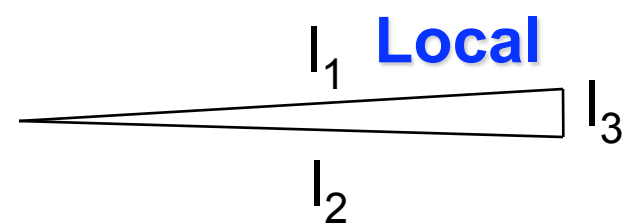
# Take One-point Distribution Function



- The one-point distribution of WMAP map looks pretty Gaussian.
  - Left to right: Q (41GHz), V (61GHz), W (94GHz).
- Deviation from Gaussianity is small, if any.

# Triangles on the Sky: Angular Bispectrum

- Non-zero bispectrum means the detection of non-Gaussianity. **It's always easy to look for deviations from zero!**
- There are many triangles to look for, but...
  - Will focus on two classes



- "Squeezed" parameterized by  $f_{NL}^{\text{local}}$
- "Equilateral" parameterized by  $f_{NL}^{\text{equil}}$

# No Detection at $\geq 95\% \text{CL}$

- $-9 < f_{\text{NL}}(\text{local}) < 111$  (95% CL)
- $-151 < f_{\text{NL}}(\text{equilateral}) < 253$  (95% CL)
- These numbers mean that the primordial curvature perturbations are Gaussian to **0.1% level**.
  - This result provides the strongest evidence for quantum origin of primordial fluctuations during inflation.

# Check List #4: Scale Invariance

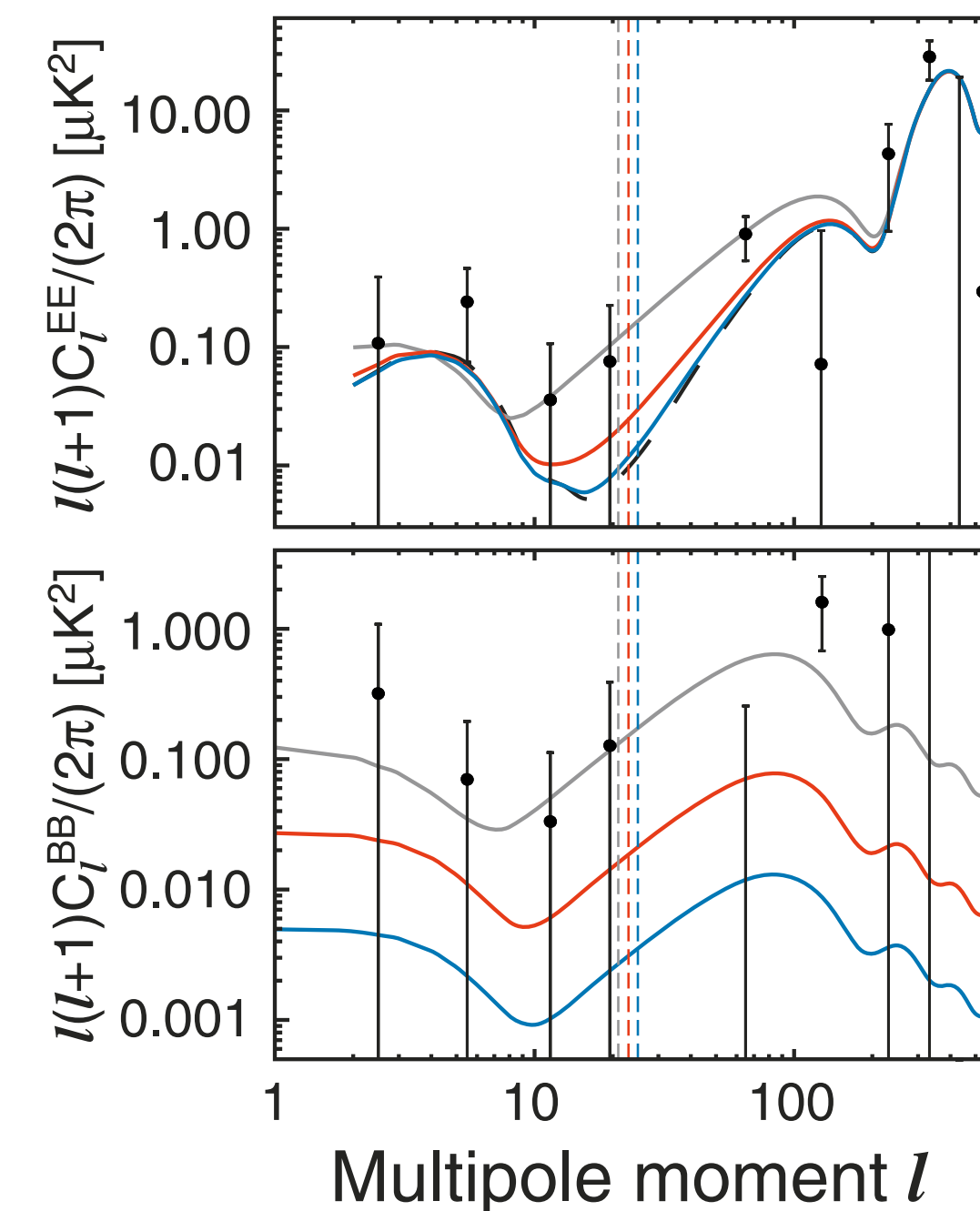
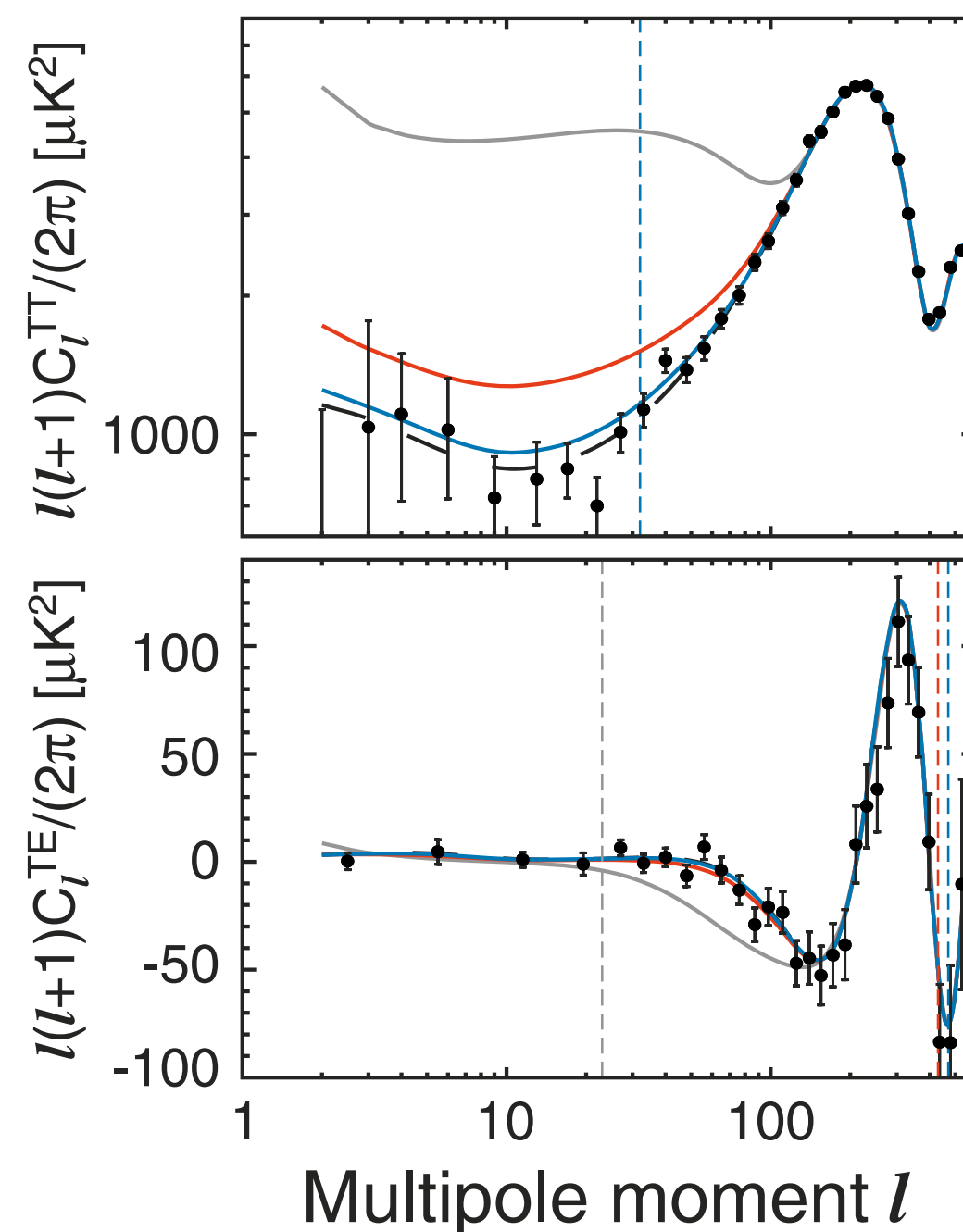
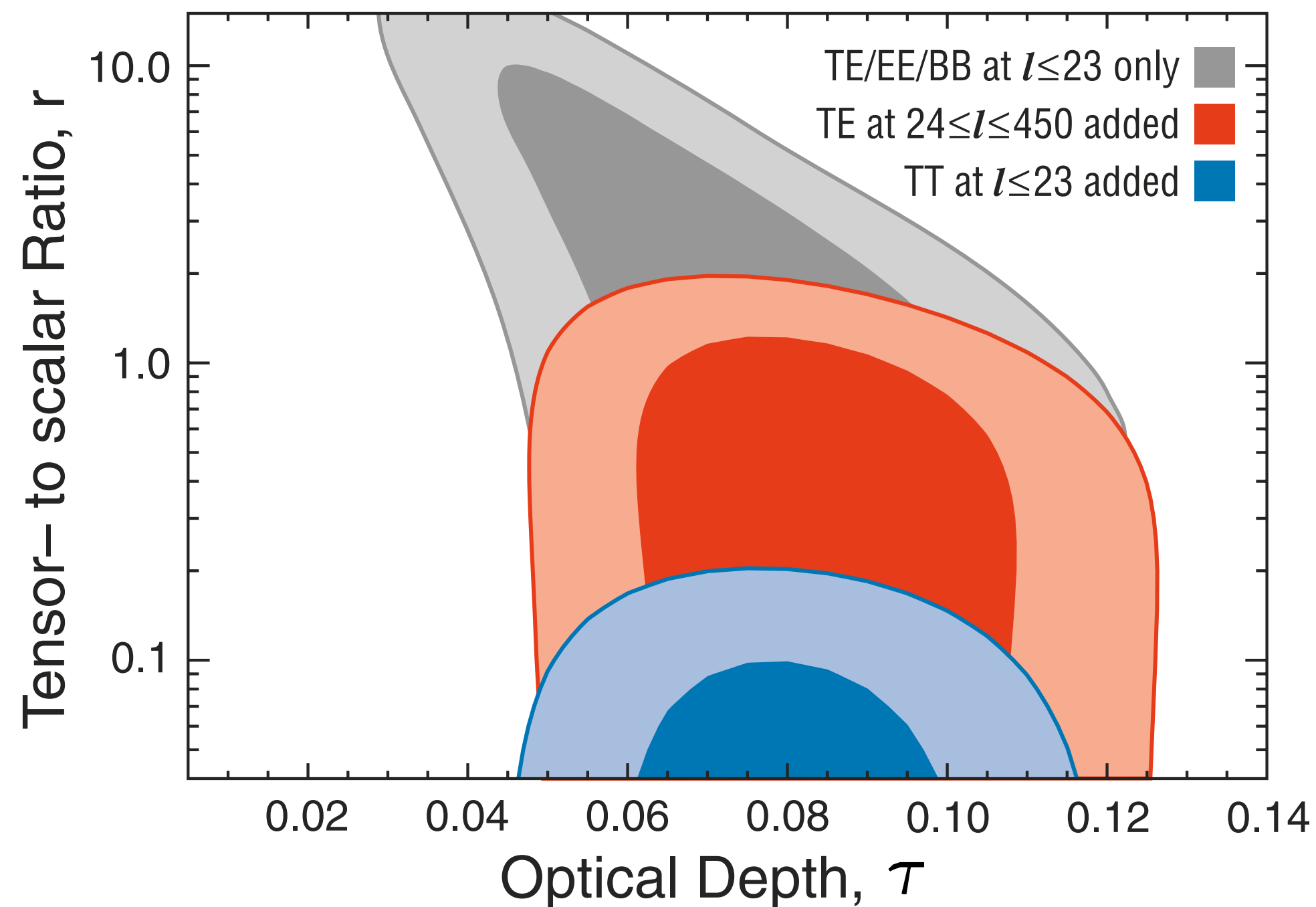
- For a power-law power spectrum (no  $dn_s/d\ln k$ ):
  - WMAP-only:  $n_s=0.963 (+0.014) (-0.015)$
  - WMAP+BAO+SN:  $n_s=0.960 \pm 0.013$ 
    - **3.1 sigma away from  $n_s=1$**

# Check List #5: Gravitational Waves

- How do WMAP data constrain the amplitude of primordial gravitational waves?
- We use “ $r$ ” to parameterize the amplitude of GWs relative to the density fluctuations (or the scalar curvature (metric) perturbations)
  - When  $r=1$ , we have equal amount of scalar and tensor metric perturbations.

# Pedagogical Explanation

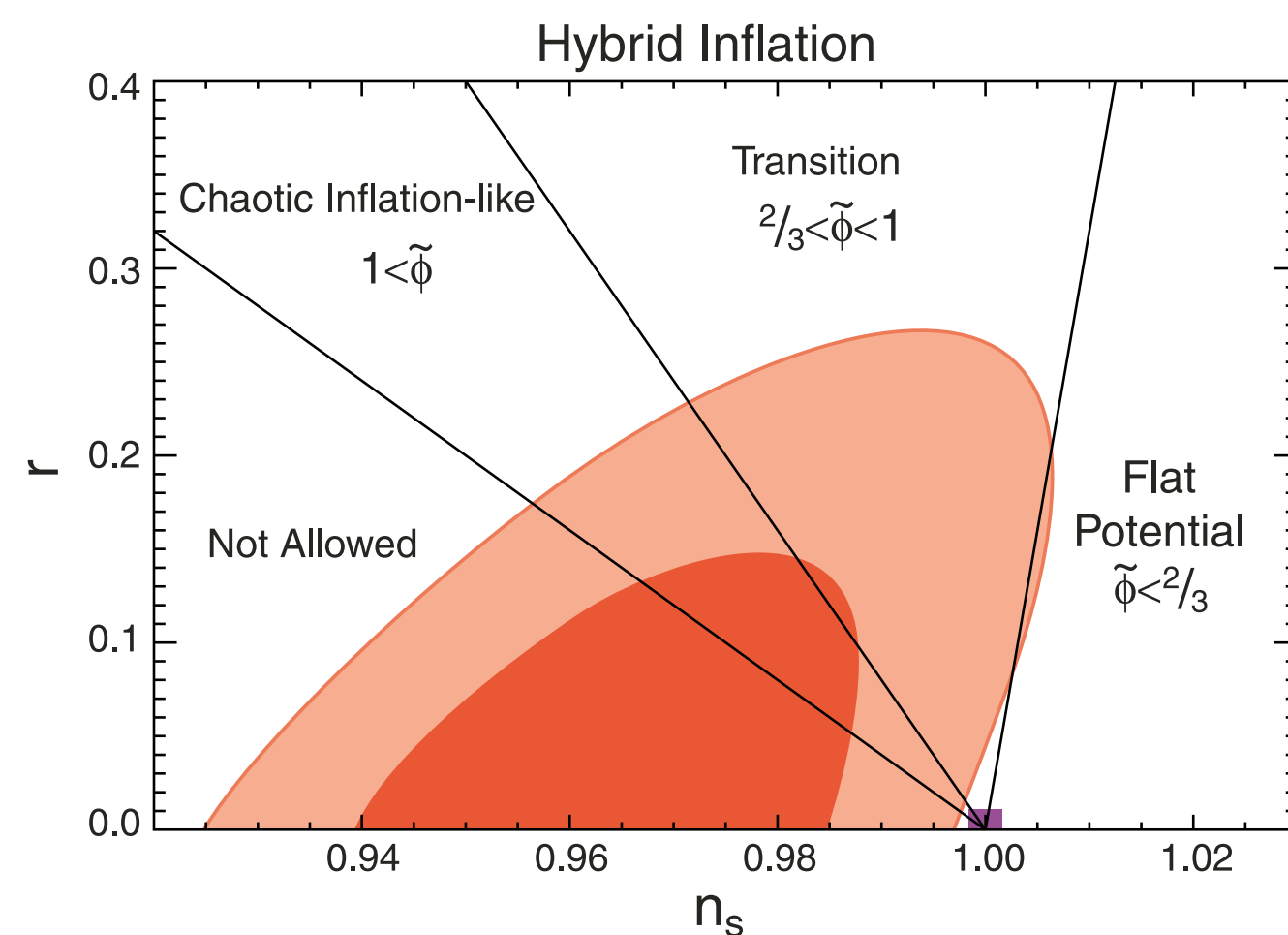
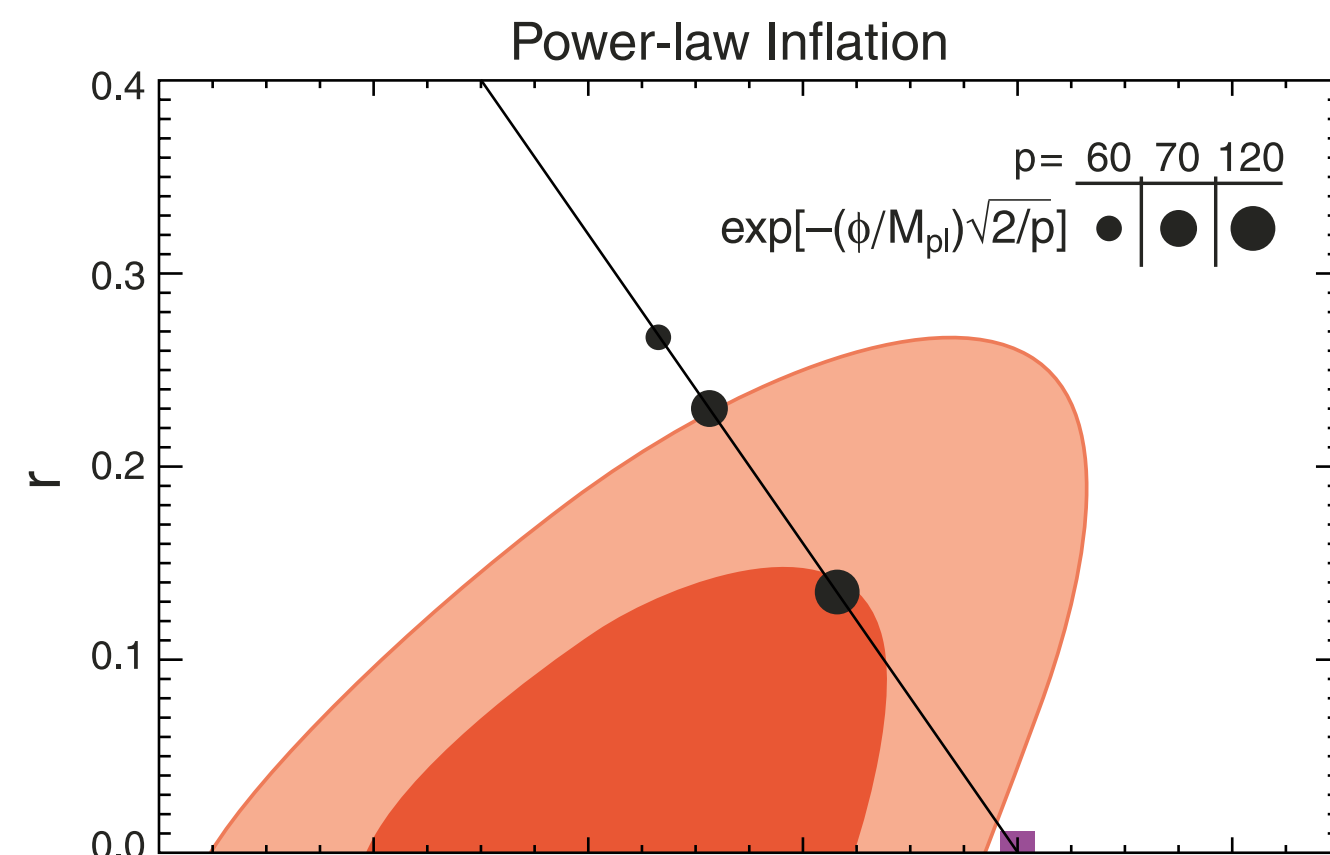
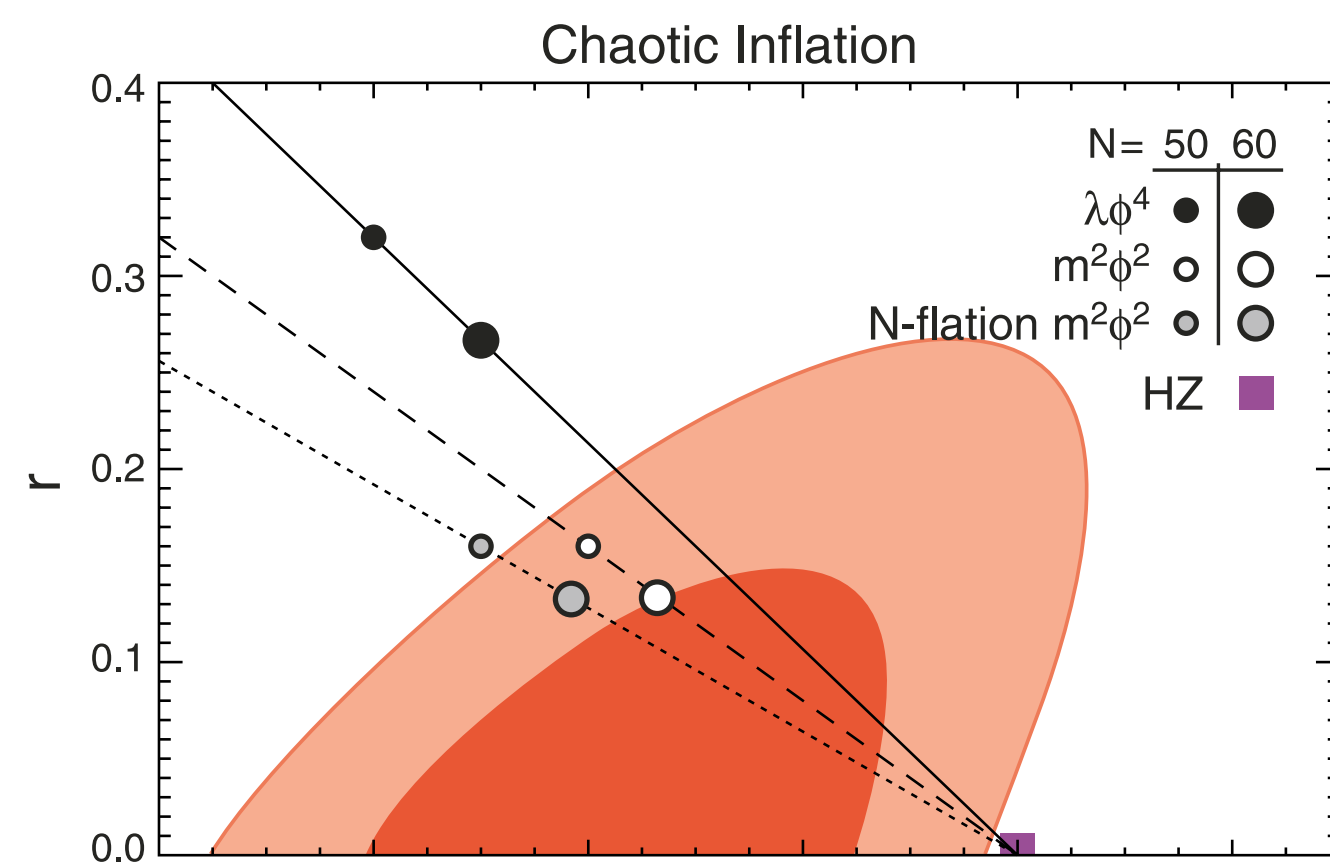
*Komatsu et al.*



- If all the other parameters ( $n_s$  in particular) are fixed...
  - Low- $l$  polarization gives  $r < 20$  (95% CL)
  - + high- $l$  polarization gives  $r < 2$  (95% CL)
  - + low- $l$  temperature gives  $r < 0.2$  (95% CL)

# Lowering a “Limbo Bar”

- $\lambda\varphi^4$  is totally out. (unless you invoke, e.g., non-minimal coupling, to suppress  $r$ ..)
- $m^2\varphi^2$  is within 95% CL.
  - Future WMAP data would be able to push it to outside of 95% CL, if  $m^2\varphi^2$  is not the right model.
- N-flation  $m^2\varphi^2$  (Easter&McAllister) is being pushed out
- PL inflation [ $a(t)\sim t^p$ ] with  $p<60$  is out.
- A blue index ( $n_s>1$ ) region of hybrid inflation is disfavored





# Grading Inflation

- **Flatness:** Curvature  $< 1.3\%$
- **Non-adiabaticity:**  $< 8.9\%$
- **Non-Gaussianity:**  $< 0.1\%$
- **Tilt** (for  $r=0$ ):  $n_s = 0.960 \pm 0.013$  [68% CL]
- **Gravitational waves:**  $r < 0.22$ 
  - $n_s = 0.970 \pm 0.015$  [68% CL]
  - $n_s > 1$  disfavored at 95% CL regardless of  $r$

# Summary

- A simple inflation model ( $\sim 25$  years old) fits the WMAP data, as well as the other astrophysical data sets.
- **We did everything we could do to find deviations from the simple inflation model (curvature, non-adiabaticity, non-gaussianity), but failed.**
- Significant improvements in limits on the deviations
  - Most notably,  $r < 0.22$  (95% CL), and  $n_s > 1$  is now disfavored regardless of  $r$ .
  - Good News: Many popular inflation models have been either ruled out, or being in danger!

# Looking Ahead...

- With more WMAP observations, exciting discoveries may be waiting for us. Two examples for which we might be seeing some hints from the 5-year data:
  - Non-Gaussianity: If  $f_{\text{NL}} \sim 50$ , we will see it at the 3 sigma level with 9 years of data.
  - Gravitational waves ( $r$ ) and tilt ( $n_s$ ) :  $m^2\phi^2$  can be pushed out of the favorable parameter region
    - $n_s > 1$  would be convincingly ruled out regardless of  $r$ .
- Beyond WMAP: detection of gravitational waves?